

# Data-Efficient Robot Learning

Marc Deisenroth

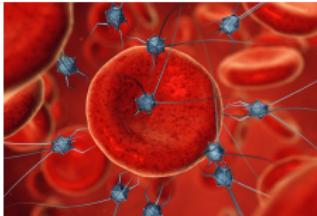
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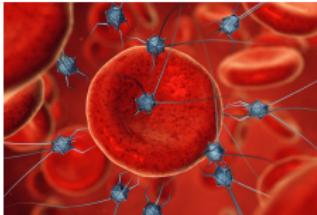
Creative Machine Learning



- **Vision:** Autonomous robots support humans in everyday activities ➤ **Fast learning** and **automatic adaptation**



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- Currently: **Data-hungry learning** or **human guidance**

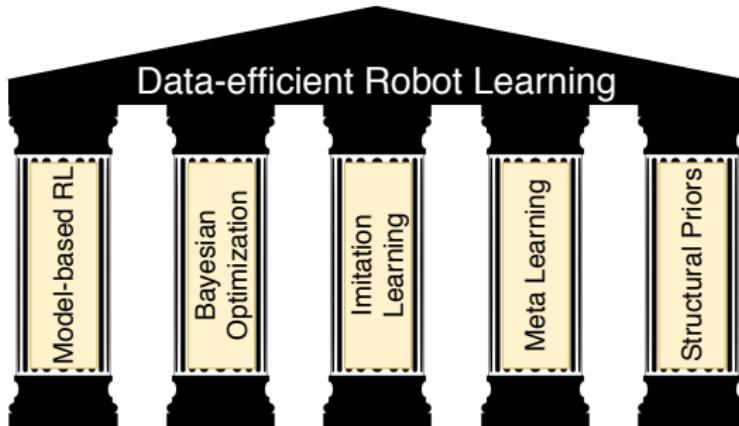


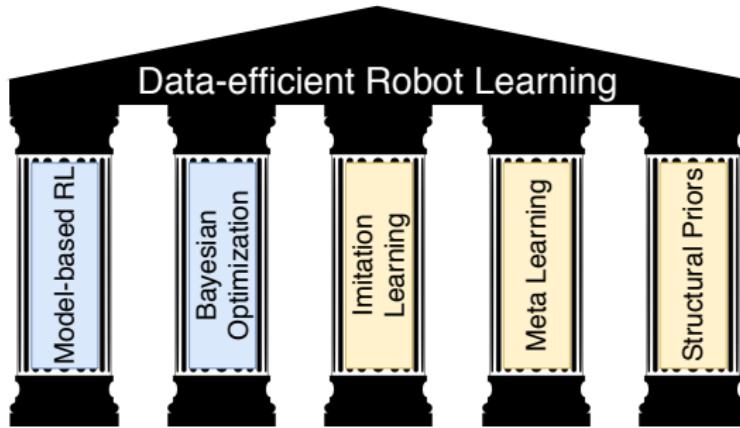
- **Vision:** Autonomous robots support humans in everyday activities ➤ **Fast learning** and **automatic adaptation**
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Fully **autonomous learning and decision making with little data** in  
real-life situations

## Data-Efficient Robot Learning

Ability to learn and make decisions in physical domains without requiring large quantities of data

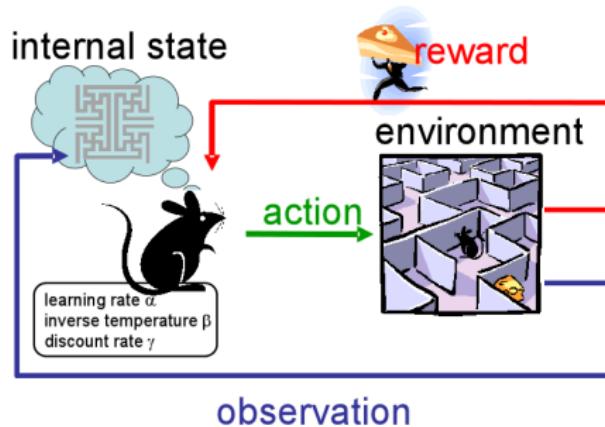




Two approaches toward data-efficient robot learning:

- 1** Model-based reinforcement learning
- 2** Bayesian optimization

# Reinforcement Learning



- Learn to solve a task
- Trial-and-error interaction with the environment
- Feedback via reward/cost function

$$x_{t+1} = f(x_t, u_t) + w, \quad u_t = \pi(x_t, \theta)$$

Diagram illustrating the Reinforcement Learning update rule:

- State**: Represented by  $x_t$ , feeds into the **Transition function** ( $f$ ) and the **Policy** ( $\pi$ ).
- Control**: Represented by  $u_t$ , is generated by the **Policy** ( $\pi$ ).
- Policy**: Represented by  $\pi$ , takes **State** ( $x_t$ ) and **Policy parameters** ( $\theta$ ) as inputs.
- Policy parameters**: Represented by  $\theta$ , are updated based on the **Transition function** output ( $x_{t+1}$ ).

