

# The Performance of **Jet** Reconstruction and Distinguishment among Multi-jet Events at CEPC



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On the behalf of the CEPC Collaboration

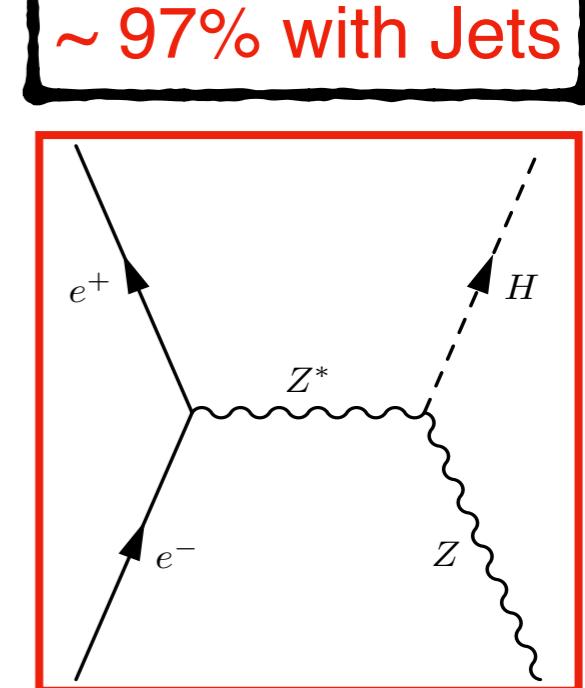
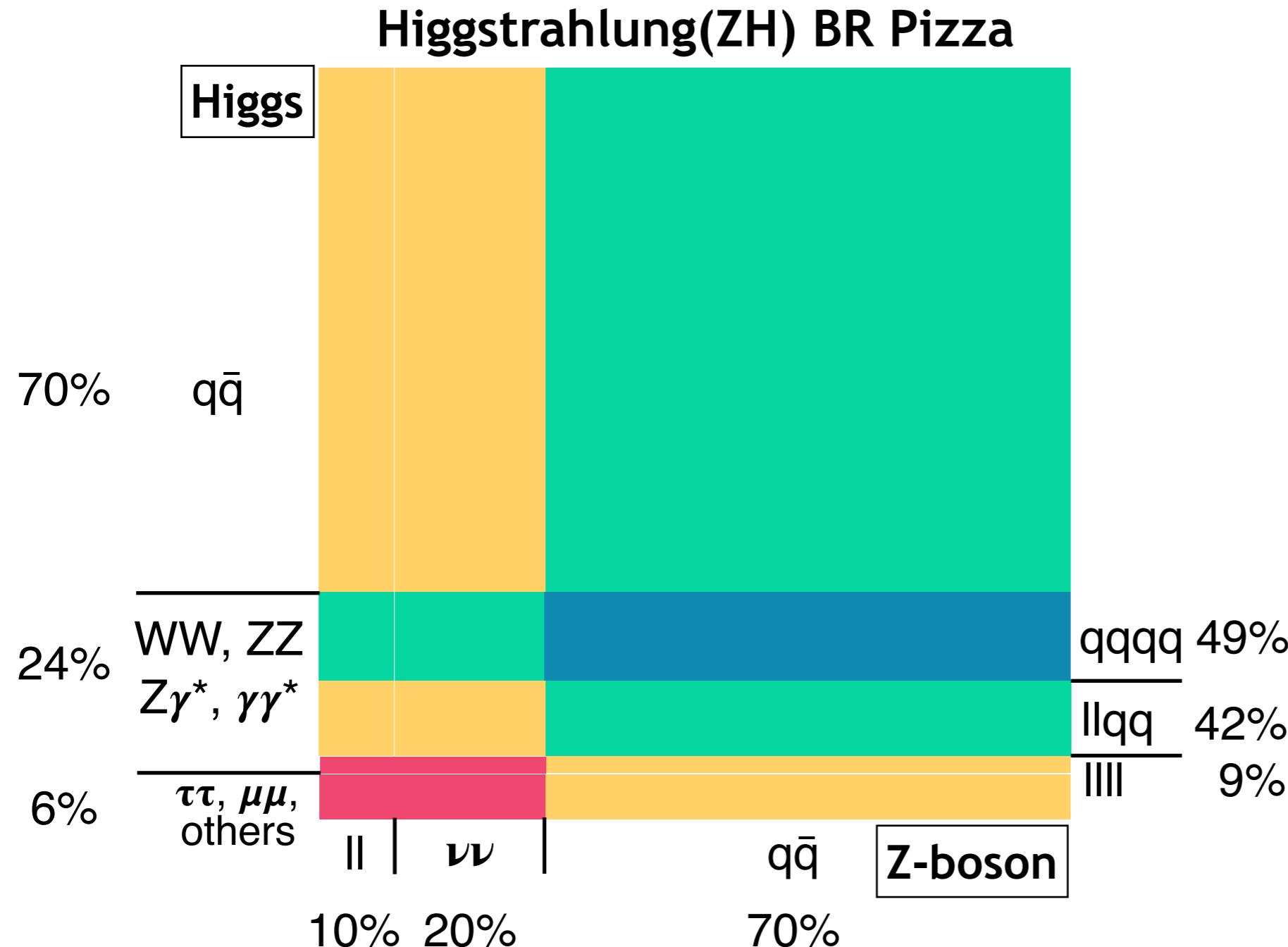
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Feb 05 - Feb 07, 2020



# Jets at the Higgs Signal



- Circular Electron Positron Collider (CEPC) is a future collider aims to precisely measure the properties of the Higgs boson.
- Up to **97%** of Higgstrahlung(ZH) final-states associates to jets.
- Jets are also critical for many EW precision measurements.



# of jets	Probability	1/3 of ZH events
0	2.44%	<ul style="list-style-type: none"><li>• Major SM Higgs decay modes.</li><li>• 1 color singlet could be identified. (Single Z or Higgs boson)</li></ul>
2	29.73%	
4	59.58%	<b>2/3 of ZH events</b> <ul style="list-style-type: none"><li>• Dominance statistic of <math>ZH \rightarrow q\bar{q}q\bar{q}</math>.</li><li>• Major uncertainty is on wrong jet pairing. (<b>Potential huge impact</b>)</li></ul>
6	8.23%	

- 67% (4 + 6 jets) needs **dedicated color-singlet identification**: grouping the hadronic final-state particles into color-singlets (Z, W, H,  $\gamma^*$ ). Can be done via jet clustering and pairing.
- **Jet clustering**, ee- $k_t$ , is also essential for **differential** Higgs & EW precision measurements (e.g. TGCs).



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BM1: MASSIVE bosons

invariant mass resolutions

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BM2: Jet energy and angular differential response



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BM3: # of jet identification &  
thrust based algorithm for 2-jet

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BM4: Separation of  $WW$ ,  $ZZ$ , and  $ZH$  decay to  $qqqq$  final state

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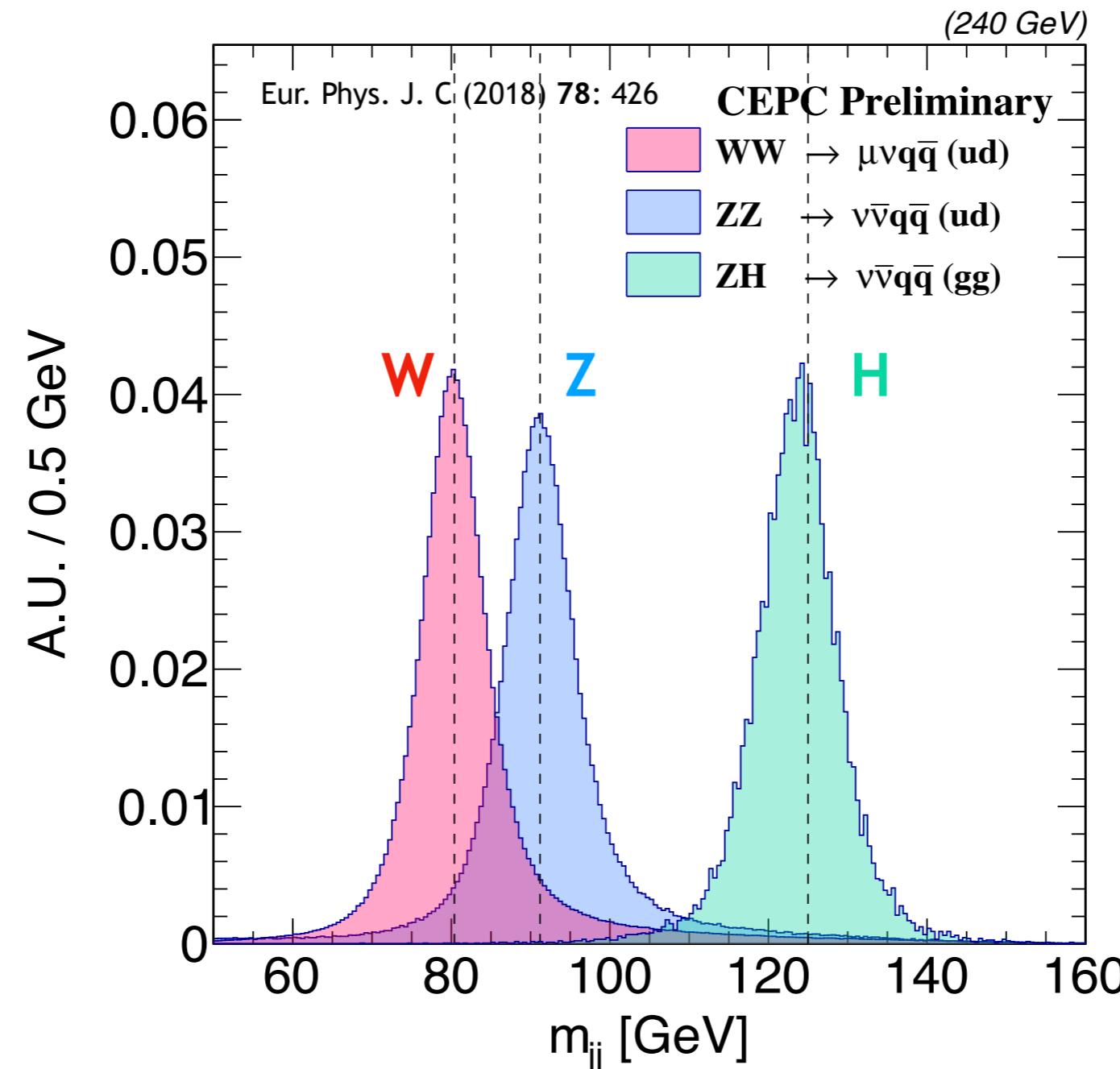
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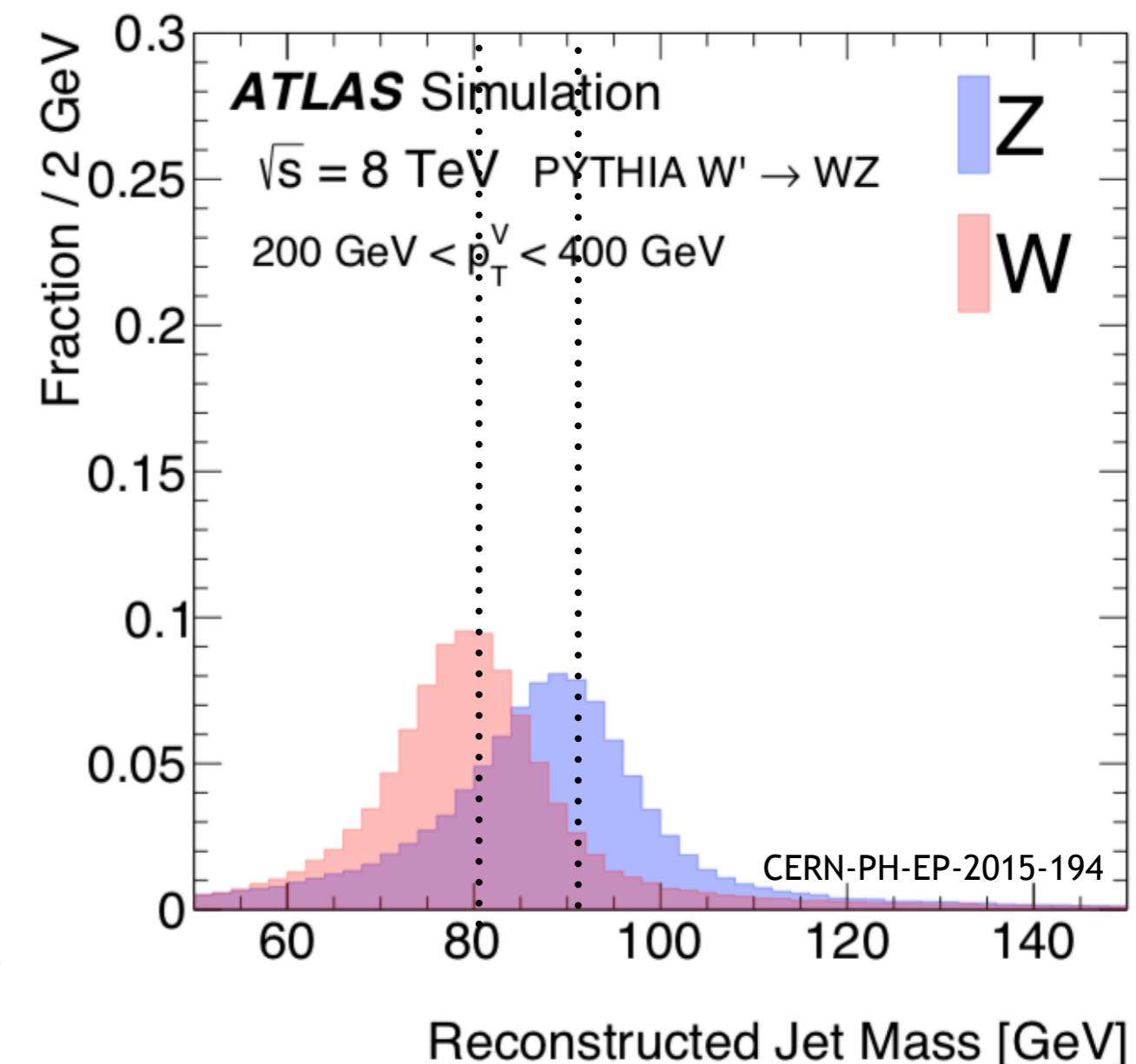
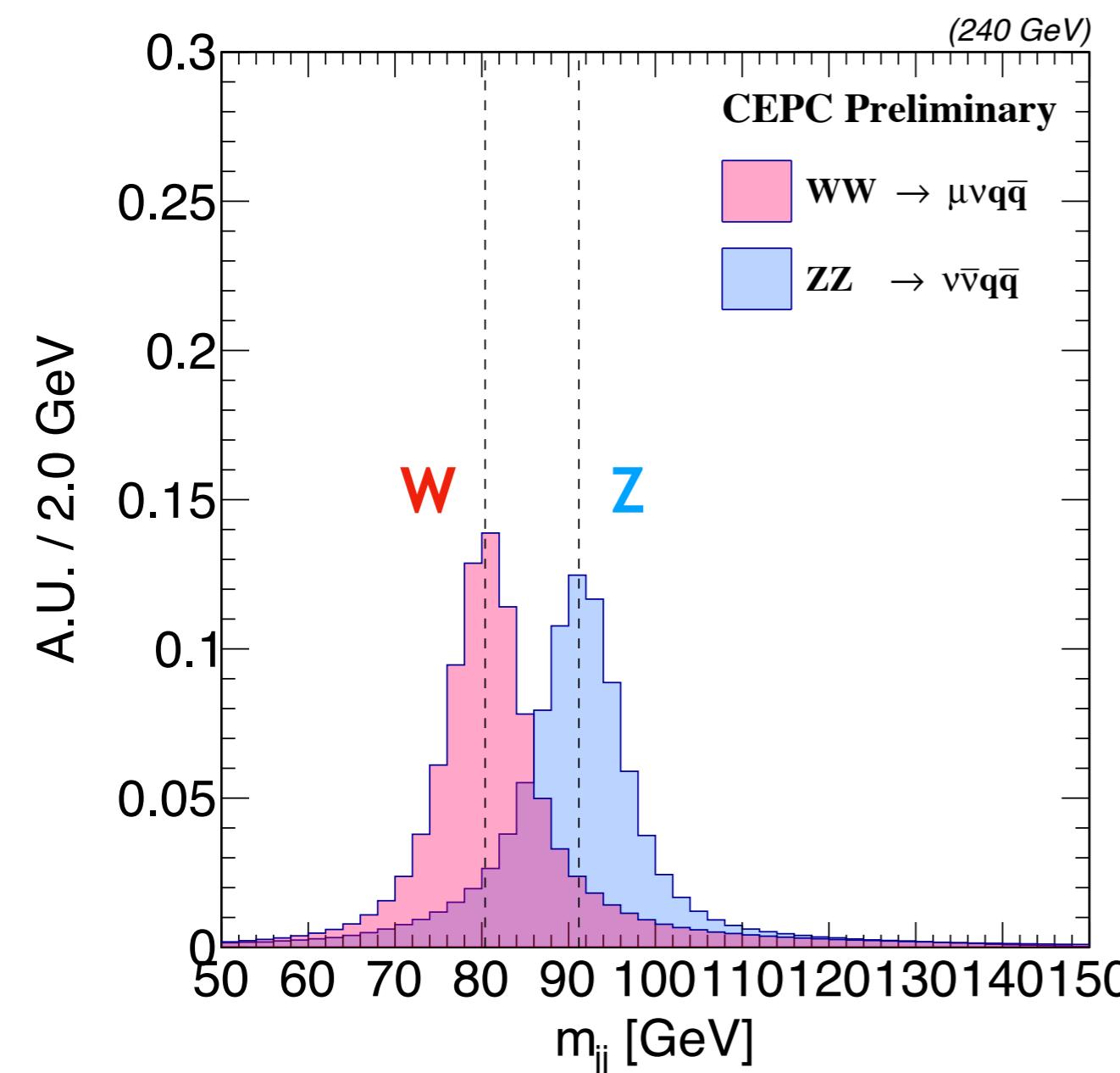
# BM1: Massive Boson Mass Resolution



- W-, Z-, and Higgs-boson masses in dijet final state can be well separated at CEPC.
- Z- and W-boson could be separated  $\approx 2\sigma$ , and the Higgs Boson Mass Resolution = 3.8% achieving the CEPC baseline.



# BM1: Massive Boson Mass Resolution



- The separation of Z- and W-boson at CEPC is much better than ATLAS as it should be, because of the better collision environment and detector response.



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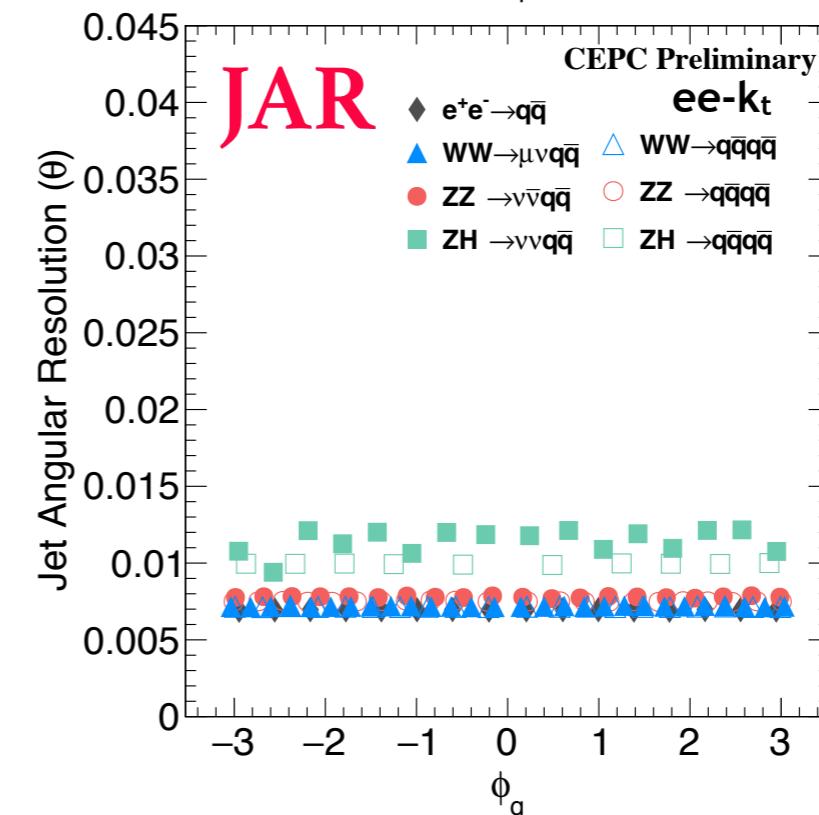
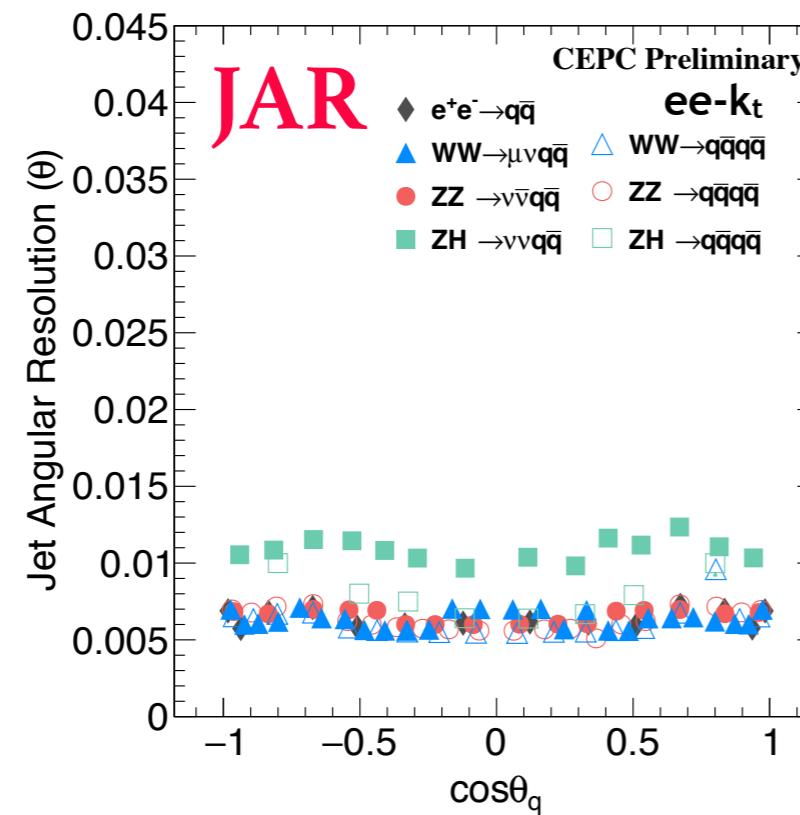
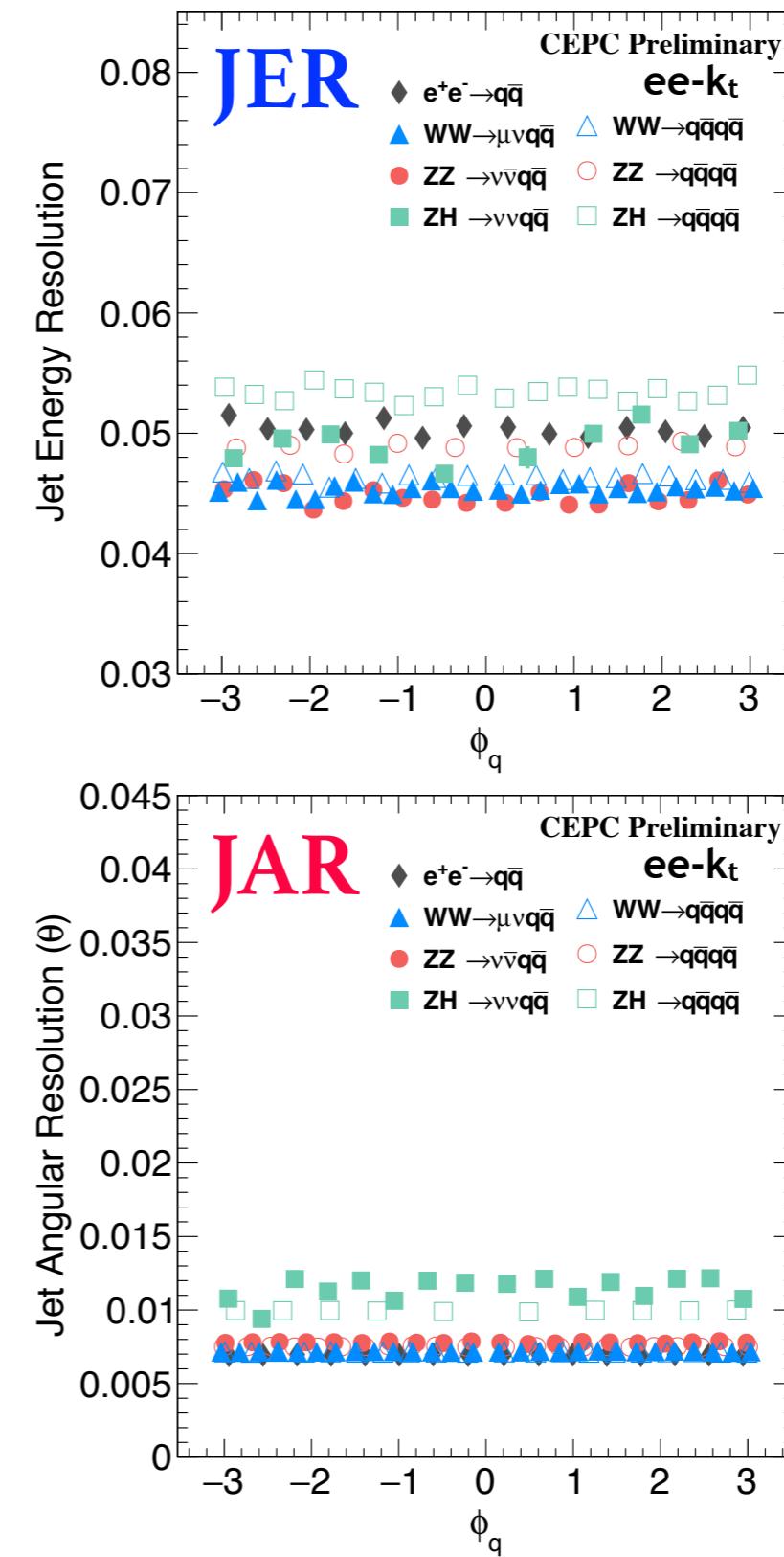
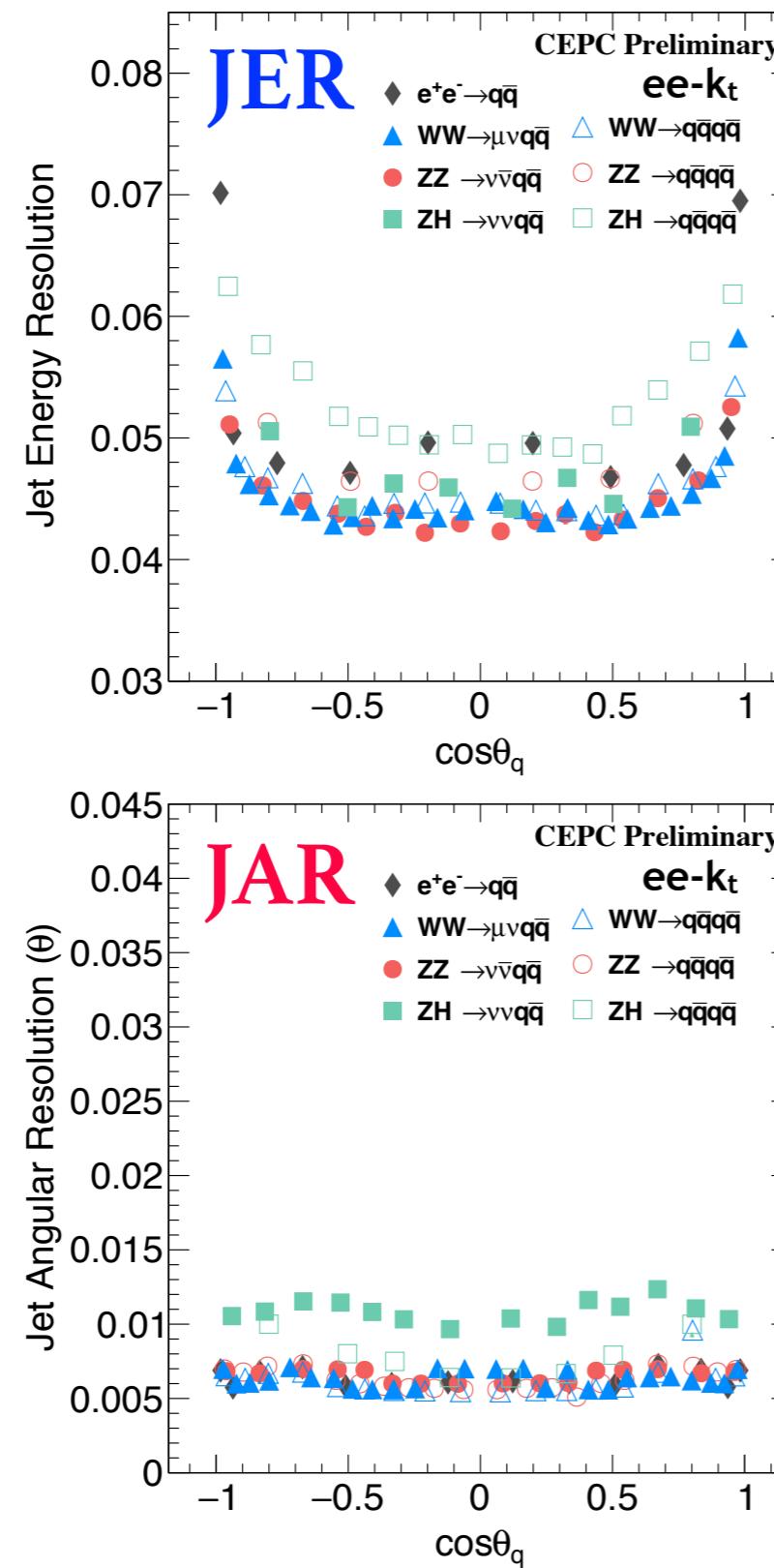
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BM2: Jet energy and angular differential response



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## BM3: JER &amp; JAR

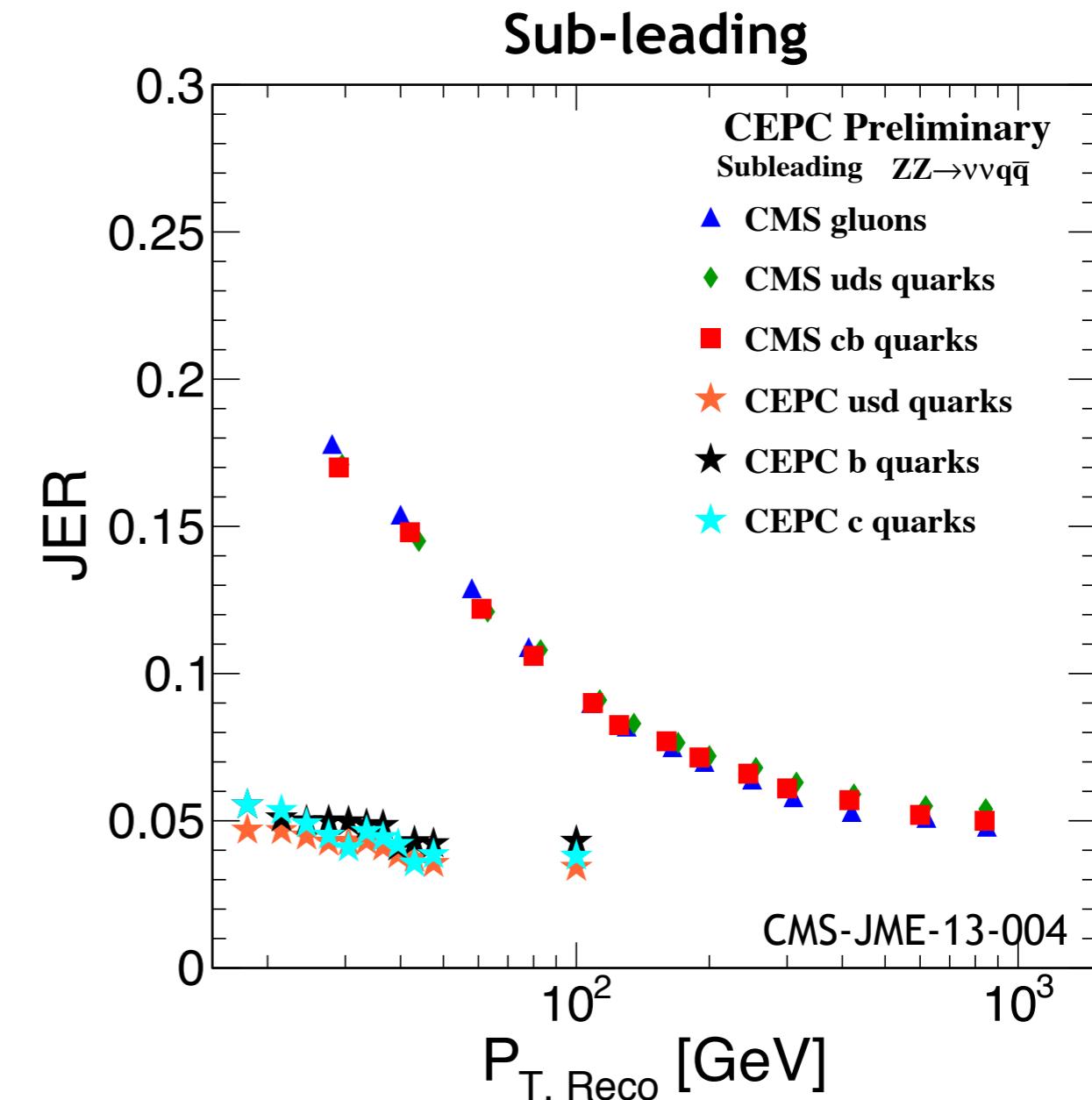
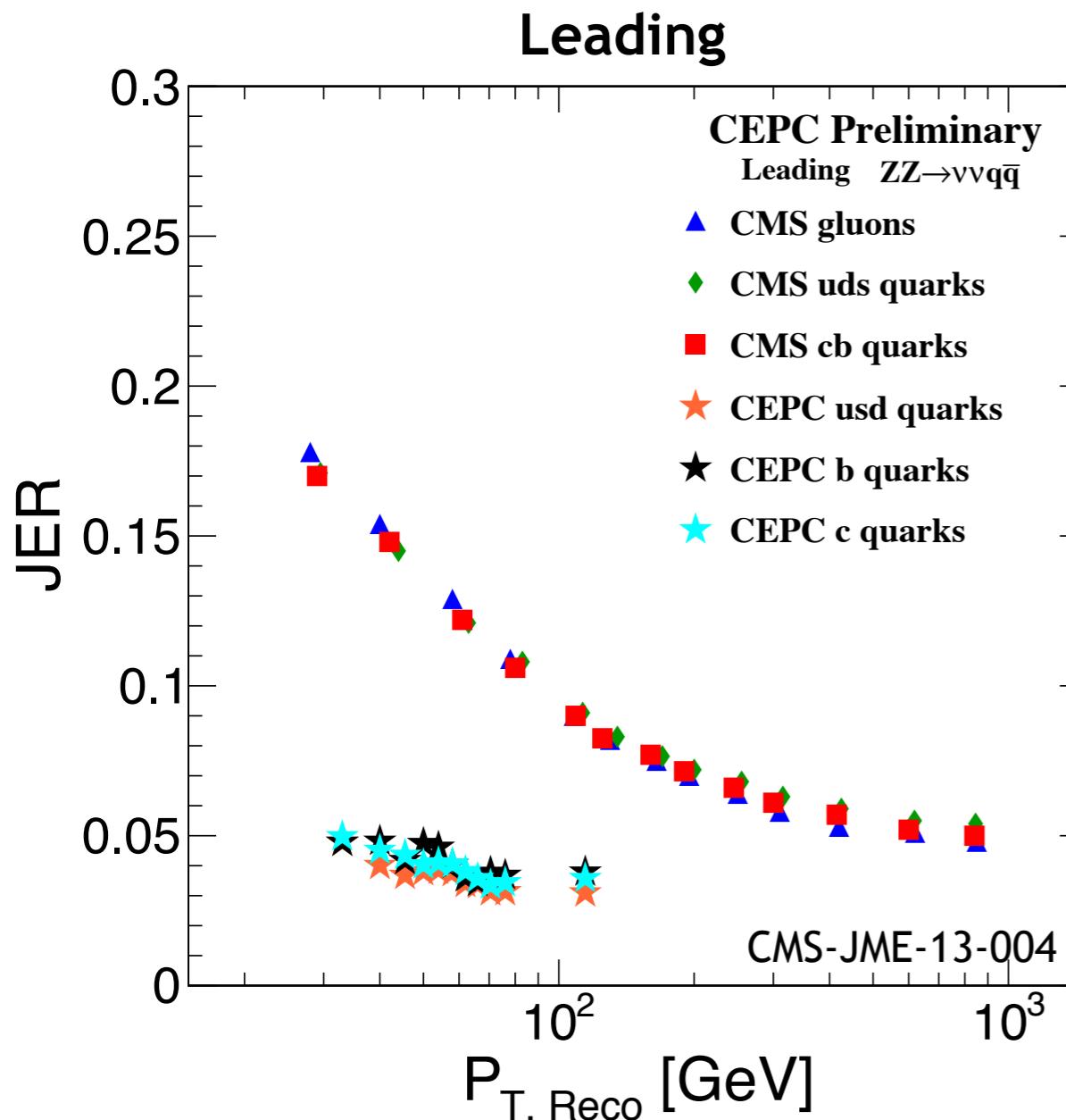


- JER is around 4.5%, and JAR is around 1% in barrel region;
- The difference between 2 and 4 jets final-state is controlled within 1% level.



