

Alloy cheat sheet

Propositional Logic:

\neg	negation	!, not
\wedge	conjunction	&&, and
\vee	disjunction	, or
\rightarrow	implication	=>, implies
\leftrightarrow	equivalence	<=>, iff

First Order Logic:

$(\forall x)P[x]$	universal quantifier	all x : X P
$(\exists x)P[x]$	existential quantifier	some x : X P
$(\exists!x)P[x]$	uniqueness quantifier	one x : X P
$(\exists_0^1x)P[x]$	at most one quantifier	lone x : X P
$(\forall x)\neg P[x]$	at most zero quantifier	no x : X P

Set Theory:

$\emptyset, \{\}$	the empty set	none
$\{x \in X \mid P[x]\}$	comprehension	{x : X P}
$X \subseteq Y$	set inclusion	X in Y
$x \in X$	element, singleton subset	x : one X
$x \in \wp(X)$	subset inclusion	x : set X
$x \in \wp(X), x \neq 0$	inclusion, nonempty subset	x : some X
$x \in \wp(X), x \leq 1$	empty or singleton subset	x : lone X
$X \times Y$	cartesian product	X -> Y
$X \cup Y$	sets union	X + Y
$X \cap Y$	sets intersection	X & Y
$X \setminus Y$	sets difference	X - Y
dom, U	entire domain set	univ

Relational Algebra:

id, I	identity relation	iden
$R \subseteq A \times B$	binary relation	R : A -> B
$R \bowtie S$	relational join	R.S, S[R]
R^{-1}	inverse/transpose relation	~R
R^+	transitive closure	^R
R^*	reflexive-transitive closure	*R
$S \triangleleft R$	domain restriction	S <: R
$R \triangleright S$	range restriction	R :> S
$R \oplus S$	relational override	R ++ S

Function Properties:

$f : A \nrightarrow B$	partial function	$f : A \rightarrow \text{none } B$
$f : A \rightarrow B$	total function	$f : A \rightarrow \text{one } B$
$f : A \nrightarrowtail B$	partial injection	$f : A \text{ none} \rightarrow \text{none } B$
$f : A \rightarrowtail B$	total injection	$f : A \text{ none} \rightarrow \text{one } B$
$f : A \twoheadrightarrow B$	partial surjection	$f : A \text{ some} \rightarrow \text{none } B$
$f : A \twoheadrightarrowtail B$	total surjection	$f : A \text{ some} \rightarrow \text{one } B$
$f : A \leftrightarrow B$	bijective function	$f : A \text{ one} \rightarrow \text{one } B$

Cardinality & Arithmetic:

$\#X, X $	set cardinality	$\#X$
$1, 2, 3, \dots$	integer literals	$1, 2, 3, \dots$
$x + y$	integer addition	$x + y, \text{ add}[x, y]$
$x - y$	integer subtraction	$x - y, \text{ sub}[x, y]$
$x \geq y, x \leq y$	integer comparisons	$x \geq y, x \leq y$
$x > y, x < y$	strict comparisons	$x > y, x < y$
more arithmetic functionality with open util/integer:		
$x' = x + 1$	successor function	$\text{next}[x]$
$x \cdot y$	integer multiplication	$\text{mul}[x, y]$
x / y	integer division	$\text{div}[x, y]$
$x \bmod y$	remainder division	$\text{rem}[x, y]$

Sequences & Lists:

$s = \langle a_0 a_1 \dots a_n \rangle$	ordered sequence	$\text{seq } s$
$s \frown t$	concatenation	$s.\text{append}[t]$
$s_{(0)} = a_0$	head function	$s.\text{first}$
$s_{[1]} = \langle a_1 a_2 \dots a_n \rangle$	tail function	$s.\text{rest}$

more ordered sequences functionality with open util/sequence:

Alloy Language Expressions:

signature	$\text{sig } name \{ \}$
fields	$\text{sig } name \{ field : S \}$
abstract/instance	$\text{abstract sig } A \{ \}; \text{ sig } B, C \text{ extends } A \{ \}$
domain/subset	$\text{sig } A \{ \}; \text{ sig } S \text{ in } A \{ \}$
shortcuts	$\text{let } n1 = s1.\text{field1}, n2 = s2.\text{field2} \mid \{ n1 = n2 \}$
facts	$\text{fact } \{ \text{nop} : \text{human} \mid p \text{ in } p.\text{mother} \ \&\& \text{father} = \sim \text{child} \}$
predicates	$\text{pred contains}[b : \text{Book}, n : \text{Name}, d : \text{Addr}] \{ n \rightarrow d \text{ in } b.\text{addr} \}$
functions	$\text{fun lives_at}[b : \text{Book}, n : \text{Name}] : \text{set Addr} \{ b.\text{addr}[n] \}$
conditional	$\text{fun case}[n : \text{Int}] : \text{Int} \{ n > 0 \Rightarrow 1 \text{ else } 0 \}$
assertion check	$\text{assert nSelfF}\{ \text{no } m : \text{Man} \mid m = m.\text{father} \} \text{ check nSelfF for 4}$
consistency check	$\text{pred Test}[M : \text{machine}] \{ \text{doThis} \} \text{ run Test for 4 but 1 machine}$

Further information from: alloy.mit.edu