Lista 3 de CM300

1. Calcule as soluções das equaçõs abaixo.

(a)
$$3x + 1 = 5$$

(b)
$$\frac{2x+2}{3} = x+1$$

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$$\frac{2x+2}{3} = x+1$$
 (c) $3x + \frac{1}{3} = 4x - 2$

(d)
$$-2x + 1 = 2x - 1$$

(e)
$$2x - 1 = 2x - 1$$

(e)
$$2x - 1 = 2x - 1$$
 (f) $2(3x - 1) = 4x - 1$

(g)
$$-3x + 1 = 2x$$

(h)
$$\frac{2x}{3} + 1 = \frac{3}{2}$$

(h)
$$\frac{2x}{3} + 1 = \frac{3}{2}$$
 (i) $\frac{3x - 4}{5} = 4x - \frac{1}{5}$

$$(j) \frac{-3x+2}{4} = -\frac{x}{4} + 2$$

2. Encontre o conjunto solução das inequações abaixo.

(a)
$$2x + 2 \le -5$$

(b)
$$-3x - 1 > 1$$

(c)
$$2(3x-1) < \frac{3x}{2}$$

$$(d) \frac{2x-1}{-2} \ge 2x$$

(e)
$$-\frac{x}{2} - \frac{1}{3} > 2x + \frac{1}{4}$$

(d)
$$\frac{2x-1}{-2} \ge 2x$$
 (e) $-\frac{x}{2} - \frac{1}{3} > 2x + \frac{1}{4}$ (f) $\frac{2x-3}{4} < 3(x-1)$

(g)
$$\frac{x-1}{3} > 0$$

(h)
$$\frac{4x-2}{3} \ge 4x - \frac{2}{3}$$

(g)
$$\frac{x-1}{3} > 0$$
 (h) $\frac{4x-2}{3} \ge 4x - \frac{2}{3}$ (i) $2(-2x+1) \le \frac{1}{2}\left(x + \frac{1}{2}\right)$

3. Encontre as soluções das equações abaixo.

(a)
$$x^2 = x + 6$$

(b)
$$2x^2 + 3x + 4 = 0$$

(c)
$$\frac{x^2}{2} + 4x + 8 = 0$$

(d)
$$x^2 + 4x + 3 = -x(x+1)$$
 (e) $2x(-x+1) = \frac{1}{2}$

(e)
$$2x(-x+1) = \frac{1}{2}$$

$$(f) 5x^2 = -4x$$

(g)
$$-x^2 + 7x + 10 = -2x^2 + x + 1$$

(h)
$$4x^2 - 8x - 1 = 0$$

(i)
$$-x^2 + 8x = 20$$

(j)
$$x^2 - \frac{3}{4} = 0$$

(k)
$$\frac{x^2}{2} - \frac{x}{8} = 0$$

$$(1) -x^2 + 10x - 21 = 0$$

(m)
$$x^2 + 4x + 1 = 0$$

(n)
$$-4x^2 + 4x + 19 = 0$$

(o)
$$\frac{7}{2}x^2 + \sqrt{2}x - 1 = 0$$

4. Encontre o conjunto solução das inequações abaixo.

(a)
$$x^2 - 2x - 3 \le 0$$

(b)
$$x^2 + 9x + 18 > 0$$

(c)
$$2x^2 + x \ge 0$$

(d)
$$x^2 + 3 < 0$$

(e)
$$-2x^2 + 2 > 2x^2 + 8x + 4$$

(f)
$$-x^2 + 5 < 0$$

(g)
$$x^2 - 6 > -x(x+1)$$

(h)
$$x^2 - 8x > 16$$

(i)
$$x^2 - 2x + 1 \ge 2x - 1$$

(j)
$$x(x+1) \le \frac{1}{2}$$

(k)
$$2x(5x+3) < 2x^2 - 1$$

(1)
$$3x + 1 \ge 4x^2 + 10x + 1$$

(m)
$$(x+1)^2 + 3 > 0$$

(n)
$$x(2x+1) + \frac{9}{4} \le x(x-2)$$

(o)
$$-x^2 + x \ge -4x^2 + 2x$$

(p)
$$3x(x+1) < 2x^2 + 7x - 5$$

(q)
$$3x^2 + 2x - \frac{1}{2} < -3x^2 + 3x + \frac{1}{2}$$
 (r) $25x^2 + 10x + 1 > 0$