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# Compare to CMS at LHC



- JER at CEPC is better than CMS as it should be; **2-4 times** better in the same energy regions.



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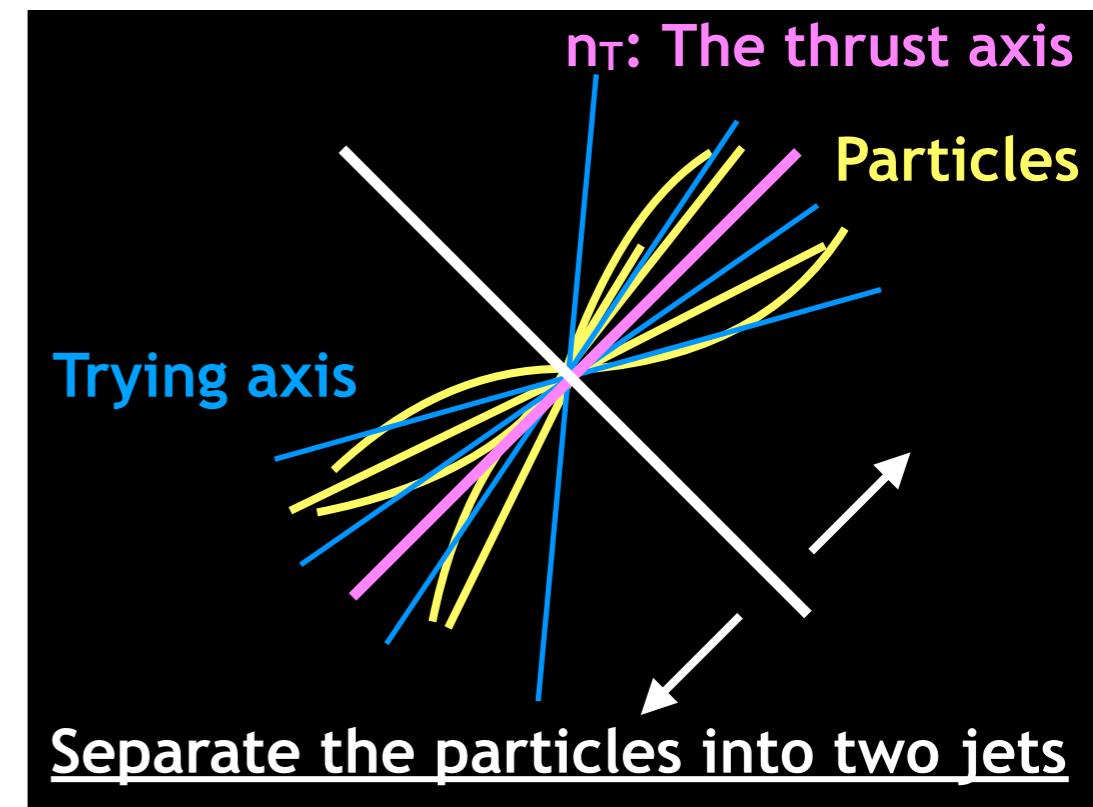


# BM3: Thrust Based Algorithm

$$T \equiv \max \frac{\sum_j^N |P_j \cdot n_T|}{\sum_i^N |P_i|}$$

$P_i$  or  $P_j$ : Momentum of each particle

$n_T$ : A unit vector ( $\sin\theta \times \cos\phi, \sin\theta \times \sin\phi, \cos\theta$ )

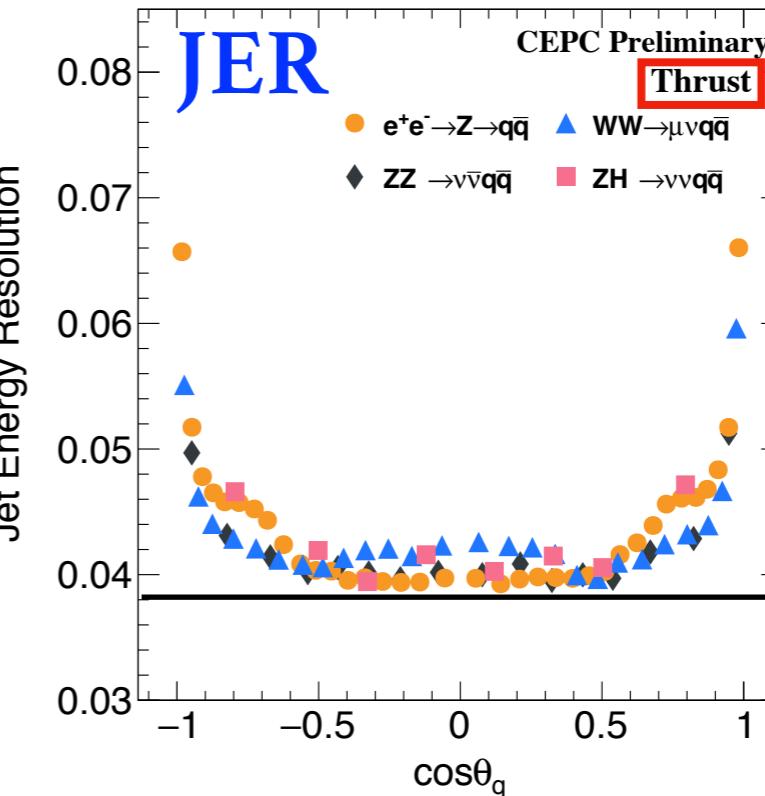
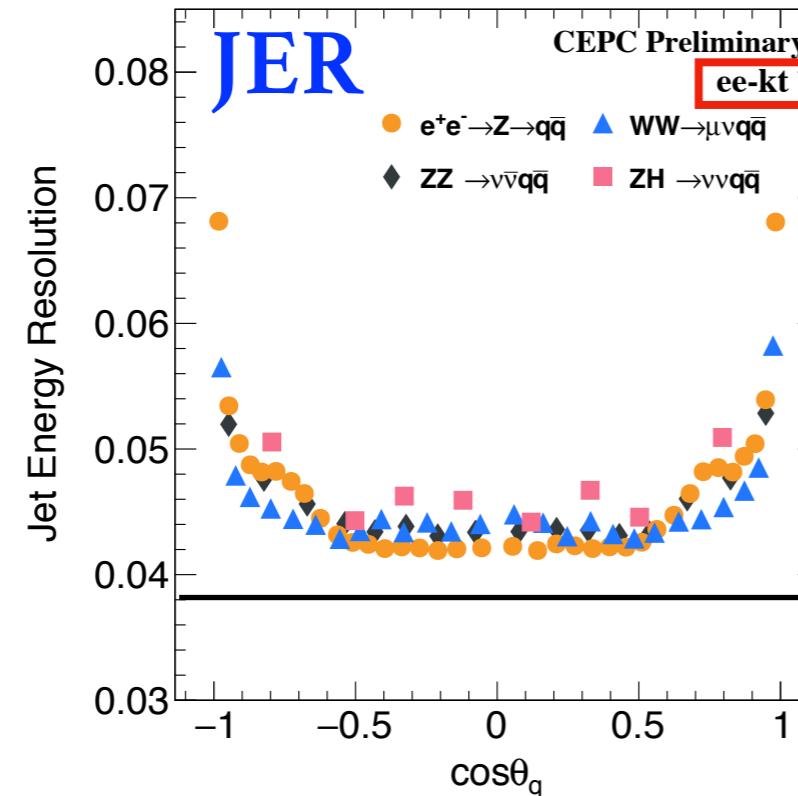


- “Thrust” is one kind of event-shape variables.
- The nature clustering idea for the **back-to-back di-jet topology**.
  1. Boost the system back to the rest frame.
  2. Find the thrust axis which has highest momentum efflux.
  3. Divide system into 2 hemispheres with the thrust axis, and each of them is identified as a jet.
- Applicable to all of **2-jet final-states** at CEPC.  
(2-jet final-states could be identified with **efficiency×purity = 88.4%.**)

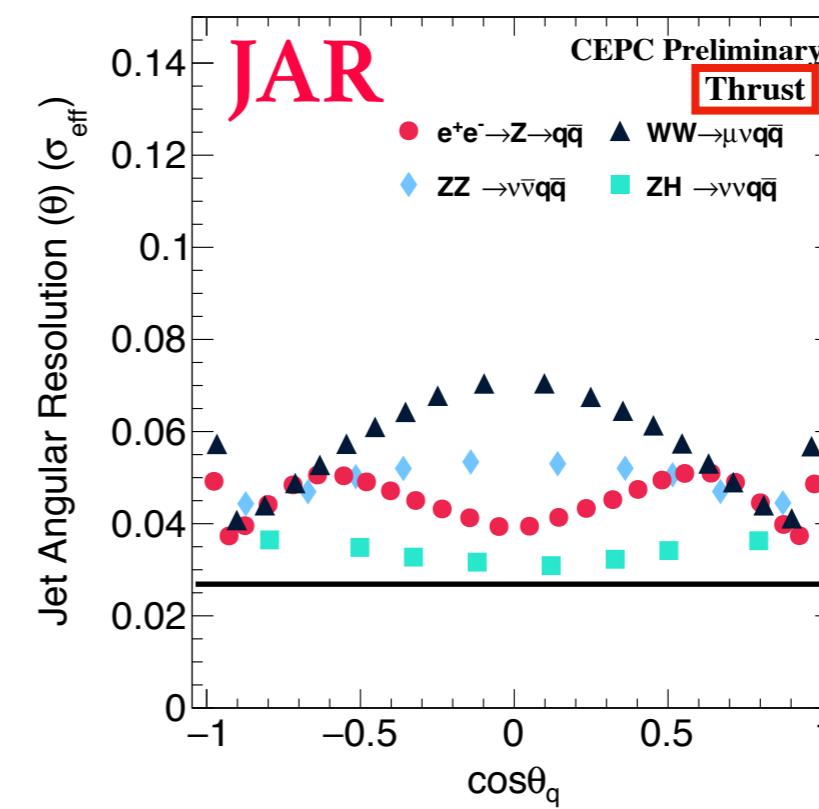
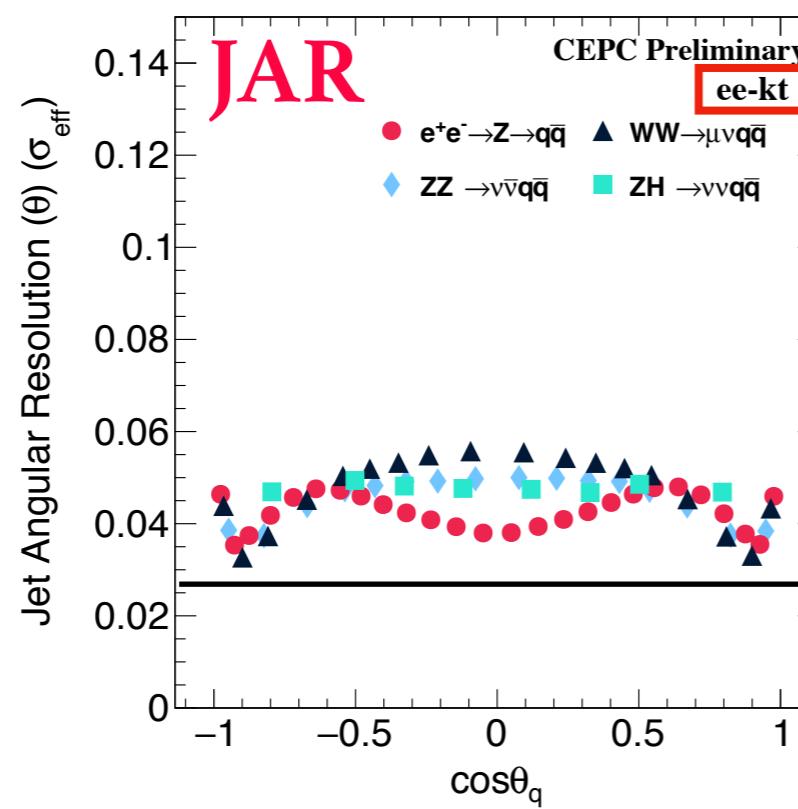


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# BM3: JER & JAR (ee- $k_t$ – Thrust)



JERs are improved 20% w.r.t ee- $k_t$



JARs are improved 20% w.r.t ee- $k_t$

- Improvement may come from boosting the system back to the rest frame.



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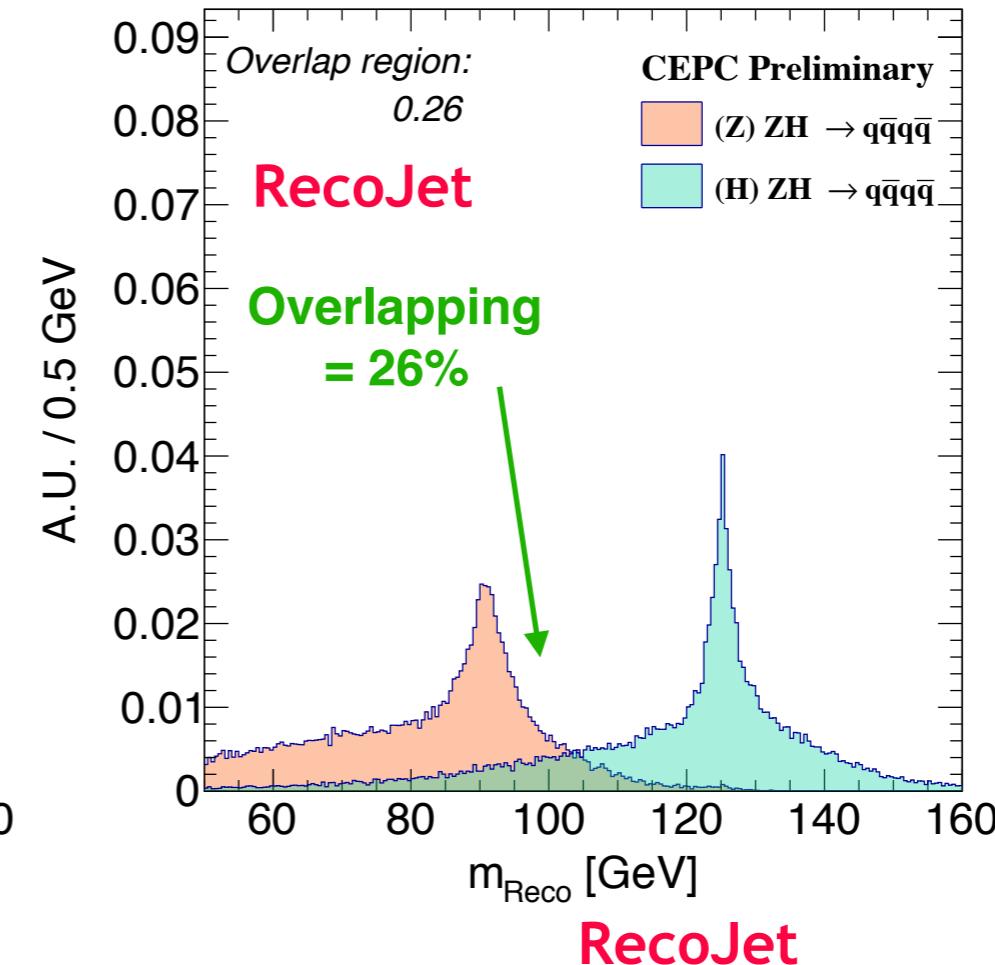
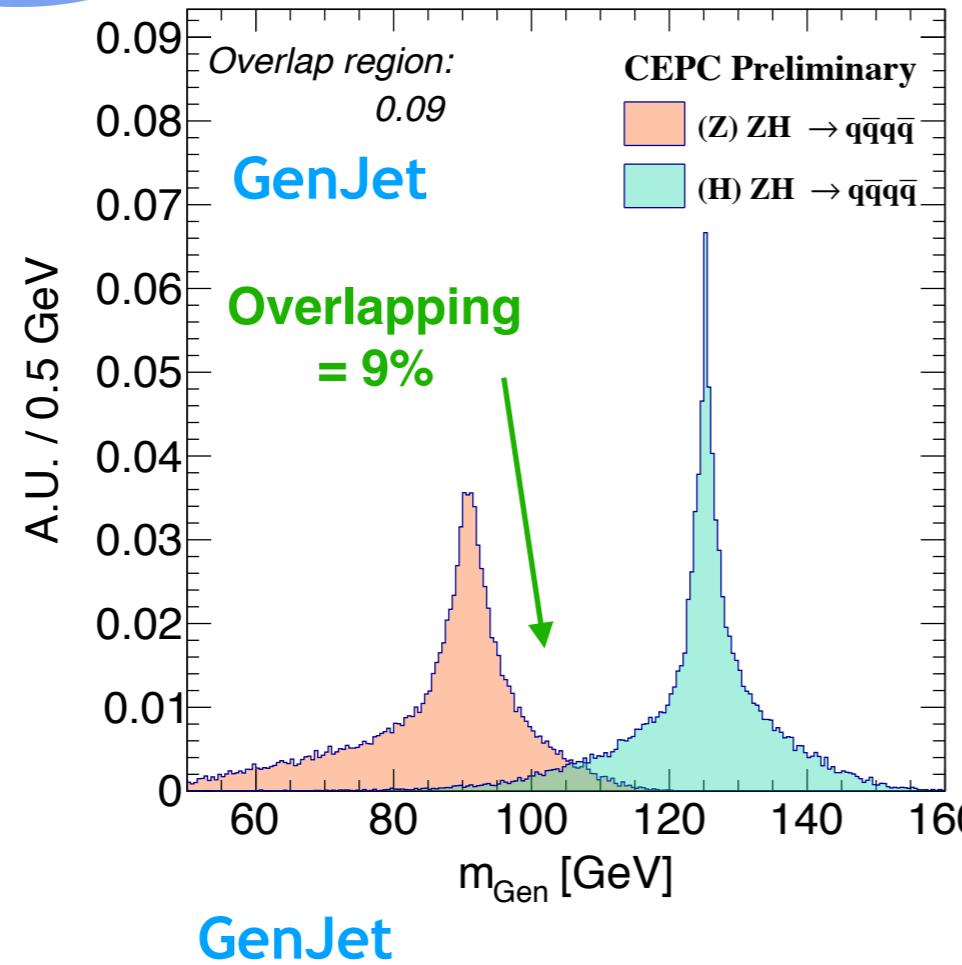
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# BM4: WW, ZZ, ZH to 4-jet Separation



Sample \ Assignment(%)	WW	ZZ	ZH
WW	63.24	18.95	17.81
ZZ	16.09	57.89	26.02
ZH	9.99	13.84	<b>76.17</b>

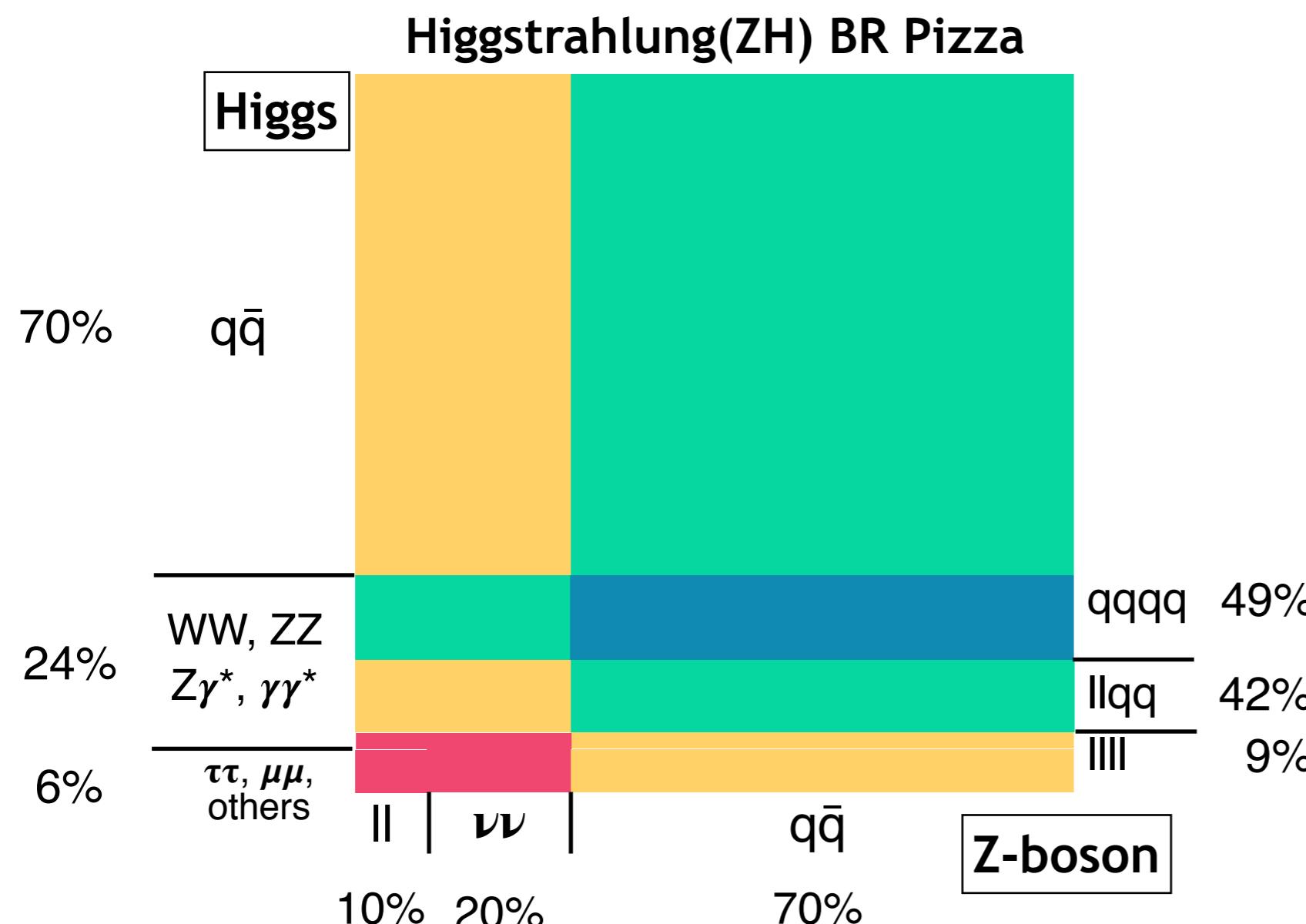
Sample \ Assignment(%)	WW	ZZ	ZH
WW	64.98	19.07	15.94
ZZ	26.51	50.54	22.96
ZH	20.29	22.93	<b>56.77</b>

- $\chi^2$  method is employed.
- The *Efficiency x Purity* of ZH identification is expected **18%** in the  $5 \text{ ab}^{-1}$  data.
- The statistical uncertainty of ZH to full hadronic final-state could achieve **0.25%** after considering the WW and ZZ as bkg.

$$\chi^2 = \frac{|(m_{ij} - m_{\text{boson}})|^2 + |(m_{ij} - m_{\text{boson}})|^2}{\sigma^2}$$

## ■ Jets are crucial for the CEPC Higgs physics

- 97% of ZH events involve jets
- 1/3 of ZH events only come from single Z or Higgs boson.
- 2/3 of ZH events have more than one boson (e.g.  $ZH \rightarrow q\bar{q}q\bar{q}$ ) - need color singlet identification algorithm.



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1/3      2/3

~ 97% with Jets



- I. **BMR < 4% is critical. Achieved at the CEPC baseline (3.8%)**
  - \* W, Z, Higgs boson can be efficiently separated at both semi-leptonic & full hadronic final-state.
  - \* Exploit Z-boson di-jet recoil mass to distinguish the ZH from ZZ process (main background).
- II. Jet energy resolution ~ 3-5% & Jet angular resolution ~ 1%.
- III. 2-jet final-states could be identified with *efficiency* $\times$ *purity* = 88.4%.
  - \* Clustering by dedicated the jet clustering algorithm, **thrust based algorithm**.
  - \* Thrust based algorithm is recommended for 2-jet final-states because it brings the JER and JAR **20%** improvement.
- IV. Need a better color-singlet identification algorithm for full hadronic final-state.
  - \* The statistical uncertainty of ZH to full hadronic final-state is expected to be **0.25%** currently when considering the WW and ZZ as background.

# Thank for your attention

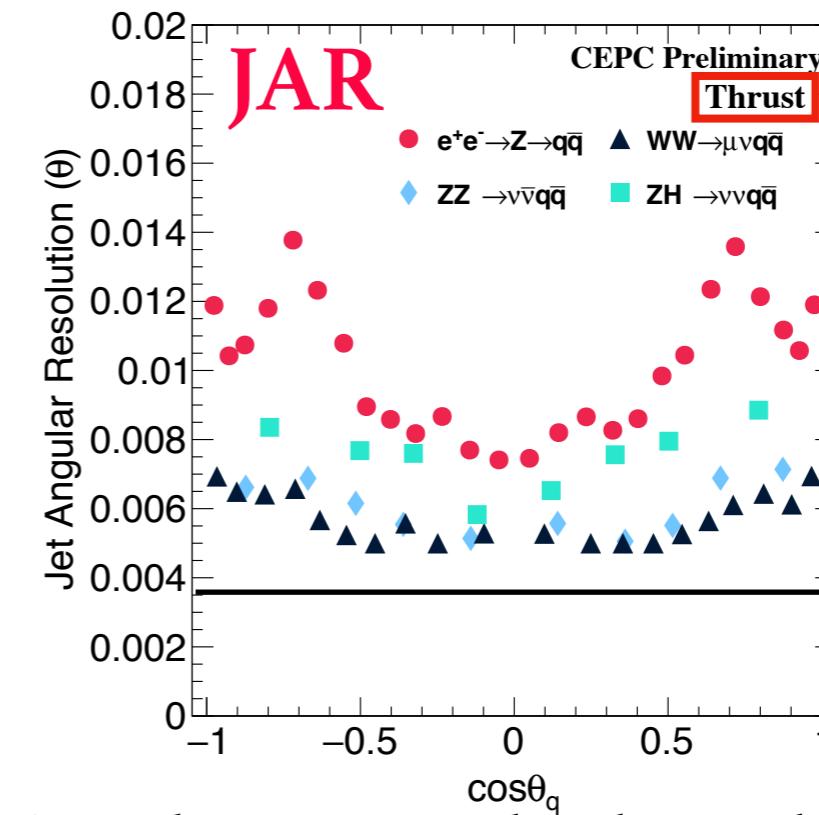
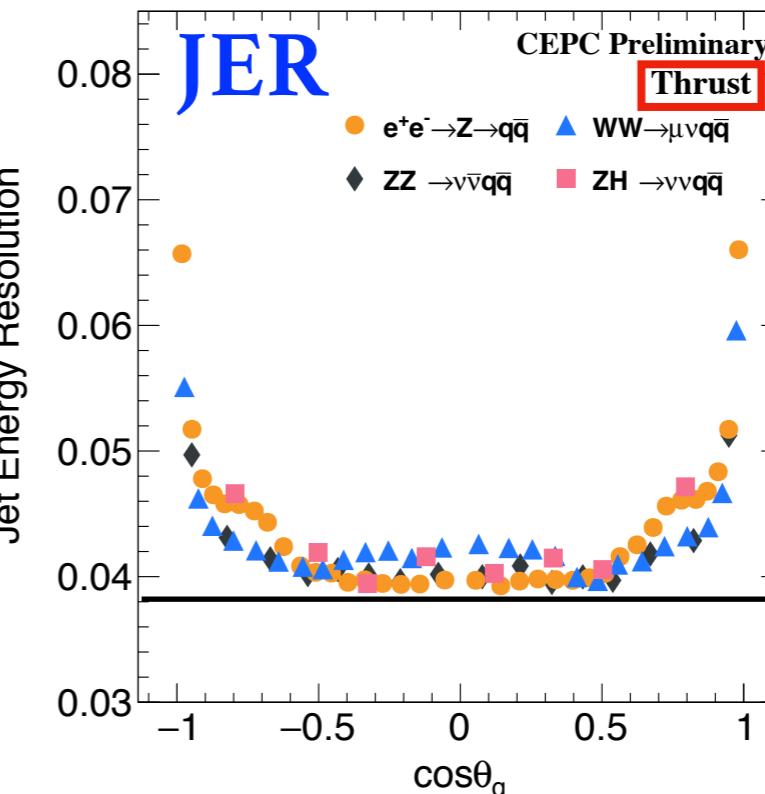
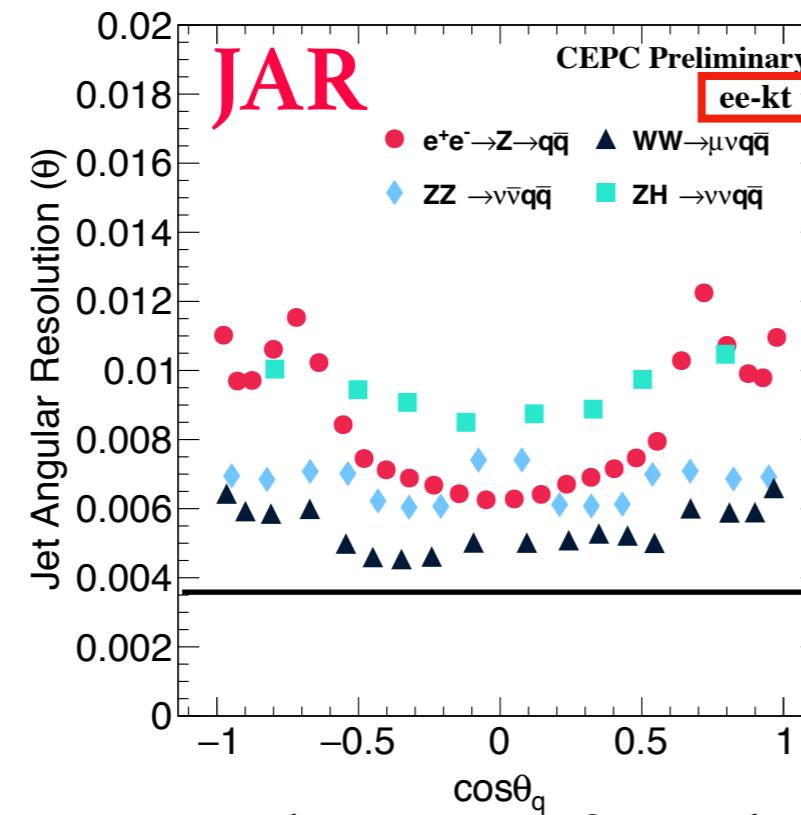
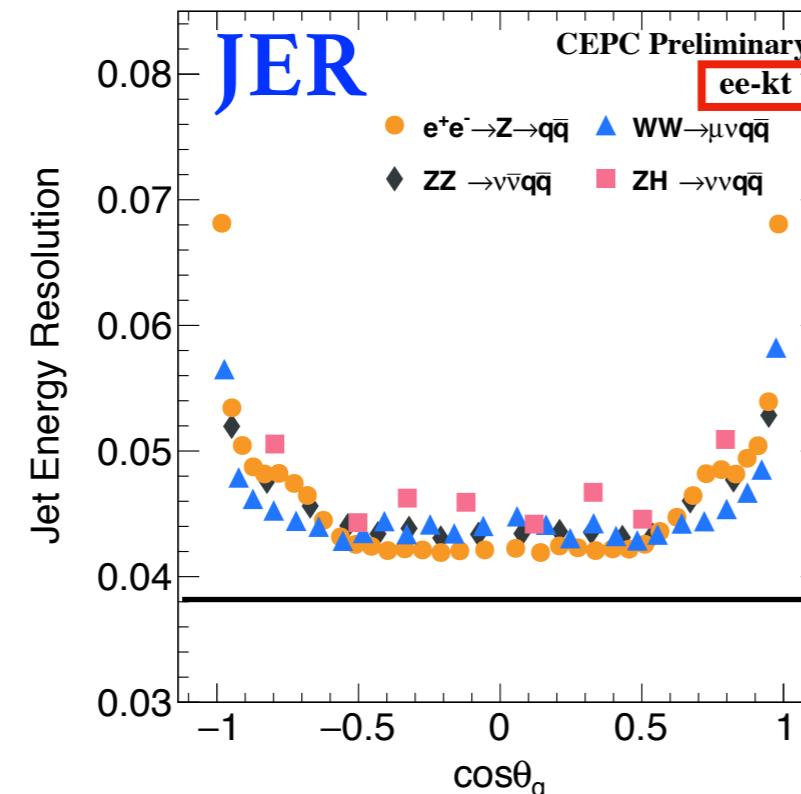


# Back up



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# BM3: JER & JAR (ee- $k_t$ – Thrust)



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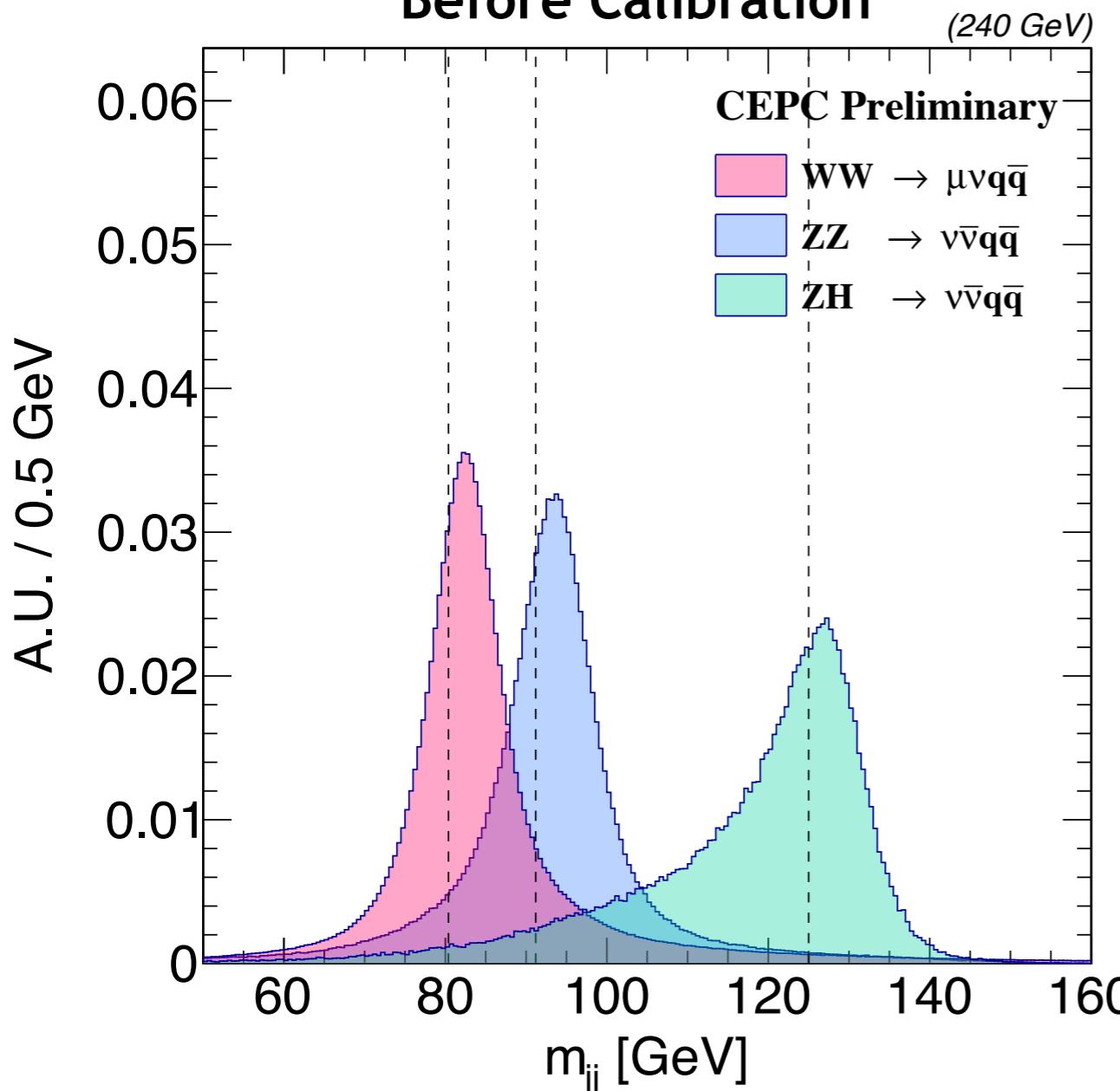
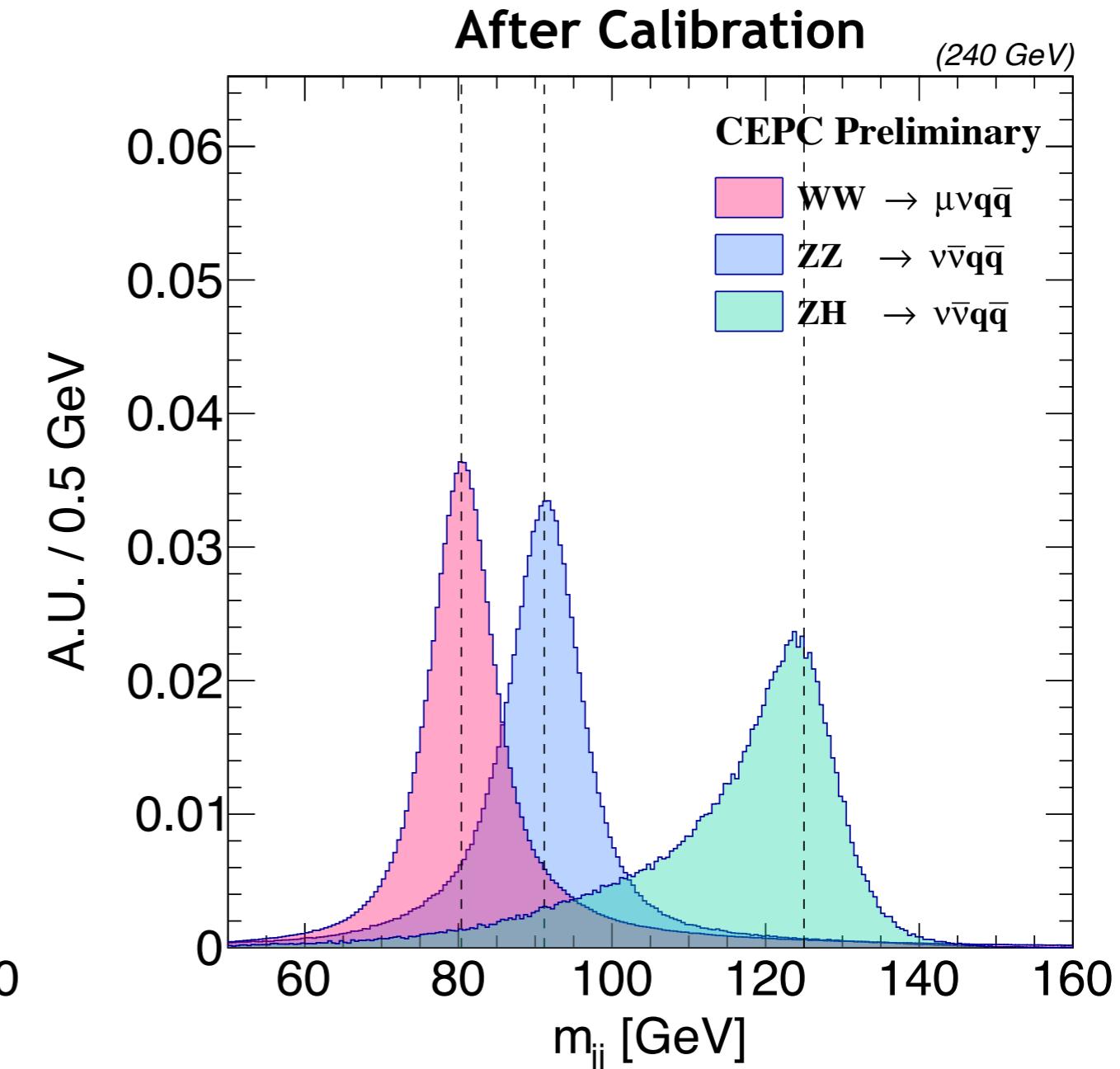
JARs are improved 20% w.r.t ee- $k_t$

- Improvement maybe came from boosting the system back to the rest frame with the neutrons' information.



