

# Artificial Intelligence Principles

6G7V0011 - 1CWK100

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## Uninformed Search Algorithms

- Review

- Search Concepts and Properties

- Breadth First Search

- Depth First Search

- Depth First Search - Improved

- Summay

## Uninformed Search Algorithms

- Review

- Search Concepts and Properties

- Breadth First Search

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- Depth First Search - Improved

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- Artificial Intelligence and SOTA techniques
- Agents and Rational agents
- Four types of agent programs
  1. Simple reflex agent
  2. Model-based agent
  3. Goal-based agent
  4. Utility-based agent
- **Graph search and Tree (tree-like) search**

- Frontier, Fringe, Openset
- Reached, closedset
- Expansion
- Exploration strategy - Depth first? Breadth first? etc.

**Openset:** is the set of nodes we choose currently from - that is, it contains all the nodes we might be interested in looking at next.

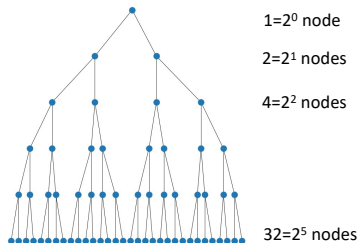
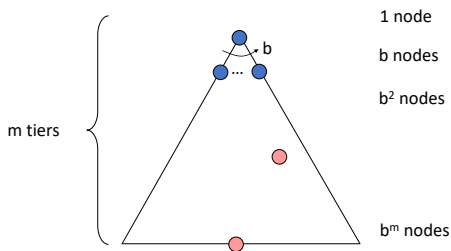
**frontier** or **fringe:** meaning 'a set of nodes to be expanded. Without causing confusions, we will use them all in the course.

**Closedset:** is the set of nodes we've already considered.

Sometimes, a Closedset is also called **reached**, meaning 'a set of nodes that are explored already'. Similarly, we will use both terms in this course without causing confusions.

**Exploration strategy is the key question!**

# Search Algorithm Properties



- **Complete:** Guaranteed to find a solution if one exists?
  - **Optimal:** Guaranteed to find the least cost path?
  - **Time** complexity?
  - **Space** complexity?
- Key factors of a search tree
    1.  $b$  is the branching factor
    2.  $m$  is the maximum depth
    3. solutions at various depths

$$\text{Node number: } b^0 + b^1 + b^2 + \dots + b^m = \sum_{i=0}^m b^i \sim \mathcal{O}(b^m)$$

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## Algorithm 1: Pseudocode of Breath First Search

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**Input:** Initial state  $s$ , goal state  $g$

**Output:** A *node* helps to retrieve a solution (path)  $\mathcal{P}$ , or failure

```
1: node  $\leftarrow$  with  $s$  as state
2: if  $s == g$  then
3:   return node
4: end if
5:  $\mathcal{O} \leftarrow$  node, an FIFO queue
6:  $\mathcal{C} \leftarrow \emptyset$ 
7: while  $\mathcal{O} \neq \emptyset$  do
8:   parent  $\leftarrow$  the first node in  $\mathcal{O}$ 
9:    $\mathcal{C} \leftarrow$  parent.state
10:  for child in successor (of the current parent) do
11:     $v \leftarrow$  child.state
12:    if  $v$  is not in  $\mathcal{C}$  and child is not in  $\mathcal{O}$  then
```

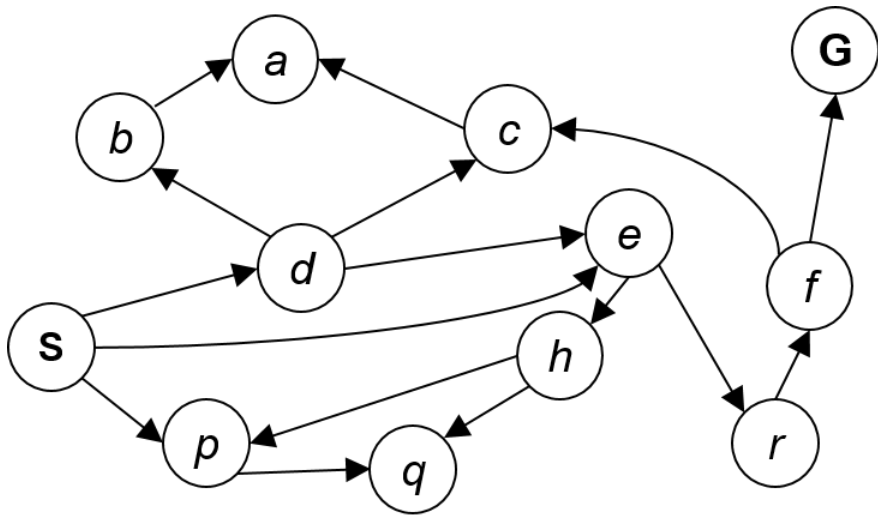
# Breath First Search (BFS) - graph II

```
13:         if  $v == g$  then  
14:             return child  
15:         end if  
16:         add child to the end of  $\mathcal{O}$   
17:     end if  
18: end for  
19: end while  
20: return failure
```