Annotations:

- Transition function**: Red text below the arrows pointing from State to  $x_{t+1}$  and from State to  $u_t$ .

$$\mathbf{x}_{t+1} = f(\mathbf{x}_t, \mathbf{u}_t) + \mathbf{w}, \quad \mathbf{u}_t = \pi(\mathbf{x}_t, \boldsymbol{\theta})$$

State       Control       Policy 
  
**Transition function**

## Objective (Controller Learning)

Find policy parameters  $\boldsymbol{\theta}^*$  that minimize the expected long-term cost

$$J(\boldsymbol{\theta}) = \sum_{t=1}^T \mathbb{E}[c(\mathbf{x}_t) | \boldsymbol{\theta}], \quad p(\mathbf{x}_0) = \mathcal{N}(\boldsymbol{\mu}_0, \boldsymbol{\Sigma}_0).$$

Instantaneous cost  $c(\mathbf{x}_t)$ , e.g.,  $\|\mathbf{x}_t - \mathbf{x}_{\text{target}}\|^2$

- ▶ Typical objective in **optimal control** and **reinforcement learning** (Bertsekas, 2005; Sutton & Barto, 1998)

## Objective

Minimize expected long-term cost  $J(\theta) = \sum_t \mathbb{E}[c(x_t)|\theta]$

## PILCO Framework: High-Level Steps

- 1 Probabilistic model for transition function  $f$ 
  - ▶ System identification

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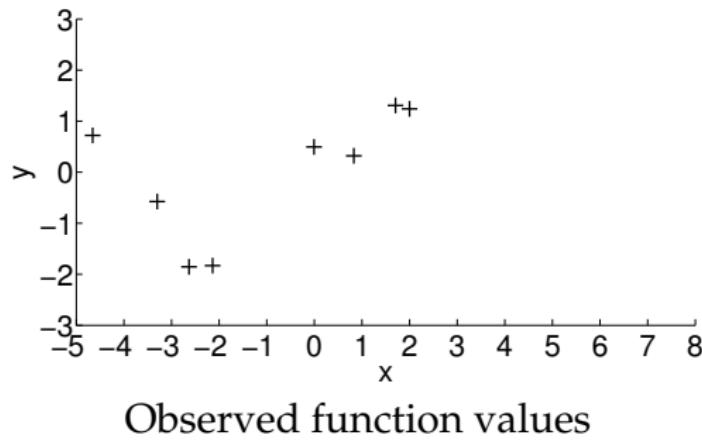
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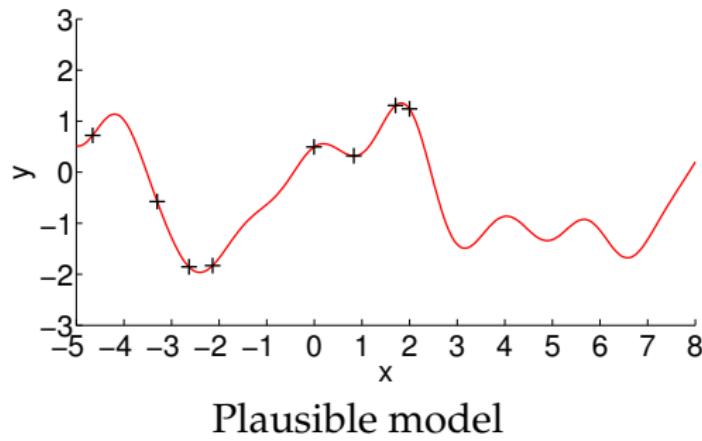
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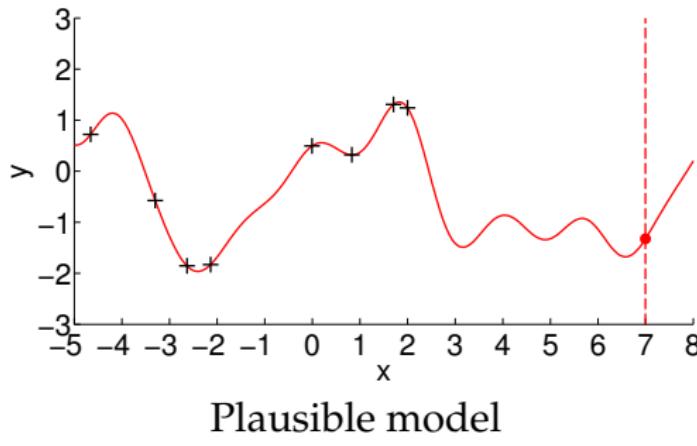
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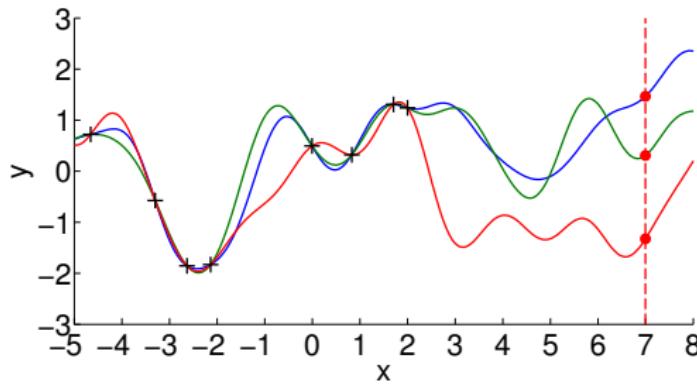


