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#### $1 \quad \text{Utils}$

#### 1.1 Makefile

```
1 CXX = g++
2 CXXFLAGS = -fsanitize=address,undefined -fno-omit-frame-pointer -g -Wall -5
      Wshadow -std=c++17 -Wno-unused-result -Wno-sign-compare -Wno-char-
      subscripts #-fuse-ld=gold
4 clear:
      find . -maxdepth 1 -type f -executable -exec rm {} +
      g++-g $(f).cpp $(CPPFLAGS) -o $(f)
      ./$(f)
9
10
11 runci:
12
      g++ -g $(f).cpp $(CPPFLAGS) -o $(f)
      ./\$(f) < \$(f).txt
14
15 runp:
      python3 $(f).py
17
18 runpt:
      python3 $(f).py < $(f).txt
```

### 1.2 Mini Template Cpp

```
#include <bits/stdc++.h>
3 using namespace std;
5 #define _ ios_base::sync_with_stdio(0); cin.tie(0);
7 #define int
                          long long int
8 #define double
                          long double
9 #define endl
                          "\n"
10 #define print_v(a)
                          for(auto x : a) cout << x << " "; cout << endl</pre>
                          for(int i=s;i<e;i++)</pre>
#define f(i,s,e)
12 #define rf(i,e,s)
                          for(int i=e-1;i>=s;i--)
14 #define dbg(x) cout << #x << " = " << x << endl;
16 void solve() {}
18 int32_t main() { _
19
      int t = 1; // cin >> t;
20
      while (t--)
21
      //while(cin >> a >> b)
          solve():
23
24
      return 0;
26
27 }
```

## 1.3 Template Cpp

```
1 #include <bits/stdc++.h>
2 using namespace std;
4 #define _ ios_base::sync_with_stdio(0); cin.tie(0);
6 #define int
                          long long int
7 #define double
                          long double
                          "\n"
8 #define endl
9 #define print_v(a)
                          for(auto x : a) cout << x << " "; cout << endl</pre>
10 #define print_vp(a)
                          for(auto x : a) cout << x.F << " " << x.S << endl
11 #define print2(a,x,y) for(int i = x; i < y; i++) cout << a[i] << " "; cout
      << endl
12 #define f(i,s,e)
                          for(int i=s;i<e;i++)</pre>
                          for(int i=e-1;i>=s;i--)
13 #define rf(i,e,s)
15 #define dbg(x) cout << #x << " = " << x << endl;
16 #define bug(...)
                          __f (#__VA_ARGS__, __VA_ARGS__)
18 const int INF = 0x7f3f3f3f;
19 const int MAX = 1e8+10; // 10^6 + 10
21 string to_upper(string a) { for (int i=0;i<(int)a.size();++i) if (a[i]>='a
      ' && a[i] <= 'z') a[i] -= 'a' - 'A'; return a; }
22 string to_lower(string a) { for (int i=0;i<(int)a.size();++i) if (a[i]>='A
       ' && a[i] <= 'Z') a[i] += 'a' - 'A'; return a; }
23 bool prime(int a) { if (a==1) return 0; for (int i=2;i<=round(sqrt(a));++i
      ) if (a%i==0) return 0; return 1; }
25 template <typename Arg1 > void __f (const char* name, Arg1&& arg1) { cout
       << name << " : " << arg1 << endl: }
26 template <typename Arg1, typename... Args > void __f (const char* names,
      Arg1&& arg1, Args&&... args) {
       const char* comma = strchr (names + 1, ',');
      cout.write (names, comma - names) << " : " << arg1 << " | "; __f (
      comma + 1, args...);
29 }
32 vector < vector < int >> graph;
33 vector < bool > vis;
35 void solve() {
37 }
39 int32_t main() { _
      clock_t z = clock();
41
42
      int t = 1; // cin >> t;
      while (t--)
      //while(cin >> a >> b)
45
           solve();
47
48
```

```
cerr << fixed << "Run Time : " << ((double)(clock() - z) /</pre>
      CLOCKS_PER_SEC) << endl;
      return 0;
50
51 }
        Files
1 #!/bin/bash
3 for c in {a..f}; do
      cp temp.cpp "$c.cpp"
      echo "$c" > "$c.txt"
      if [ "$c" = "$letter" ]; then
           break
      fi
9 done
        Template Python
1 import sys
2 import math
3 import bisect
4 from sys import stdin, stdout
5 from math import gcd, floor, sqrt, log
6 from collections import defaultdict as dd
7 from bisect import bisect_left as bl,bisect_right as br
9 svs.setrecursionlimit(100000000)
11 inp
          =lambda: int(input())
         =lambda: input().strip()
12 strng
          =lambda x,l: x.join(map(str,l))
         =lambda: list(input().strip())
14 strl
15 mul
         =lambda: map(int,input().strip().split())
         =lambda: map(float,input().strip().split())
16 mulf
         =lambda: list(map(int,input().strip().split()))
17 seq
        =lambda x: int(x) if (x==int(x)) else int(x)+1
20 ceildiv=lambda x,d: x//d if (x\%d==0) else x//d+1
22 flush =lambda: stdout.flush()
23 stdstr =lambda: stdin.readline()
24 stdint =lambda: int(stdin.readline())
25 stdpr =lambda x: stdout.write(str(x))
```

