

① The acceleration of a particle is  $-21 \text{ ft/sec}^2$

initial velocity  $4 \text{ ft/sec}$

initial distance  $14 \text{ ft}$

velocity $\rightarrow -21t + 4$
distance $\rightarrow -\frac{21}{2}t^2 + 4t + 14$

$$\int -21 dt$$

$$\frac{dv}{dt} = -t$$

$$-21t + C$$

$$-21t + 4 \rightarrow v(t)$$

$$\int -21t dt + \int 4 dt$$

$$-\frac{21}{2}t^2 + 4t + C = s(t)$$

$$-\frac{21}{2}t^2 + 4t + 14 = s(t)$$

② initial 100 230 after 3 days

$$\left( \frac{dA}{dt} = Ar \right)$$

$$\frac{1}{A} dA = r dt \quad \int \frac{1}{A} dA = \int r dt$$

$$\ln|A| + C_1 = rt + C_2$$

①

$$\ln|A| = rt + C$$

$$A = e^{rt+C}$$

$$A = e^{rt} e^C$$

$$A = C e^{rt}$$

$$230 = 100 e^{r \cdot 3}$$

②

$$\frac{\ln(2.3)}{3} = r \Rightarrow r \approx .2776$$

$$A = 100 e^{\frac{\ln(2.3)}{3} t}$$

③

$$A = 100 e^{\frac{\ln(2.3)}{3} 14}$$

$$A \approx 100 \cdot 48.759948107$$

$$A \approx 4875.9948107$$

After 14 days, the population is around 4.876 ants

③

$$(a) \frac{dH}{dt} = -k(H-8)$$

$$(b) \frac{1}{H-8} dH = -k dt$$

$$\int \frac{1}{H-8} dH = \int -k dt$$

$$\ln(H-8) + C_1 = -kt + C_2$$

$$\ln(H-8) = -kt + C$$

$$H-8 = e^{-kt+C}$$

$$H = e^{-kt} C + 8$$

$$\rightarrow H = (H_0 - 8)e^{-kt} + 8$$

$$21 = 8 + (27-8)e^{-k}$$

$$\frac{13}{19} = e^{-k}$$

$$-\ln\left(\frac{13}{19}\right) = k \approx 0.379$$

↓

$$H(t) = 19e^{-kt} + 8 //$$

$$(c) 37 = 19e^{+0.379t} + 8$$

$$\ln \frac{29}{19}$$

$$\frac{\ln \frac{29}{19}}{\ln \frac{13}{19}} \approx -1.114278$$

It was discontinued approximately  
1.114278 hours after