

Dados:  $Q = 0.08 \text{ m}^3/\text{s}$ ,  $T = 25.0^\circ\text{C}$ ,  $g = 9.81 \text{ m/s}^2$ ,  $\gamma = 9781.0207 \text{ N/m}^3$ ,  $\mu = 0.0009 \text{ N}\cdot\text{s}\cdot\text{m}^{-2}$ ,  $P_{\text{vr}} = 1.6926 \text{ m}$ ,  $b = 0.5 \text{ m}$ .

1. Altura,  $H_{\text{vr}}$ .

$$H_{\text{vr}} = \left( \frac{Q}{1.848b} \right)^{\frac{3}{2}} \Rightarrow H_{\text{vr}} = \left( \frac{0.08 \text{ m}^3/\text{s}}{1.848 \cdot 0.5 \text{ m}} \right)^{\frac{3}{2}} \Rightarrow \boxed{H_{\text{vr}} = 0.0255 \text{ m}}$$

2. Distância entre vertedor e seção inicial do ressalto  $L_{\text{m}}$ , profundidade crítica  $y_{\text{c}}$ , e altura da lâmina d'água no início do ressalto  $y_1$ .

$$y_{\text{c}} = \sqrt[3]{\frac{Q^2}{gb^2}} \Rightarrow y_{\text{c}} = \sqrt[3]{\frac{0.08^2 (\text{m}^3/\text{s})^2}{9.81 \text{ m/s}^2 \cdot 0.5^2 \text{ m}^2}} \Rightarrow \boxed{y_{\text{c}} = 0.1377 \text{ m}}$$

$$L_{\text{m}} = H_{\text{vr}} \left( \frac{P_{\text{vr}}}{H_{\text{vr}}} \right)^{0.54} \Rightarrow L_{\text{m}} = 0.0255 \text{ m} \left( \frac{1.6926 \text{ m}}{0.0255 \text{ m}} \right)^{0.54} \Rightarrow \boxed{L_{\text{m}} = 0.3561 \text{ m}}$$

$$y_1 = \frac{1.414y_{\text{c}}}{\sqrt{2.56 + \frac{P_{\text{vr}}}{y_{\text{c}}}}} \Rightarrow y_1 = \frac{1.414 \cdot 0.1377 \text{ m}}{\sqrt{2.56 + \frac{1.6926 \text{ m}}{0.1377 \text{ m}}}} \Rightarrow \boxed{y_1 = 0.0505 \text{ m}}$$

3. Velocidade do escoamento no início do ressalto,  $v_1$ .

$$v_1 = \frac{Q}{y_1 b} \Rightarrow v_1 = \frac{0.08 \text{ m}^3/\text{s}}{0.0505 \text{ m} \cdot 0.5 \text{ m}} \Rightarrow \boxed{v_1 = 3.1677 \text{ m/s}}$$

4. Número de Froude na seção 1,  $F_1$ .

$$F_1 = \frac{v_1}{\sqrt{gy_1}} \Rightarrow F_1 = \frac{3.1677 \text{ m/s}}{\sqrt{9.81 \text{ m/s}^2 \cdot 0.0505 \text{ m}}} \Rightarrow \boxed{F_1 = 4.5}$$

5. Altura da lâmina d'água no final do ressalto  $y_2$ .

$$y_2 = \frac{y_1}{2} \left( \sqrt{1 + 8F_1^2} - 1 \right) \Rightarrow y_2 = \frac{0.0505 \text{ m}}{2} \left( \sqrt{1 + 8 \cdot 4.5^2} - 1 \right) \Rightarrow \boxed{y_2 = 0.2972 \text{ m}}$$

6. Perda de energia  $E_{\text{n}}$ , comprimento do ressalto  $L_{\text{r}}$ , e velocidade no final do ressalto  $v_2$ .

$$E_{\text{n}} = \frac{(y_2 - y_1)^3}{4y_1 y_2} \Rightarrow E_{\text{n}} = \frac{(0.2972 \text{ m} - 0.0505 \text{ m})^3}{4 \cdot 0.0505 \text{ m} \cdot 0.2972 \text{ m}} \Rightarrow \boxed{E_{\text{n}} = 0.25 \text{ m}}$$

$$v_2 = \frac{Q}{y_2 b} \Rightarrow v_2 = \frac{0.08 \text{ m}^3/\text{s}}{0.2972 \text{ m} \cdot 0.5 \text{ m}} \Rightarrow \boxed{v_2 = 0.5384 \text{ m/s}}$$

$$L_{\text{r}} = c(y_2 - y_1) \Rightarrow L_{\text{r}} = 5.0(0.2972 \text{ m} - 0.0505 \text{ m}) \Rightarrow \boxed{L_{\text{r}} = 1.2334 \text{ m}}$$

7. Velocidade média,  $U_{\text{m}}$ .

$$U_{\text{m}} = \frac{v_1 + v_2}{2} \Rightarrow U_{\text{m}} = \frac{3.1677 \text{ m/s} + 0.5384 \text{ m/s}}{2} \Rightarrow \boxed{U_{\text{m}} = 1.853 \text{ m/s}}$$

8. Tempo médio de mistura,  $T_{\text{m}}$ .

$$T_{\text{m}} = \frac{L_{\text{r}}}{U_{\text{m}}} \Rightarrow T_{\text{m}} = \frac{1.2334 \text{ m}}{1.853 \text{ m/s}} \Rightarrow \boxed{T_{\text{m}} = 0.6656 \text{ s}}$$

9. Gradiente de velocidade médio,  $G_{\text{m}}$ .

$$G_{\text{m}} = \sqrt{\frac{\gamma E_{\text{n}}}{\mu T_{\text{m}}}} \Rightarrow G_{\text{m}} = \sqrt{\frac{9781.0207 \text{ N/m}^3 \cdot 0.25 \text{ m}}{0.0009 \text{ N}\cdot\text{s}\cdot\text{m}^{-2} \cdot 0.6656 \text{ s}}} \Rightarrow \boxed{G_{\text{m}} = 2031.1054 \text{ s}^{-1}}$$