27 mod=100000007

35 def ident(\*args):

if len(args) == 1:

return args[0]

29 #main code

31 a = None 32 b = None 33 lista = None

28

```
return args
40
41 def parsin(*, l=1, vpl=1, s=" "):
42
          if vpl == 1: return ident(input())
          else: return list(map(ident, input().split(s)))
44
      else:
45
          if vpl == 1: return [ident(input()) for _ in range(1)]
46
          else: return [list(map(ident, input().split(s))) for _ in range(l)
47
48
49
50 def solve():
      pass
    if __name__ == '__main__':
54 def main():
      st = clk()
      escolha = "in"
58
      #escolha = "num"
      match escolha:
          case "in":
61
               # êl infinitas linhas agrupadas de 2 em 2
               # pra infinitos valores em 1 linha pode armazenar em uma lista
               while True:
                   global a, b
                   try: a, b = input().split()
66
                   except (EOFError): break #permite ler todas as linahs
      dentro do .txt
                   except (ValueError): pass # consegue ler éat linhas em
68
      branco
69
                       a, b = int(a), int(b)
70
                   solve()
          case "num":
               global lista
               # int 1; cin >> 1; while(1--){for(i=0; i<vpl; i++)}
               # retorna listas com inputs de cada linha
               # leia l linhas com vpl valores em cada uma delas
77
                   # caseo seja mais de uma linha, retorna lista com listas
78
      de inputs
               lista = parsin(1=2, vpl=5)
79
               solve()
80
81
      sys.stderr.write(f"Run Time : {(clk() - st):.6f} seconds\n")
83
84 main()
```

# 2 Strings

#### 2.1 Ocorrencias

```
2 * @brief str.find() aprimorado
3 * Oparam str string to be analised
      Oparam sub substring to be searched
* @return vector<int> com indices de todas as êocorrncias de uma
      substring em uma string
7 vector<int> ocorrencias(string str,string sub){
                                                                              6 }
      vector < int > ret;
      int index = str.find(sub);
10
      while (index!=-1) {
          ret.push_back(index);
12
13
          index = str.find(sub,index+1);
      }
15
                                                                              5 }
16
      return ret;
                                                                               2.6
        Chaves Colchetes Parenteses
1 def balanced(string) -> bool:
     stack = []
                                                                              6 }
     for i in string:
         if i in '([{': stack.append(i)
         elif i in ')]}':
             if (not stack) or ((stack[-1],i) not in [('(',')'), ('[',']'),
                                                                               3.1
      ('{','}')]):
                 return False
             else:
10
                 stack.pop()
12
13
     return not stack
  2.3 Split
                                                                                  }
1 //split a string with a delimiter
2 //eg.: split("á01, tudo bem?", " ") -> ["á01,", "tudo", "bem?"]
                                                                             10 }
4 vector<string> split(string in, string delimiter){
      vector < string > numbers;
      string token = "";
      int pos;
      while(true){
          pos = in.find(delimiter);
          if(pos == -1) break;
10
```

token = in.substr(0, pos);

in = in.erase(0, pos + delimiter.length());

numbers.push\_back(token);

numbers.push\_back(in);

return numbers;

12

13 14

15

16 17 }

#### 2.4 Uppercase

```
1 string to_upper(string a) {
2    for (int i=0;i<(int)a.size();++i)
3         if (a[i]>='a' && a[i]<='z')
4         a[i]-='a'-'A';
5    return a;
6 }</pre>
```

