

Surname (COGNOME)	SOLUTION
Name	
POLIMI Personal Code	
Signature	

Politecnico di Milano, 15 February, 2024

Course on Advanced Computer Architectures

Prof. C. Silvano

EX1	(6 points)	
EX2	(4 points)	
EX3	(3 points)	
EX4	(2 points)	
Q1	(5 points)	
Q2	(5 points)	
QUIZZES	(8 points)	
TOTAL	(33 points)	

EXERCISE 1 – Tomasulo (6 points)

Please consider one iteration of the following assembly loop code:

```

LOOP:  lw $t1,VECTA($t0)
I2:    lw $t2,VECTB($t0)
I3:    add $t3,$t1,$t2
I4:    add $t4,$t3,$t3
I5:    sw $t3,VECTC($t0)
I6:    sw $t4,VECTD($t0)
I7:    addi $t0,$t0,4
I8:    bne $t0,$t5,LOOP
    
```

to be executed on a CPU_I with dynamic scheduling based on **TOMASULO algorithm** with all cache HITS, a single Common Data Bus and:

- 2 RESERVATION STATIONS (**RS1, RS2**) for 2 LOAD/STORE units (**LDU1, LDU2**) with latency 6
- 2 RESERVATION STATIONS (**RS3, RS4**) for 2 ALU/BR FUs (**ALU1, ALU2**) with latency 2

1. Please complete the following table for CPU_I :

INSTRUCTION	ISSUE	START EXEC	WRITE RESULT	Hazards Type	RSi	UNIT
LOOP: lw \$t1,VECTA(\$t0)	1	2	8	None	RS1	LDU1
I2: lw \$t2,VECTB(\$t0)	2	3	9	None	RS2	LDU2
I3: add \$t3,\$t1,\$t2						
I4: add \$t4,\$t3,\$t3						
I5: sw \$t3,VECTC(\$t0)						
I6: sw \$t4,VECTD(\$t0)						
I7: addi \$t0,\$t0,4						
I8: bne \$t0,\$t5,LOOP						

2. Calculate the CPI_I :

$CPI_I =$ _____

Let's assume to execute the same loop iteration on a CPU_2 with dynamic scheduling based on **TOMASULO algorithm** with all cache HITS, a single Common Data Bus and **more reservation stations** as follows:

- 4 RESERVATION STATIONS (**RS1, RS2, RS3, RS4**) for 2 LOAD/STORE units (**LDU1, LDU2**) with latency 6
- 4 RESERVATION STATIONS (**RS5, RS6, RS7, RS8**) for 2 ALU/BR FUs (**ALU1, ALU2**) with latency 2

3. Please complete the following table for CPU_2 :

INSTRUCTION	ISSUE	START EXEC	WRITE RESULT	Hazards Type	RSi	UNIT
LOOP: lw \$t1, VECTA(\$t0)	1	2	8	None	RS1	LDU1
I2: lw \$t2, VECTB(\$t0)	2	3	9	None	RS2	LDU2
I3: add \$t3, \$t1, \$t2						
I4: add \$t4, \$t3, \$t3						
I5: sw \$t3, VECTC(\$t0)						
I6: sw \$t4, VECTD(\$t0)						
I7: addi \$t0, \$t0, 4						
I8: bne \$t0, \$t5, LOOP						

4. Calculate the CPI_2 :

$CPI_2 =$ _____

5. Calculate the **Speedup** obtained by adding more reservation stations:

Speedup = _____

Feedback:

INSTRUCTION	ISSUE	START EXEC	WRITE RESULT	Hazards Type	RSi	UNIT
LOOP: lw \$t1, VECTA(\$t0)	1	2	8	None	RS1	LDU1
I2: lw \$t2, VECTB(\$t0)	2	3	9	None	RS2	LDU2
I3: add \$t3, \$t1, \$t2	3	10	12	(RAW \$t1) RAW \$t2	RS3	ALU1
I4: add \$t4, \$t3, \$t3	4	13	15	RAW \$t3	RS4	ALU2
I5: sw \$t3, VECTC(\$t0)	9	13	19	STRUCT RS1 RAW \$t3	RS1	LDU1
I6: sw \$t4, VECTD(\$t0)	10	16	22	RAW \$t4	RS2	LDU2
I7: addi \$t0, \$t0, 4	13	14	16	STRUCT RS3	RS3	ALU1
I8: bne \$t0, \$t5, LOOP	16	17	19	STRUCT RS4 (RAW \$t0)	RS4	ALU2