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# Jet Energy Calibration

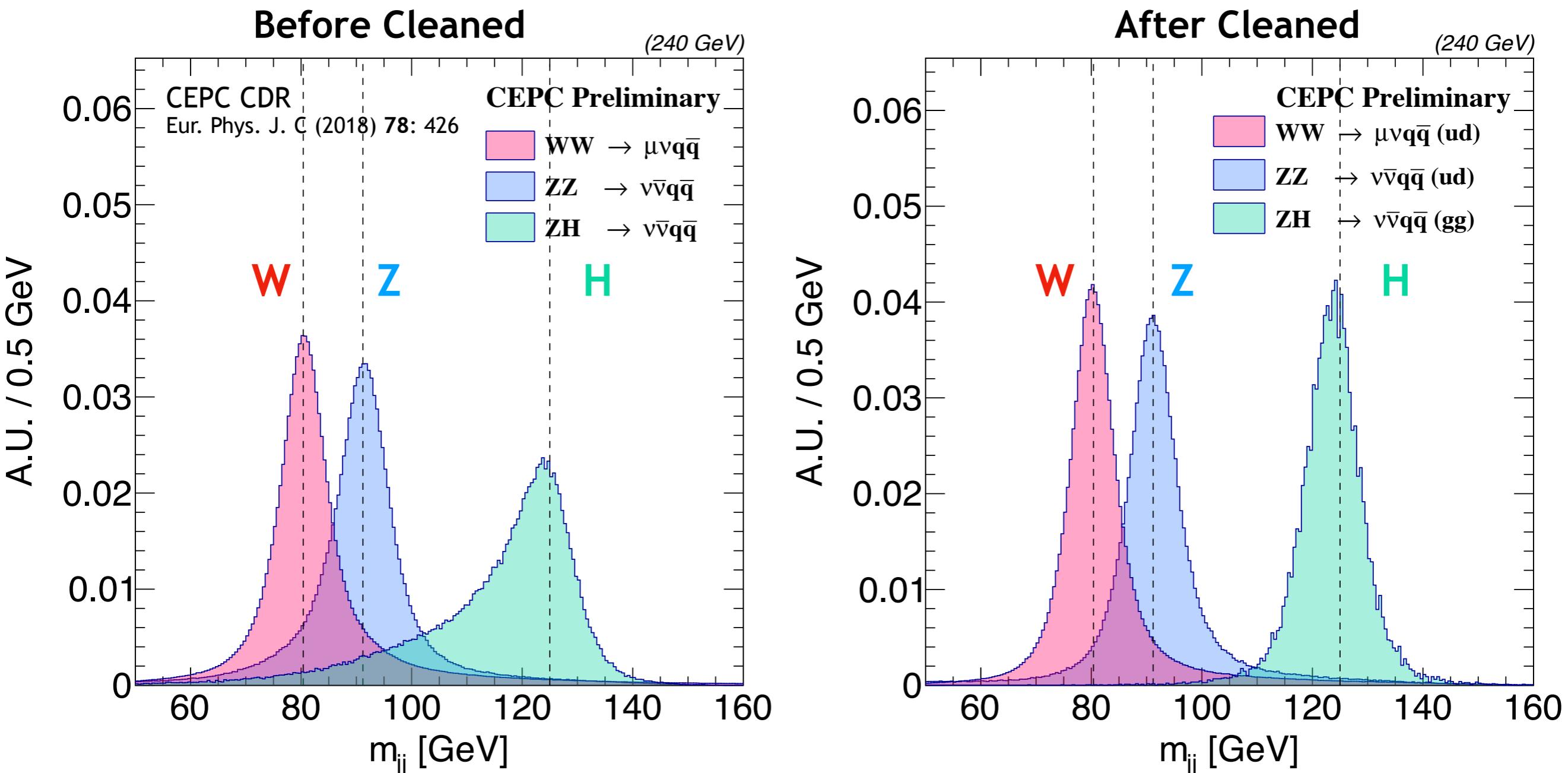
**Before Calibration****After Calibration**

- Since the double-counting effect, jet energy would be overestimated.
- According to MC true energy and  $\cos\theta$  distribution, JES can be used to calibrate the dijet invariant mass back to the value we put into simulation.
- After calibration, boson mass resolution is improved about **1%**.



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# BM1: Massive Boson Mass Resolution

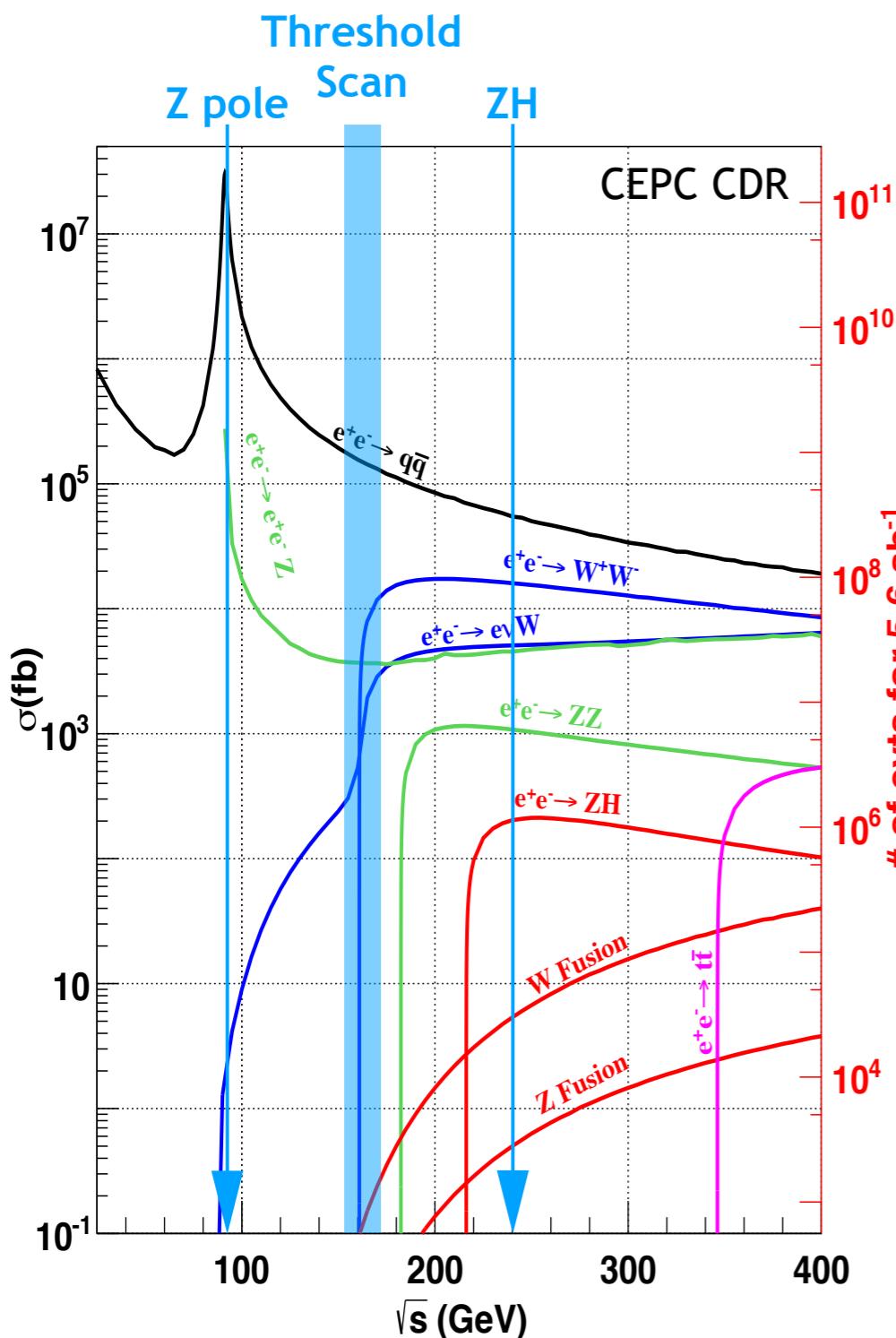


- W-, Z-, and Higgs-boson masses in dijet final state can be well separated at CEPC.
- After cleaned, Z- and W-boson could be separated  $\approx 2\sigma$ , and the Higgs Boson Mass Resolution = 3.8% achieving the CEPC baseline.

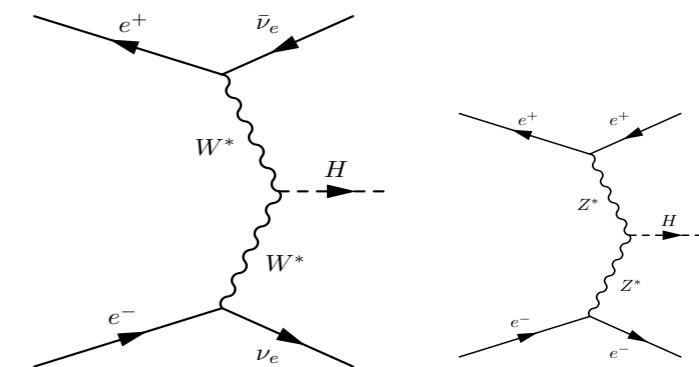
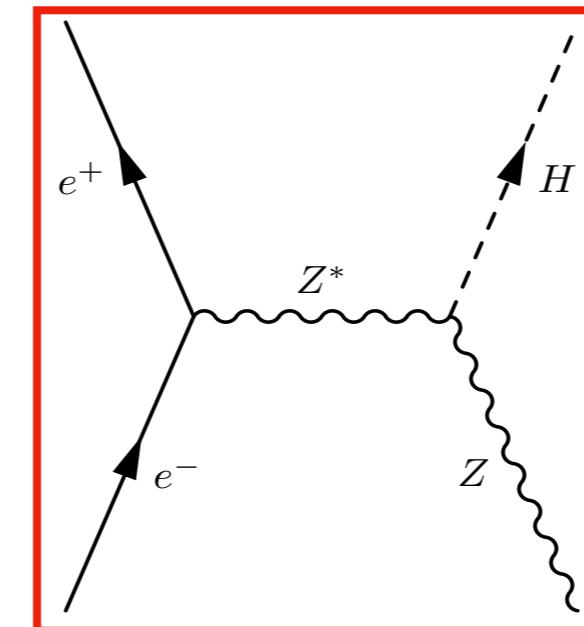
Cleaned: Select the light flavor jet event with low energy ISR, low energy neutrino inside jet, and within  $|\cos\theta| < 0.85$ .



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# Higgs Production at CEPC



Process	Cross section(fb)	Events in $5.6 \text{ ab}^{-1}$
$e^+e^- \rightarrow ZH$	196.2	$1.10 \times 10^6$
$e^+e^- \rightarrow \nu_e \bar{\nu}_e H$	6.19	$3.47 \times 10^4$
$e^+e^- \rightarrow e^+e^- H$	0.28	$1.57 \times 10^3$
Total	203.7	$1.14 \times 10^6$

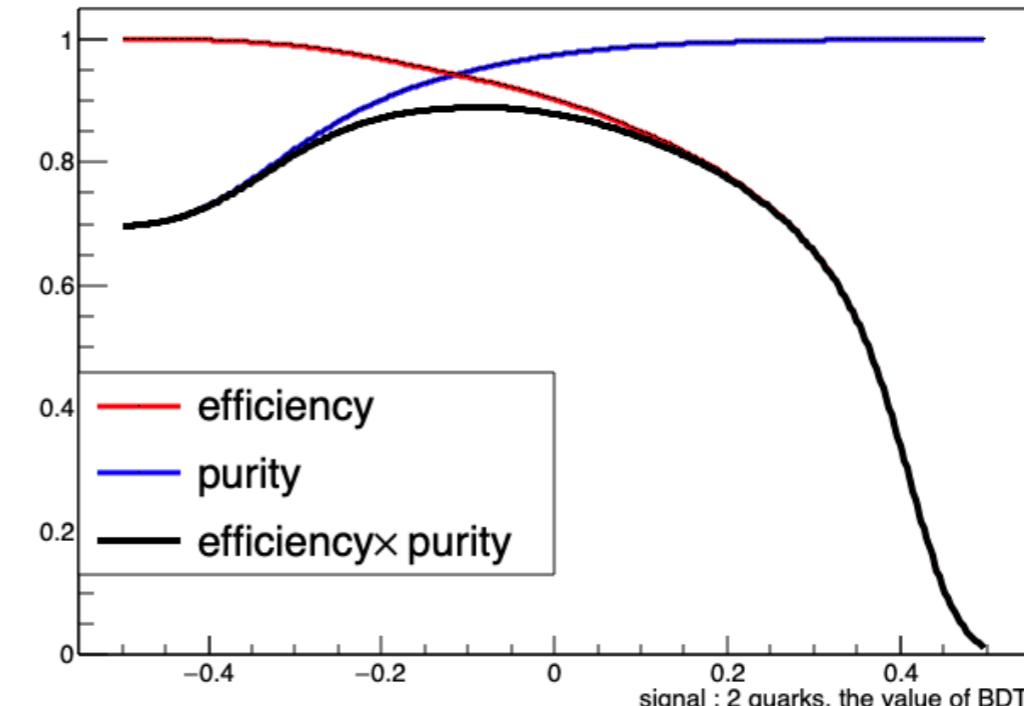
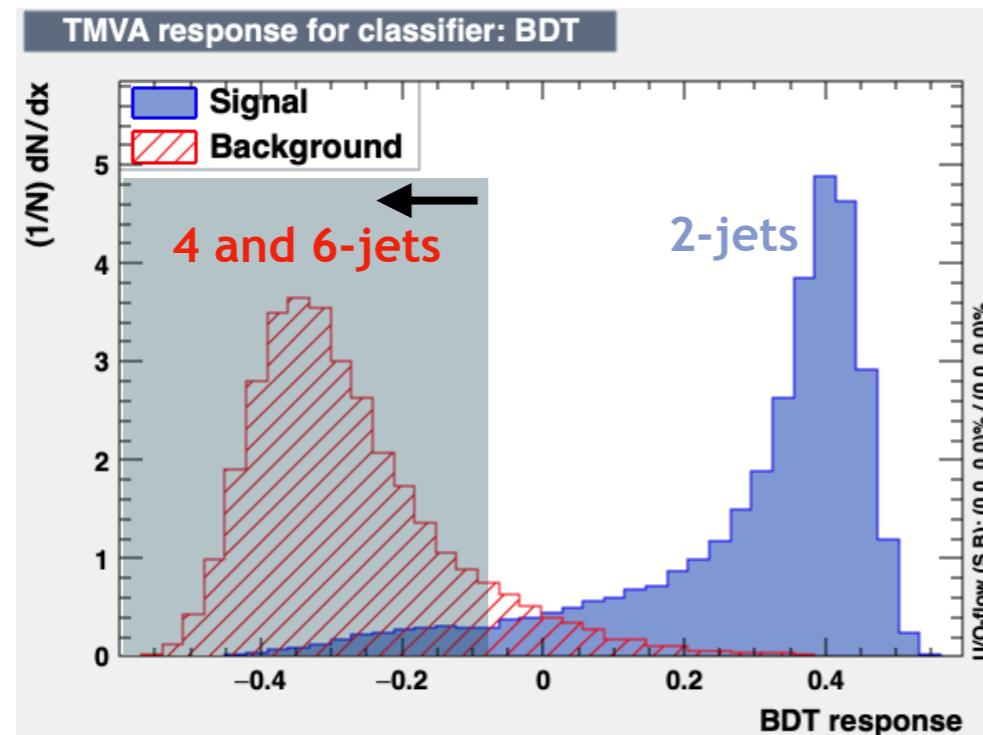
S : B = 1 : (100 ~ 1000)

- Observables: Higgs mass, CP,  $\sigma(ZH)$ , event rate ( $\sigma(ZH, vvH) * \text{Br}(H \rightarrow X)$ ), Diff. distributions  
→ Absolute Higgs width, branching ratio, couplings



# BM2: Preliminary Number of Jet Identification

Yong-Feng Zhu



Samples:

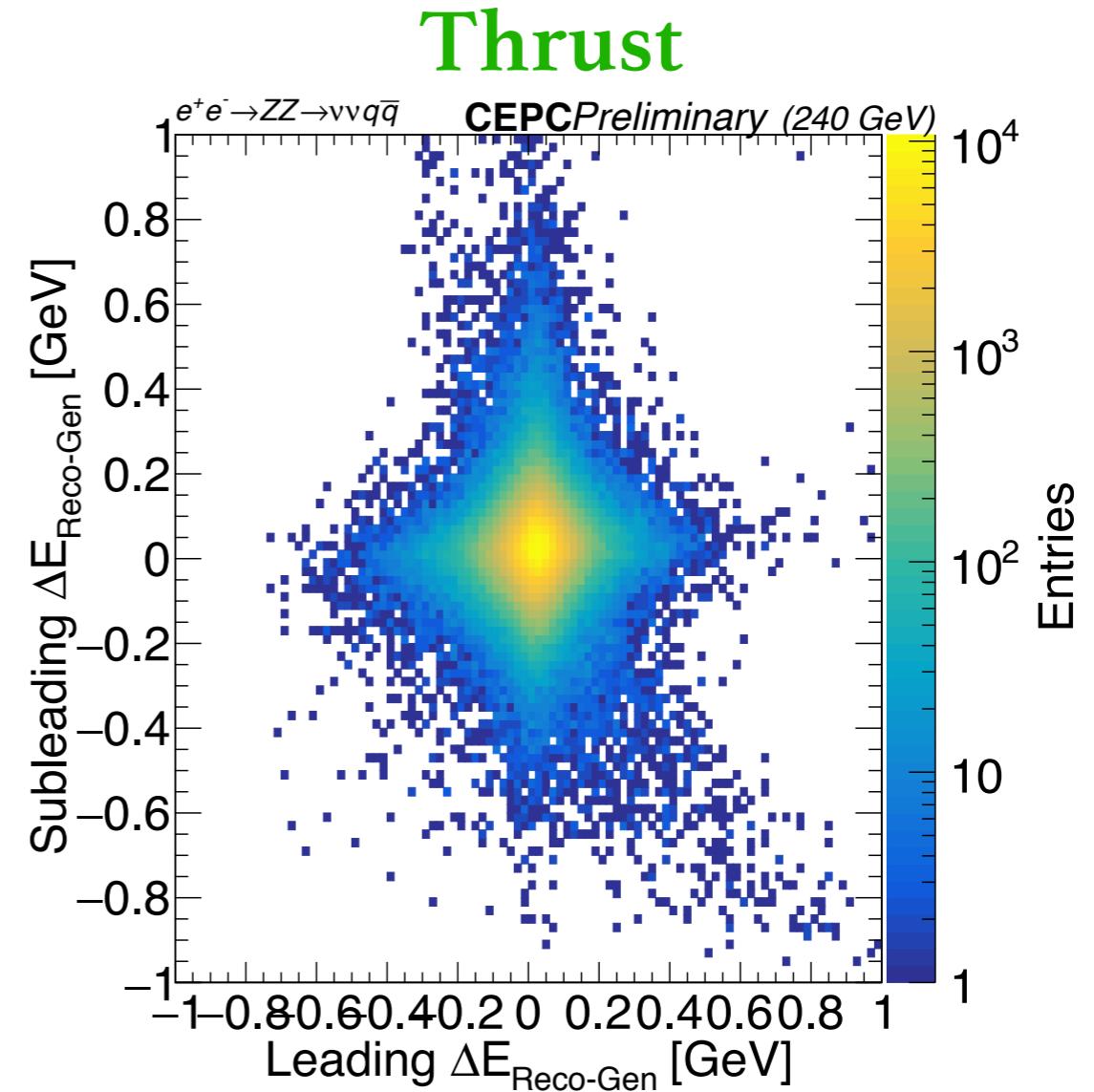
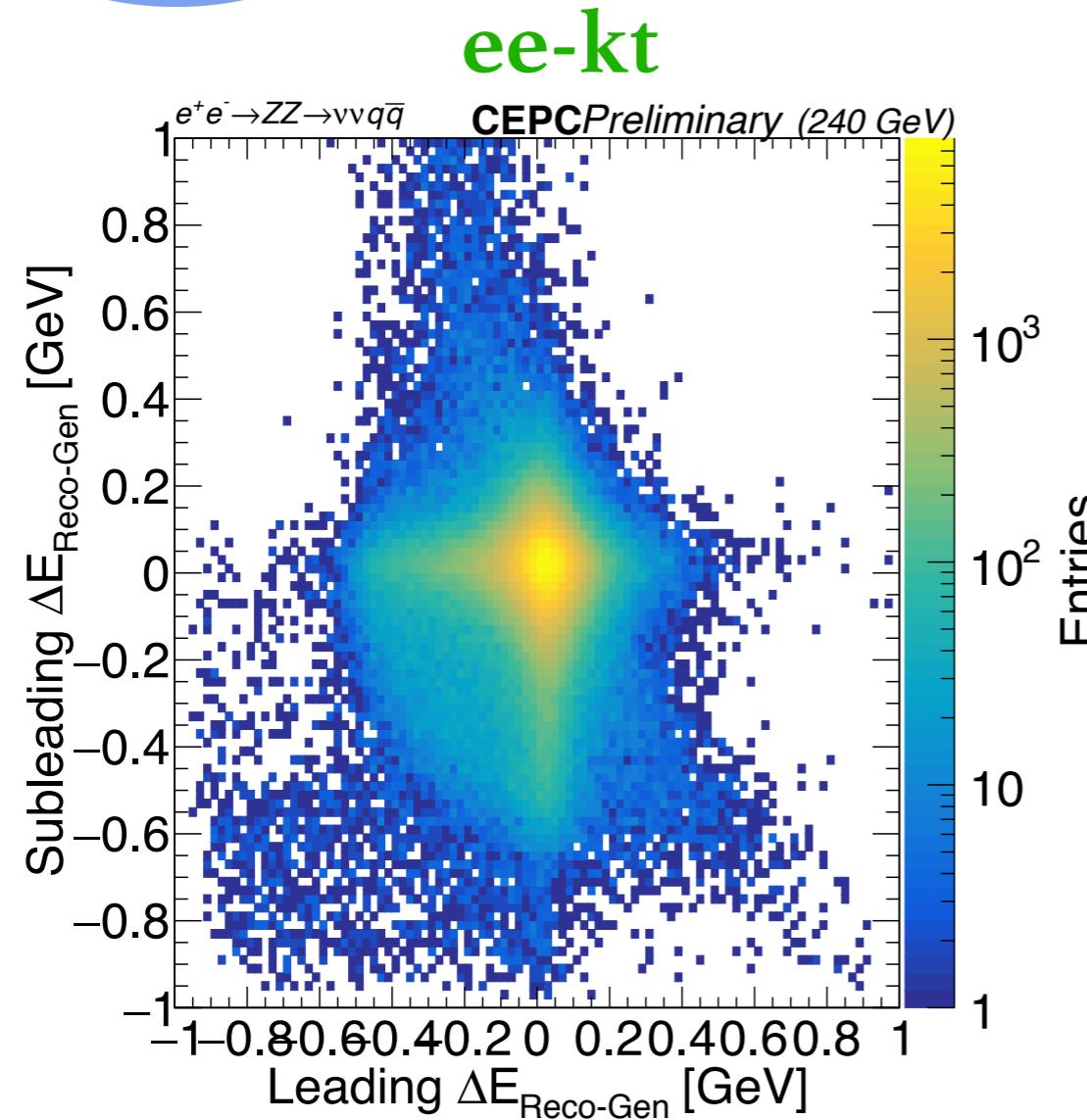
- $e^+e^- \rightarrow q\bar{q}$  (2 jets)
- $ZZ \rightarrow q\bar{q}q\bar{q}$  (4 jets)
- $W^+W^- \rightarrow q\bar{q}q\bar{q}$  (4 jets)
- $ZH \rightarrow q\bar{q}q\bar{q}$  (4 jets)
- $ZH \rightarrow q\bar{q}H \rightarrow qqqqqqq$  (6 jets)

Signal	<i>Efficiency <math>\times</math> Purity</i>
2 jets	88.4%
6 jets	1.8%

20 event-shape variables are combined with the multi-variate analysis (MVA) to separate 2, 4, and 6 jets final-states.



# BM3: Thrust Jet Clustering Method



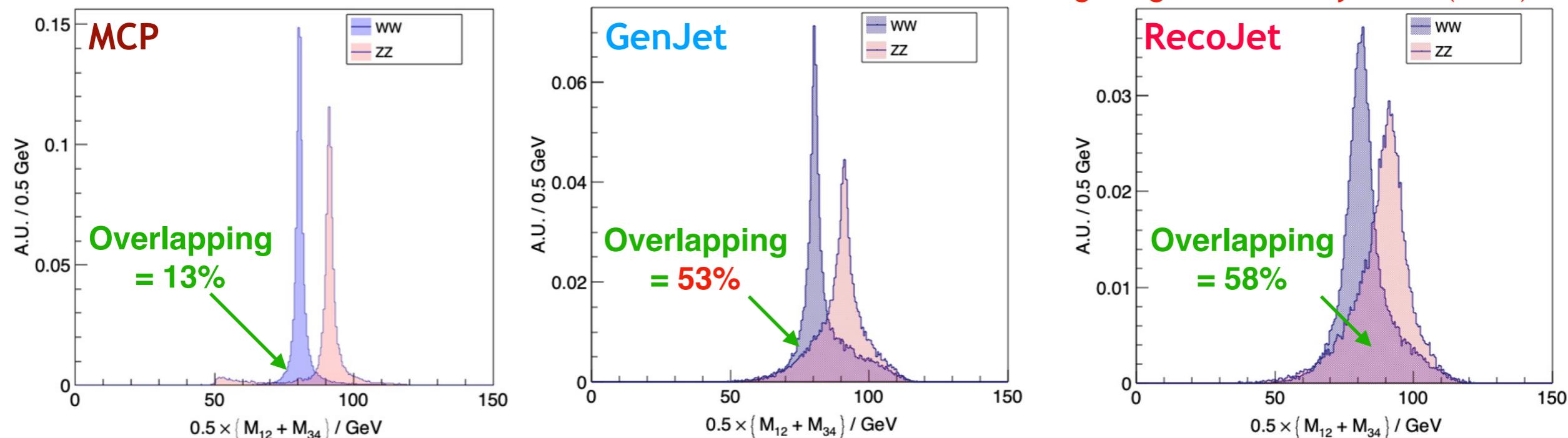
- Identify the 2 jets final-state event with  $(\text{Efficiency} \times \text{Purity}) = 88.4\%$ , the thrust jet clustering method could be employed.
- After “cleaned” selection, the thrust method has **significant tail suppressed**  
→ expected to have improvement on jet energy and angular response.

Cleaned: Select the light flavor jet event with low energy ISR, low energy neutrino inside jet, and within  $|\cos\theta| < 0.85$ .