### 2.5 Ispalindrome

```
bool isPalindrome(string S){
string P = S;
reverse(P.begin(), P.end()); // Reverte P
return (S == P); //retorna true se verdadeiro, false se falso
}
```

#### 2.6 Lowercase

```
1 string to_lower(string a) {
2    for (int i=0;i<(int)a.size();++i)
3        if (a[i]>='A' && a[i]<='Z')
4         a[i]+='a'-'A';
5    return a;
6 }</pre>
```

#### 3 Matematica

### 3.1 Mdc Multiplo

```
int mdc_many(vector<int> arr) {
   int result = arr[0];
   for (size_t i = 1; i < arr.size(); i++) {
      result = mdc(arr[i], result);

   if(result == 1)
      return 1;
   }
   return result;
}</pre>
```

## 3.2 Mmc Multiplo

```
int mmc(vector<int> arr) {
   int result = arr[0];
   for(size_t i = 1; i < arr.size(); i++)
        result = (arr[i] * result / mmc_util(arr[i], result ));
   return ans;
}</pre>
```

# 3.3 Fast Exponentiation

```
1 const int mod = 1e9+7;
2 int fexp(int a, int b)
3 {
4    int ans = 1;
```

```
while (b)
                                                                              19 bool prime(int n) {
      {
                                                                                     if (n < 2) return 0;
          if (b & 1)
                                                                                     if (n <= 3) return 1;
                                                                                     if (n % 2 == 0) return 0:
             ans = ans * a \% mod;
          a = a * a % mod;
                                                                                     int r = __builtin_ctzint(n - 1), d = n >> r;
9
                                                                              23
          b >>= 1:
10
      }
                                                                                     // com esses primos, o teste funciona garantido para n <= 2^64
11
                                                                                     // funciona para n <= 3*10^24 com os primos ate 41
      return ans;
12
                                                                                     for (int a: {2, 325, 9375, 28178, 450775, 9780504, 795265022}) {
                                                                                         int x = pow(a, d, n);
                                                                              28
  3.4 Sieve
                                                                                         if (x == 1 \text{ or } x == n - 1 \text{ or a } \% n == 0) continue;
                                                                              29
                                                                                         for (int j = 0; j < r - 1; j++) {
1 // Crivo de óEratstenes para gerar primos éat um limite 'lim'
                                                                                             x = mul(x, x, n);
2 // Complexidade: O(n log log n), onde n é o limite
                                                                                             if (x == n - 1) break;
3 const int ms = 1e6 + 5:
4 bool notPrime[ms]; // notPrime[i] é verdadeiro se i ano é um únmero
                                                                                         if (x != n - 1) return 0;
5 int primes[ms], qnt; // primes[] armazena os únmeros primos e qnt é a
                                                                                     return 1:
      quantidade de primos encontrados
                                                                              38 }
7 void sieve(int lim)
                                                                                 3.6
                                                                                      Mdc
    primes[qnt++] = 1; // adiciona 1 como um únmero primo se ele for ávlido
                                                                               int mdc(int x, int v) {
      no problema
                                                                                     return y ? mdc(y, x % y) : abs(x);
   for (int i = 2: i <= lim: i++)
11
      if (notPrime[i])
12
                                                                                      Fatorial Grande
        continue:
                                            // se i ano é primo, pula
13
      primes[qnt++] = i;
                                             // i é primo, adiciona em primes
14
                                                                               void multiply(vector<int>& num, int x) {
      for (int j = i + i; j \le \lim_{j \to i} j + = i) // marca todos os umltiplos de i_2
                                                                                    int carrv = 0:
       como ãno primos
                                                                                    for (int i = 0; i < num.size(); i++) {</pre>
        notPrime[j] = true;
                                                                                        int prod = num[i] * x + carry;
17 }
                                                                                        num[i] = prod % 10;
18 }
                                                                                        carry = prod / 10;
        Miller-rabin
                                                                                    while (carry != 0) {
                                                                                        num.push_back(carry % 10);
                                                                                        carry /= 10;
1 // Miinter-Rabin
                                                                                    }
                                                                              11
                                                                              12 }
_3 // Testa se n eh primo, n <= 3 * 10^18
                                                                              14 vector < int > factorial(int n) {
5 // O(log(n)), considerando multiplicacao
                                                                                    vector<int> result:
6 // e exponenciacao constantes
                                                                                    result.push back(1):
                                                                              16
                                                                                    for (int i = 2; i <= n; i++) {
                                                                              17
8 int mul(int a, int b, int m) {
                                                                                        multiply(result, i);
      int ret = a*b - int((long double)1/m*a*b+0.5)*m;
9
                                                                              19
      return ret < 0 ? ret+m : ret;</pre>
10
                                                                                    return result;
11 }
                                                                              21 }
12
13 int pow(int x, int y, int m) {
                                                                                       Sieve Linear
      if (!v) return 1:
15
      int ans = pow(mul(x, x, m), v/2, m);
      return y%2 ? mul(x, ans, m) : ans;
                                                                               1 // Sieve de Eratosthenes com linear sieve
17 }
                                                                               2 // Encontra todos os únmeros primos no intervalo [2, N]