$$CPI_1 = \# \text{ clock cycles} / IC = 22 / 8 = 2,75$$

INSTRUCTION	ISSUE	START EXEC	WRITE RESULT	Hazards Type	RSi	UNIT
LOOP: lw \$t1, VECTA(\$t0)	1	2	8	None	RS1	LDU1
I2: lw \$t2, VECTB(\$t0)	2	3	9	None	RS2	LDU2
I3: add \$t3, \$t1, \$t2	3	10	12	(RAW \$t1) RAW \$t2	RS5	ALU1
I4: add \$t4, \$t3, \$t3	4	13	15	RAW \$t3	RS6	ALU2
I5: sw \$t3, VECTC(\$t0)	5	13	19	RAW \$t3	RS3	LDU1
I6: sw \$t4, VECTD(\$t0)	6	16	22	RAW \$t4	RS4	LDU2
I7: addi \$t0, \$t0, 4	7	13	16	STRUCT ALU1 + CDB	RS7	ALU1
I8: bne \$t0, \$t5, LOOP	8	17	19	RAW \$t0	RS8	ALU2

$$CPI_2 = \# \text{ clock cycles} / IC = 22 / 8 = 2,75$$

There is **no speedup** in adding more reservation stations.

In Tomasulo, the potential WAW and WAR hazards are already solved by Register Renaming

Only the hazards that have caused the introduction of some stalls are reported in the table, while other potential hazards are either omitted or put into brackets.

EXERCISE 2 on REORDER BUFFER (4 points)

Let's consider the following assembly loop where registers \$R1 and \$R2 are initialized at 0 and 40 respectively:

```

LOOP:  LD $F2, 0 ($R1)
I2:    ADDD $F4, $F2, $F2
I3:    SD $F4, 0 ($R1)
I4:    ADDI $R1, $R1, 4
I5:    BNE $R1, $R2, LOOP # branch predicted ad taken
    
```

- How many loop iterations? *10 iterations*

Then execute the loop by the *Speculative Tomasulo* architecture with an **8-entry ROB** and:

- 4 Load Buffers (Load1, Load2, Load3, Load4);
- 2 FP Reservation Stations (FP1, FP2)
- 2 Integer Reservation Stations (Int1, Int2)
- Please update the following ROB and Rename Tables until the ROB becomes **full** while the first instruction is still in execution due to a cache miss (*)

ROB Table

ROB#	Instruction	Dest.	Resource Allocation	Ready /Status	Spec.	
ROB0	LOOP: LD \$F2, 0 (\$R1)	\$F2	Load1	No, exec. (*)	No	HEAD
ROB1	I2: ADDD \$F4, \$F2, \$F2	\$F4	FP1	No, issued	No	
ROB2	I3: SD \$F4, 0 (\$R1)	Mem	--	No, issued	No	
ROB3	I4: ADDI \$R1, \$R1, 8	\$R1	Int1	No, issued	No	
ROB4	I5: BNE \$R1, \$R2, LOOP	--	Int2	No, issued	No	
ROB5	LOOP: LD \$F2, 0 (\$R1)	\$F2	Load 2	No, issued	Yes	
ROB6	I2: ADDD \$F4, \$F2, \$F2	\$F4	FP2	No, issued	Yes	
ROB7	I3: SD \$F4, 0 (\$R1)	Mem	--	No, issued	Yes	

Rename Table:

Reg#	ROB#
\$F0	--
\$F2	ROB0, ROB5
\$F4	ROB1, ROB6
\$F6	--
\$F8	--

Please complete the unrolled version of the loop with unrolling factor 2:

LOOP:	LD \$F2, 0 (\$R1)
I2:	ADDD \$F4, \$F2, \$F2
I3:	SD \$F4, 0 (\$R1)
I4:	LD \$F6, 4 (\$R1)
I5:	ADDD \$F8, \$F6, \$F6
I6:	SD \$F8, 4 (\$R1)
I7:	ADDI \$R1, \$R1, 8
I8:	BNE \$R1, \$R2, LOOP

- How many loop iterations? *5 iterations*

Then execute the unrolled version of the loop by the **Speculative Tomasulo** architecture with an **8-entry ROB** and:

- 4 Load Buffers (Load1, Load2, Load3, Load4);
- 2 FP Reservation Stations (FP1, FP2)
- 2 Integer Reservation Stations (Int1, Int2)
- Please update the following ROB and Rename Tables until the ROB becomes full while the first instruction is still in execution due to a cache miss:

ROB Table

ROB#	Instruction	Dest.	Resource Allocation	Ready /Status	Spec.	
ROB0	LOOP:LD \$F2, 0 (\$R1)	\$F2	Load1	No, exec. (*)	No	HEAD
ROB1	I2: ADDD \$F4, \$F2, \$F2	\$F4	FP1	No, issued	No	
ROB2	I3: SD \$F4, 0 (\$R1)	Mem	--	No, issued	No	
ROB3	I4: LD \$F6, 4 (\$R1)	\$F6	Load2	No, issued	No	
ROB4	I5: ADDD \$F8, \$F6, \$F6	\$F8	FP2	No, issued	No	
ROB5	I6: SD \$F8, 4 (\$R1)	Mem	--	No, issued	No	
ROB6	I7: ADDI \$R1, \$R1, 8	\$R1	Int1	No, issued	No	
ROB7	I8: BNE \$R1, \$R2, LOOP	--	Int2	No, issued	No	