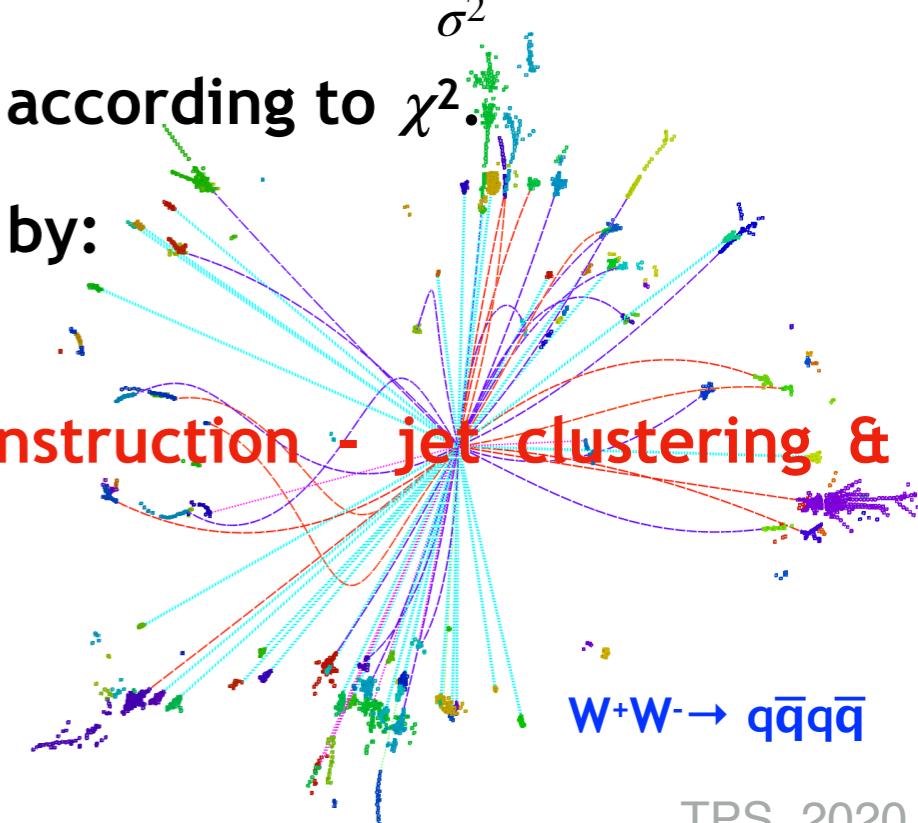
# BM4: WW & ZZ to 4 Jets Separation

Yong-Feng Zhu—Eur. Phys. J. C (2019) 79:274

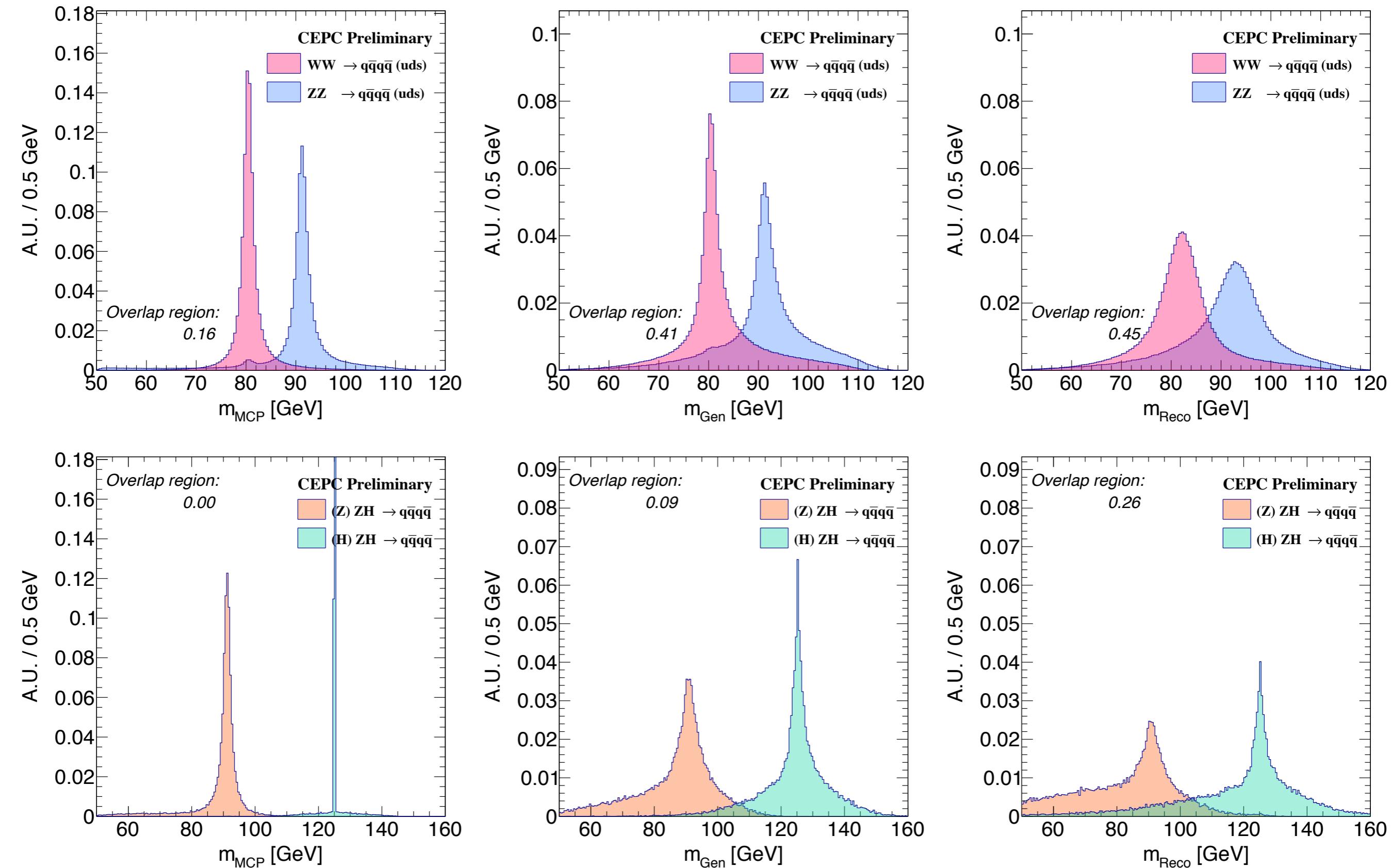


- Low energy jet (20-120 GeV)
- Typical multiplicity could be  $10^2$ .
- GenJet and RecoJet are clustered by ee-kt and paired according to  $\chi^2$ .
- WW & ZZ to 4 jets final-state separation is determined by:
  1. (13%) Intrinsic boson mass/width (10 GeV)
  2. (53%) Wrong jet pairing for color singlet reconstruction - jet clustering & pairing.
  3. (58%) Detector response

$$\chi^2 = \frac{|(m_{ij} - m_{boson})|^2 + |(m_{ij} - m_{boson})|^2}{\sigma^2}$$

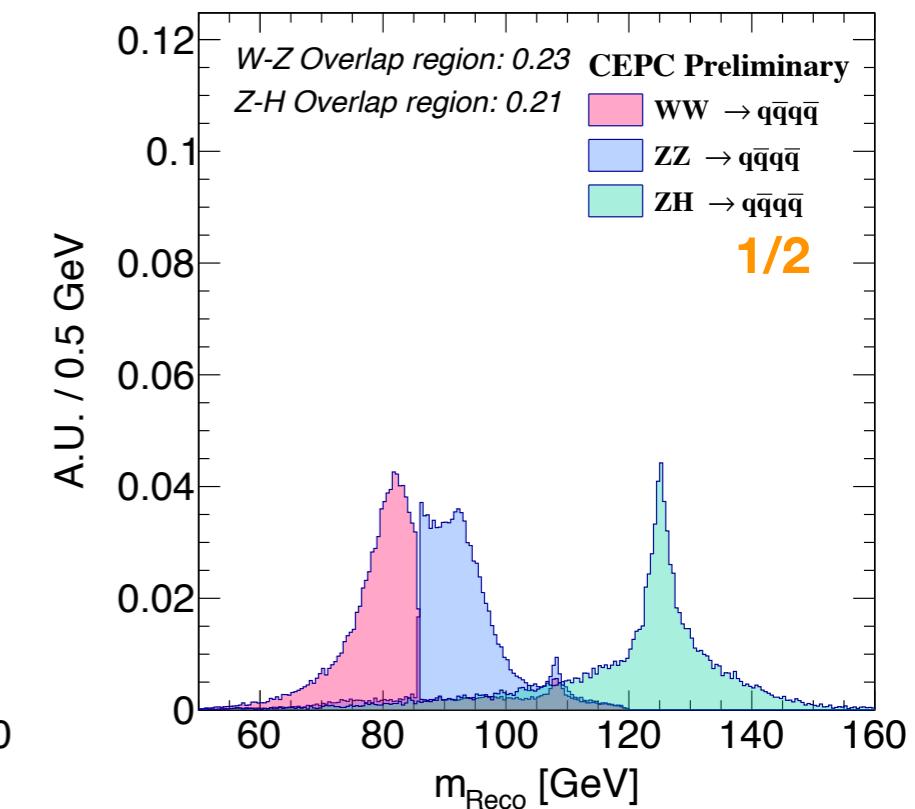
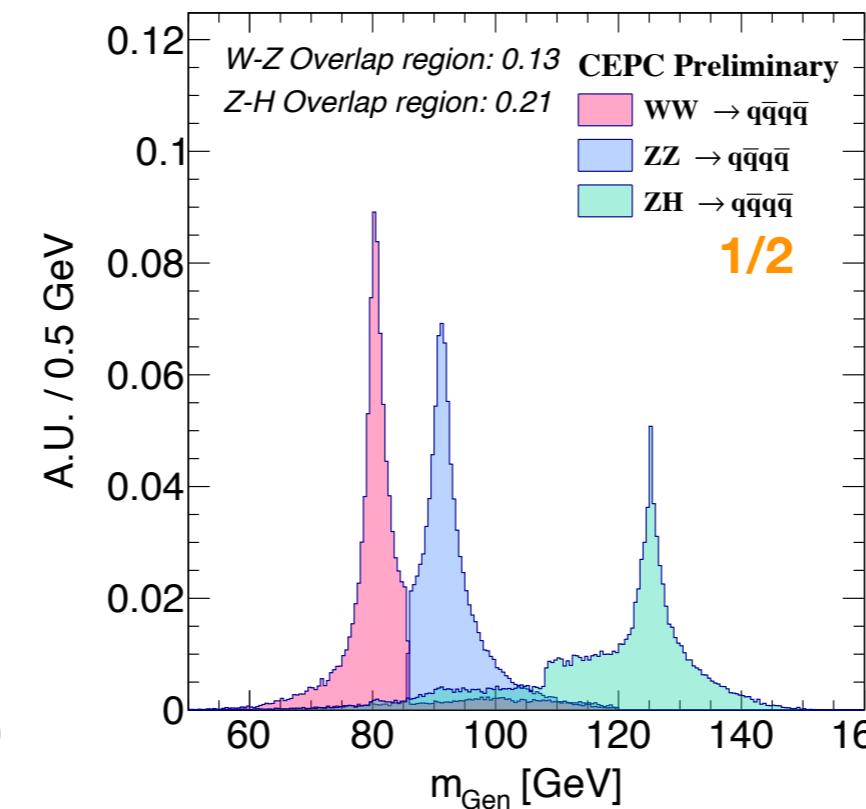
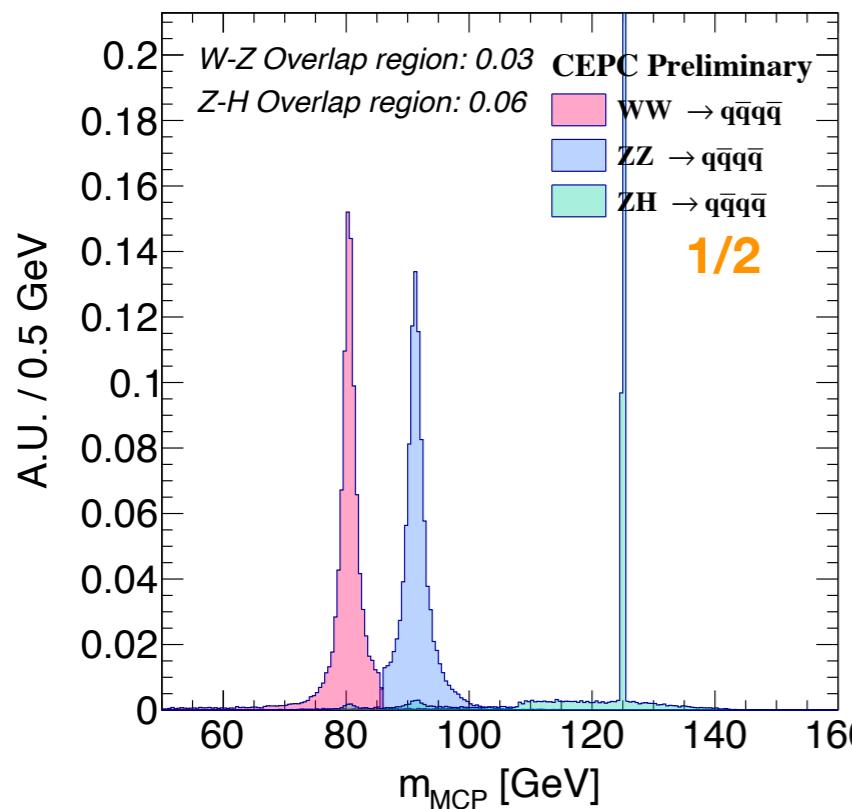
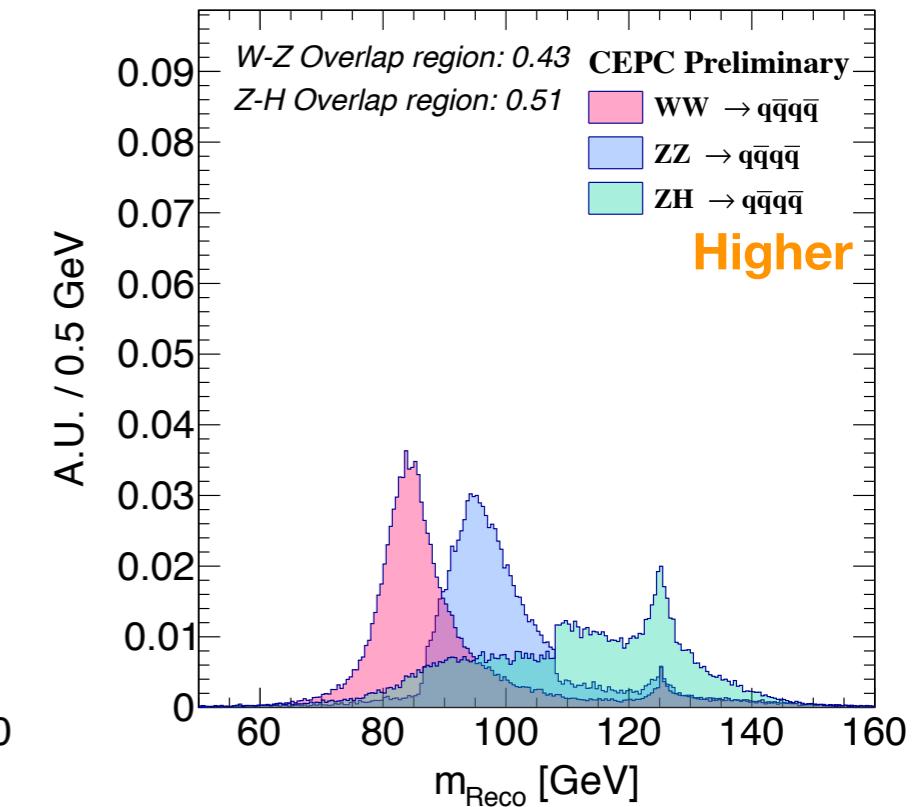
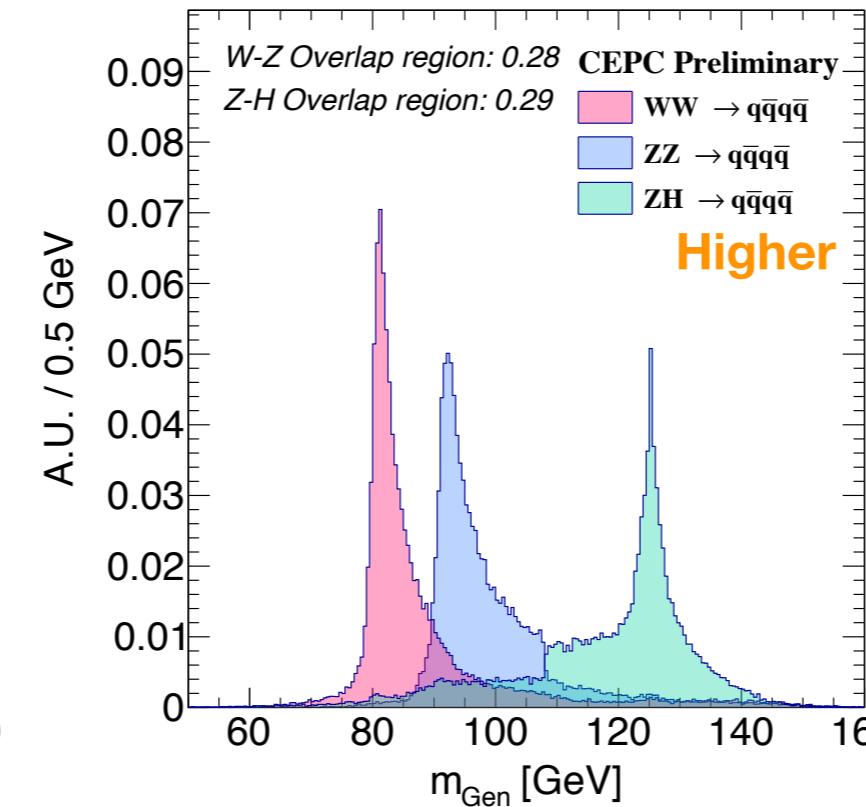
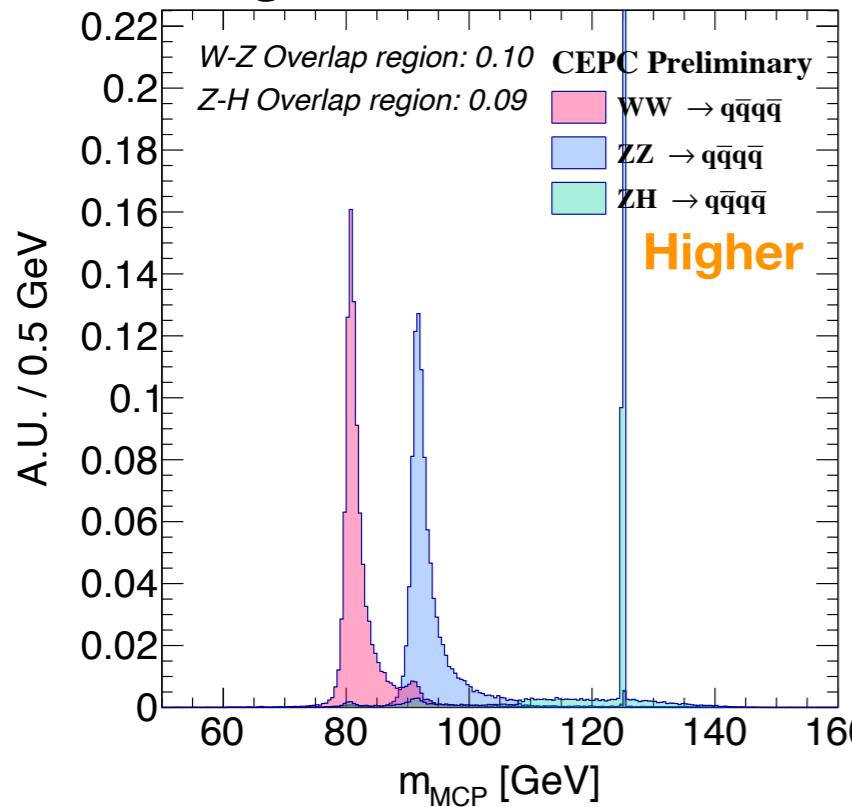


# WW, ZZ, and ZH Full Hadronic



# Mixing Signal & BKG

# WW, ZZ, ZH Full Hadronic Separation



First Row: After reconstructed  $m_1$ ,  $m_2$ , higher one would be chosen

Second Row: After reconstructed  $m_1$ ,  $m_2$ , and then  $(m_1 + m_2) / 2$ . (Higgs still chosen the higher one)



# BM4: ZH Full Hadronic Identification

- According to the final results, the following estimation could be declared:  
The identified efficiency of ZH signal is 60% with background, 20% ZZ and 10% WW.  
The cross section of ZZ is 5 times amount than ZH, 10 times from WW.

	Efficiency	XS	Purity	
WW	10%	10	→	100
ZZ	20%	5	→	100
ZH	60%	1	→	60

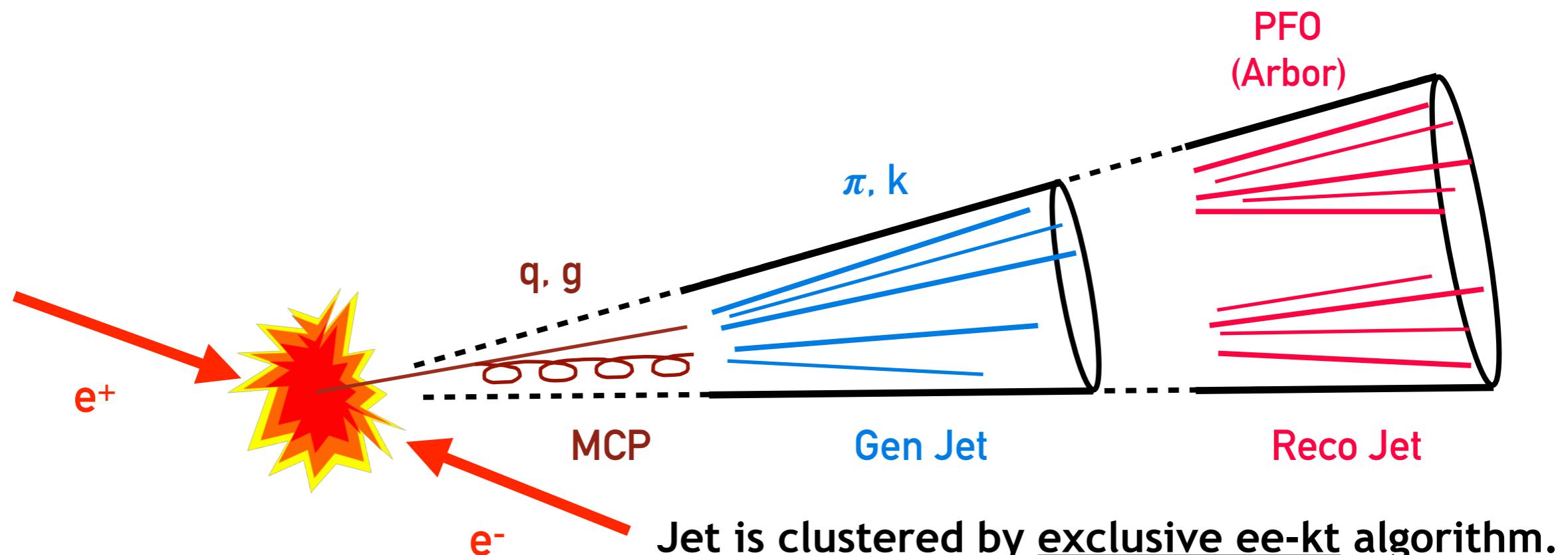
Efficiency x Purity  
 $60\% \times 30\% = 18\%$



# of ZH = 500,000 in the  $5 \text{ ab}^{-1}$   
 $500,000 \times 18\% = 150,000$  could be identified  
 $1 / \sqrt{150,000} = 0.25\%$



- **MCP** represents initial parton of MC quark. The original state of quark.
- **GenJets** are grouped all MC particles except neutrinos with  $c\tau > 1$  cm through exclusive ee-kt jet clustering algorithm.
- **RecoJets** are grouped with the particle flow objects by exclusive ee-kt jet clustering algorithm.

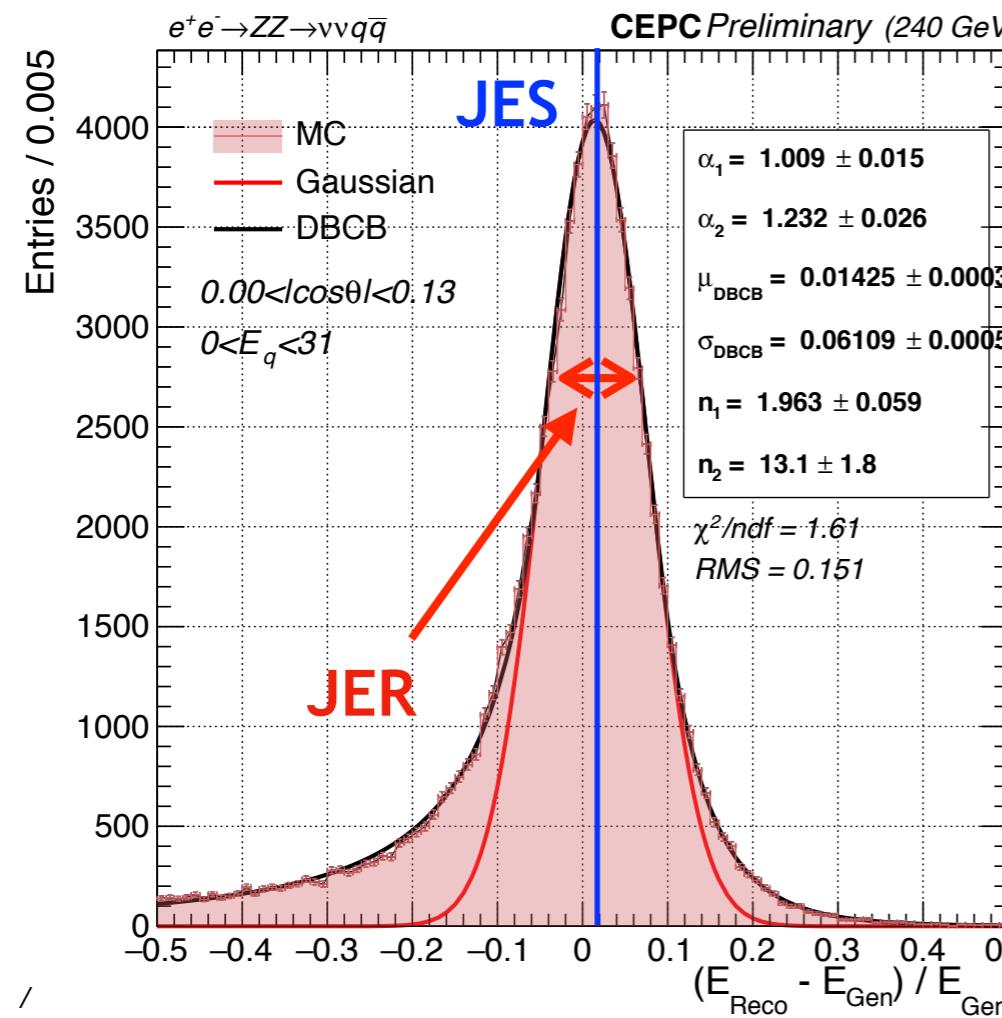




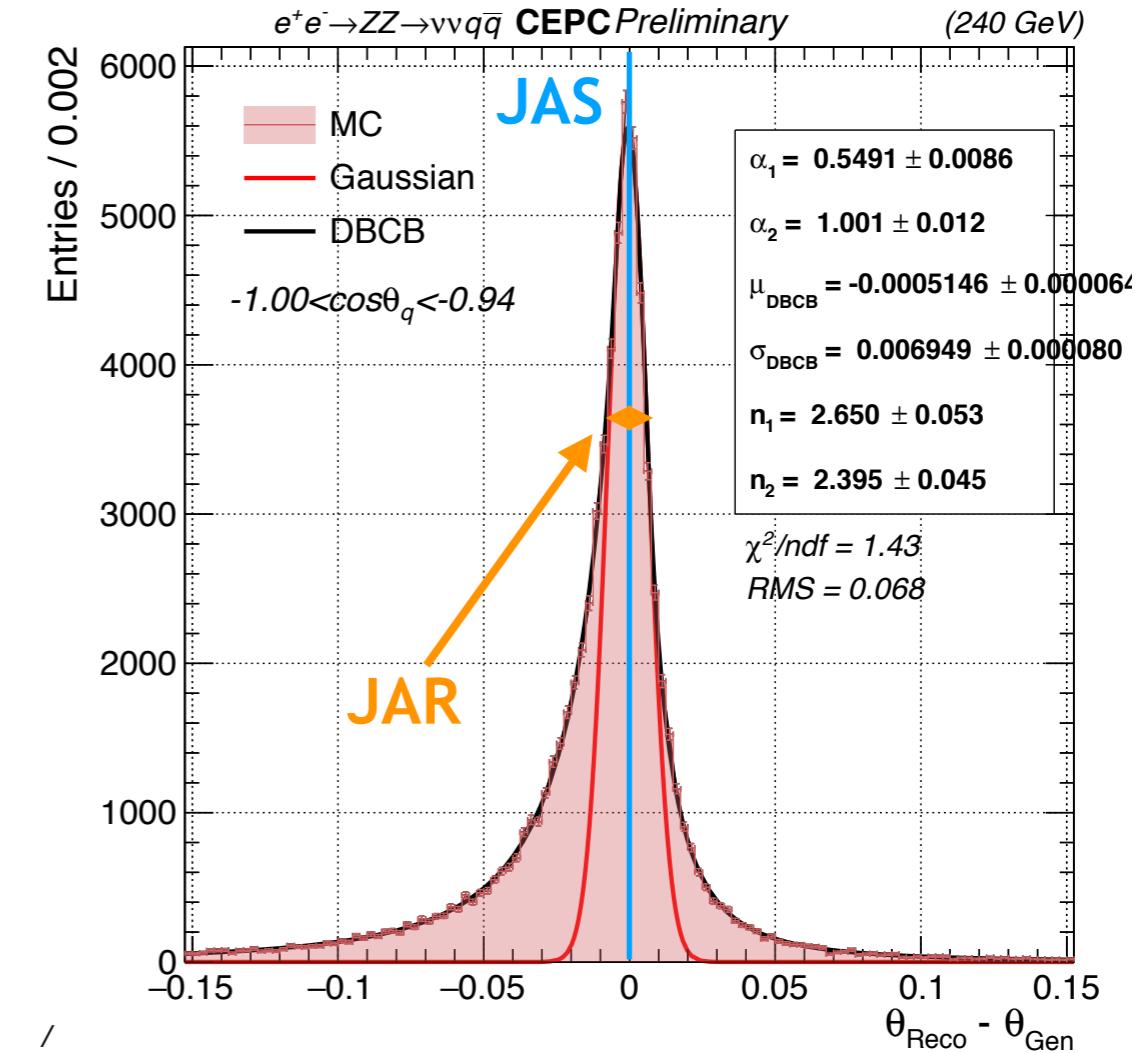
# Quantify the Performance

- Double-sided crystal ball(DBCB) function is used to extract energy and angular resolution and scale.

## Jet Energy Scale (JES) Jet Energy Resolution (JER)



## Jet Angular Scale (JAS) Jet Angular Resolution (JAR)

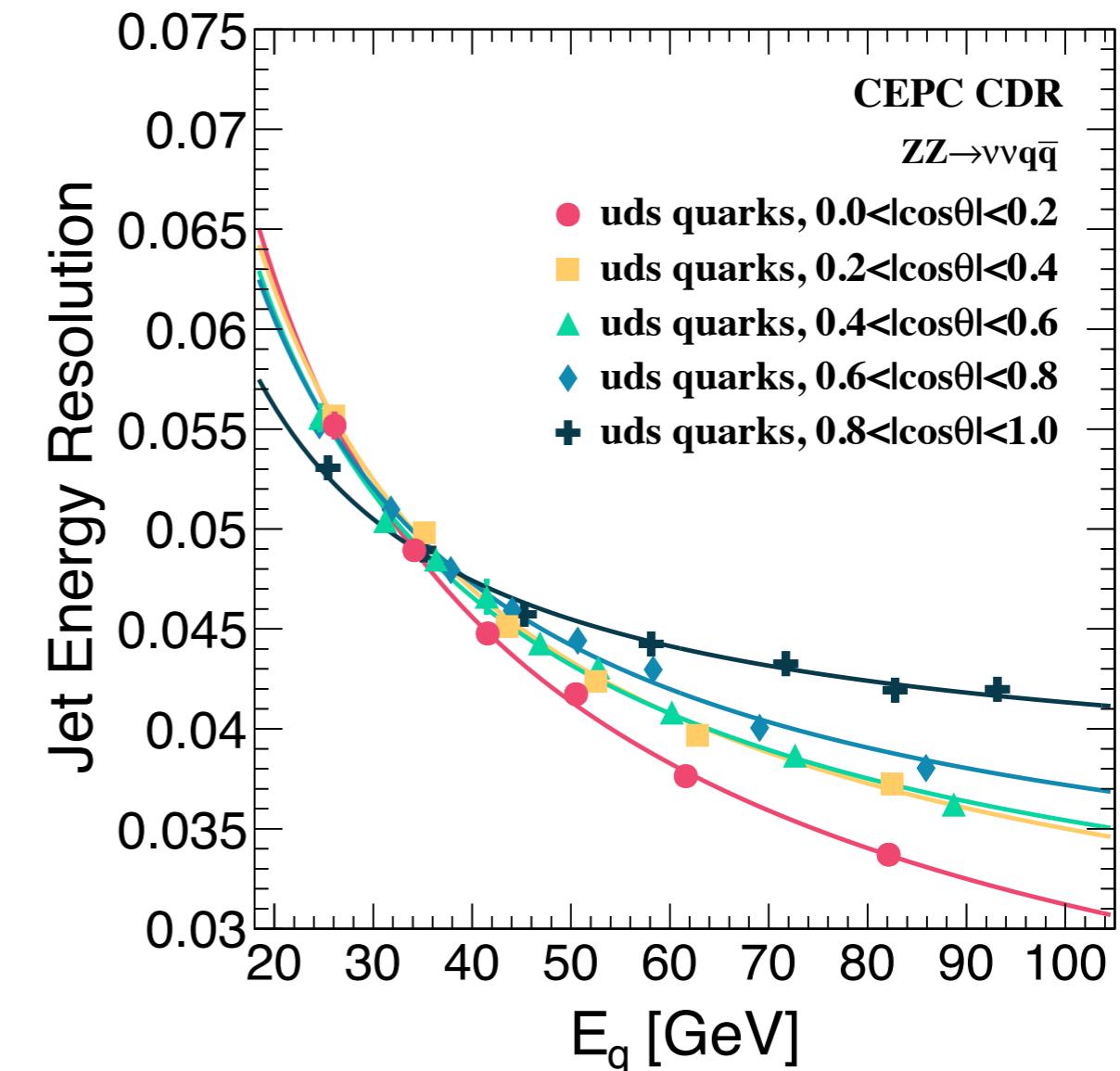
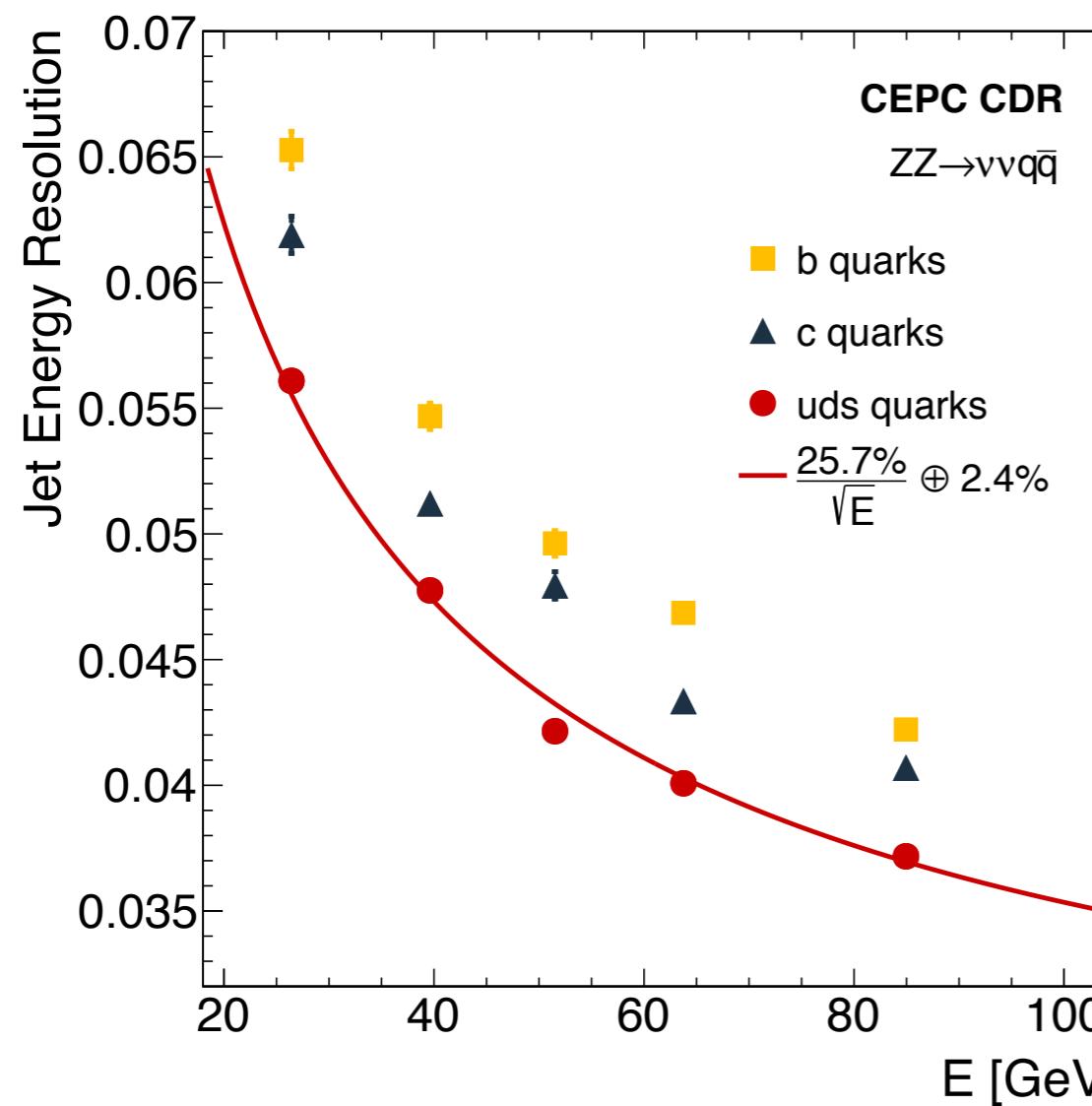


Relative difference : 
$$\frac{E_{\text{Reco}} - E_{\text{Gen}}}{E_{\text{Gen}}}$$

