# Performance of Optimization Algorithms

Design Optimization TMKT48



#### Performance of optimizations

- Different optimization algorithms are best for different problems
- We want to compare the algorithms
  - Can help us to choose optimization algorithm
  - Can be used to optimize the parameters of the optimization algorithm – Meta-optimization



#### Benchmarking Optimization Algorithms

- You want to choose the method that you think is best for your problem
- 1. Try to optimize simple mathematical functions that you think are similar to the problem that you really want to optimize
  - Linear/non-linear, uni-/multimodal, ...?
- Optimize the mathematical functions numerous times with each candidate optimization algorithm
- Order the optimization algorithms according to accuracy, robustness, efficiency, user friendliness etc.
- 4. Choose the most suitable optimization algorithms

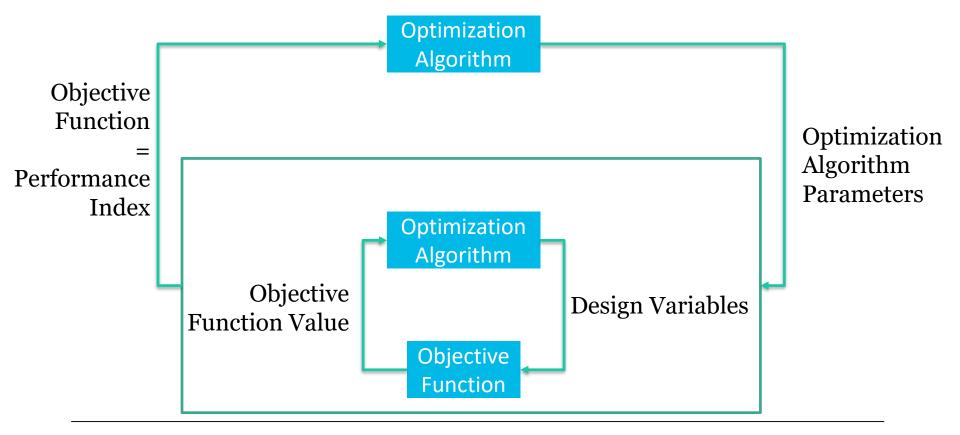


# Meta-Optimization



#### Meta-optimization

Optimization of the parameters of the algorithm







- We want a performance index that combines
  - Accuracy
  - Required number of function evaluations
- This will be a measure of the efficiency of the optimization algorithm



- P<sub>opt</sub> is the probability of finding the optimum
- N<sub>eval</sub> is the required number of function evaluations
- The probability of not finding the optimum is

$$1 - P_{opt}$$

• The probability of NOT finding the optimum during m optimizations is

$$(1-P_{opt})^m$$



- P<sub>opt</sub> is the probability of finding the optimum
- N<sub>eval</sub> is the required number of function evaluations
- The probability of finding the optimum during m optimizations is

$$1 - (1 - P_{opt})^m$$



- P<sub>opt</sub> is the probability of finding the optimum
- N<sub>eval</sub> is the required number of function evaluations

$$1 - (1 - P_{opt})^m$$

• The number of optimizations, m, that we can perform depends on the available number of function evaluations and  $N_{\rm eval}$ 

$$m = \frac{N_{available}}{N_{eval}}$$

• The value of  $N_{available}$  does not depend on the optimization algorithm and can therefore be set to any number. It is here set to 100.

$$m = \frac{100}{N_{eval}}$$



- P<sub>opt</sub> is the probability of finding the optimum
- N<sub>eval</sub> is the required number of function evaluations
- The performance index is therefore

$$1 - (1 - P_{opt})^{100/N_{eval}}$$

• It can be seen as the probability of finding the optimum if we can afford 100 function evaluations.



- P<sub>opt</sub> is the probability of finding the optimum
- N<sub>eval</sub> is the required number of function evaluations
- The performance index is

$$1 - (1 - P_{opt})^{100/N_{eval}}$$

P <sub>opt</sub>	N <sub>eval</sub>	Performance Index
0.5	100	0.5
0.25	100	0.25
0.25	50	0.44

• High  $P_{opt}$  and low  $N_{eval}$  leads to high performance index



#### Question

• What happens if two optimization algorithms both have an accuracy of 100%

- Both get Performance Index = 1
- Choose the one that requires the least number of function evaluations



#### The Suggested Performance Index

- Advantages
  - Enables comparison of optimization algorithm performances
- Disadvantages
  - Will return 1 regardless of the required number of evaluations if 100% accuracy.
    - The one with the fewest required number of evaluations is the best
  - The criterion for a successful optimization affects the result



### **Questions?**