Rename Table:

Reg#	ROB#
\$F0	--
\$F2	ROB0
\$F4	ROB1
\$F6	ROB3
\$F8	ROB4

EXERCISE 3 – CACHE MEMORIES (3 points)

Let's consider 32-block main memory with a **fully-associative** 4-block cache and LRU cache replacement policy. The addresses are expressed as:

Memory Block Addresses: $[0, 1, 2, \dots, 31]_{10}$

Cache Block Addresses: $[a, b, c, d]$

At cold start the cache is empty, then there is the following sequence of memory accesses.

- Assuming the **Write Allocate** and **Write Back** cache policies, complete the following table:

	Type of memory access	Memory Address	HIT / MISS Type	Cache Tag	Cache Block Address	Dirty bit	Write-back in memory
1	read	$[12]_{10}$	Cold start MISS	$[01100]_2$	a	0	no
2	write	$[12]_{10}$	HIT	$[01100]_2$	a	1	no
3	write	$[10]_{10}$	<i>Cold start MISS</i>	<i>$[01010]_2$</i>	<i>b</i>	<i>1</i>	<i>no</i>
4	read	$[10]_{10}$	<i>HIT</i>	<i>$[01010]_2$</i>	<i>b</i>	<i>1</i>	<i>no</i>
5	read	$[26]_{10}$	<i>Cold start MISS</i>	<i>$[11010]_2$</i>	<i>c</i>	<i>0</i>	<i>no</i>
6	write	$[7]_{10}$	<i>Cold start MISS</i>	<i>$[00111]_2$</i>	<i>d</i>	<i>1</i>	<i>no</i>
7	read	$[12]_{10}$	<i>HIT</i>	<i>$[01100]_2$</i>	<i>a</i>	<i>1</i>	<i>no</i>
8	read	$[4]_{10}$	<i>Conflict MISS</i>	<i>$[00100]_2$</i>	<i>b</i>	<i>0</i>	<i>Yes: WB in $[10]_{10}$</i>
9	write	$[26]_{10}$	<i>HIT</i>	<i>$[11010]_2$</i>	<i>c</i>	<i>1</i>	<i>no</i>
10	write	$[18]_{10}$	<i>Conflict MISS</i>	<i>$[10010]_2$</i>	<i>d</i>	<i>1</i>	<i>Yes: WB in $[7]_{10}$</i>
11	read	$[5]_{10}$	<i>Conflict MISS</i>	<i>$[00101]_2$</i>	<i>a</i>	<i>0</i>	<i>Yes: WB in $[12]_{10}$</i>
12	write	$[24]_{10}$	<i>Conflict MISS</i>	<i>$[11000]_2$</i>	<i>b</i>	<i>1</i>	<i>No</i>

Calculate the Miss Rate:

$$\text{Miss Rate} = \text{Number of misses} / \text{Number of memory access} = 8 / 12 = 0,67$$

EXERCISE 4 – VECTOR PROCESSORS (2 points)

Let's consider the following code executed by a Vector Processor with:

- Vector Register File composed of 32 vectors of 8 elements per 64 bits/element;
- Scalar FP Register File composed of 32 registers of 64 bits;
- One Load/Store Vector Unit with operation chaining and memory bandwidth 64 bits;
- One ADD/SUB Vector Unit with operation chaining;
- One MUL/DIV Vector Unit with operation chaining.

L.V V1, RX # Load vector from memory address RX into V1
L.V V3, RY # Load vector from memory address RY into V3
MULVS.D V1, V1, F0 # FP multiply vector V1 to scalar F0
ADDVV.D V2, V1, V1 # FP add vectors V1 and V1
MULVS.D V2, V2, F0 # FP multiply vector V2 to scalar F0
ADDVV.D V3, V2, V3 # FP add vectors V2 and V3
S.V V3, RZ # Store vector V3 into memory address RZ

Please complete the following vector instruction scheduling:

0	1		L.V V1, RX	7
---	---	--	------------	---

How many convoys? **3 convoys**

How many clock cycles to execute the code? **24 clock cycles**

Vector instruction scheduling:

There are 3 convoys as follows:

- Page 8 - SOLUTION

QUESTION 1: VLIW ARCHITECTURES (5 points)

1. Describe the main concepts of Very Long Instruction Word processor architectures.

2. What are the main issues associated with VLIW architectures?

For each answer mark if it is either **TRUE** or **FALSE** and **motivate your answer**)

Answer 1: Compilers can detect parallelism only in basic blocks of the code **T F**