Difference : 
$$\theta_{\text{Reco}} - \theta_{\text{Gen}}$$

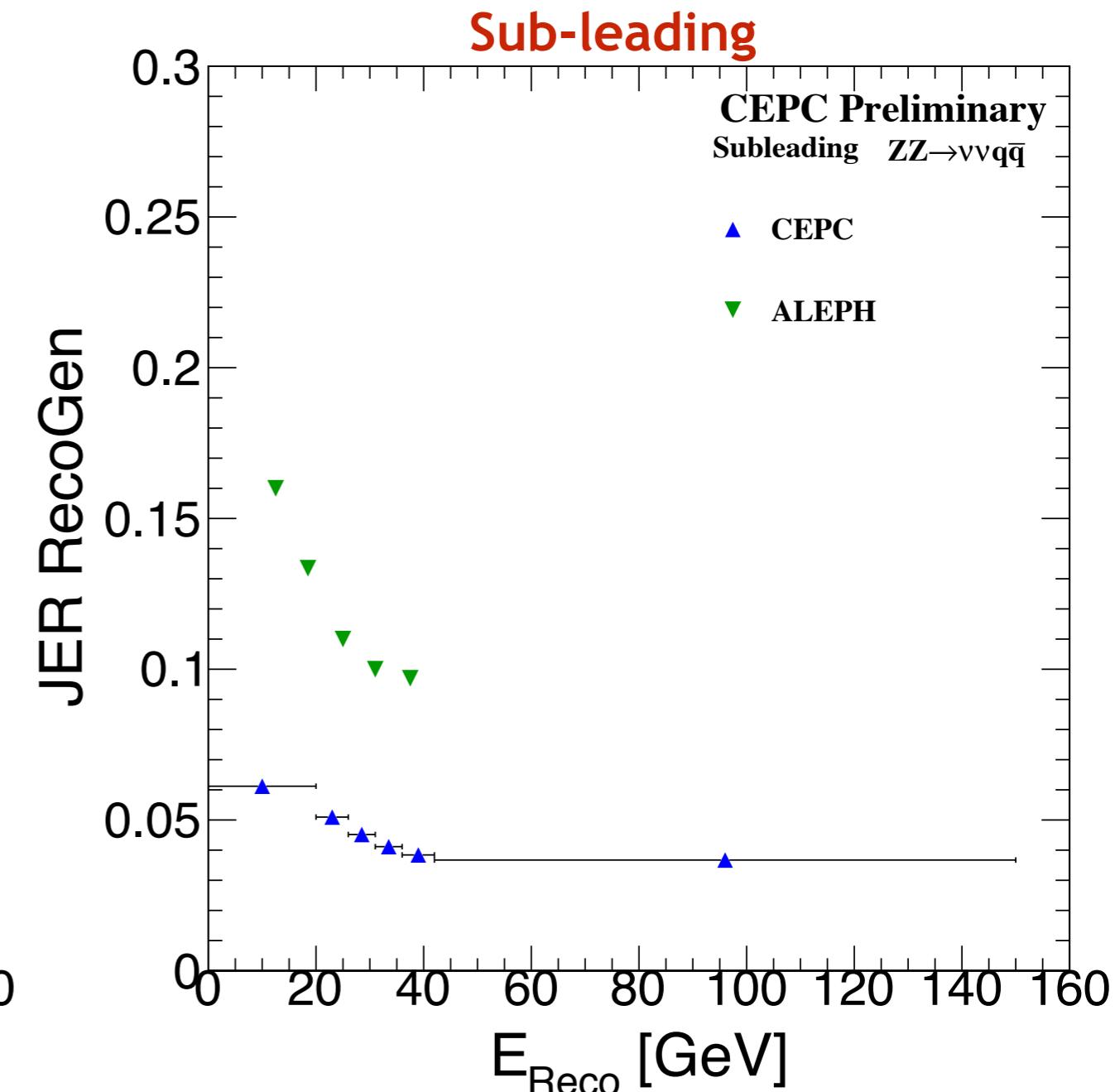
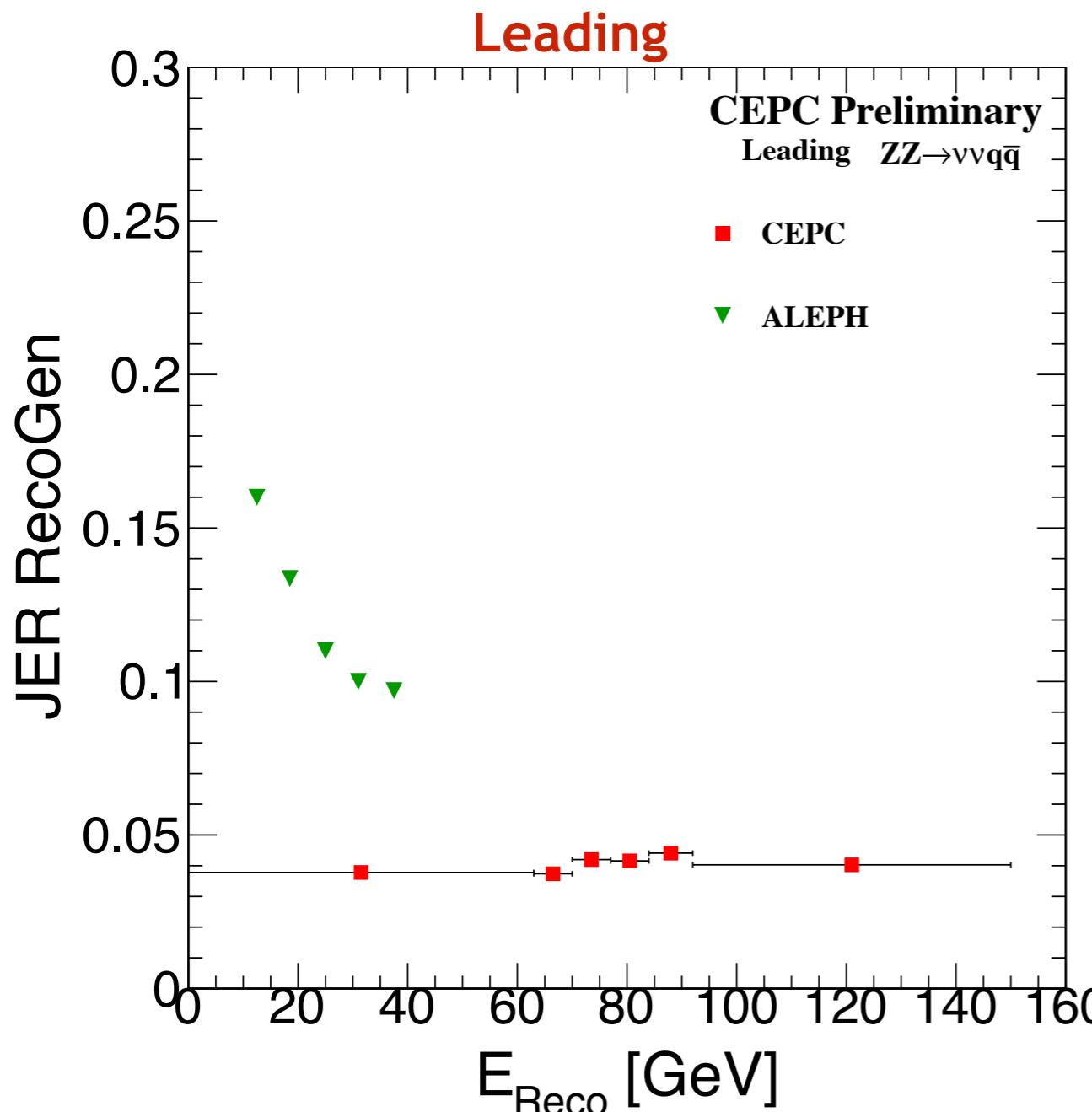
CEP<sup>c</sup>

## BM3: JER (Reco-Gen)



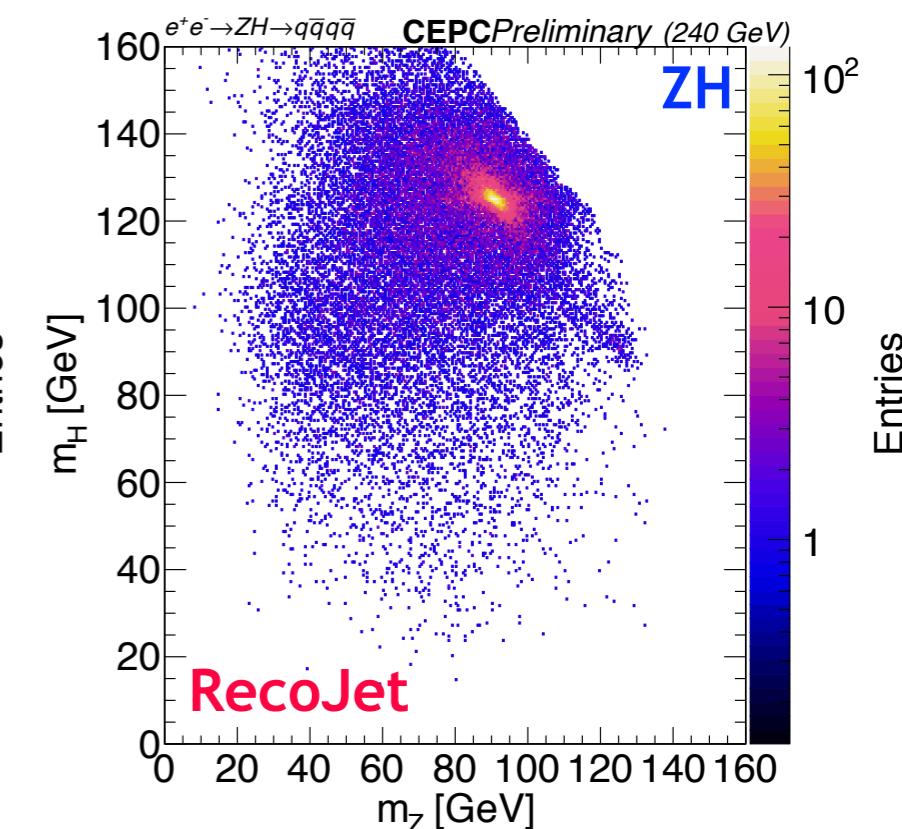
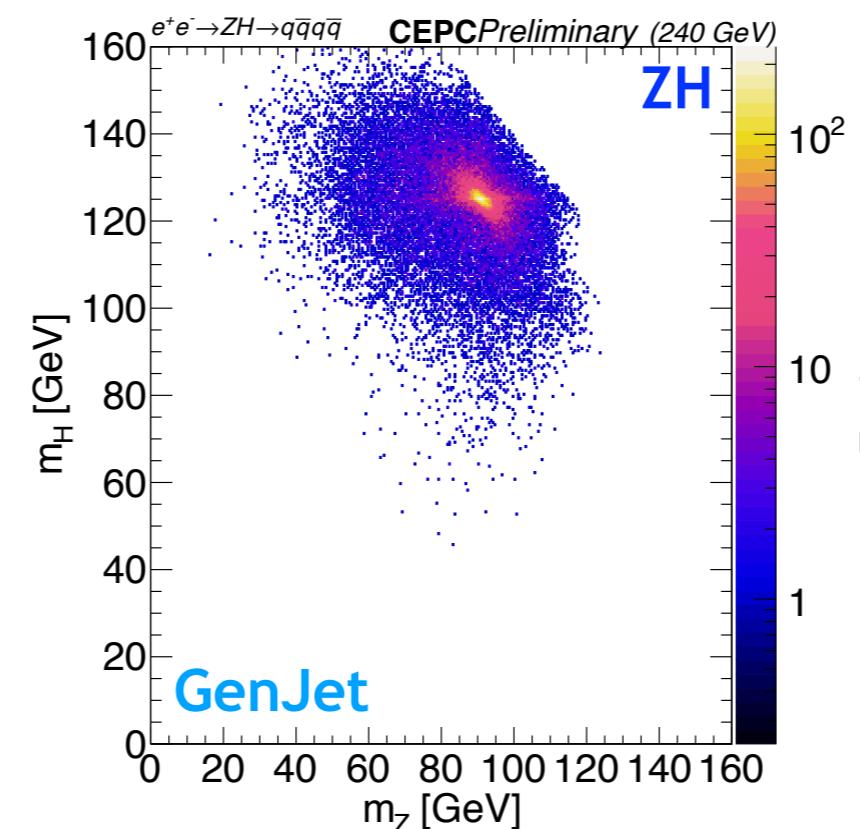
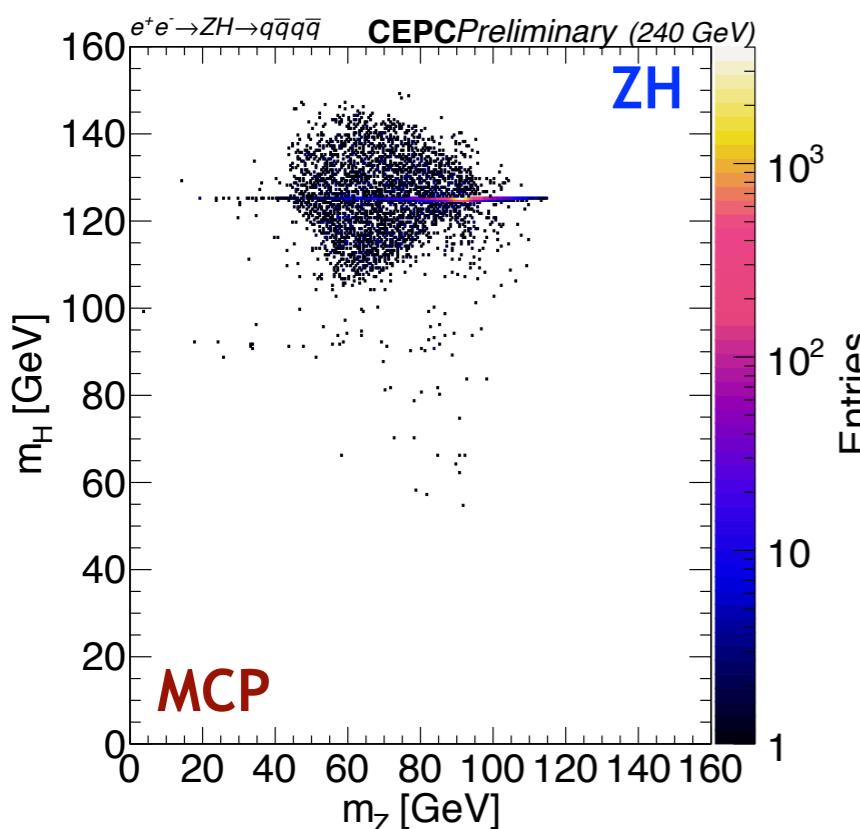
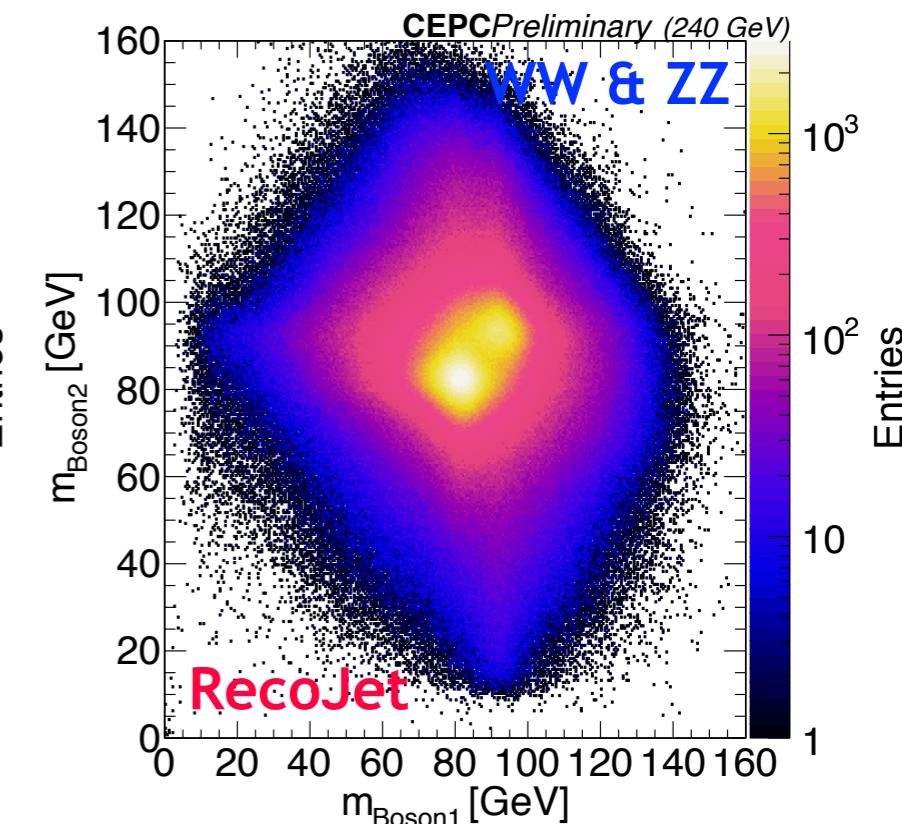
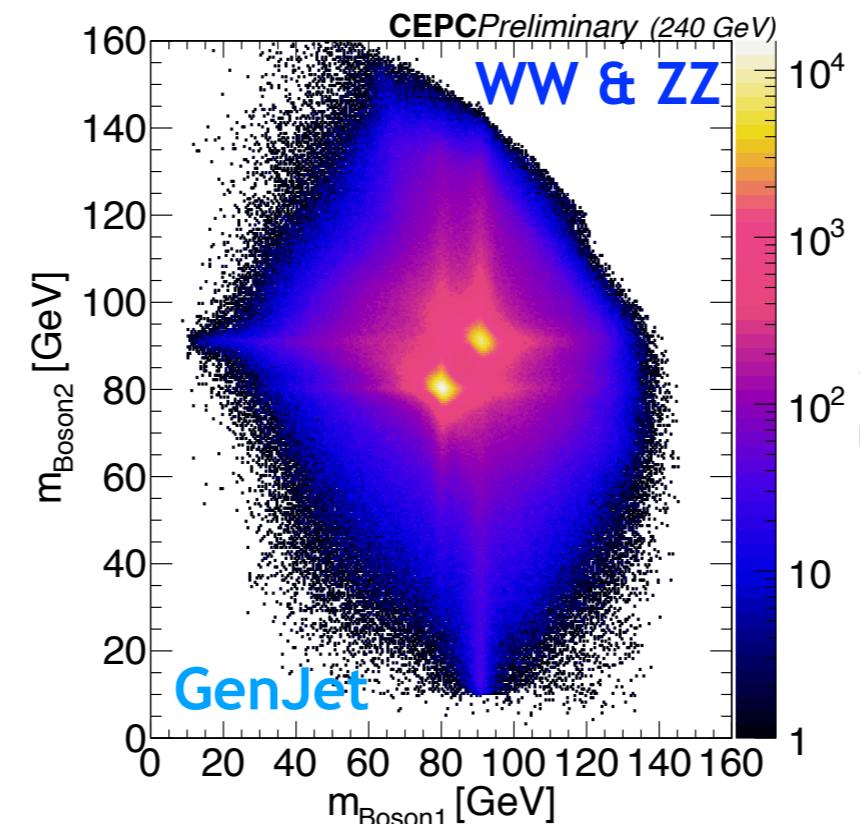
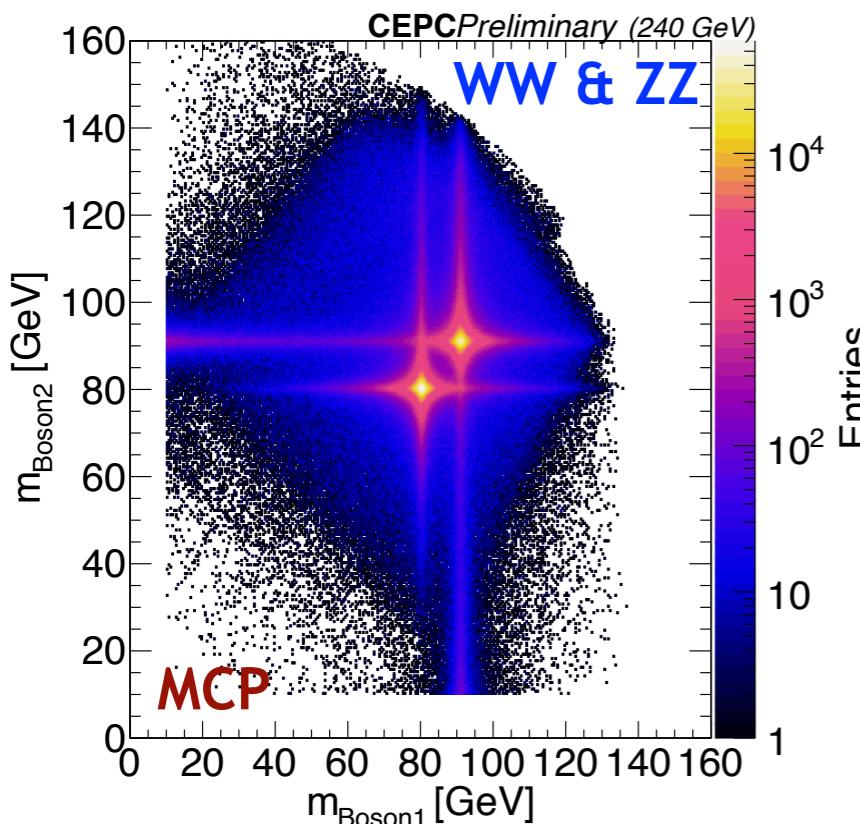
- JER also depends on jet flavors; the semi-leptonic decay from c- and b-quarks.
- For light-flavor jets with high energy and within central region of barrel, JER could reach 3%.

# Compare with ALEPH at LEP



■ Our JER is better than ALEPH.

# WW & ZZ Full Hadronic

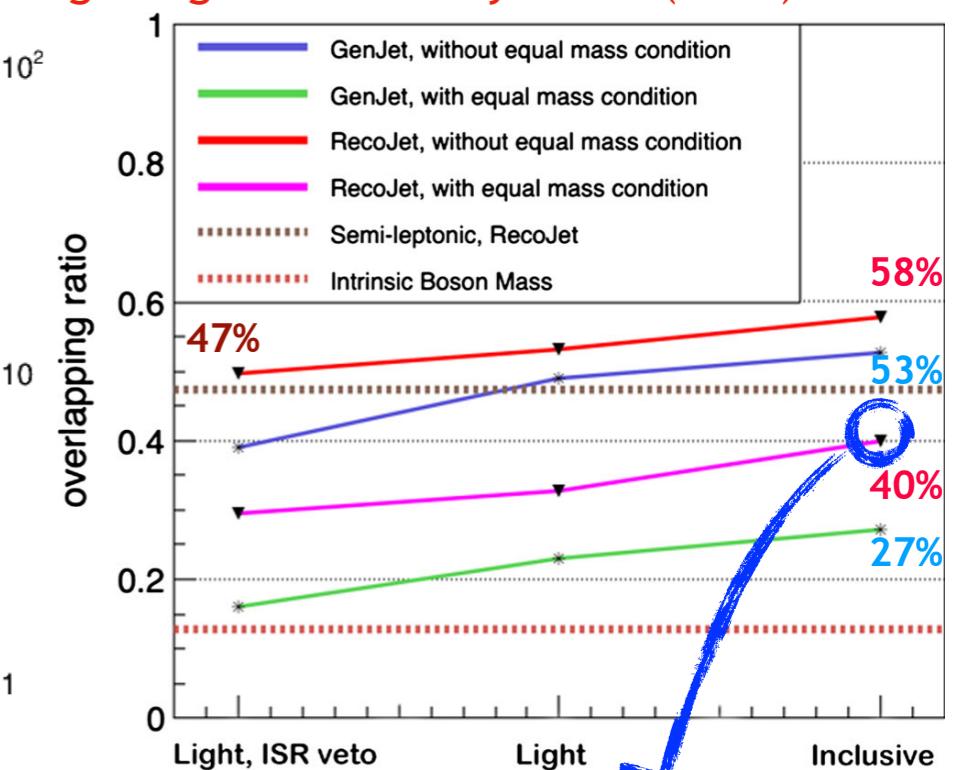
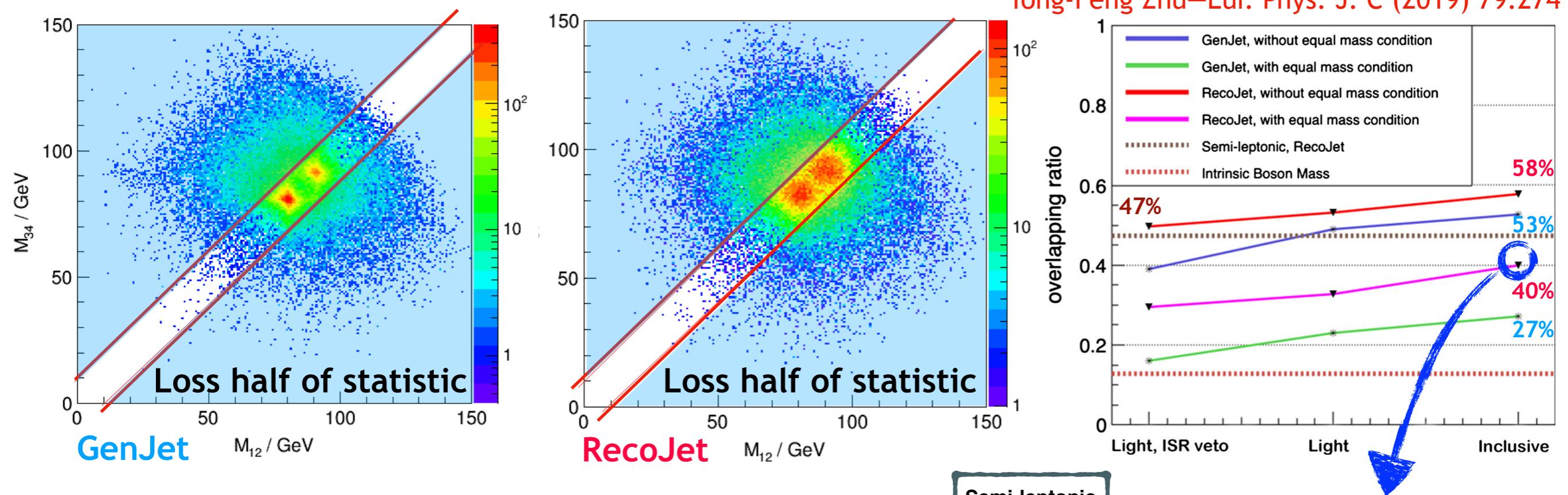




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# BM4: WW & ZZ to 4 Jets Separation

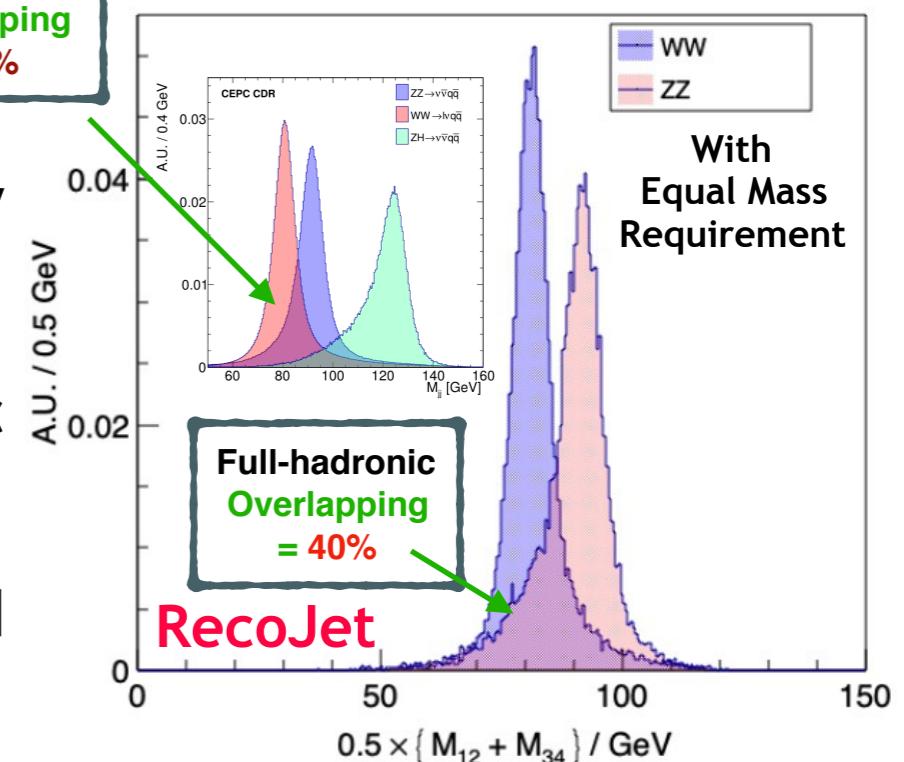
Yong-Feng Zhu—Eur. Phys. J. C (2019) 79:274



- Equal mass requirement:**  $|M_{12} - M_{34}| < 10 \text{ GeV}$

- Cost half of the statistic.
- Overlapping can be reduced from 58%/53% to 40%/27% for the RecoJet/GenJet.

Semi-leptonic  
Overlapping  
= 47%



- CEPC baseline could separate WW & ZZ with full hadronic final-state.**

- Improve from the naive jet clustering & pairing and control the ISR photon in the event.



## ■ Jets are crucial for the CEPC Higgs physics

- 97% of ZH events evolve jets
- 1/3 only come from single Z or Higgs boson.
- 2/3 has more than one boson (e.g.  $ZH \rightarrow q\bar{q}q\bar{q}$ ) - need **color singlet identification algorithm**.

### I. BMR < 4% is critical. Achieved at the CEPC baseline (3.8%)

- \* W, Z, Higgs boson can be efficiently separated at both semi-leptonic & full hadronic.
- \* By Z-boson di-jet recoil mass to distinguish the ZH from ZZ process.

### II. 2 jets final-state could be identified with *efficiency*×*purity* = 88.4%.

- \* Could be clustered by dedicated jet clustering algorithm, **thrust**.

### III. Single Jet – JER ~ 3-5% & JAR ~ 1%.

- \* Thrust clustering method is recommended for two jets final-state. It could improve the JER 20%, 40% on tail (RMS), and JAR 20%.

### IV. Need a better color singlet identification algorithm.

- \* Wrong jet pairing is the dominant effect to induce overlapping in full hadronic WW-ZZ separation.
- \* Equal mass requirements: Reduce the overlapping to be better than semi-leptonic, but very costly.
- \* Other physical impact is significant: ISR photon etc.
- \* The statistical uncertainty of ZH to full hadronic final-state could be achieved 0.25% after considering the WW and ZZ as bkg.

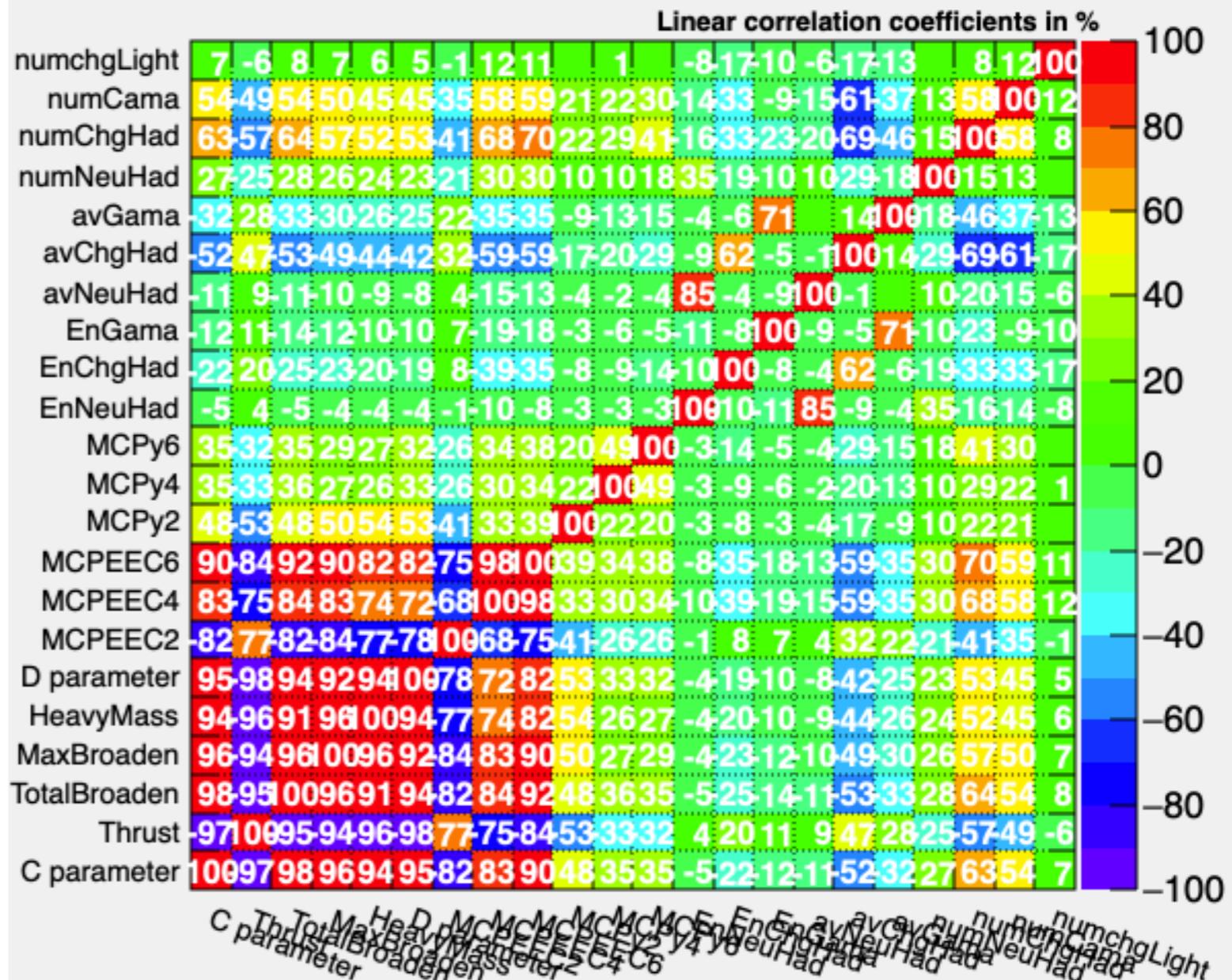


# BM2: Number of Jet Identification

Correlation Matrix (signal)

**20 Variables**

# of charge lepton	EEC 6
# of $\gamma$	EEC 4
# of charge hadron	EEC 2
# of neutro hadron	C parameter
$\bar{E}_\gamma$	D parameter
$\bar{E}_{\text{Charge hadron}}$	Heavy Mass
$\bar{E}_{\text{Neutro hadron}}$	Max Broaden
$E_\gamma$	Total Broaden
$E_{\text{Charge hadron}}$	Thrust
$E_{\text{Neutro hadron}}$	$y_{23}, y_{45}, y_{67}$



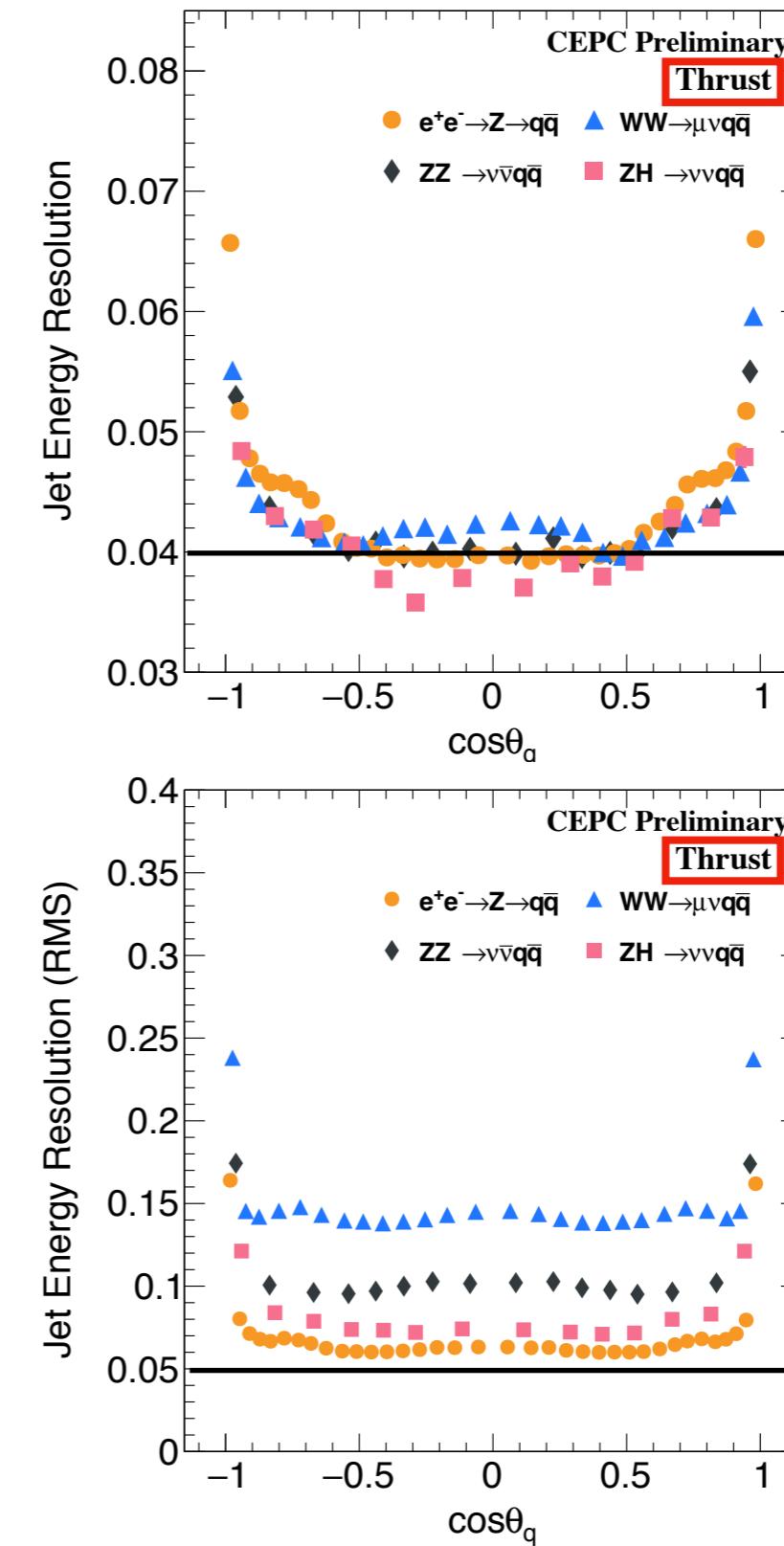
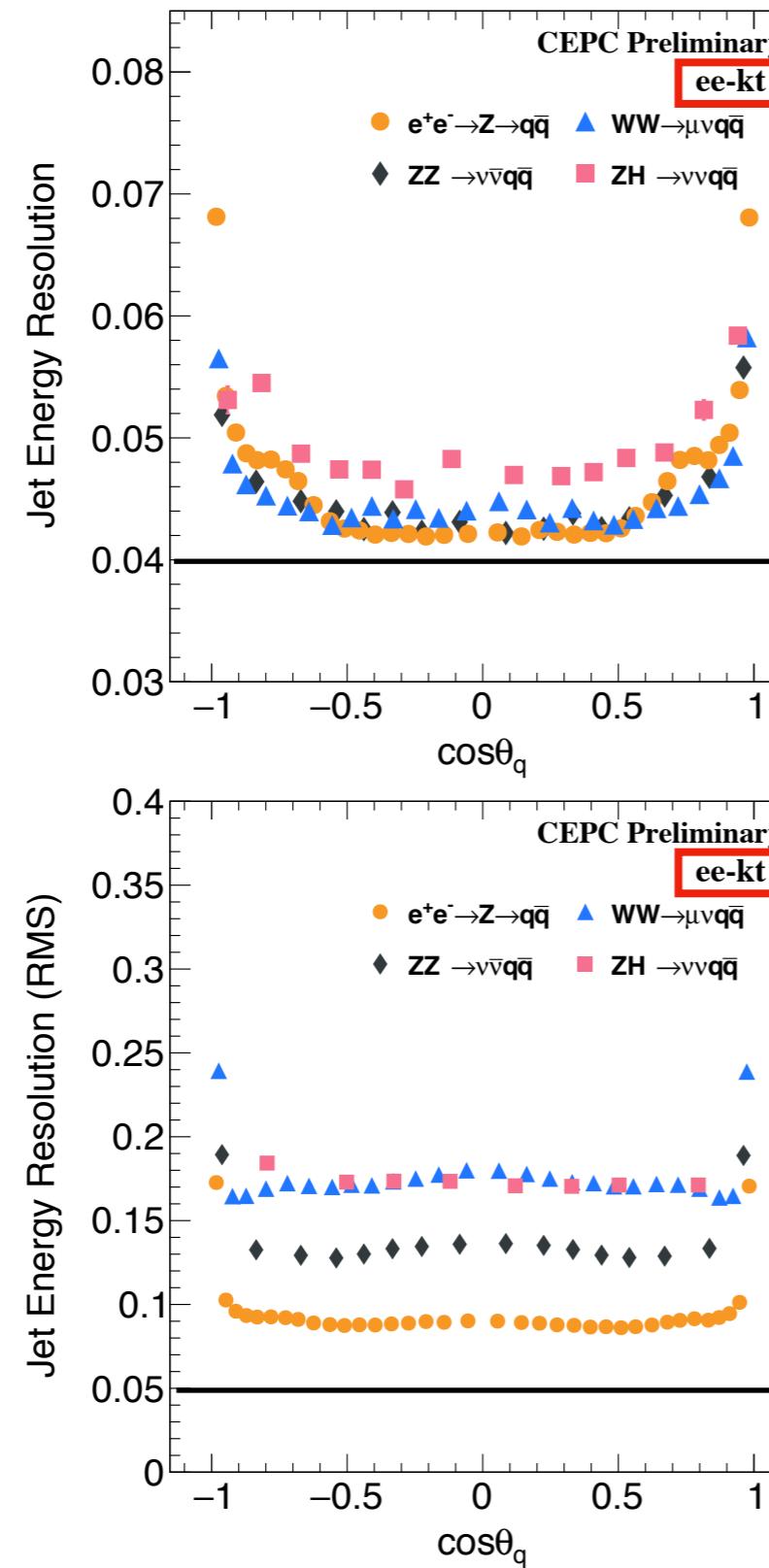
- Event-shape variables basic multi-variable analysis to separate 2, 4, and 6 jets final-state.