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Predictions? Decision Making?

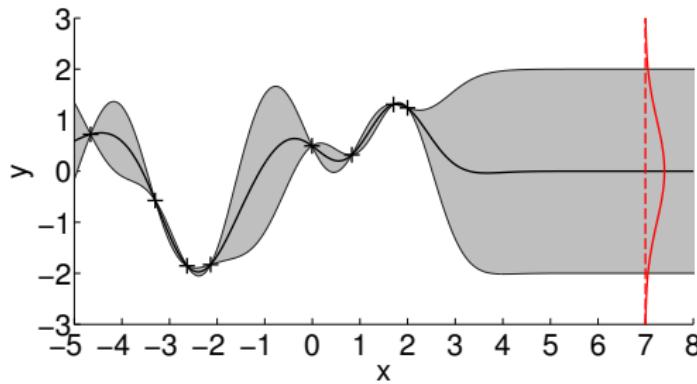
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More plausible models

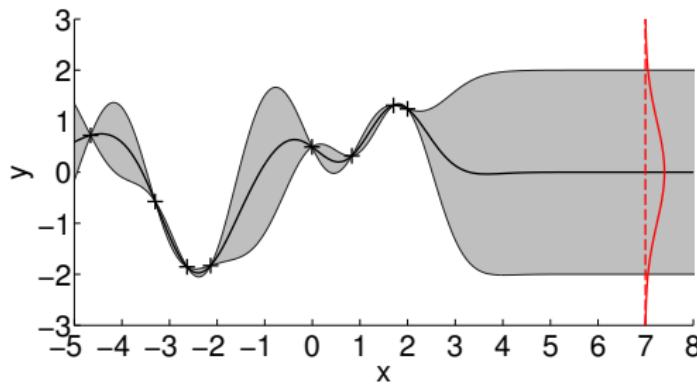
Predictions? Decision Making? Model Errors!

Model learning problem: Find a function  $f : x \mapsto f(x) = y$



Distribution over plausible functions

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Distribution over plausible functions

- ▶ Express **uncertainty** about the underlying function to be **robust to model errors**
- ▶ **Gaussian process** for model learning  
(Rasmussen & Williams, 2006)

- Flexible regression model
- Probability distribution over functions
- Fully specified by
  - Mean function  $m$  (average function)
  - Covariance function  $k$  (assumptions on structure)

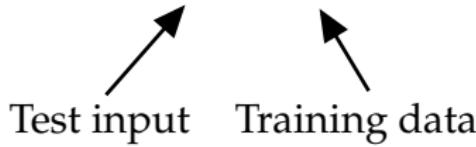
$$k(\mathbf{x}_p, \mathbf{x}_q) = \text{Cov}[f(\mathbf{x}_p), f(\mathbf{x}_q)]$$