Answer 2: Larger code size **T F**

Answer 3: Increased HW complexity

T F

Answer 4: Less code portability

T F

Answer 5: Large number of registers required for register renaming

T F

QUESTION 2: MEMORY HIERARCHY (5 points)

Let's consider the following cache optimization techniques. *Answer to the following questions:*

	Pseudo-associativity and Way Prediction	Early Restart and Critical Word First	Introducing a Victim Cache
<i>Explain the main concepts for each technique.</i>			
<i>What are the main effects of each technique on the miss rate?</i>			
<i>What are the main effects of each technique on the miss penalty?</i>			

MULTIPLE-CHOICE QUESTIONS: (8 points)

Question 1 (format Multiple Choice – Single answer)

In the speculative Tomasulo architecture, what are the hardware blocks needed to undo speculative instructions execution on mispredicted branches?

(SINGLE ANSWER)

1 point

Answer 1: Reorder Buffer; **(TRUE)**

Answer 2: Instruction Dispatcher

Answer 3: Store Buffers;

Answer 4: Reservation Stations;

Answer 5: Load Buffers;

Feedback:

The speculative Tomasulo architecture supports speculative instructions execution and branch mispredictions by using ROB entries.

Question 2 (format TRUE/FALSE)

A fine-grain multi-threading processor exploits more parallelism than a simultaneous multi-threading processor

(TRUE/FALSE)

1 point

Answer: TRUE

FALSE **(X)**

Question 3 (format TRUE/FALSE)

A VLIW processor needs multiple Program Counters to load the necessary multiple instructions.

(TRUE/FALSE)

1 point

Answer: TRUE

FALSE **(X)**

Question 4 (format Multiple Choice – Single answer)

Let's consider a 5-issue processor that can manage up to 5 simultaneous threads.

What are the values of the ideal CPI and the ideal per-thread CPI?

(SINGLE ANSWER)

1 point

Answer 1: Ideal CPI = 5 & Ideal per-thread CPI = 1

Answer 2: Ideal CPI = 1 & Ideal per-thread CPI = 0.2

Answer 3: Ideal CPI = 0.20 & Ideal per-thread CPI = 1 **(TRUE)**

Answer 4: Ideal CPI = 0.25 & Ideal per-thread CPI = 5

Answer 5: Ideal CPI = 5 & Ideal per-thread CPI = 0.20

Question 5 (format Multiple Choice – Single answer)

Let's consider a (2,1) Correlating Branch Predictor with 4K total entries.

How many Branch History Tables?

How many entries per BHT?

How many bits per entry?

(SINGLE ANSWER)

1 point

Answer 1: 4 BHTs | 1K entries | 1-bit per entry **(TRUE)**

Answer 2: 2 BHTs | 2K entries | 1-bit per entry

Answer 3: 2 BHTs | 2K entries | 2-bit per entry

Answer 4: 1 BHT | 4K entries | 1-bit per entry

Question 6 (format Multiple Choice – Single answer)

Using a 5-stage *optimized pipeline with the “early evaluation of PC”* for branch instructions, how many stalls we need to introduce to execute the following assembly code?

```
ld $t1, AA($t6)
beq $t1, $t0, LABEL
```

Answer 1: 1

Answer 2: 2 **(TRUE)**

Answer 3: 3

Answer 4: none

(SINGLE ANSWER)

1 point

Complete the following pipeline scheme to motivate your answer:

ld \$t1, AA(\$t6)	IF	ID	EX	ME	WB ↓				
beq \$t1, \$t0, LABEL		IF	ID stall	ID stall	ID	EX	ME	WB	

Question 7 (complete table format)

2 points

Let's consider the following access patterns on a **4-processor** system with a direct-mapped, write-back cache with one cache block per processor and a two-cache block memory.

Assume the **MESI protocol** is used with **write-back** caches, **write-allocate**, and **write-invalidate** of other caches.

Please **COMPLETE** the following table:

Cycle	After Operation	P0 cache block state	P1 cache block state	P2 cache block state	P3 cache block state	Mem. at bl. 0 up to date?	Mem. at bl. 1 up to date?
1	P0: Read Bl. 1	Excl (1)	Invalid	Invalid	Invalid	Yes	Yes
2	P2: Read Bl. 0	Excl (1)	Invalid	Excl (0)	Invalid	Yes	Yes
3	P3: Read Bl. 0	Excl (1)	Invalid	Shared (0)	Shared (0)	Yes	Yes
4	P1: Write Bl. 0	Excl (1)	Mod (0)	Invalid	Invalid	No	Yes
5	P0: Write Bl. 1	Mod (1)	Mod (0)	Invalid	Invalid	No	No
6	P3: Read Bl. 1	Shared(1)	Mod (0)	Invalid	Shared (1)	No	Yes