Yong-Feng Zhu

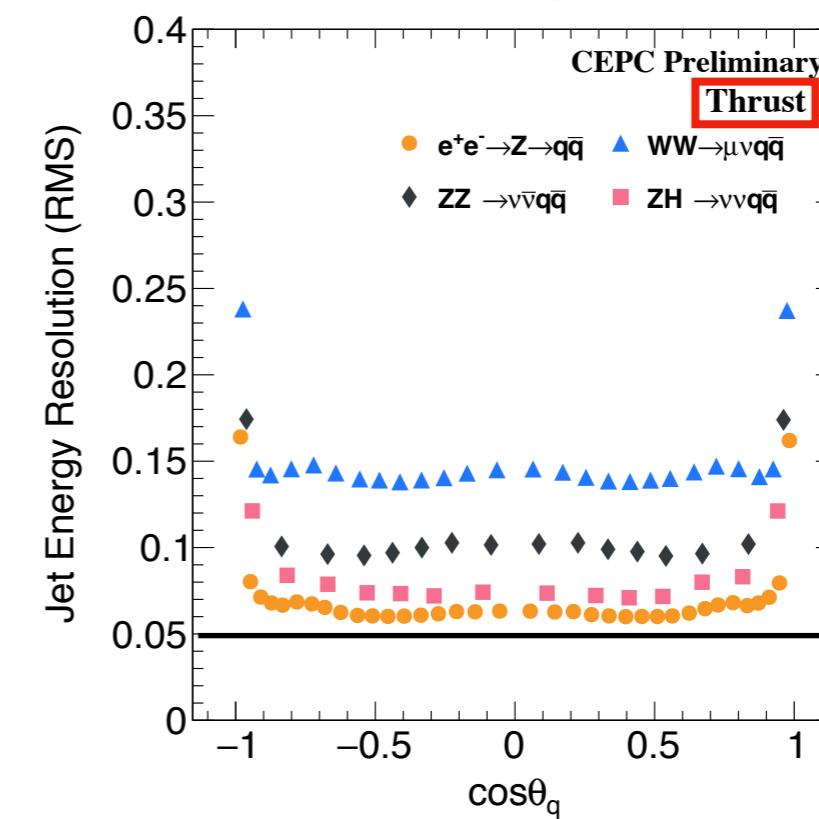
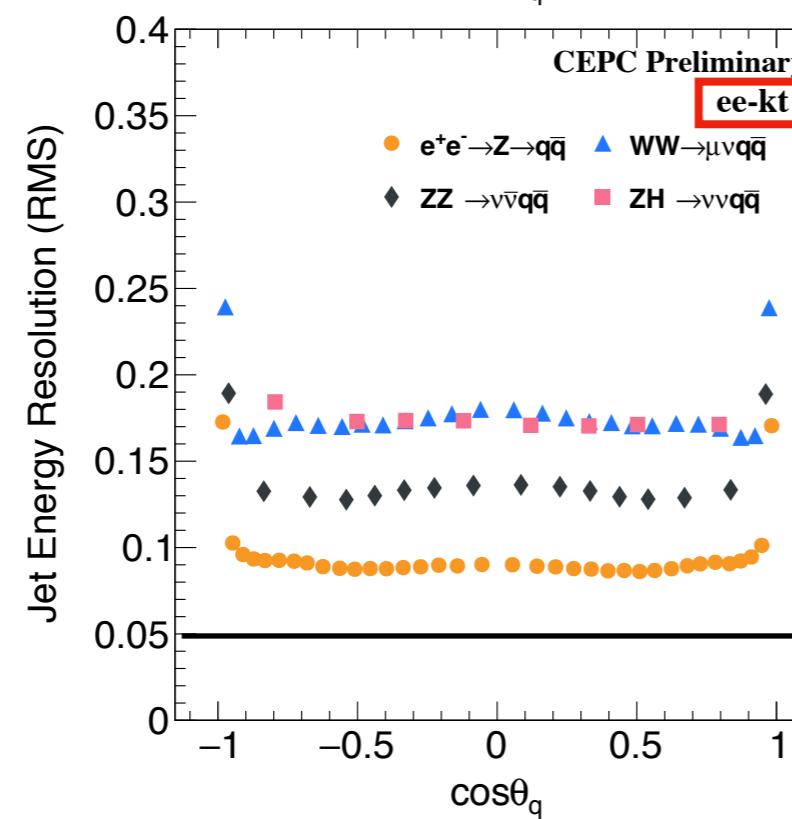


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# BM3: JER (ee- $k_t$ —Thrust)



Improved 20%  
w.r.t ee- $k_t$

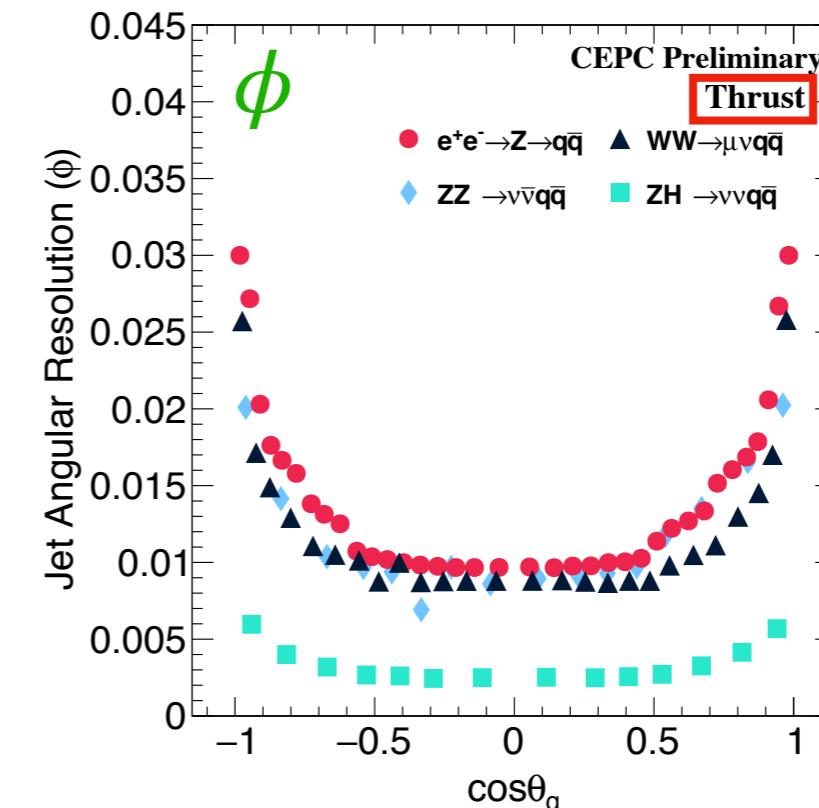
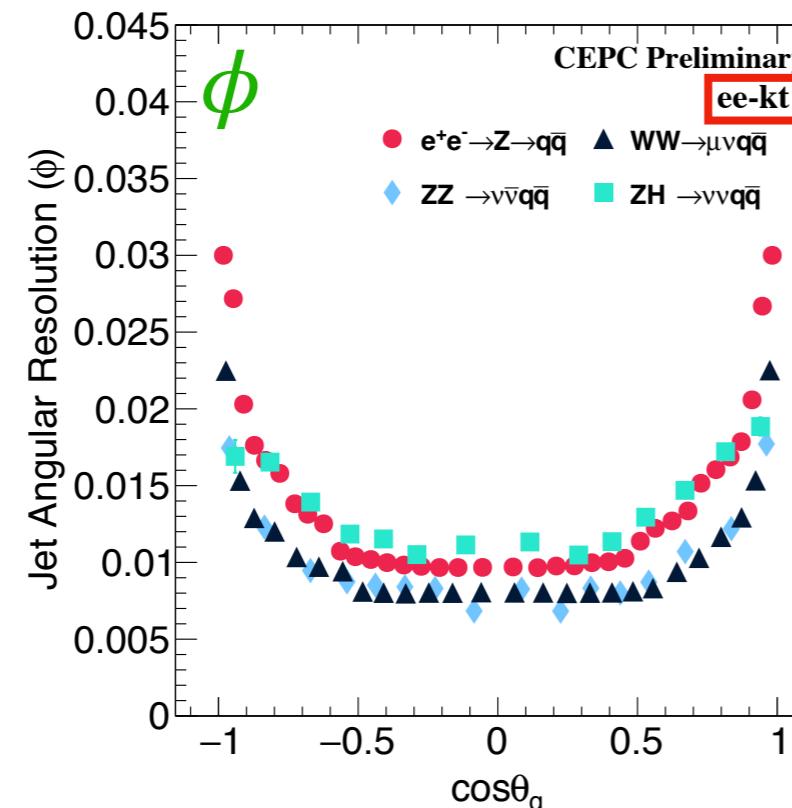
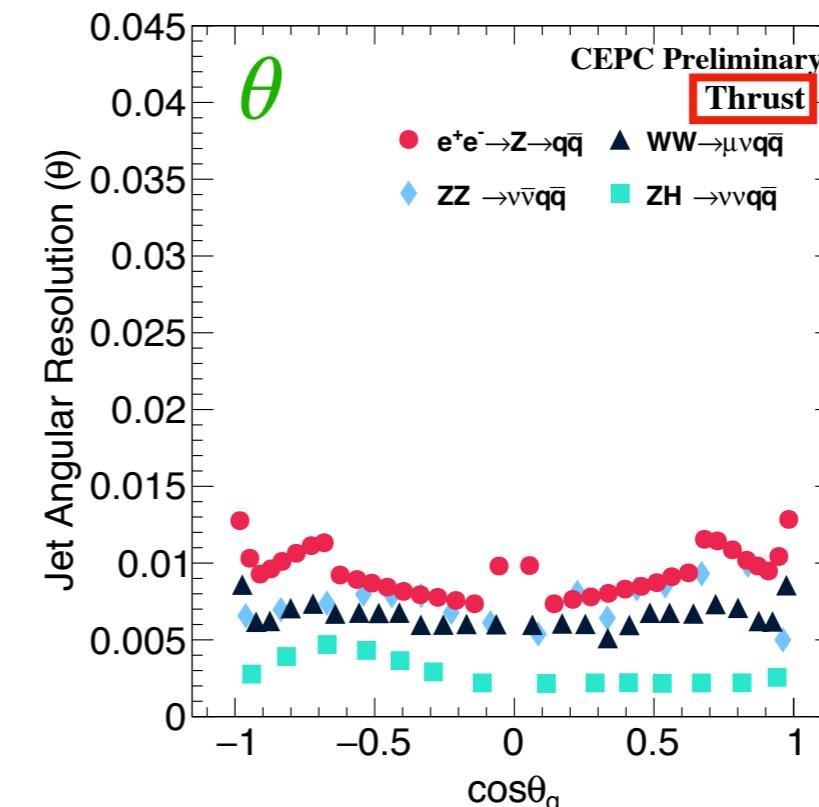
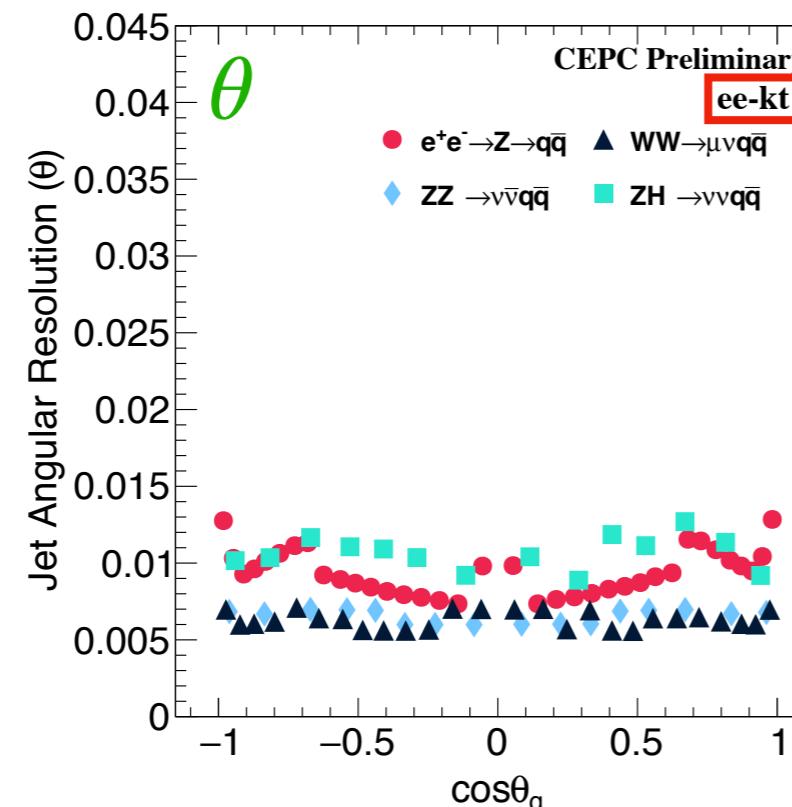


Improved 40%  
w.r.t ee- $k_t$

- Improvement maybe came from boosting the system back to the rest frame with the neutrons' information.



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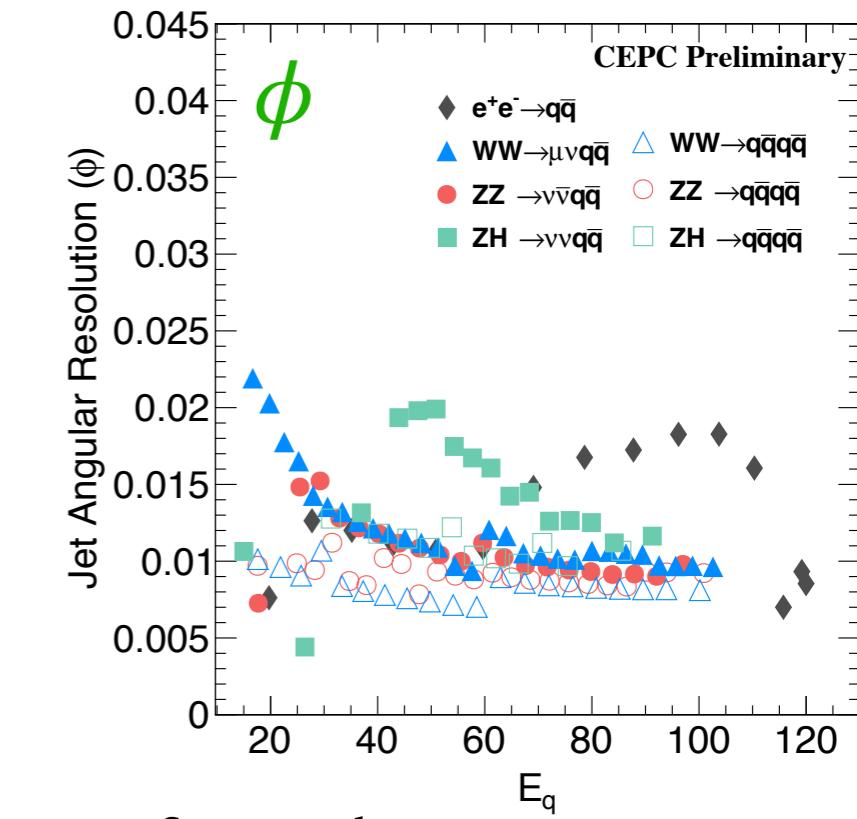
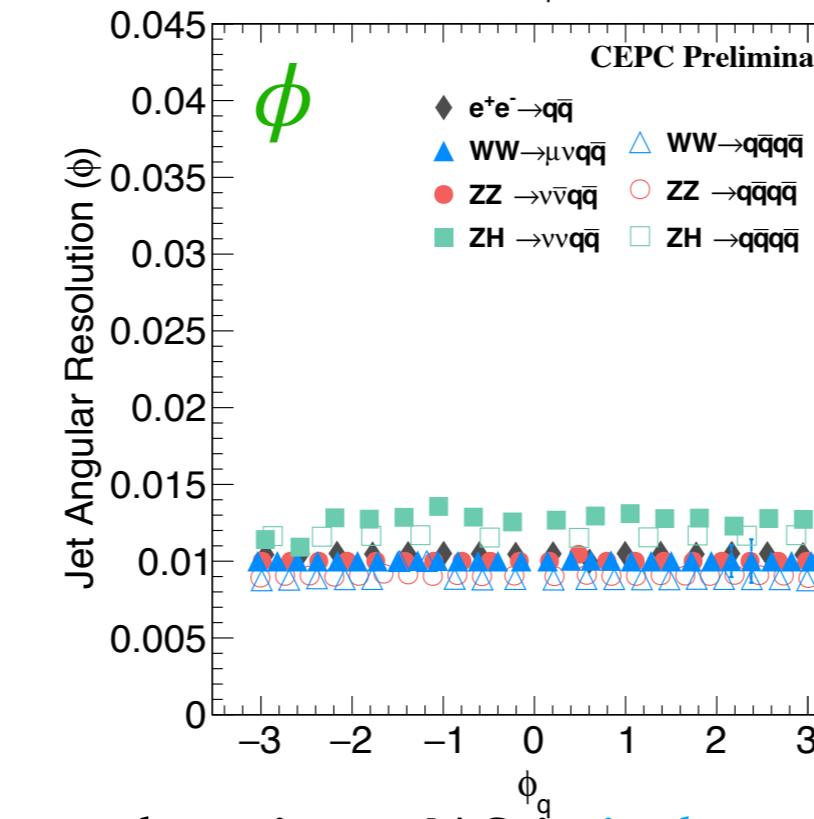
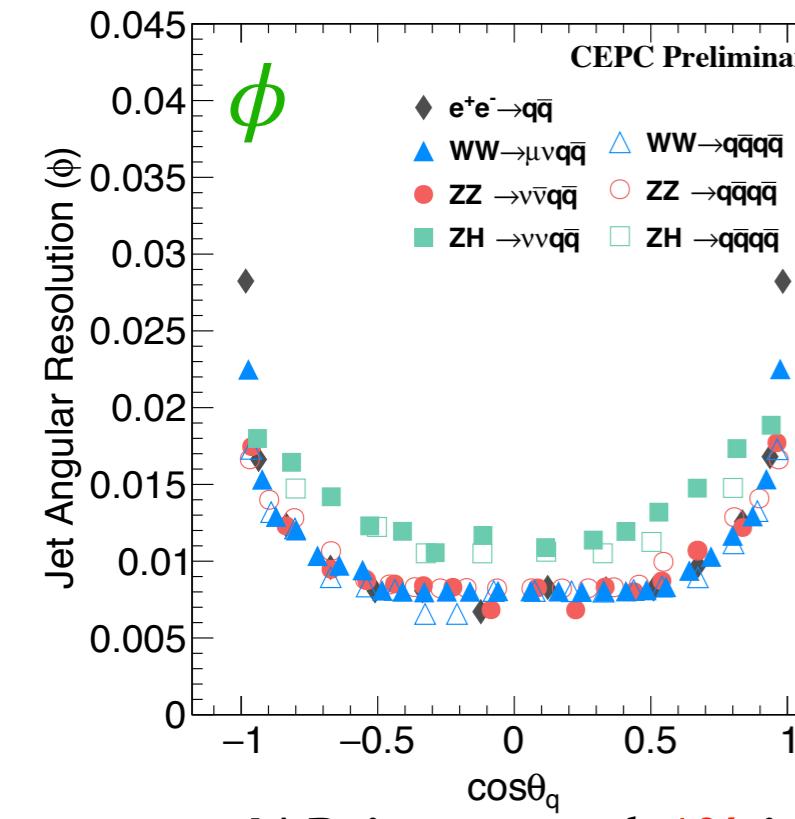
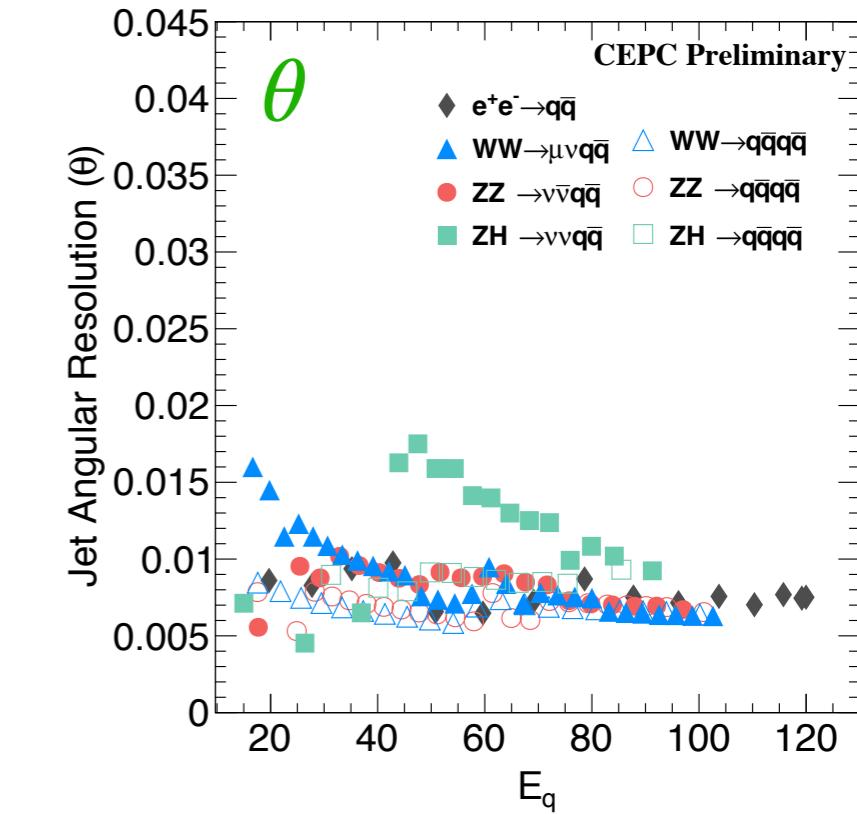
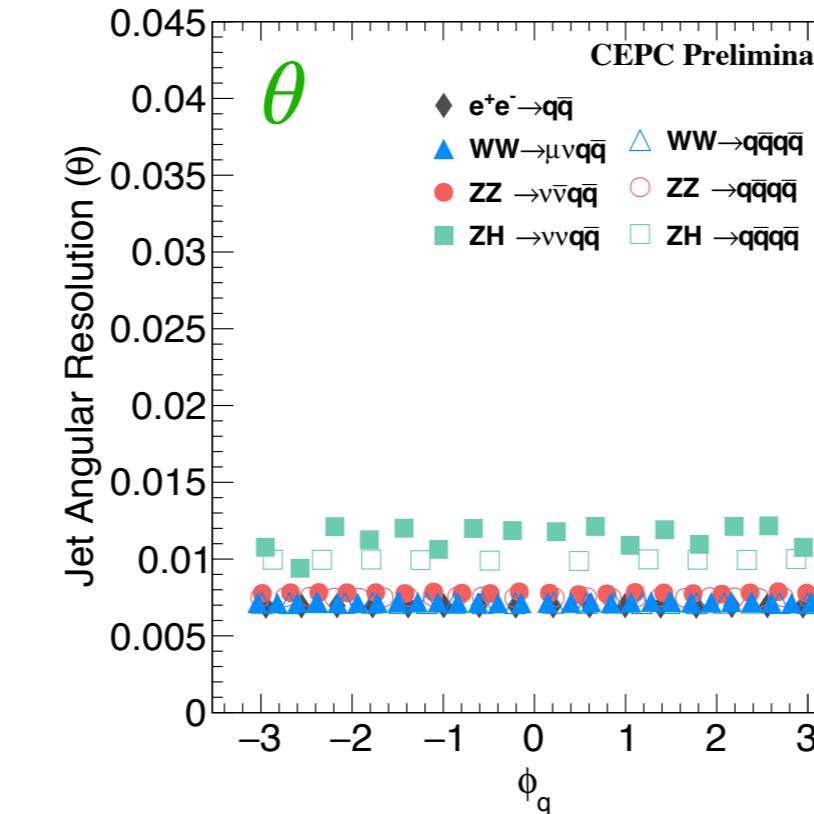
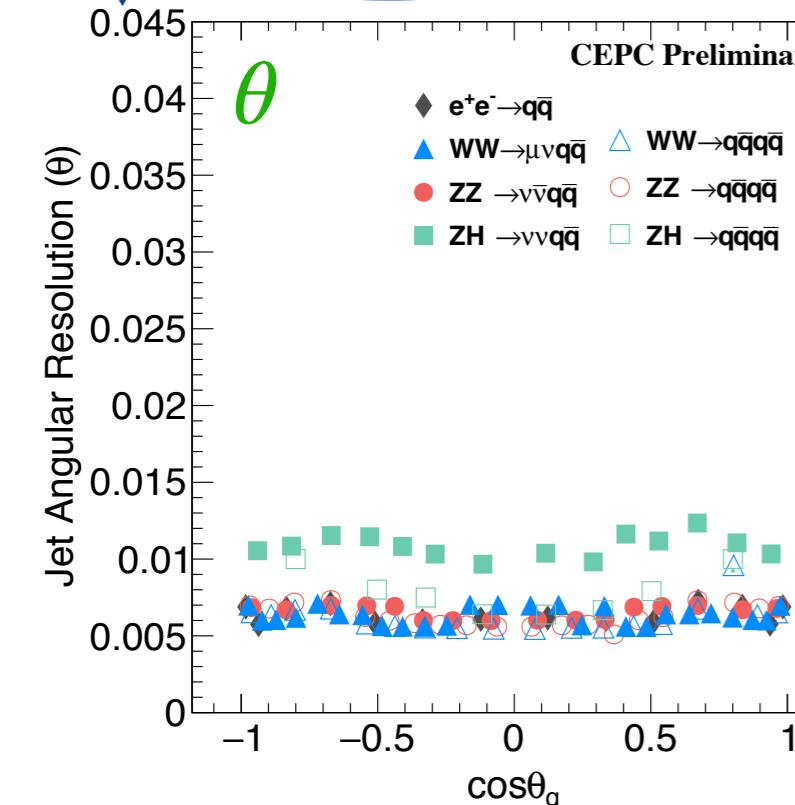
BM3: JAR (ee-k<sub>t</sub>—Thrust)

- Both of jet  $\theta$  and  $\phi$  angular resolution are also improved by thrust method, 20%.



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BM3: JAR



■ JAR is around 1% in barrel region; JAS is independent of  $\phi$  and energy.

■ The difference between 2 and 4 jets final-state is controlled within 1% level.

