## Summer Session II 2018

- 1. From last time
  - a. Finished filling out the binary code table for our edge-detector circuit
  - b. Table repeated below

Present State	Binary	Pres	ent S	tate	Input	Next State			Output
Present State	Code	Α	В	С	х	A'	B'	C'	z
i	000	0	0	0	0	0	0	1	0
i	000	0	0	0	1	0	1	0	0
0	001	0	0	1	0	0	1	1	0
0	001	0	0	1	1	1	0	0	0
1	010	0	1	0	0	1	0	1	0
1	010	0	1	0	1	1	1	0	0
00	011	0	1	1	0	0	1	1	0
00	011	0	1	1	1	1	0	0	0
01	100	1	0	0	0	1	0	1	1
01	100	1	0	0	1	1	1	0	1
10	101	1	0	1	0	0	1	1	1
10	101	1	0	1	1	1	0	0	1
11	110	1	1	0	0	1	0	1	0
11	110	1	1	0	1	1	1	0	0

- c. Use above to create K-maps
  - i. Inputs are the concatenation of the current state variables A, B, C, and the input x
  - ii. Outputs of each K-map are the next state variables A', B', C' and the output z
    - 1. Need to create 4 different K-maps, one for each variable
  - iii. Since state 111 wasn't assigned, combinations of that with x are don't cares

Α		AB					В		AB					С		AB			
		00	01	11	10				00	01	11	10	]			00	01	11	10
	00	0	1	(1)	1			00	0	0	0	0			00	1_	1	1	1
<u> </u>	01	0	1	1	1			01	1	1	1	1		Сх	01	0	0	0	0
Сх	11	[1	1	d	1)		Сх	11	0	0	d	0		CX	11	0	0	d	0
	10	0	0	d	0			10	1	1	d	1			10	1	1	d	1
A = E	$A = B\overline{C} + A\overline{C} + Cx$					$B = \tilde{C}$	$\overline{x} + 0$	$C\bar{x}$	ı				$C = \bar{x}$	;					

- d. Use above derivations from K-maps to design initial combinational circuit
- e. Create K-map based on value to determine the output combinational circuit
  - i. Remember, Moore models don't use the input to determine the current output
    - 1. Therefore, K-map for z only uses A, B, and C
  - ii. Mealy model difference
    - 1. Mealy models use the current input to determine the current output
    - 2. Final K-map for output z would incorporate current flip-flop values as well as input x

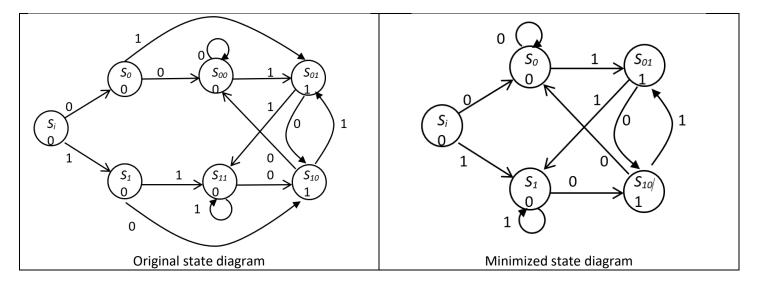
Z		AB				
		00	01	11	10	
_	0	0	0	0	1	
С	1	0	0	0	[1]	
			z = ,	ΑĒ		

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- 2. Mealy model versus Moore
  - a. In general, Mealy model usually involves less circuitry
    - i. In this case, it does
    - ii. Only need two DFFs to remember previous bit
    - iii. XOR those values with input to give final output

## 3. Minimization

- a. Did the 7-state Moore model edge detector earlier
- b. Can minimize this down to 5 states, as shown below