18
                                                                               3 // Complexidade: O(N)
```

```
q.push(u);
                                                                                                     d[u] = d[v] + 1;
5 const int N = 10000000;
                                                                                 23
6 vector <int > lp(N + 1); // lp[i] = menor fator primo de i
                                                                                                     p[u] = v;
                                                                                                }
7 vector<int> pr;
                    // vetor de primos
                                                                                            }
                                                                                 26
9 for (int i = 2; i <= N; ++i)</pre>
                                                                                        }
                                                                                 27
10 {
                                                                                 28 }
      if (lp[i] == 0)
11
                                                                                 30 //pra uma bfs que n guarda o backtracking:
          lp[i] = i;
                                                                                 31 void bfs(int p) {
13
                                                                                        memset(visited, 0, sizeof visited);
           pr.push_back(i);
14
      }
15
                                                                                        queue < int > q;
      for (int j = 0; i * pr[j] <= N; ++j)
                                                                                        q.push(p);
16
                                                                                 34
17
                                                                                 35
          lp[i * pr[j]] = pr[j];
                                                                                        while (!q.empty()) {
                                                                                 36
           if (pr[j] == lp[i])
                                                                                 37
                                                                                            int curr = q.top();
20
                                                                                 38
                                                                                            q.pop();
                                                                                            if (visited[curr]==1) continue;
               break;
                                                                                 39
                                                                                            visited[curr]=1:
22
                                                                                 40
      }
23
                                                                                 41
                                                                                            // process current node here
                                                                                            for (auto i : adj[curr]) {
                                                                                 43
        Mmc
                                                                                                 q.push(i);
int mmc(int x, int y) {
     return (x && y ? (return abs(x) / mdc(x, y) * abs(y)) : abs(x | y));
3 }
                                                                                    4.2 Dijkstra
       Grafos
                                                                                  vector < vector < pair < int , int >>> adj;
                                                                                  2 int n, s;
  4.1 Bfs
                                                                                  4 vector < int > d(n, LLINF);
1 // BFS com informacoes adicionais sobre a distancia e o pai de cada
                                                                                  5 vector < int > p(n, -1);
                                                                                  6 vector < bool > used(n);
2 // Complexidade: O(V + E), onde V eh o numero de vertices e E o numero de 7
                                                                                  8 //Complexidade: O((V + E) \log V)
3 vector < vector < int >> adj; // liqa de adjacencia
                                                                                  9 void dijkstra(int s) {
4 int n, s; // n = numero de vertices, s = vertice inicial
                                                                                        priority_queue < pair < int , int > , vector < pair < int , int > > , greater < pair <</pre>
6 vector < bool > used(n);
                                                                                        int, int>>> q;
7 vector < int > d(n), p(n);
                                                                                        q.push({0, s});
                                                                                 12
                                                                                        while (!q.empty()) {
9 void bfs(int s) {
                                                                                            int v = q.top().second;
      queue < int > q;
                                                                                 15
                                                                                            q.pop();
                                                                                            if (used[v]) continue;
      q.push(s);
                                                                                 16
12
      used[s] = true;
                                                                                 17
                                                                                            used[v] = true;
      d[s] = 0;
                                                                                            for (auto edge : adj[v]) {
13
                                                                                 18
      p[s] = -1;
                                                                                                 int to = edge.first, len = edge.second;
14
                                                                                 19
                                                                                                 if (d[v] + len < d[to]) {</pre>
      while (!q.empty()) {
                                                                                                     d[to] = d[v] + len;
16
          int v = q.front();
                                                                                                     p[to] = v;
17
                                                                                 22
           q.pop();
                                                                                                     q.push({d[to], to});
18
                                                                                 23
           for (int u : adj[v]) {
                                                                                                }
```