# Event-shape Variables

## Heavy Jet Mass

$$M_1^2 = \frac{1}{(\sqrt{s})^2} \left( \sum_i^N P_i \right)^2$$

$$M_2^2 = \frac{1}{(\sqrt{s})^2} \left( \sum_i^N P_i \right)^2$$

## Jet Broadening

$$B_1 = \frac{1}{2 \sum_{j=1}^N |P_j|} \sum_{i=1}^N |P_i \times n_T|, (P_i \times n_T) > 0$$

$$B_2 = \frac{1}{2 \sum_{j=1}^N |P_j|} \sum_{i=1}^N |P_i \times n_T|, (P_i \times n_T) < 0$$

## Jet Transition variable, $y_{23}$ , $y_{45}$ , $y_{67}$ ee-kt jet clustering algorithm

$$d_{ij} = 2\min(E_i^2, E_j^2)(1 - \cos\theta_{ij})$$

## C and D Parameter

$$L^{ab} = \frac{1}{\sum_{j=1}^N |P_j|} \sum_{i=1}^N \frac{P_i^a P_i^b}{|P_i|}$$

$$C = 3(\lambda_1\lambda_2 + \lambda_1\lambda_3 + \lambda_2\lambda_3)$$

$$D = 27\lambda_1\lambda_2\lambda_3$$

## Energy-Energy Correlation

$$EEC = \frac{1}{\sigma_{tot}} \sum_{ij} \int d\sigma \frac{E_i E_j}{Q^2} \delta(\cos\chi - \cos\theta_{ij})$$

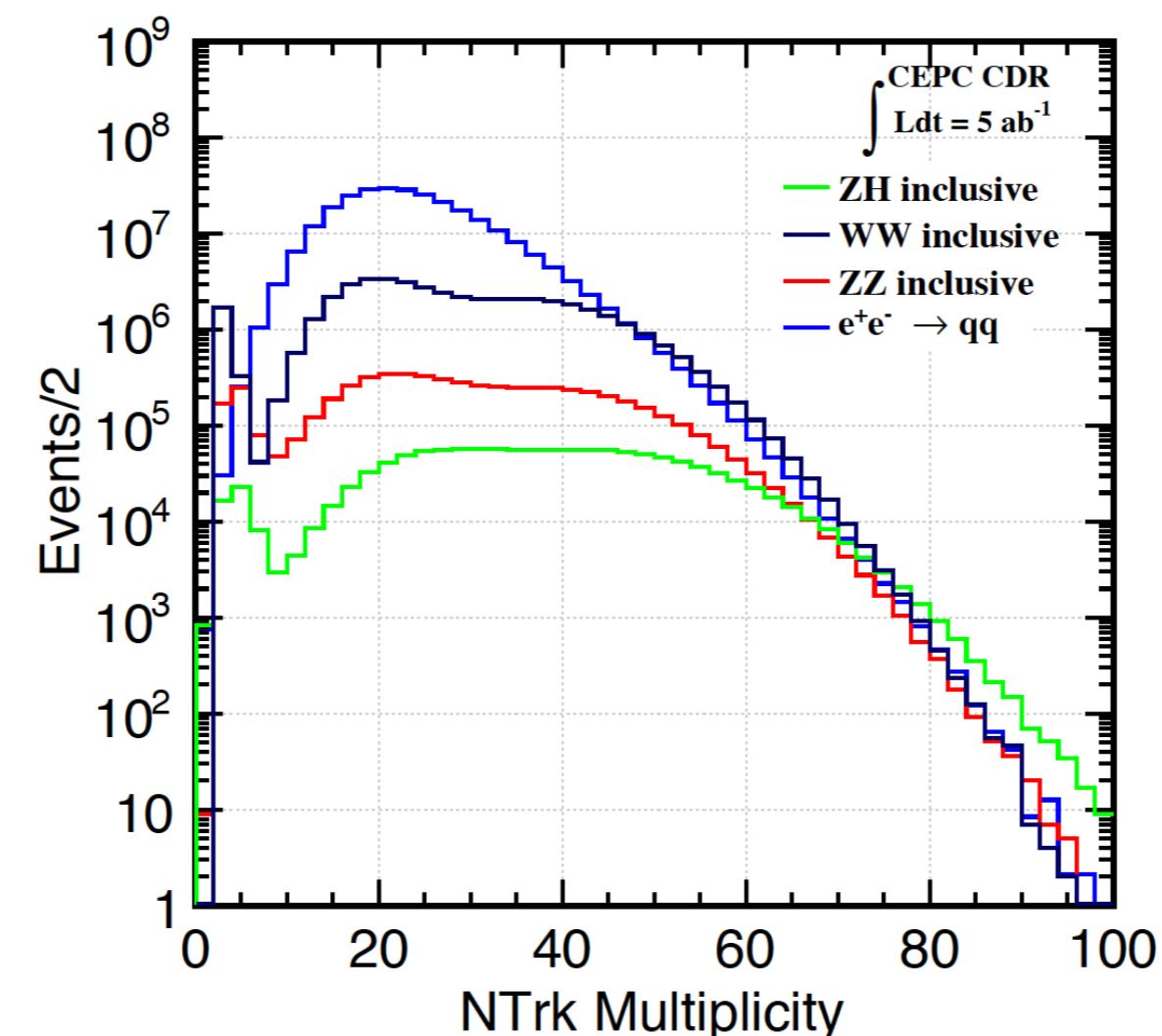
$$likelihood = \frac{\sum (P1_i) \times P2_i}{\sqrt{\sum (P1_i \times P2_i) \times \sum (P2_i \times P2_i)}}$$

# Double-sided Crystal Ball

$$f(x|\alpha_1, \alpha_2, n_1, n_2, \bar{x}, \sigma) = \begin{cases} \left(\frac{n_1}{|\alpha_1|}\right)^{n_1} e^{-\frac{|\alpha_1|^2}{2}} \left(\frac{n_1}{|\alpha_1|} - |\alpha_1| - \frac{x - \bar{x}}{\sigma}\right)^{-n_1} & \frac{x - \bar{x}}{\sigma} < -\alpha_1 \\ e^{-\frac{1}{2}\left(\frac{x - \bar{x}}{\sigma}\right)^2} & -\alpha_1 < \frac{x - \bar{x}}{\sigma} < \alpha_2 \\ \left(\frac{n_2}{|\alpha_2|}\right)^{n_2} e^{-\frac{|\alpha_2|^2}{2}} \left(\frac{n_2}{|\alpha_2|} - |\alpha_2| - \frac{x + \bar{x}}{\sigma}\right)^{-n_2} & \alpha_2 < \frac{x - \bar{x}}{\sigma} \end{cases}$$



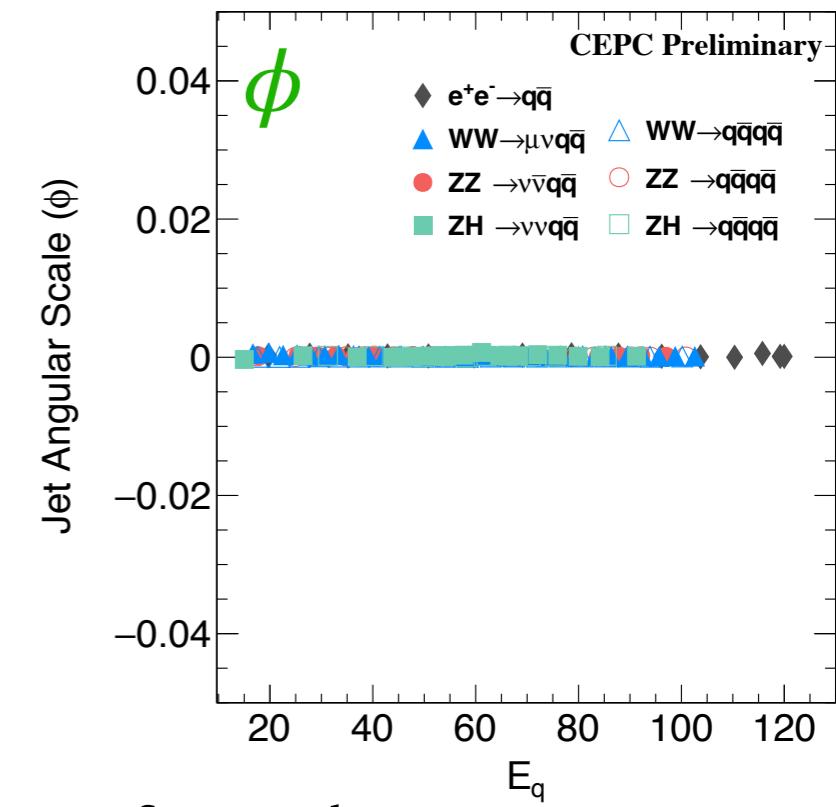
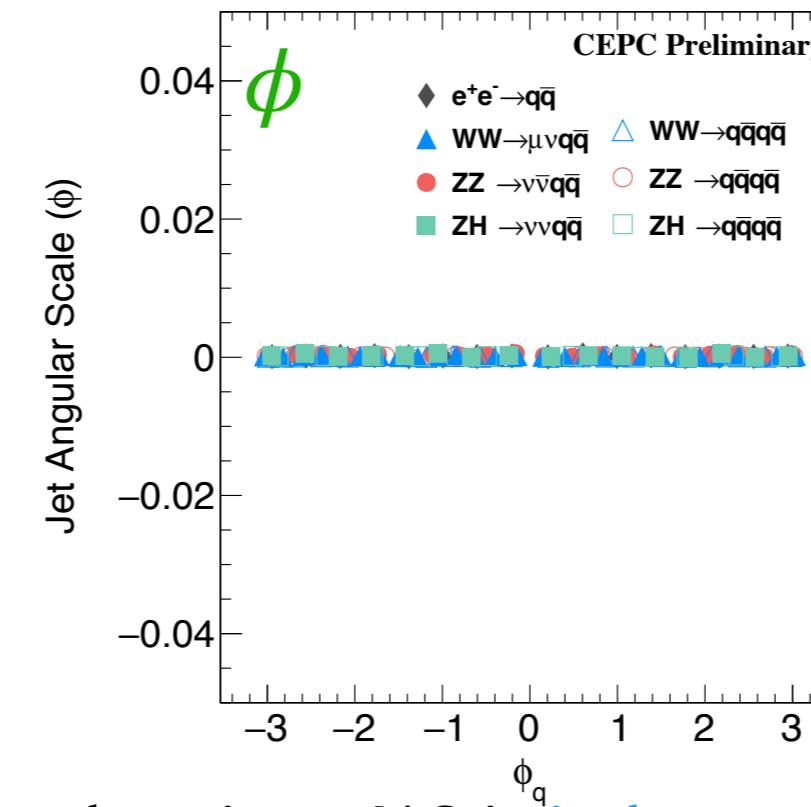
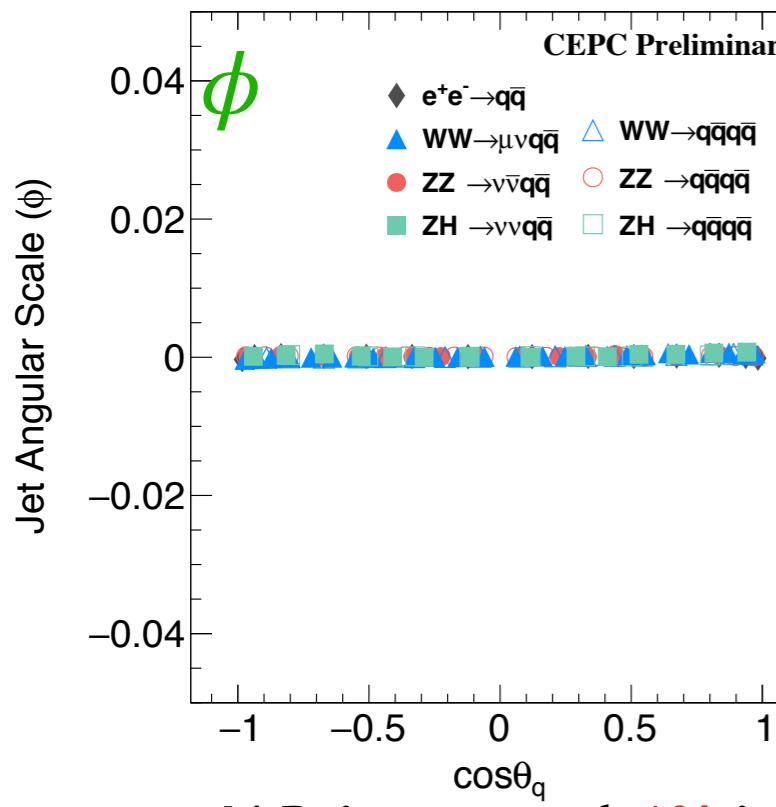
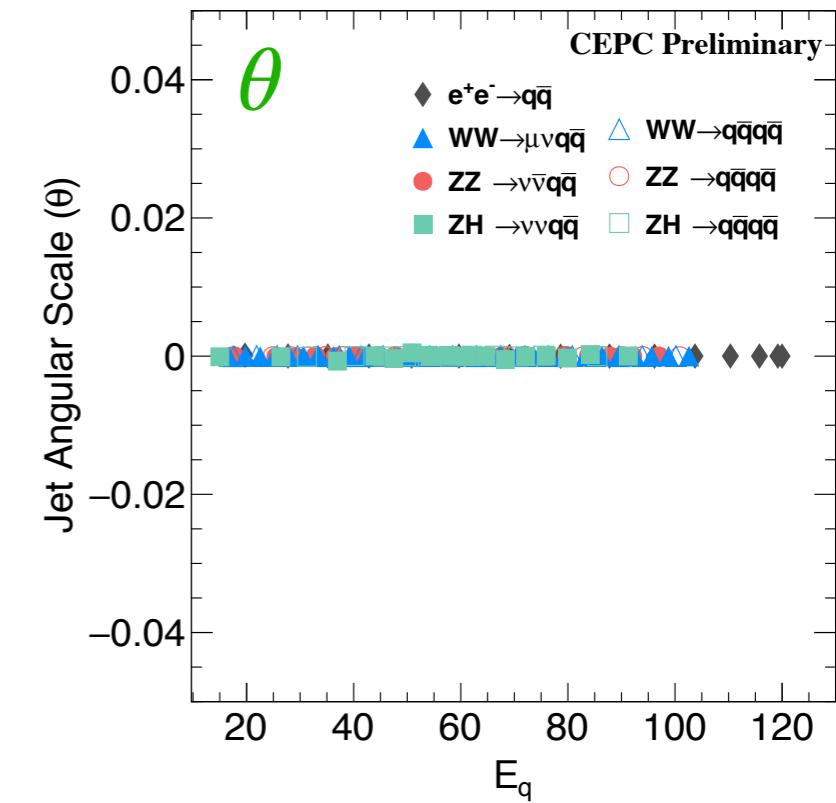
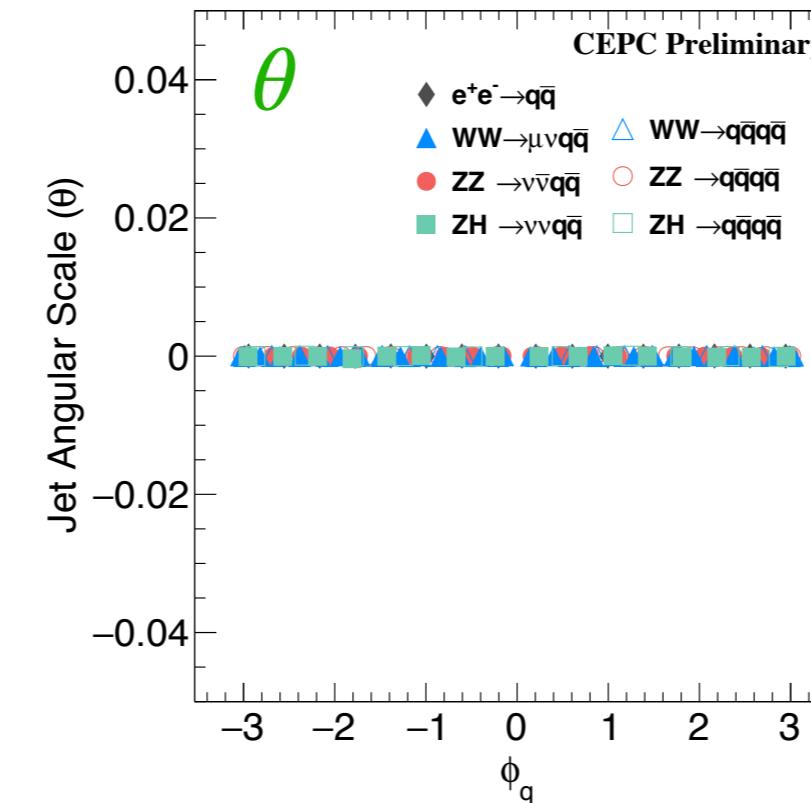
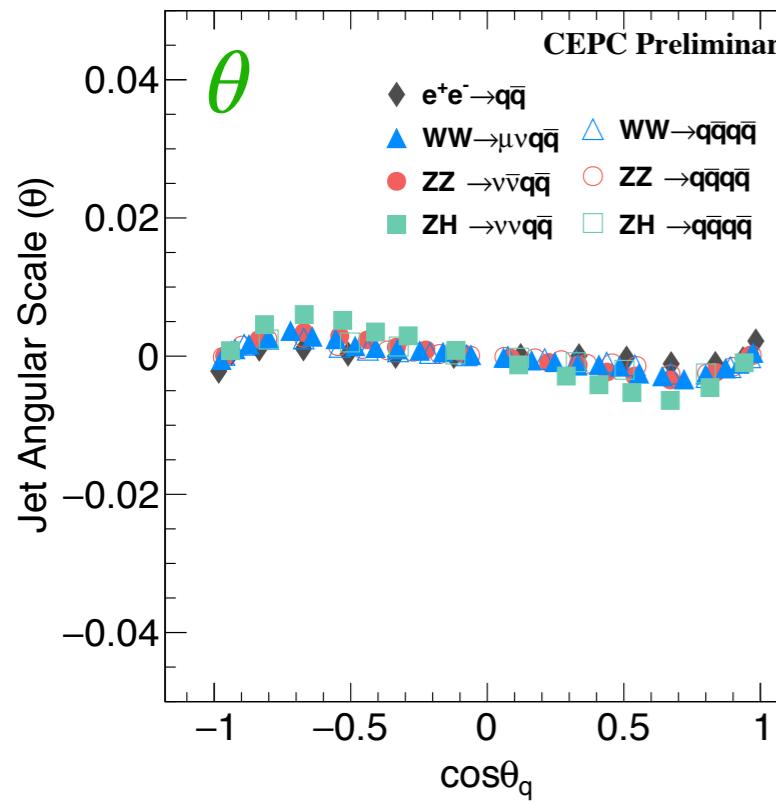
# Jet Multiplicity





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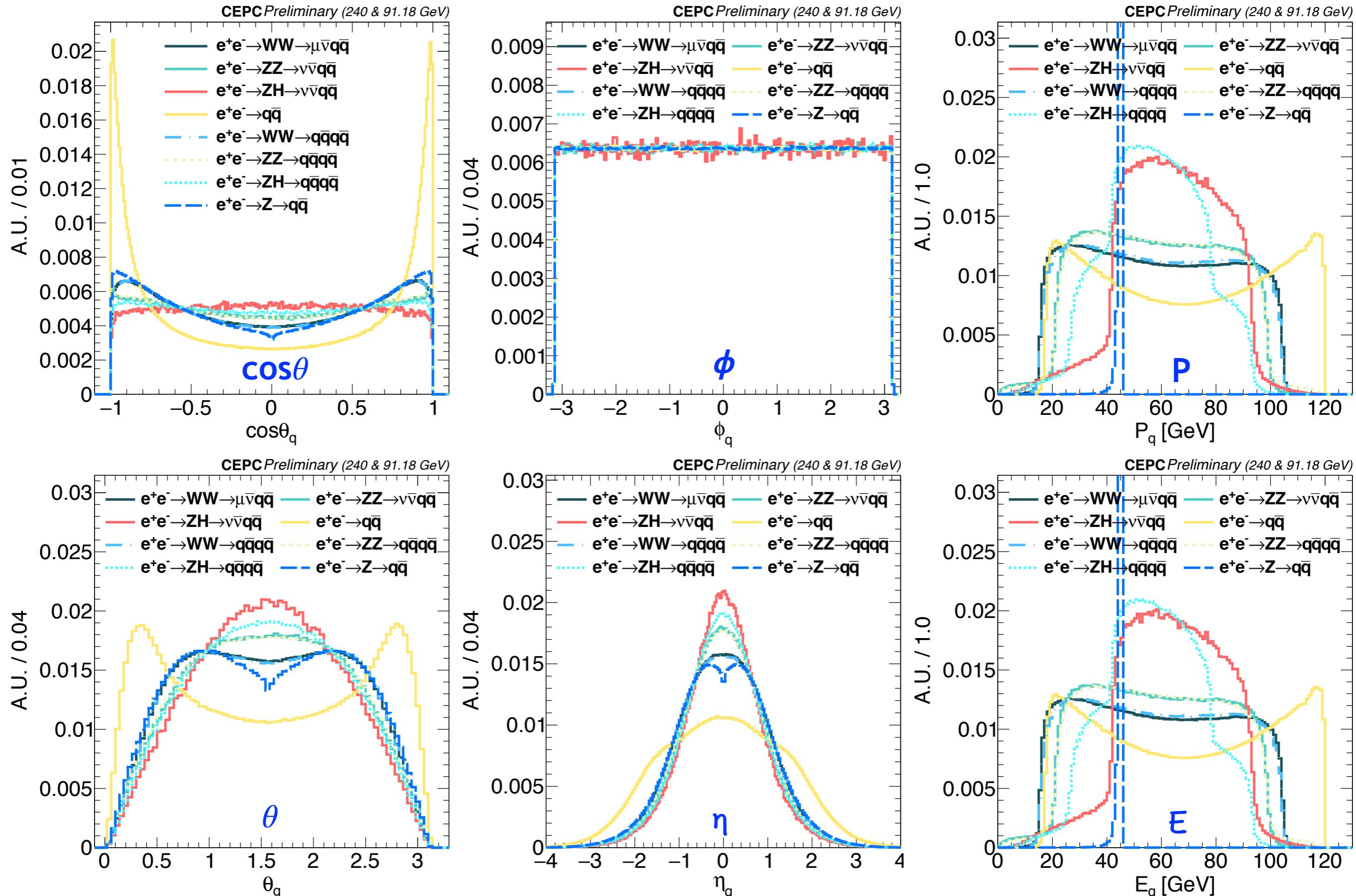
## BM3: JAS (Reco-Gen)



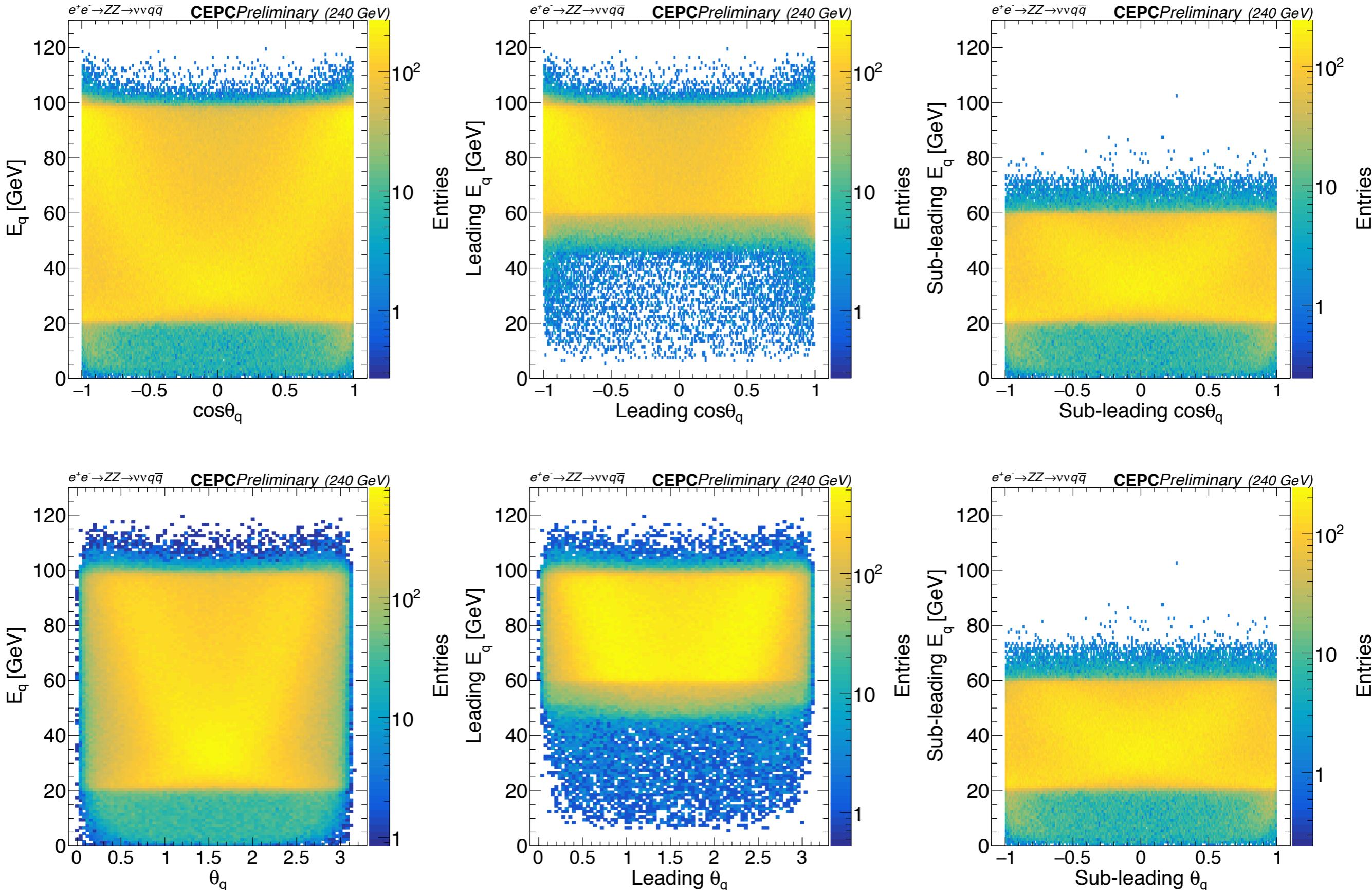
■ JAR is around 1% in barrel region; JAS is independent of  $\phi$  and energy.

■ The difference between 2 and 4 jets final-state is controlled within 1% level.

# Kinematic Summary Plots(Parton level)



# E as the function of the polar angle

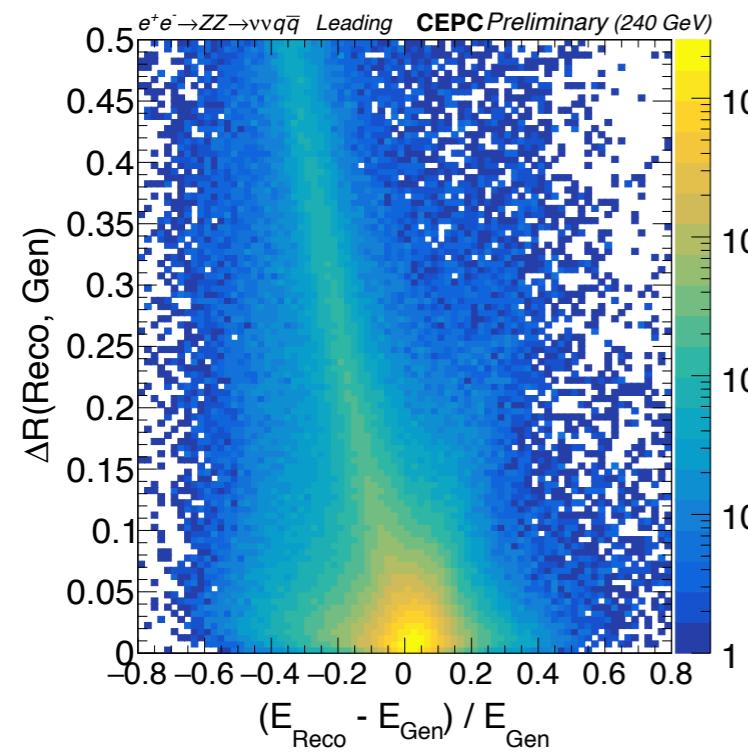




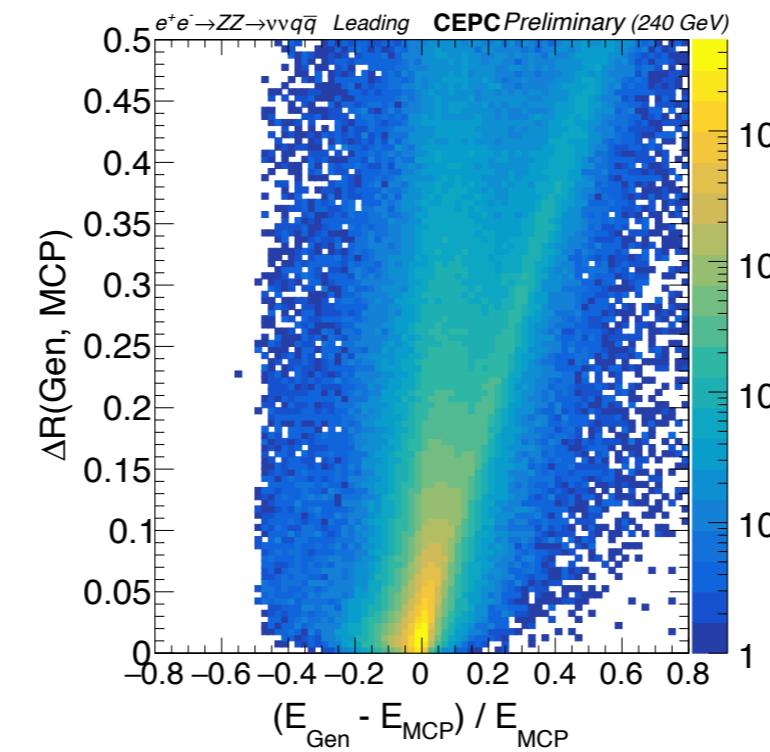
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# $\Delta R$ as the function of $\Delta E$

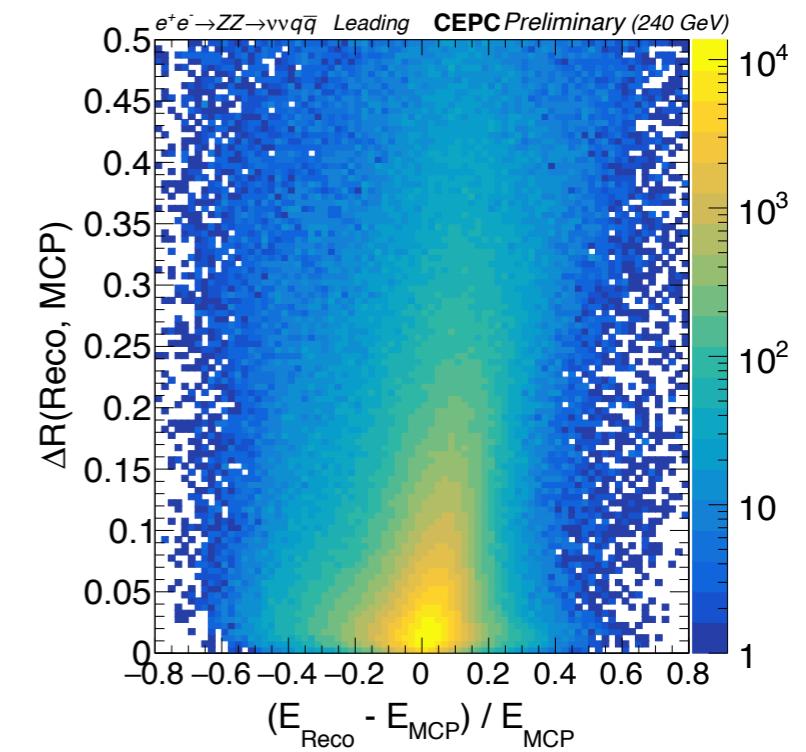
**Leading, Gen-MCP**



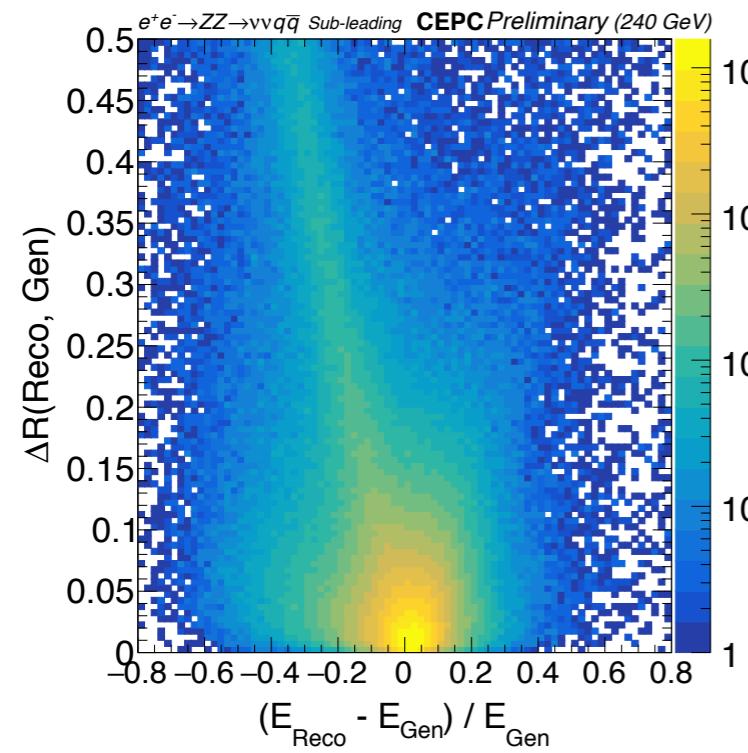
**Leading, Reco-Gen**



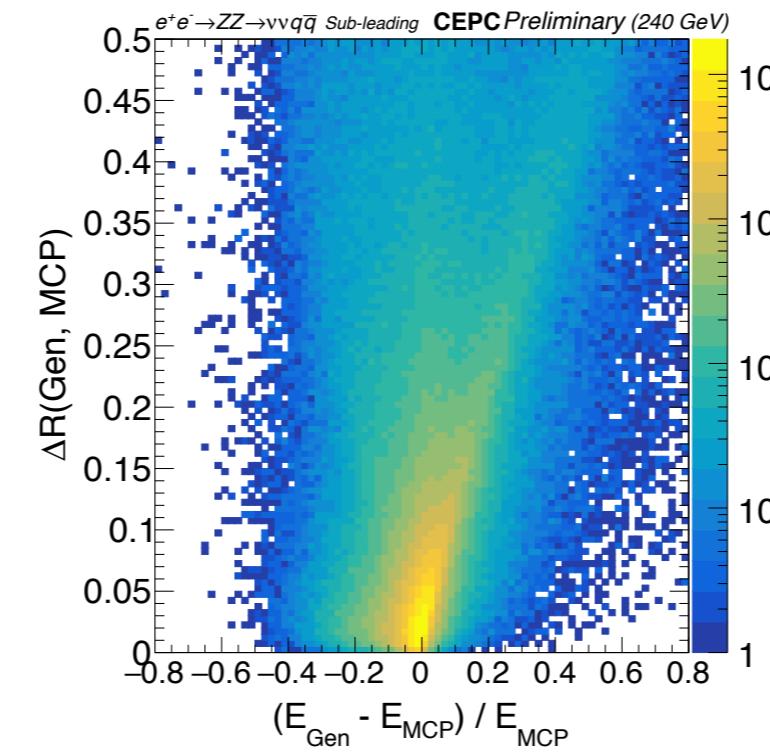
**Leading, Reco-MCP**



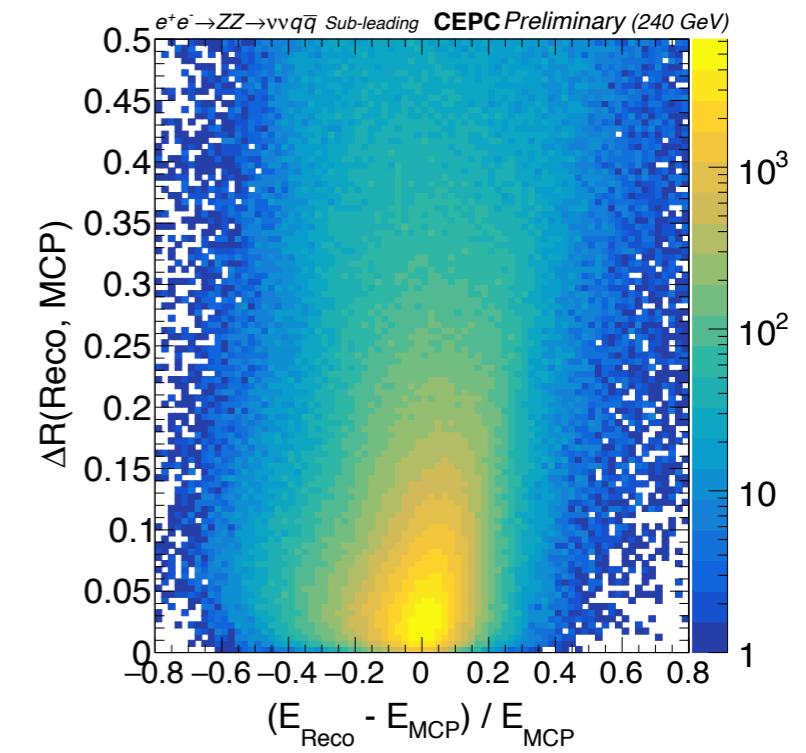
**Sub-leading, Gen-MCP**



**Sub-leading, Reco-Gen**



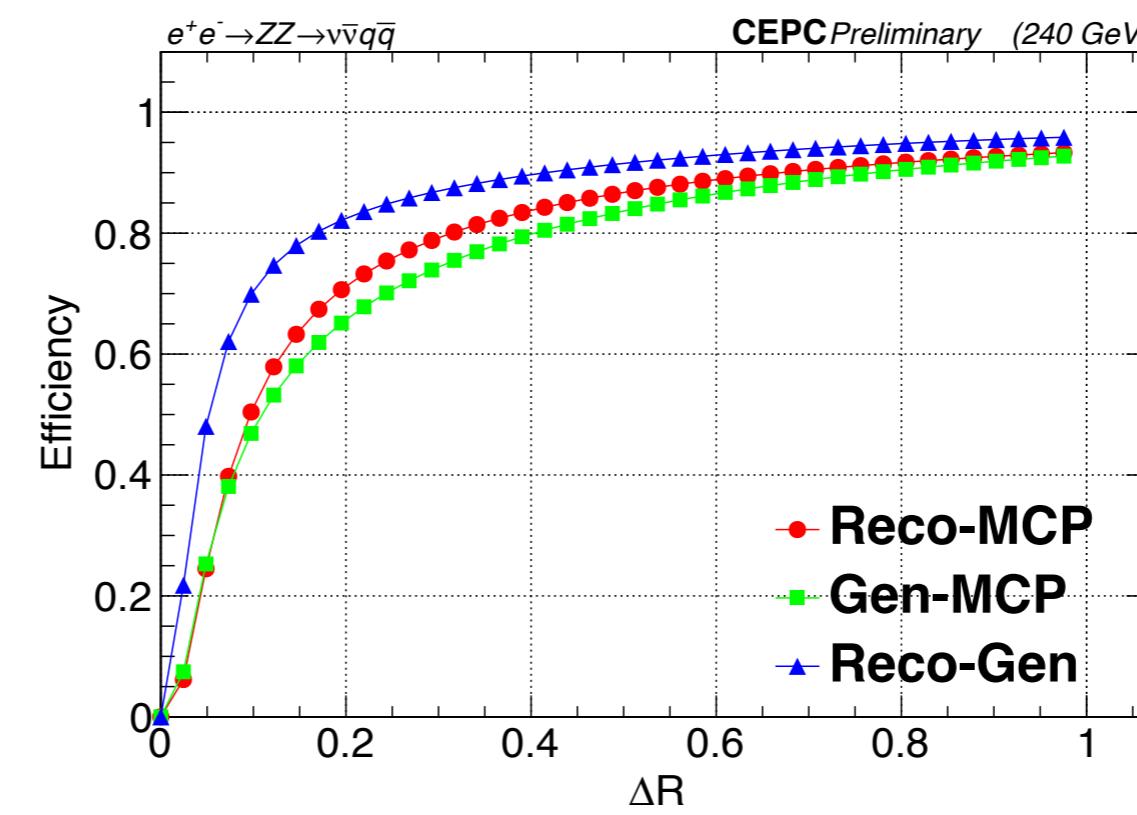
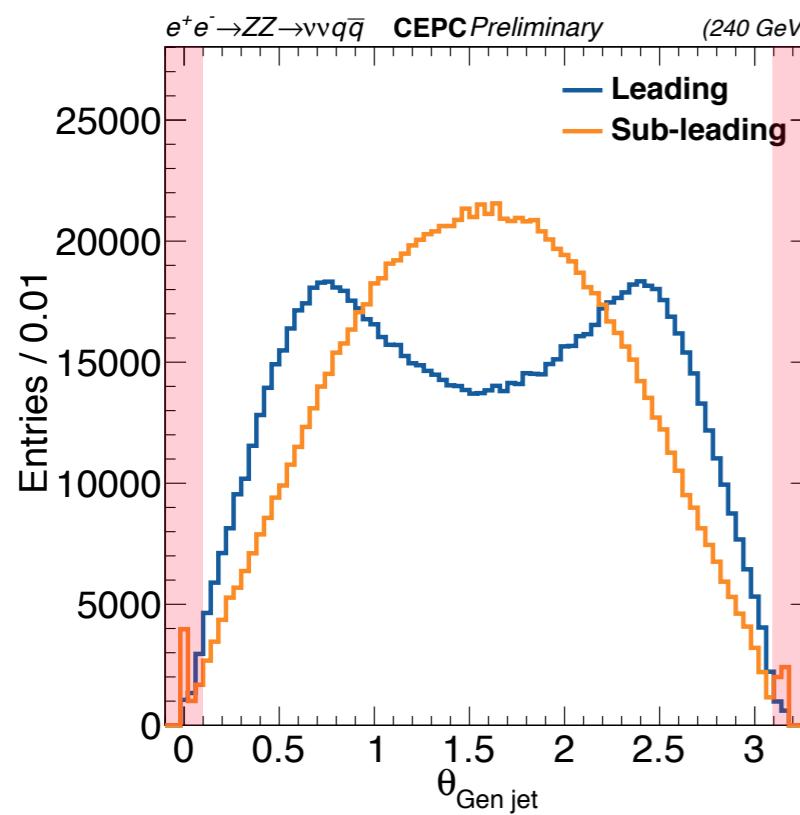
**Sub-leading, Reco-MCP**



The jet clustering brings a significant uncertainty.



