

**MATH 260, Homework 4, Spring '14**

**Due: February 7, 2014**

**Honor Code:**

**Name:**

1) Consider the augmented matrix below.

$$\mathbf{A} = \left[ \begin{array}{ccc|c} 1 & 1 & -2 & -1 \\ 0 & -1 & 2 & 3 \\ 3 & 2 & -4 & 0 \\ 4 & 3 & -6 & -1 \end{array} \right]$$

a) (4 pts) Write the linear system the augmented matrix above represents.

b) (16 pts) Use Gauss-Jordan elimination to put the above augmented matrix in reduced row-echelon form (RREF). Specify the operations used at each step.

c) (2 pts) What rank does the augmented matrix have?

d) (3 pts) Give the solution(s), if any, of the linear system you wrote in part (a).

2) Consider the augmented matrix below.

$$\mathbf{B} = \left[ \begin{array}{ccc|c} 1 & 0 & 1 & 3 \\ 0 & 1 & 1 & 1 \\ 0 & 1 & a & 1 \end{array} \right]$$

a) (4 pts) What value(s), if any, of  $a$  make the associated linear system have an infinite number of solutions?

b) (4 pts) What value(s), if any, of  $a$  make the associated linear system have no solution?

c) (4 pts) What value(s), if any, of  $a$  make the associated linear system have a unique solution?