## 1 Data with Debye-Waller factor correction for direct comparisson with QMC

Our QMC collaborators compute  $S(\mathbf{Q})$ , which is related to our measurement as

$$I(t) = I_{\text{TOF}=\infty}(1 + DW_t(S(\boldsymbol{Q}) - 1)) \tag{1}$$

where  $DW_t$  is the TOF dependent Debye-Waller factor. Previously we presented our collaborators the data which did not have a Debye-Waller factor correction. Here we make a correction, also noting that we only made measurements in situ and at  $t=6\mu s$ . With these two measurements one can solve for the spin structure factor

$$I_t \equiv \frac{I(t=0)}{I(t)} = \frac{1 + DW_0(S(\mathbf{Q}) - 1)}{1 + DW_t(S(\mathbf{Q}) - 1)}$$
(2)

$$\Rightarrow S(\mathbf{Q}) = \frac{I_t(1 - DW_t) - (1 - DW_0)}{DW_0 - I_t DW_t}$$
 (3)

In the long time limit  $(DW_t = 0)$ , and for negligible wavefunction size in the lattice  $(DW_0 = 1)$  this reduces to  $S(\mathbf{Q}) = I_t$ .

The data including this Debye-Waller factor correction is shown in Fig. 1 and also attached to the email.

Figure 1: Top row shows our raw data, which corresponds to ratio of CCD counts A2/A1, and CCD counts for A1, A2 respectively. Middle row shows the ratio of in-situ and TOF data for each of the three quantities. Bottom row, left panel shows the Debye-Waller factor for the in-situ picture and the 6  $\mu$ s TOF picture as a function of angle along chamber. The A1 Debye-Waller factor goes to 1 for both in-situ and TOF at  $30^{\circ}$ , which corresponds to zero momentum transfer. Bottom row, right panels show the spin structure factor determined from our data and the Debye-Waller factor corrections.

-10° 0° 10° 20° 30

Angle along chamber

0.60

-30°

0.0

-30

-10° 0° 10° 20°

Angle along chamber

0.8

0.7

-30°

-10° 0° 10° 20° 30°

Angle along chamber