

October 24

1. (a) Given an undirected graph  $G = (V, E)$  and a set  $E' \subset E$ , briefly describe how to update Kruskal's algorithm to find the minimum spanning tree that includes all edges from  $E'$ . Assume  $E'$  doesn't have a cycle.  
(b) Assume you are given a graph  $G = (V, E)$  with positive and negative edge weights and an algorithm that can return a minimum spanning tree when given a graph with only positive edges. Describe a way to transform  $G$  into a new graph  $G'$  containing only positive edge weights so that the minimum spanning tree of  $G$  can be easily found from the minimum spanning tree of  $G'$ .



2. Show that a graph has a unique minimum spanning tree if all its edges have distinct weights/costs.

