

MATHEMATICS

ASSIGNMENT - 01.

1. Define mean, mode, median.

mean : The Average value

median : The mid point

mode : The most common value.

2. Define standard deviation and variance.

standard deviation is a number that describes how spread out the values are.

A low standard deviation means that most of the numbers are close to the mean value.

A high standard deviation means that the values are spread out over a wider range.

variance is another number that indicates how spread out the values are.

standard deviation = $\sqrt{\text{variance}}$

$$S.D = \sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$

$$\text{variance} = \sigma^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

3. Define population mean and sample mean.

population is the collection of all items of interest to our study and is usually denoted with an uppercase "N"

→ Everything in the group that we want to learn about.

Population mean

$$\mu = \frac{\sum_{i=1}^N x_i}{N}$$

N = number of items in the population.

Sample:

A sample is a subset of the population and is denoted with a lowercase n .

A part of population drawn according to a rule or plan for concluding characteristics is called sample.

The number of items in a sample is called sample size.

$$\text{sample mean } \bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$

n = number of items in the sample

4. Find mean, median, mode and standard deviation for each data set.

a: 7, 11, 16, 14, 11, 13, 19, 13, 13.

$$\text{mean} = \frac{7+11+16+14+11+13+19+13+13}{9}$$

$$\boxed{\text{mean} = 13}$$

median: n is odd.

Data in sorted order: 7, 11, 11, 13, 13, 13, 14, 16, 19

If n is odd, median is $\left(\frac{n+1}{2}\right)^{\text{th}}$ term.

$$\therefore \boxed{\text{median} = 13}$$

mode: The most common value = 13.

standard deviation

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$

$$\sum_{i=1}^9 (x_i - \bar{x})^2 = 36 + 4 + 9 + 1 + 4 + 0 + 36 + 0 + 0$$
$$= 90.$$

$$\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2 = \frac{1}{9}(90) = 10$$

$$\sigma = \sqrt{10} = 3.162$$

$$\boxed{\text{standard deviation} = 3.162}$$

b, 16, 15, 16, 17, 19, 12, 14, 9

$$\text{mean} = \frac{16+15+16+17+19+12+14+9}{8}$$

$$\boxed{\text{mean} = 14.75}$$

median:- Here n value is Even = 8.

$$\text{median} = \frac{\left(\frac{n}{2}\right)^{\text{th}} + \left(\frac{n}{2}+1\right)^{\text{th}}}{2}$$

9, 12, 14, 15, 16, 16, 17, 19

$$= \frac{15+16}{2}$$

$$\boxed{\text{median} = 15.5}$$

mode : common value = 16.

standard deviation

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$

$$= \sqrt{\frac{1}{8} (1.5625 + 0.0625 + 1.5625 + 5.0625 + 18.0625 + 7.5625 + 0.5625 + 33.0625)}$$

$$= \sqrt{8.4375}$$

$$\boxed{SD = 2.9047}$$

c; 27, 66, 24, 81, 50, 40, 74, 81, 97.

$$\text{mean} = \frac{27+66+24+81+50+40+74+81+97}{9}$$

$$\boxed{\text{mean} = 60}$$

median = n is odd $\therefore \left(\frac{n+1}{2}\right)^{\text{th}}$ term.

24, 27, 40, 50, 66, 74, 81, 81, 97

$$\boxed{\text{median} = 66}$$

mode = The most common value = 81.

$$\text{standard deviation: } \sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$

$$= \sqrt{\frac{1}{9} (1089 + 36 + 1296 + 441 + 100 + 400 + 196 + 441 + 1369)}$$

$$= \sqrt{596.444}$$

$$\boxed{SD = 24.42}$$