Items	(Reco-Gen)	(Gen-MCP)
$\theta_{\text{Gen jet}} > 0.1 \text{ \& } \theta_{\text{Gen jet}} < 3.1$	✓	✓
$\Delta R(\text{Reco-MCP}) < 0.1$	✓	✗



Efficiency =  
$$\frac{\# \text{ of leftover event}}{\# \text{ of total event}}$$

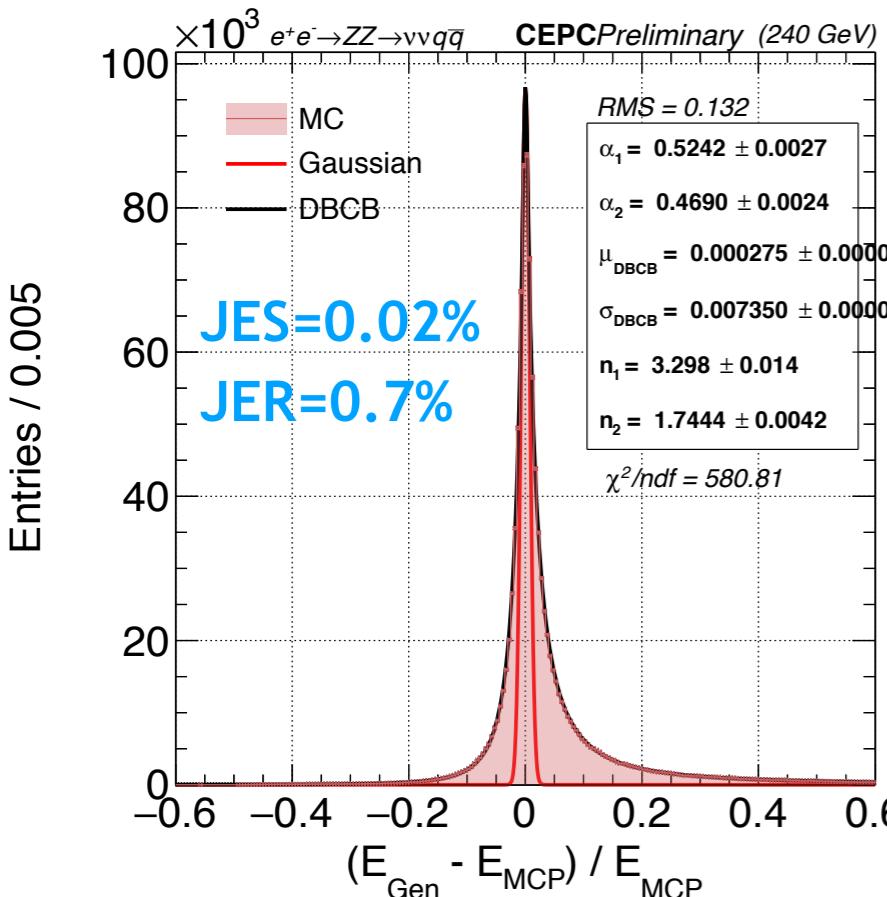
$$\Delta R = \sqrt{\Delta\phi^2 + \Delta\eta^2}$$



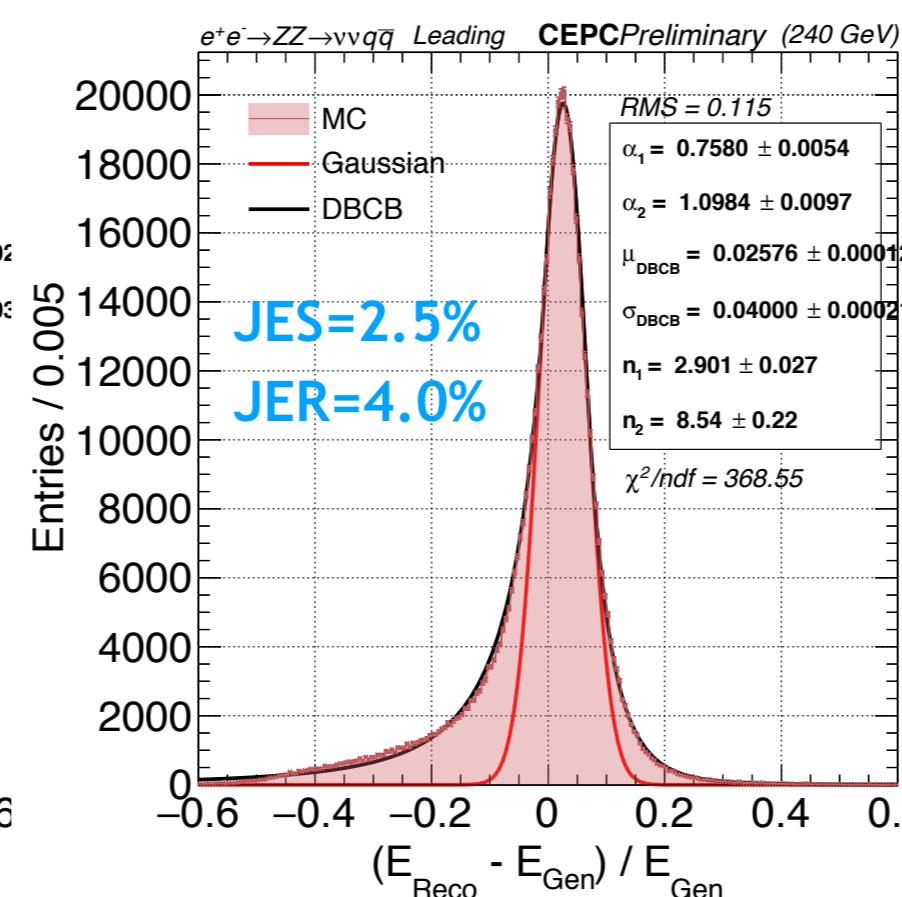
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# Leading JER & JES

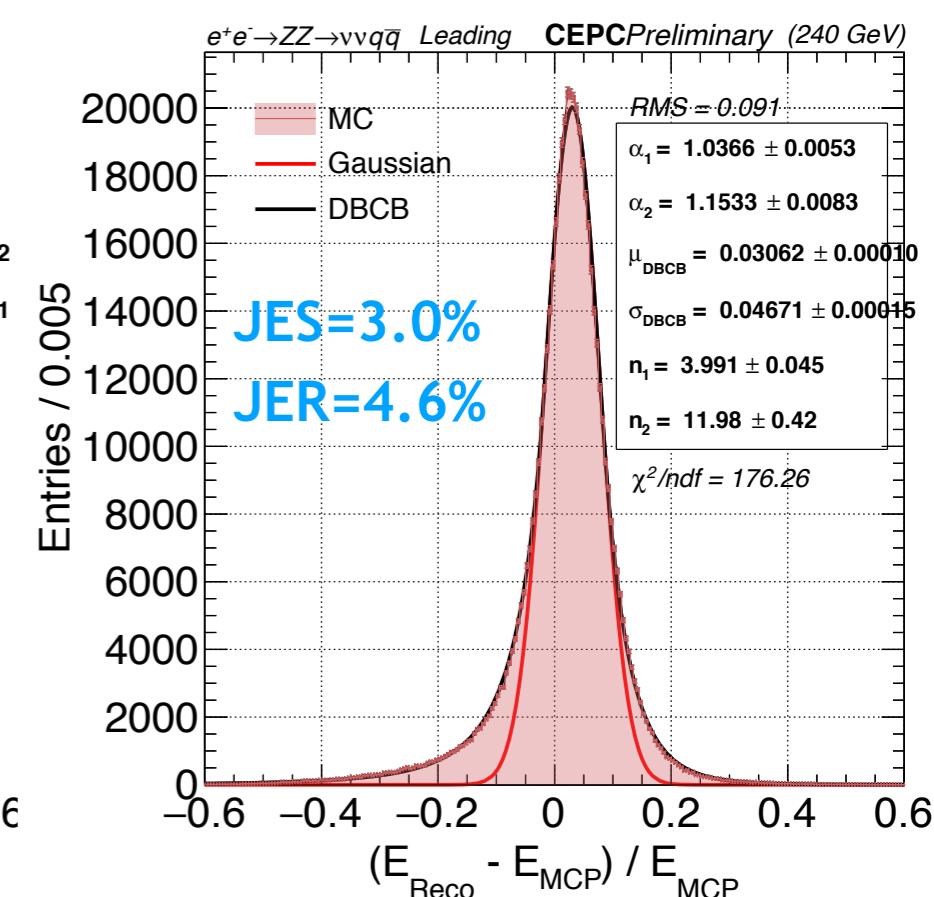
Gen-MCP



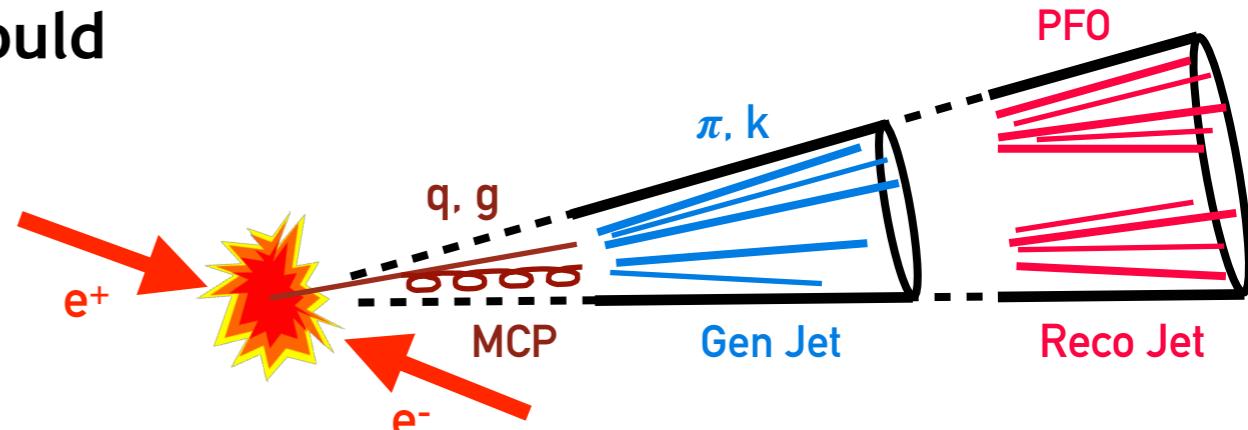
Reco-Gen



Reco-MCP



- JER/JES between Reco jet and MCP would combine the effects of two previous stages.

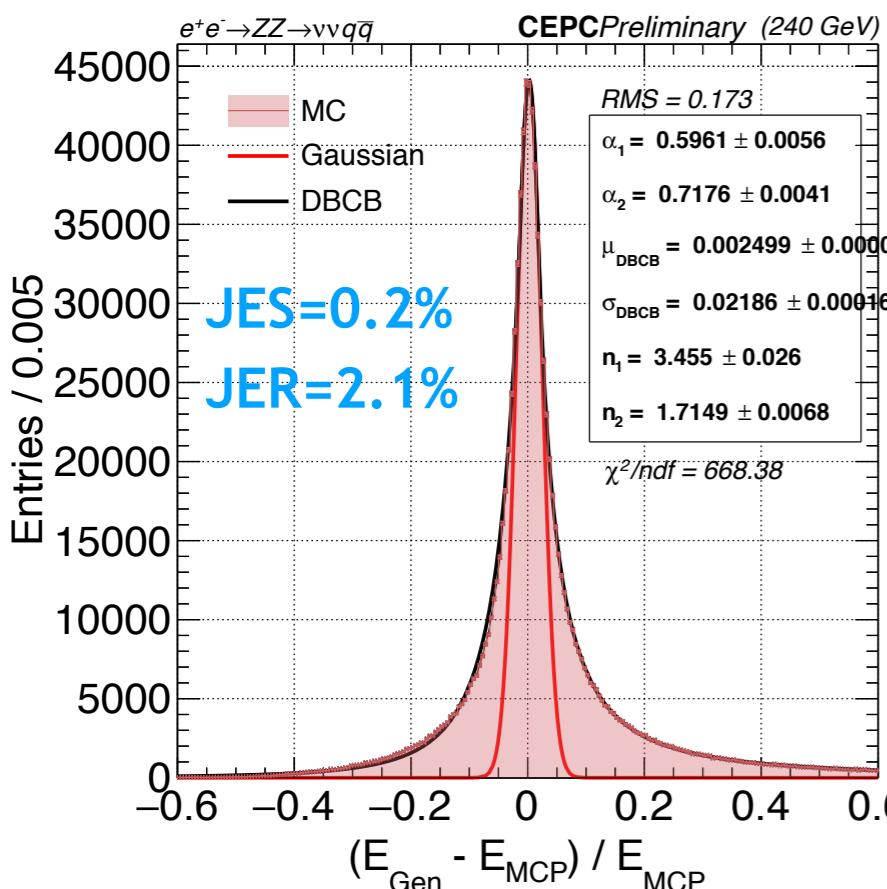




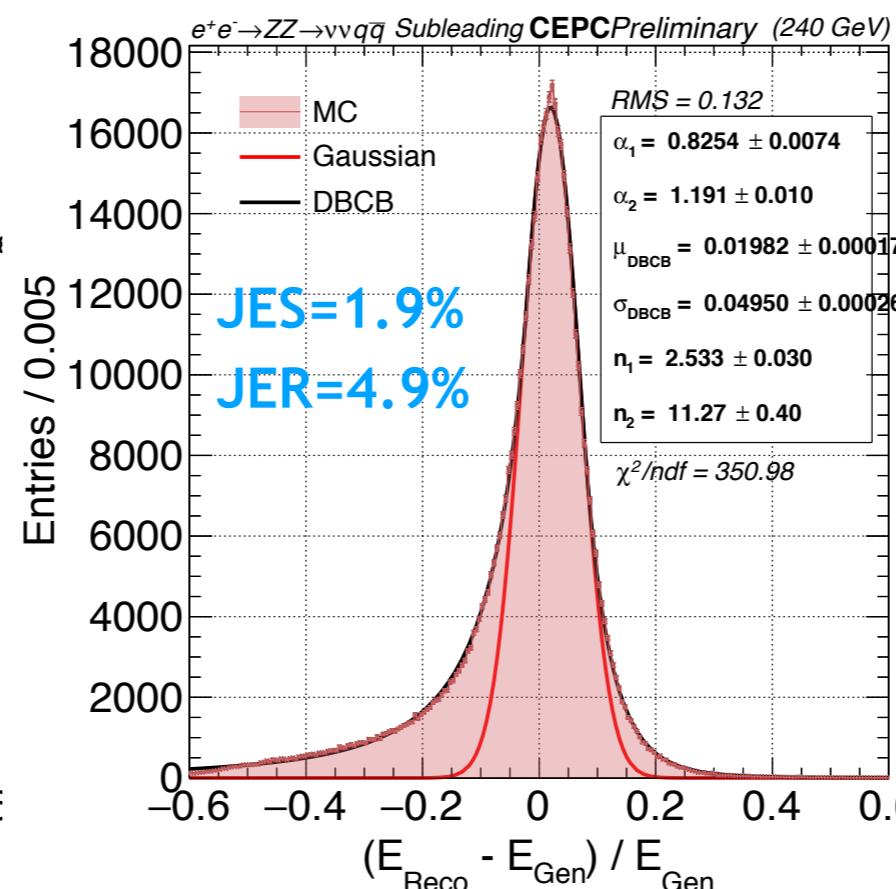
CEPC

# Sub-leading JER & JES

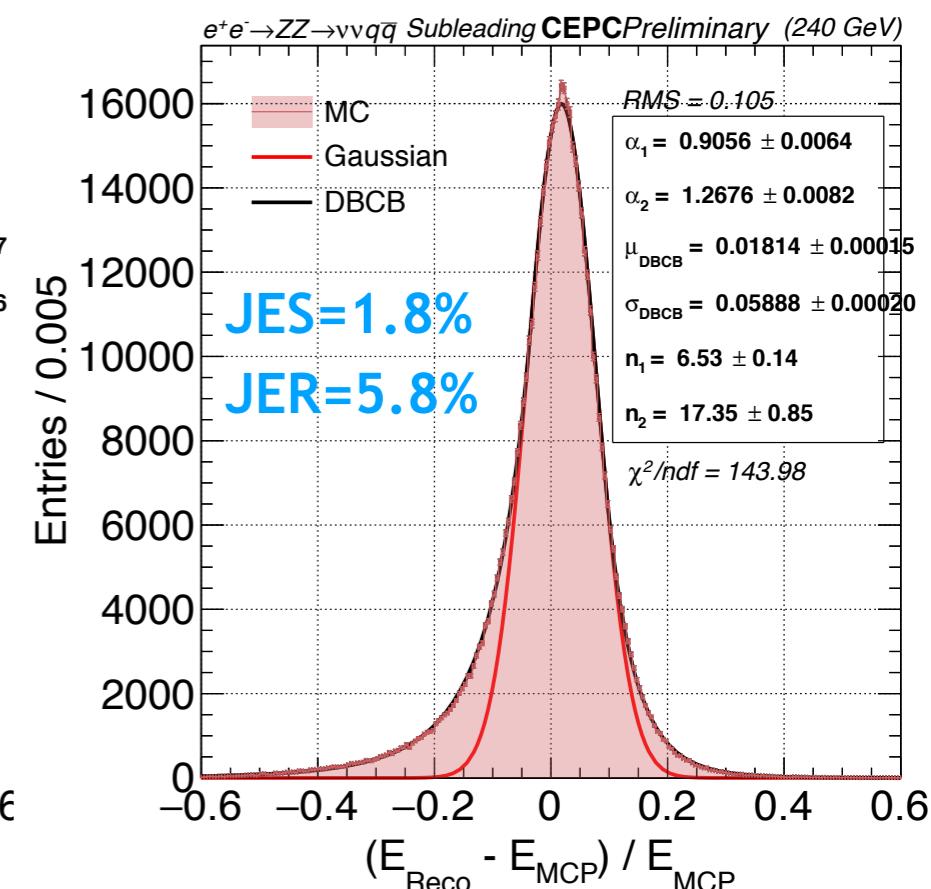
Gen-MCP



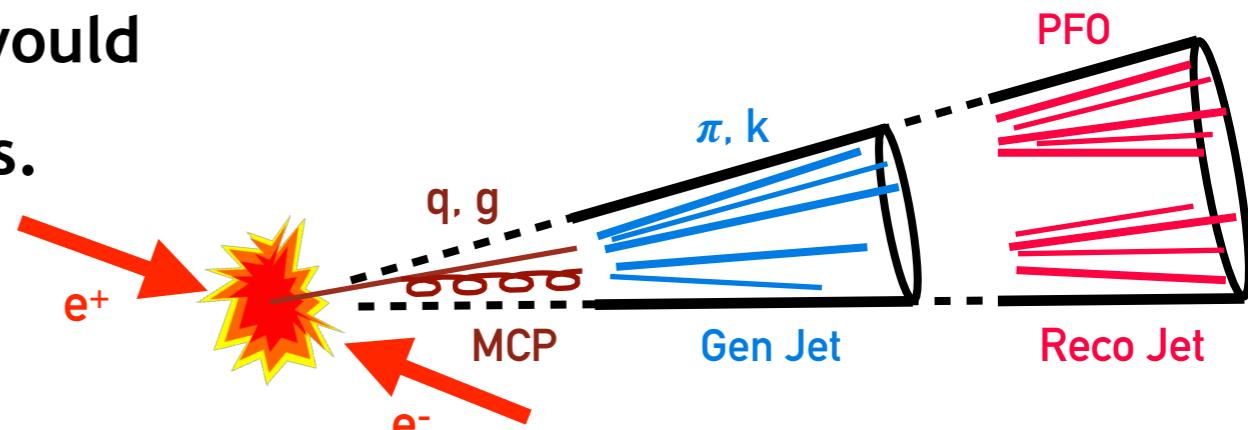
Reco-Gen

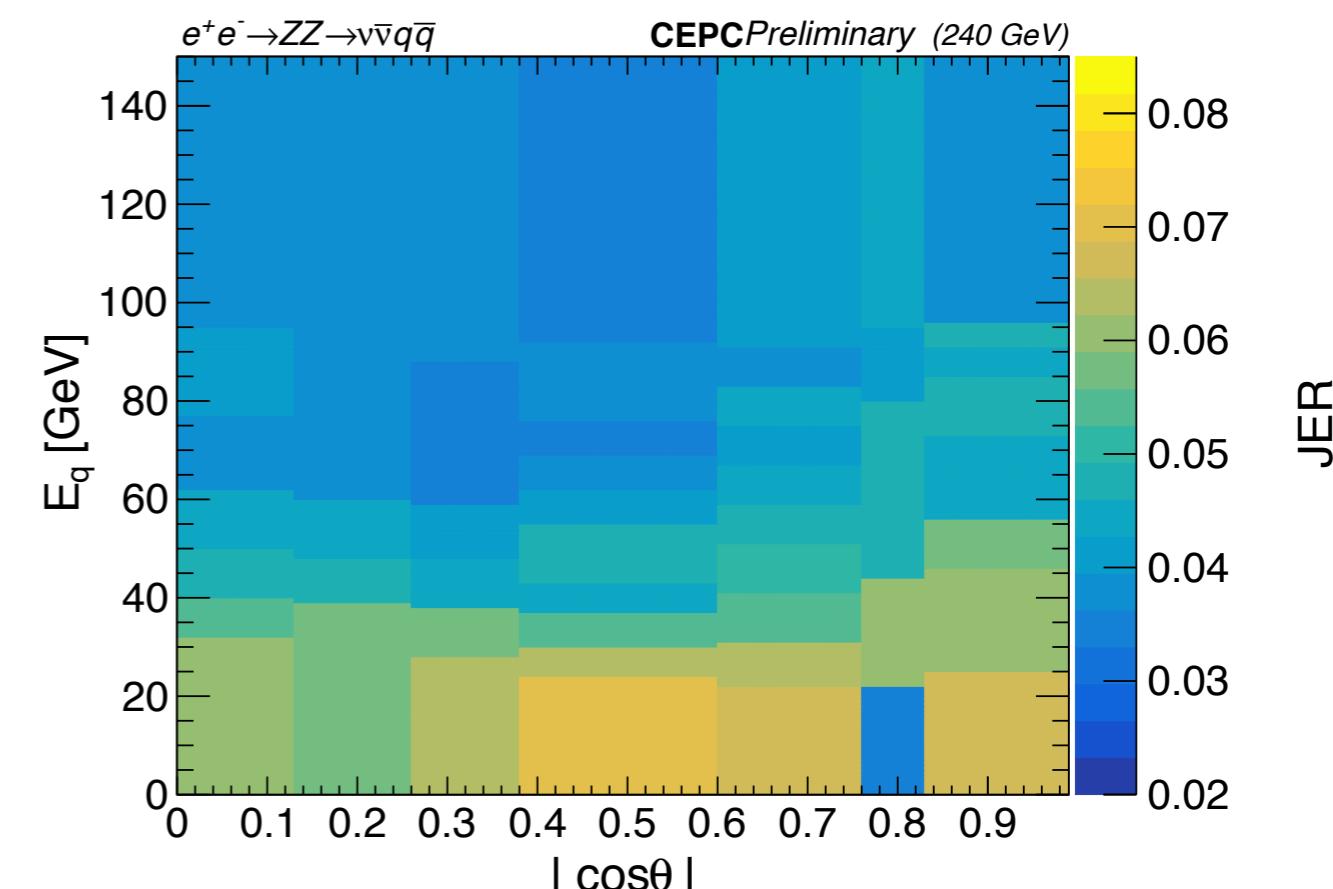
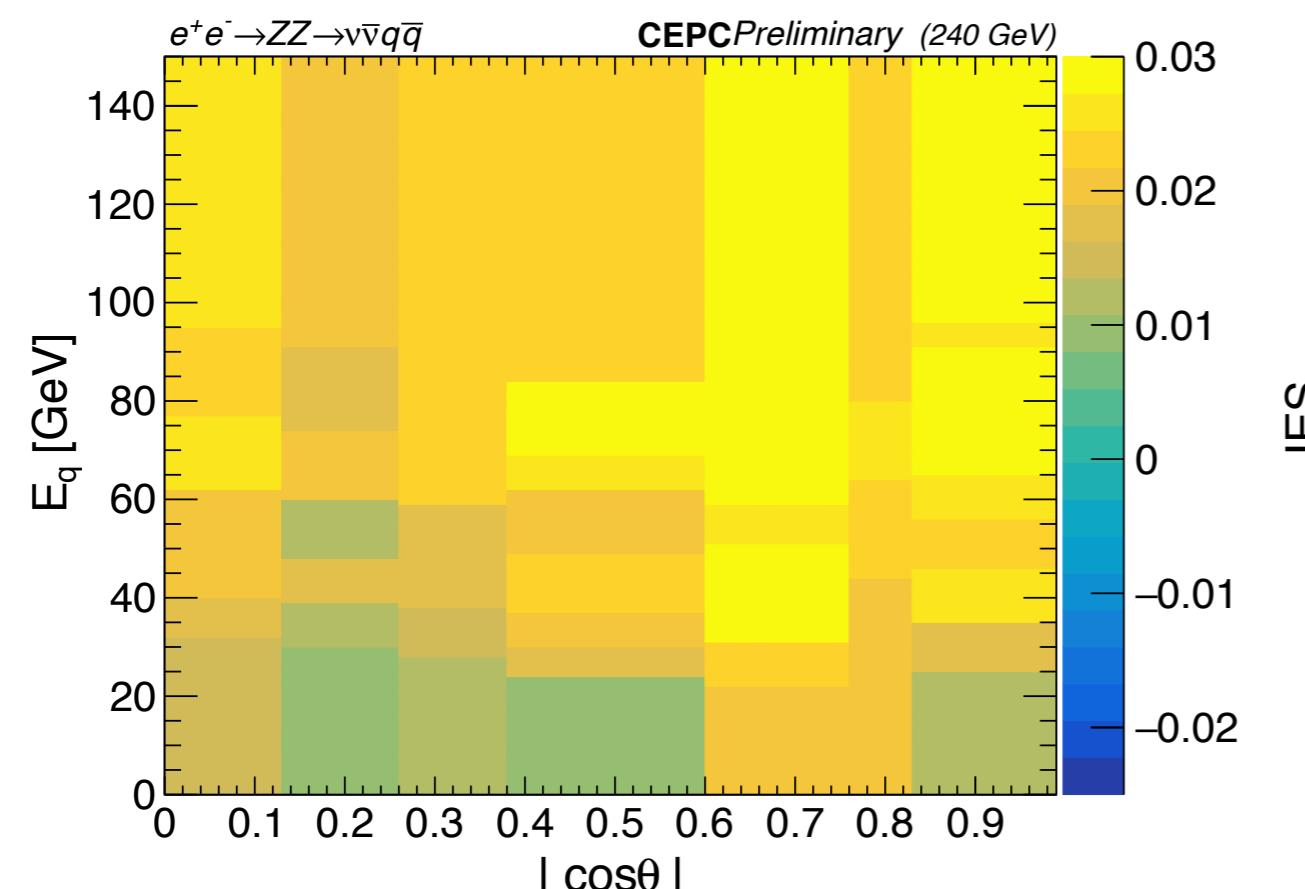


Reco-MCP

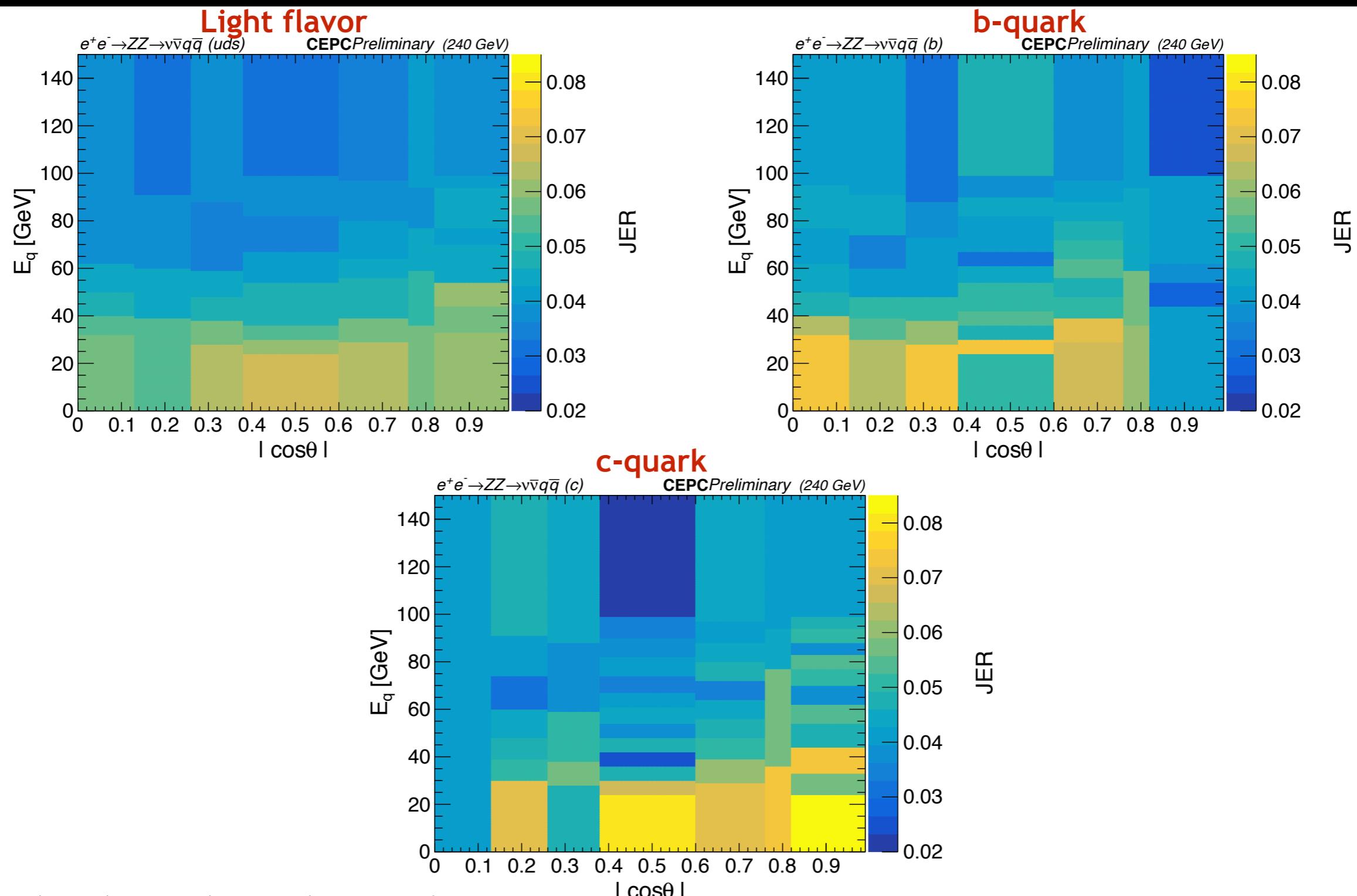


- JER/JES between Reco jet and MCP would combine the effects of two previous stages.





# JER in Phase Space

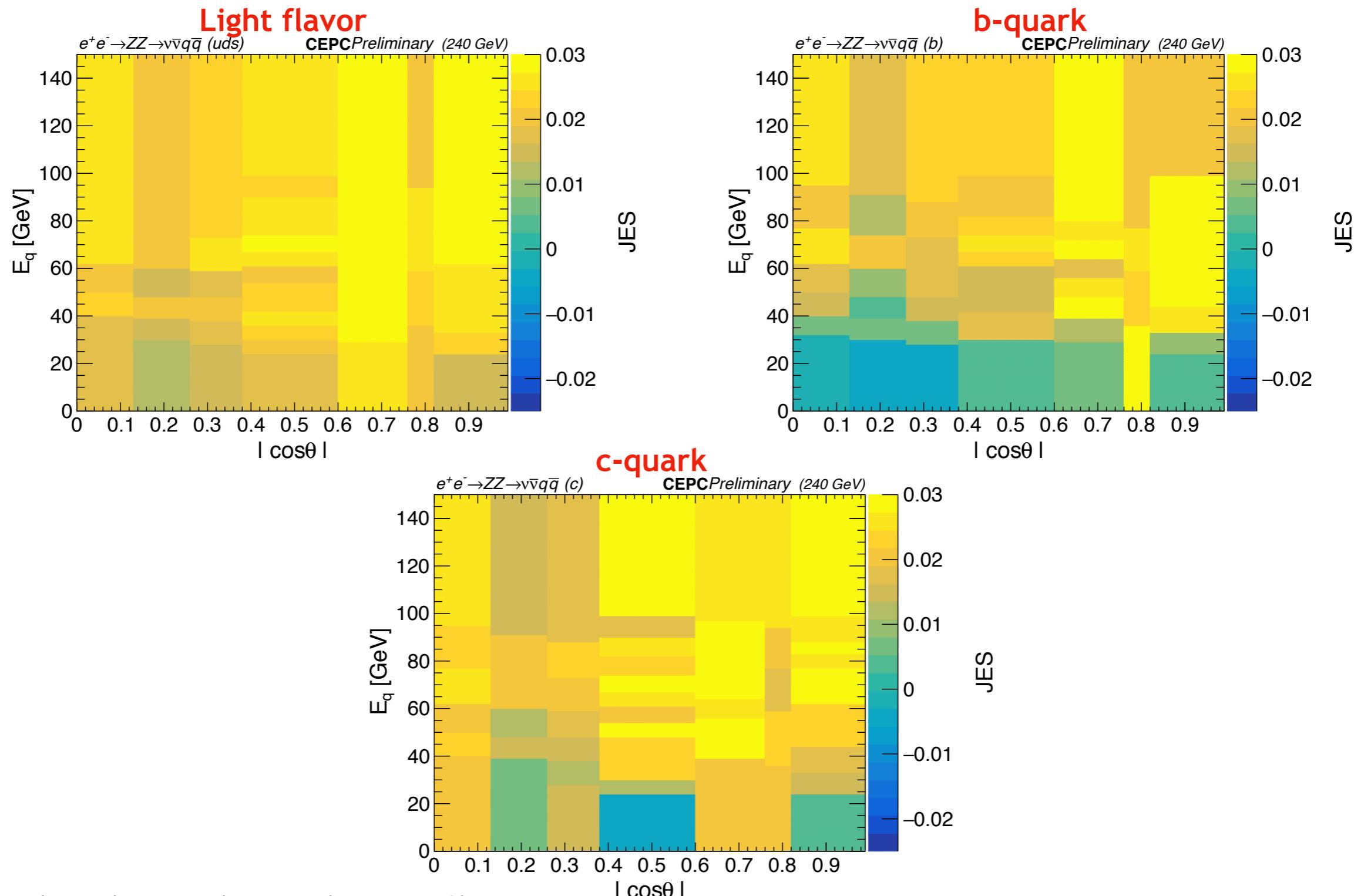


- JER also depends on the jet flavor.
- Higher jet energy and within central region of barrel, JER has impressive performance.



CEPC

# JES in Phase Space



- JES also depends on the jet flavor.
- Light flavor jet has higher energy deviation.