12

19

10

15

20

21

if (!used[u]) {

used[u] = true;

25

26

}

}

```
9
                                                                                     while (!st.empty()) {
29 //Complexidade: O(V)
                                                                                          int curr = st.top();
                                                                               11
30 vector<int> restorePath(int v) {
                                                                                          st.pop();
                                                                               12
      vector < int > path;
                                                                                          if (visited[curr]==1)continue;
31
      for (int u = v; u != -1; u = p[u])
                                                                                          visited[curr]=1:
           path.push_back(u);
                                                                                          // process current node here
33
      reverse(path.begin(), path.end());
34
                                                                               16
      return path;
                                                                                          for (auto i : adj[curr]) {
36 }
                                                                                              st.push(i);
                                                                               18
                                                                               19
       Kruskal
                                                                                     }
                                                                               21
1 //vector<pair<int,int>> arestas[MAXN] em que cada aresta[i] contem o peso
      e o vertice adiacente
                                                                                      Outros
2 //vector < peso, conexao >
3 vector < pair < int , int >> adj[MAXN];
4 vector<pair<int,int>> adjtree[MAXN];
                                                                                      Binarysearch
5 vector < pair < int , pair < int , int >>> kruskadj;
6 int cost:
                                                                               int BinarySearch(<vector>int arr, int x){
7 void kruskal(){
                                                                                     int k = 0:
      for(int i = 1; i < MAXN; i++) {</pre>
                                                                                     int n = arr.size();
          for(auto j:adj[i]){
               kruskadj.push_back({j.first,{i,j.second}});
10
                                                                                     for (int b = n/2: b >= 1: b /= 2) {
          }
11
                                                                                          while (k+b < n \&\& arr[k+b] <= x) k += b;
12
      sort(kruskadj.begin(),kruskadj.end());
13
                                                                                     if (arr[k] == x) {
     cost=0:
                                                                                          return k;
      int r = kruskadj.size();
15
                                                                               10
      vector < int > id(r);
                                                                               11 }
      for (int i = 0; i < r; i++) id[i] = i;
      for (auto p : kruskadj){
18
                                                                                       Hoursconvert
          int x = p.second.first;
19
          int y = p.second.second;
20
                                                                               int cts(int h, int m, int s) {
21
          int w = p.first;
                                                                                     int total = (h * 3600) + (m * 60) + s;
          if (id[x] != id[y]){
                                                                                     return total;
              cost += w;
23
                                                                               4 }
24
              adjtree[x].push_back({w,y});
              int old_id = id[x], new_id = id[y];
                                                                               6 tuple < int, int, int > cth(int total_seconds) {
              for (int i = 0; i < r; i++)
                                                                                     int h = total_seconds / 3600;
                   if (id[i] == old_id) id[i] = new_id;
27
                                                                                     int m = (total_seconds % 3600) / 60;
                                                                                     int s = total_seconds % 60;
      }
29
                                                                                     return make_tuple(h, m, s);
                                                                                      Maxsubarraysum
  4.4 Dfs
                                                                               int maxSubarraySum(vector<int> x){
vector < int > adj[MAXN];
                                                                                     int best = 0, sum = 0;
3 int visited[MAXN];
                                                                                     for (int k = 0; k < n; k++) {
                                                                                          sum = max(x[k], sum+x[k]);
5 void dfs(int p) {
                                                                                          best = max(best,sum);
                                                                               6
      memset(visited, 0, sizeof visited);
      stack<int> st;
                                                                                     return best;
      st.push(p);
                                                                               9 }
```

## 5.4 Fibonacci

```
1 int fib(int n){
2     if(n <= 1){
3         return n;
4     }
5     return fib(n - 1) + fib(n - 2);
6 }</pre>
```

# 5.5 Binaryconvert

```
string decimal_to_binary(int dec) {
string binary = "";
while (dec > 0) {
   int bit = dec % 2;
   binary = to_string(bit) + binary;
```

```
dec /= 2;
      return binary;
9 }
10
int binary_to_decimal(string binary) {
      int dec = 0;
13
      int power = 0;
      for (int i = binary.length() - 1; i >= 0; i--) {
          int bit = binary[i] - '0';
15
          dec += bit * pow(2, power);
16
          power++;
      }
18
      return dec;
20 }
```