## c. Some definitions

- i. Two states  $S_i$  and  $S_j$  are *equivalent* if and only if for every possible input sequence, the same output sequence will be produced, regardless of whether  $S_i$  or  $S_j$  is the initial state
- ii. A successor to state S<sub>i</sub> is a state that it transitions to based on its input
  - 1.  $S_0$  in the unminimized FSM has  $S_{00}$  and  $S_{01}$  as its successors
  - 2. Differentiate successors based on input
    - a.  $S_{00}$  is the *O-successor* of  $S_0$
    - b.  $S_{01}$  is the 1-successor of  $S_0$
    - c. Collectively, all immediate successors of a state form the k-successors of the state
- iii. A block is a subset of states that may be equivalent
- iv. A *partition* is a set of blocks where the states in each block are not equivalent to the states in the other blocks

## 4. Partition minimization procedure

- a. Will use the unminimized edge detector FSM for the rest of this example
- b. Start with all states in one partition and in same block
  - i.  $P_1 = (S_i, S_0, S_1, S_{00}, S_{01}, S_{10}, S_{11})$
- c. Create P<sub>2</sub> by dividing states in P<sub>1</sub> that have same outputs
  - i. From definition of equivalent, states that have different outputs cannot be equivalent
  - ii.  $P_2 = (S_i, S_0, S_1, S_{00}, S_{11}) (S_{01}, S_{10})$
- d. Create P<sub>3</sub> by looking at k-successors of each state
  - i. States of a block that have k-successors that in are different blocks from others in the block must be placed in new blocks, grouped by their shared k-successors
  - ii. Look at first block  $(S_i, S_0, S_1, S_{00}, S_{11})$ 
    - 1. 0-successors for the  $(S_i, S_0, S_1, S_{00}, S_{11})$  block of  $P_2$  are  $S_0, S_{00}, S_{10}, S_{00}, S_{10}$ , respectively
      - a. Need to divide states into those that stay in the block, and those that move to the  $(S_{01}, S_{10})$  of  $P_2$
      - b. Thus, we get  $(S_i, S_0, S_{00})$  and  $(S_1, S_{11})$ .

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- 2. 1-successors for  $(S_i, S_0, S_{00})$  are  $S_1, S_{01}, S_{01}$ , respectively
  - a. So, we divide into  $(S_i)$  and  $(S_0, S_{00})$ .
- 3. 1-succesors for  $(S_1, S_{11})$  are  $S_{11}$ ,  $S_{11}$ , so it will not need to be divided.
- 4. First block of  $P_2$  will be divided into the three blocks  $(S_i)$ ,  $(S_1, S_{11})$  and  $(S_0, S_{00})$  in  $P_3$ .

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- iii. Now look at second block ( $S_{01}$ ,  $S_{10}$ )
  - 1. O-successors for the  $(S_{01}, S_{10})$  block of  $P_2$  are  $S_{10}$ ,  $S_{00}$ , respectively
  - 2. These are in different blocks from each other in  $P_2$
  - 3. Will have to divide into two separate blocks  $(S_{01})$ , and  $(S_{10})$
- iv. So  $P_3 = (S_i)(S_1, S_{11})(S_0, S_{00})(S_{01})(S_{10})$
- e. Further partitions
  - i. Once a block has one state in it, don't need to partition it further
    - 1. Will still need to use it to determine k-successors, though
  - ii. P4 and further partitions look at each multiple-element block of the previous partition to see if the k-successors of its elements lead to the same blocks of the previous partition
    - 1. If not, the block must be further divided
    - 2. If any block splits, then we must continue to another step of partitioning
    - 3. If no block splits, then we are done
  - iii. Look at P<sub>4</sub> now
    - 1. 0-successors of  $(S_1, S_{11})$  are both block  $(S_{10})$ , so that will not cause the block to split.
    - 2. 1-successors are both  $(S_1, S_{11})$ , so there is no need to separate the block further during this partitioning step
    - 3. O-successors of  $(S_0, S_{00})$  are both block  $(S_0, S_{00})$ , so that will not cause the block to split
    - 4. 1-successors are both  $(S_{01})$ , so there is no need to separate the block further during this partitioning step
  - iv. Since no block split, the final minimized partition is  $P_3 = (S_i)(S_1, S_{11})(S_0, S_{00})(S_{01})(S_{10})$ 
    - 1. This matches the five-state minimized state diagram