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# Breadth First Search



# Breadth First Search Properties

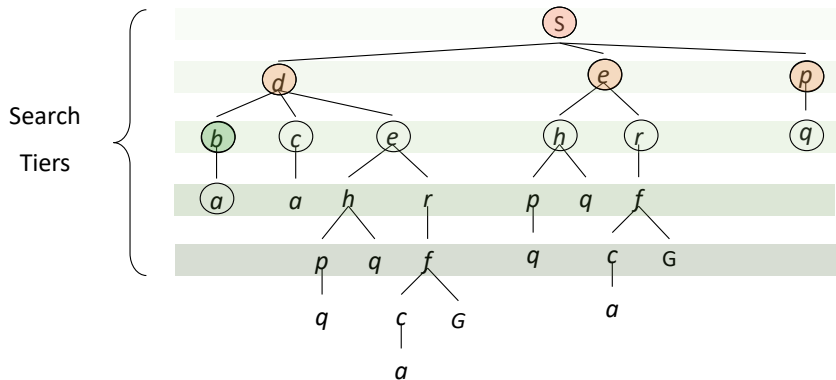
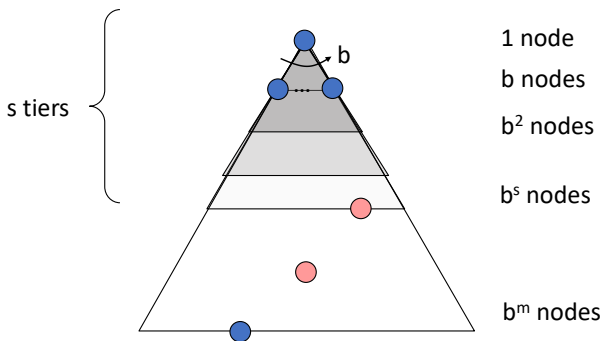


Figure 1: An example of Breadth First Search

## Breadth First Search



When search reached the shallowest solution at depth  $s$

- Has processed all nodes above depth  $s$
- Time complexity:  $\mathcal{O}(b^s)$
- Space complexity (frontier):  $\mathcal{O}(b^s)$
- Complete:  $s$  must be finite if a solution exists
- Optimal: When costs of edges are equal  $c$ .

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## Algorithm 2: Pseudocode of Depth First Search

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**Input:** Initial state  $s$ , goal state  $g$ .

**Output:** A *node* helps to retrieve a solution (path)  $\mathcal{P}$ , or failure

```
1:  $node \leftarrow$  with  $s$  as state
2:  $\mathcal{O} \leftarrow node$ , an LIFO queue
3:  $\mathcal{C} \leftarrow \emptyset$ 
4: while  $\mathcal{O} \neq \emptyset$  do
5:    $parent \leftarrow$  the last node in  $\mathcal{O}$ 
6:    $v \leftarrow parent.state$ 
7:   if  $v == g$  then
8:     return  $parent$ 
9:   end if
10:   $\mathcal{C} \leftarrow parent.state$ 
11:  for  $child$  in successor (of the current  $parent$ ) do
12:     $v \leftarrow child.state$ 
```

# Depth First Search (DFS) - graph II

```
13:    if  $v$  is not in  $\mathcal{C}$  and  $child$  is not in  $\mathcal{O}$  then  
14:        add  $child$  to  $\mathcal{O}$   
15:    end if  
16: end for  
17: end while  
18: return failure
```

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# Depth First Search

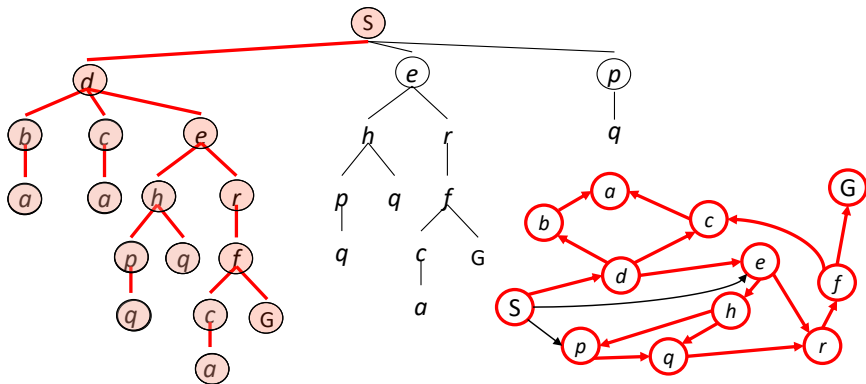
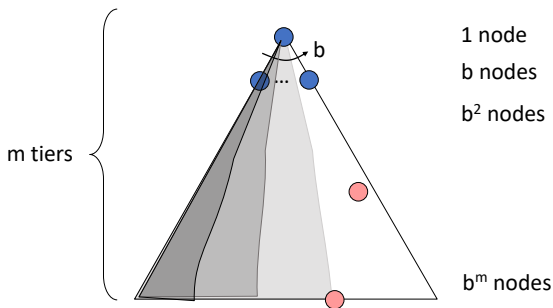


