

ASSIGNMENT-02

1. What is probability?

Probability is a number that reflects the chance or likelihood that a particular event will occur.

Probability ranges between 0 to 1.

Probability of an Event is : $\frac{\text{Number of ways it can happen}}{\text{Number of possible outcomes}}$

2. Define mutual Exclusive and mutual inclusive Events?

Mutually Exclusive Event: mutually Exclusive Events

are the events if they cannot both occur at the

same time. $\Rightarrow P(A \text{ or } B) = P(A) + P(B)$

Eg: Probability of a dice showing a number of 3 or number of 5.

$$P(3 \text{ or } 5) = P(3) + P(5) = 1/6 + 1/6 = 1/3.$$

Mutually Inclusive Events:

Mutually inclusive Events allow both Events to happen at the same time or occur in a single trial.

$$P(A \text{ or } B) = P(A) + P(B) - P(A \cap B)$$

Eg: Probability of getting an even number or number than 5 in a set of $\{1, 2, 3, 4, 5, 6, 7, 8\}$ is

$$P(\text{Even or } 5) = \frac{4}{8} + \frac{1}{8} - \frac{1}{8} = \frac{4}{8}.$$

3. Define Independent and Dependent Events.

Independent Events:-

Two Events are independent, if the outcome or occurrence of the first does not affect the

outcome or occurrence of the second. When two

Events A and B are independent, the probability of both occurring is $P(A \text{ and } B) = P(A) \cdot P(B)$.

Eg:- If we flip a coin in the air and get the outcome as Head, then again if we flip the coin but this time outcome may be Tail. In both cases, the occurrence of both events is independent of each other.

Dependent Events:

Two events are dependent if the outcome or occurrence of the first affects the outcome or occurrence of the second so that probability is changed.

→ When two events, A and B are dependent, the probability

of both occurring is $P(A \text{ and } B) = P(A) \cdot P(B|A)$.

$$P(A \text{ and } B) = P(B) \cdot P(A|B)$$

Eg:- Riya has to select two students from a class of 23 girls and 25 boys. What is the probability that both students chosen are boys?

$$\text{Total students} = 48$$

$$P(\text{Boy 1}) = 25/48$$

$$P(\text{Boy 2}) = 24/47$$

$$P(\text{Boy 1 and Boy 2}) = P(\text{Boy 1}) \cdot P(\text{Boy 2} | \text{Boy 1})$$

$$= \frac{25}{48} \cdot \frac{24}{47}$$

$$= \frac{600}{2256}$$

4. Explain conditional probability.

conditional probability is probability of an event occurring given that another event has already occurred.

$$P(A|B) = P(A \text{ and } B) / P(B).$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$P(B|A) = \frac{P(B \cap A)}{P(A)} = \frac{P(A \cap B)}{P(A)}$$

eg:- Probability that it is Friday and that a student is absent is 0.03. Since there are 5 working days in a week, the probability that it is Friday is 0.2. What is probability that a student is absent? Given that today is Friday?

$$P(\text{Friday} | \text{Absent}) = 0.03$$

$$P(\text{Friday}) = 0.2$$

$$P(\text{Absent} | \text{Friday}) = \frac{P(\text{Friday} | \text{Absent})}{P(\text{Friday})}$$

$$= \frac{0.03}{0.2} = 15\%$$

5. Explain Bayes Theorem.

Theorem can be used to determine the conditional probability of event A, given that event B has occurred, by knowing the conditional probability of event B, given the event A has occurred, as well as individual probabilities of events A and B.

$$P(A|B) = [P(B|A) \cdot P(A)] / P(B).$$

from conditional probability.

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$

$$P(A|B) \cdot P(B) = P(B|A) \cdot P(A)$$

$$P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B)}$$

$$P(B|A) = \frac{P(A|B) \cdot P(B)}{P(A)}$$

Eg:- $P(A)$ - probability that stock price increases is 5%.

$P(B)$ - probability that CEO is replaced by 20%.

$P(A|B)$ - probability of stock price increases given that the CEO has been replaced by 5%.

Find $P(B|A)$ probability of CEO replacement given the stock price has increased.

$$P(B|A) = \frac{P(A|B) \cdot P(B)}{P(A)}$$

$$= \frac{0.05 \times 0.2}{0.05}$$

$$P(B|A) = 0.2$$

6. What is the probability of spinning a prime number or an odd number on a spinner numbered 1 to 8?

$$\text{Set} = \{1, 2, 3, 4, 5, 6, 7, 8\}$$

$$\text{Set (prime)} = \{2, 3, 5, 7\}$$

$$\text{Set (odd)} = \{1, 3, 5, 7\}$$

$$\text{Set (prime or odd)} = \frac{4}{8} + \frac{4}{8} - \frac{3}{8}$$

$$= \frac{5}{8}$$

7. For numbers, one to nine, find the probability of getting a number 2 or no. less than 4?

$$\text{Set} = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$$

$$S_1 = \{2\}$$

$$S_2 = \{1, 2, 3\}$$

$$\text{probability of getting 2 or less than 4} = \frac{1}{9} + \frac{3}{9} - \frac{1}{9}$$

$$= \frac{3}{9} = \frac{1}{3}$$

8. let X and Y are two independent Events such that
 $P(X) = 0.3$ and $P(Y) = 0.7$ Find $P(X \text{ and } Y)$
 Independent Events

$$P(X \text{ and } Y) = P(X) \times P(Y)$$

$$= 0.3 \times 0.7$$

$$P(X \text{ and } Y) = 0.21$$