(r)
$$25x^2 + 10x + 1 > 0$$

Respostas:

1. (a)
$$x = \frac{4}{3}$$

(d)
$$x = \frac{1}{2}$$

(g)
$$x = \frac{1}{5}$$

(i)
$$x = -\frac{3}{17}$$

(b)
$$x = -1$$

(e)
$$x \in \mathbb{R}$$

(j)
$$x = -3$$

(c)
$$x = \frac{7}{3}$$

(f)
$$x = \frac{1}{2}$$

(h)
$$x = \frac{3}{4}$$

2. (a)
$$x \le -\frac{7}{2}$$

(c)
$$x < \frac{4}{9}$$

(e)
$$x < -\frac{7}{30}$$

$$\begin{array}{l} \text{(g) } x > 1 \\ \text{(h) } x \le 0 \end{array}$$

(b)
$$x < -\frac{2}{3}$$

(d)
$$x \le \frac{1}{6}$$

(f)
$$x > \frac{9}{10}$$

(i)
$$x \ge \frac{7}{18}$$

3. (a)
$$x = 3$$
 ou $x = -2$

(b) Não existe solução real.

(c)
$$x = -4$$

(d)
$$x = -1$$
 ou $x = -\frac{3}{2}$

(e)
$$x = \frac{1}{2}$$

4. (a)
$$-1 \le x \le 3$$

(b)
$$x < -6$$
 ou $x > -3$

(c)
$$x \le -\frac{1}{2}$$
 ou $x \ge 0$

(d) Não existe solução real.

(e)
$$x < -1 - \frac{\sqrt{2}}{2}$$
 ou $x < -1 + \frac{\sqrt{2}}{2}$ (k) $-\frac{1}{2} < x < -\frac{1}{4}$

(f)
$$x < -\sqrt{5}$$
 ou $x > \sqrt{5}$

(f)
$$x = -\frac{4}{5}$$
 ou $x = 0$

(g)
$$x = -3$$

(h)
$$x=1+\frac{\sqrt{5}}{2}$$
 ou $x=1-\frac{\sqrt{5}}{2}$

(i) Não existe solução real.

(j)
$$x = -\frac{\sqrt{3}}{4}$$
 ou $x = \frac{\sqrt{3}}{4}$

(g)
$$x < -2$$
 ou $x > \frac{3}{2}$

(h)
$$x \in IR$$

(i)
$$x \le 2 - \sqrt{2}$$
 ou $x \ge 2 + \sqrt{2}$

(j)
$$-\frac{1}{2} - \frac{\sqrt{3}}{2} \le x \le -\frac{1}{2} + \frac{\sqrt{3}}{2}$$

(k)
$$-\frac{1}{2} < x < -\frac{1}{4}$$

$$(1) -\frac{7}{4} \le x \le 0$$

(k)
$$x = 0$$
 ou $x = \frac{1}{4}$

(1)
$$x = 3$$
 ou $x = 7$

(m)
$$x = -2 - \sqrt{3}$$
 ou $x = -2 + \sqrt{3}$

(n)
$$x = \frac{1}{2} - \sqrt{5}$$
 ou $x = \frac{1}{2} + \sqrt{5}$

(o)
$$x = -\frac{\sqrt{2}}{7} - \frac{4}{7}$$
 ou $x = -\frac{\sqrt{2}}{7} + \frac{4}{7}$

(m)
$$x \in \mathbb{R}$$

(n)
$$x = -\frac{3}{2}$$

(o)
$$x \le 0$$
 ou $x \ge \frac{1}{3}$

(p) Não existe solução real.

(q)
$$-\frac{1}{3} < x < \frac{1}{2}$$

(r)
$$x \neq -\frac{1}{5}$$