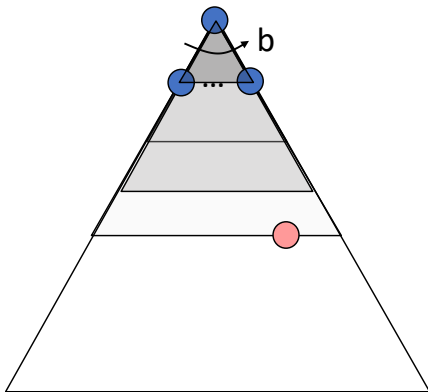
Figure 2: An example of depth first search

# Depth First Search Properties



Reached the cheapest solution with depth  $s$

- Has processed all nodes on the left (left prefix)
- Could have processed the whole tree
- Time complexity:  $\mathcal{O}(b^m)$  with finite  $m$
- Space complexity (frontier):  $\mathcal{O}(bm)$  (only siblings along path)
- Complete: Yes without cycle
- Optimal: No, 'leftmost'
- Action cost: 0



In depth first search,  $s$  could be infinite (cycles). This causes both time and space issues.

**Comprise:** Limit search depth, and then increase search depth from such as 2 to the limit. Need to judge if a solution can be found within the limited depth.



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## Algorithm 3: Pseudocode of Iterative Deepening Search

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**Input:** Initial state  $s$ , goal state  $g$ , a maximum search limit  $M$ .

**Output:** A *node* helps to retrieve a solution (path)  $\mathcal{P}$ , or failure

```
1: while  $m < M$  do
2:    $node \leftarrow$  with  $s$  as state
3:   if  $s == g$  then
4:     return  $node$ 
5:   end if
6:    $\mathcal{O} \leftarrow node$ , an LIFO queue
7:    $result \leftarrow failure$ 
8:   while  $\mathcal{O} \neq \emptyset$  do
9:      $parent \leftarrow$  the last node in  $\mathcal{O}$ 
10:     $v \leftarrow parent.state$ 
11:    if  $v == g$  then
12:      return  $parent$ 
```

# Depth First Search (DFS) - graph II

```
13:     else if depth  $\geq$  M then
14:         result = cutoff           % reached search limit.
15:     else if no cycle then
16:         for child in successor (of the current parent) do
17:             add child to the end of  $\mathcal{O}$ 
18:         end for
19:     end if
20: end while
21: end while
22: return result
```

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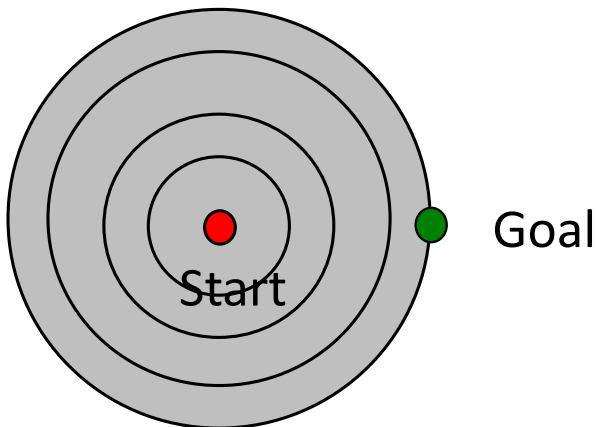


Figure 3: Search Contour of BFS

- Search in all directions
- Edge costs are equal

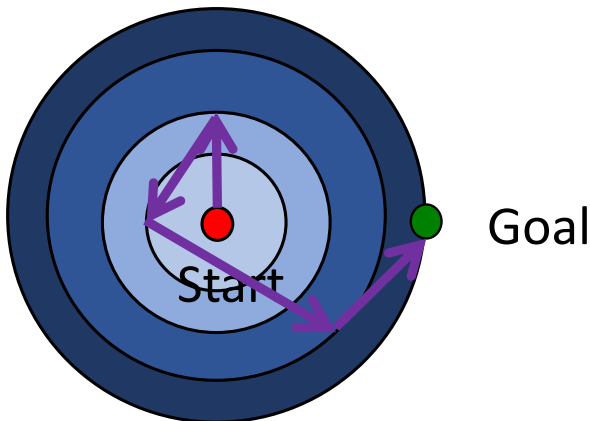


Figure 4: Search Contour of DFS

- Search in a specific direction (depth)
- Edge costs are not prioritised, not as much as depth

# Summary

We have learned:

- Depth First Search
- Breadth First Search
- Pros and Cons of each algorithm