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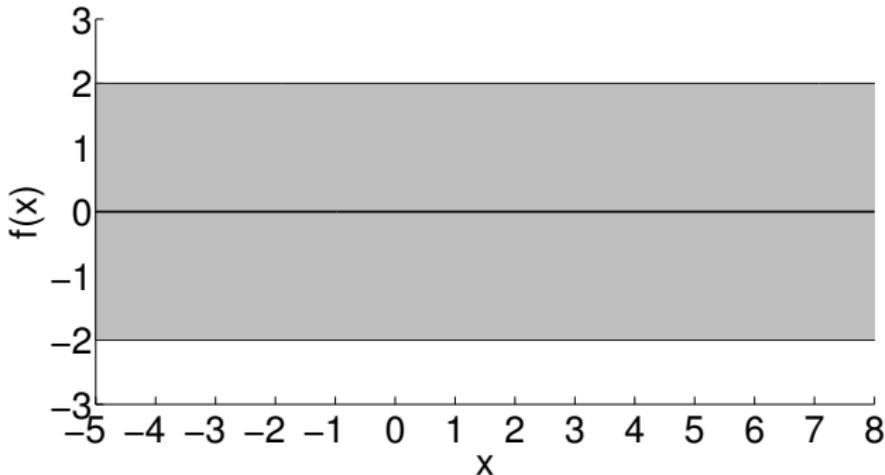
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- Predictive distribution at test input  $\mathbf{x}_*$  is Gaussian  
(Bayes' theorem):

$$p(f(\mathbf{x}_*) | \mathbf{x}_*, \mathbf{X}, \mathbf{y}) = \mathcal{N}(f(\mathbf{x}_*) | m(\mathbf{x}_*), \sigma^2(\mathbf{x}_*))$$



Test input      Training data

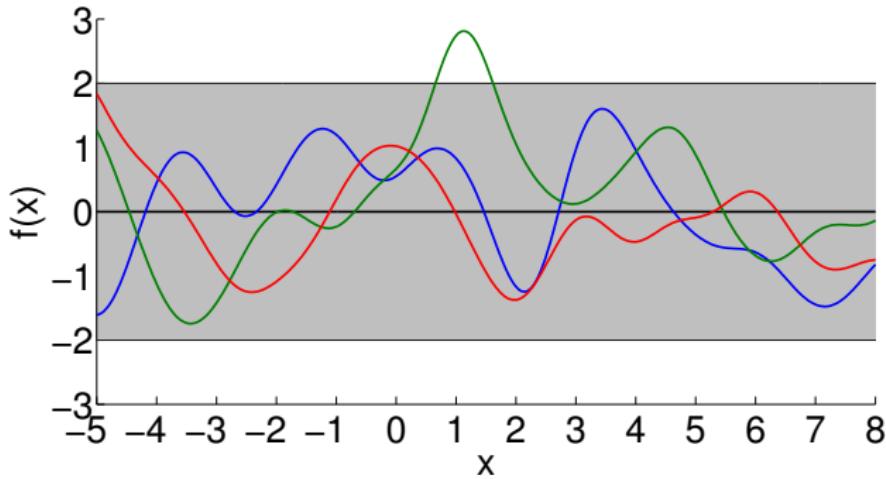


Prior belief about the function

Predictive (marginal) mean and variance:

$$\mathbb{E}[f(\mathbf{x}_*)|\mathbf{x}_*, \emptyset] = m(\mathbf{x}_*) = 0$$

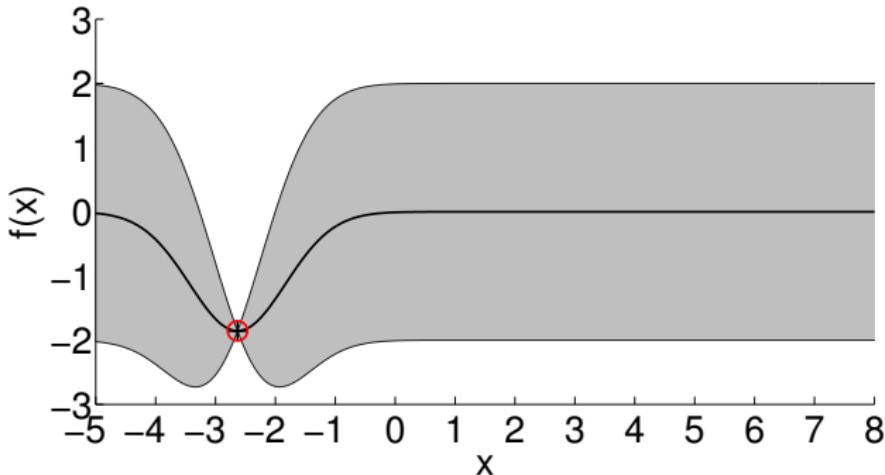
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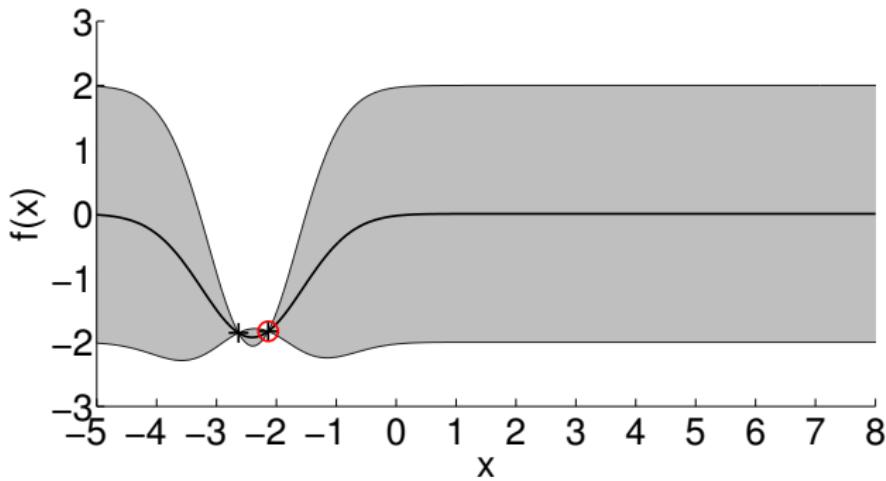


Posterior belief about the function

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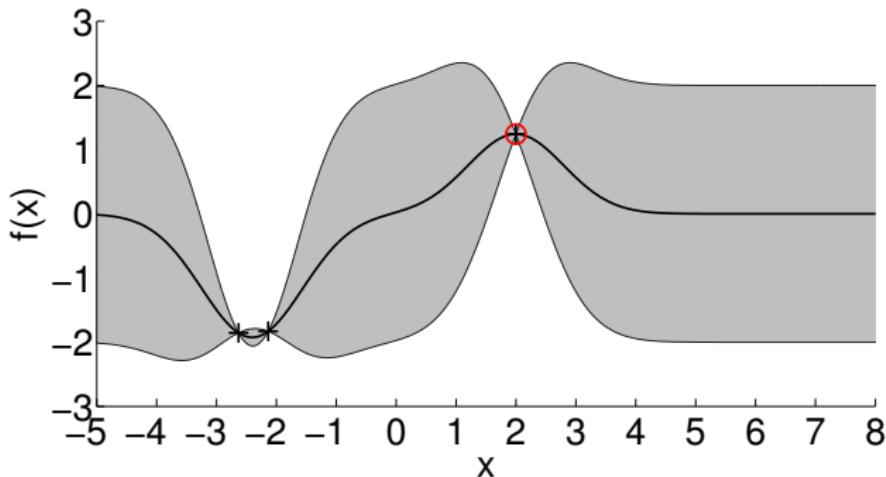


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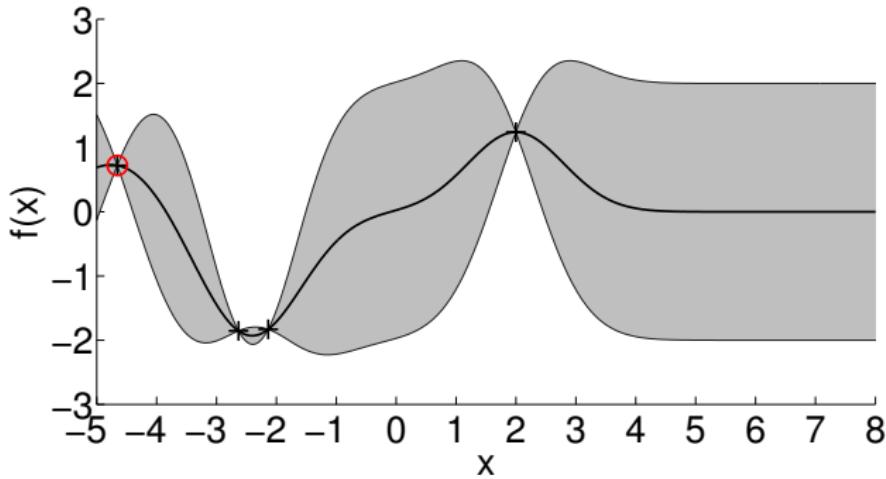


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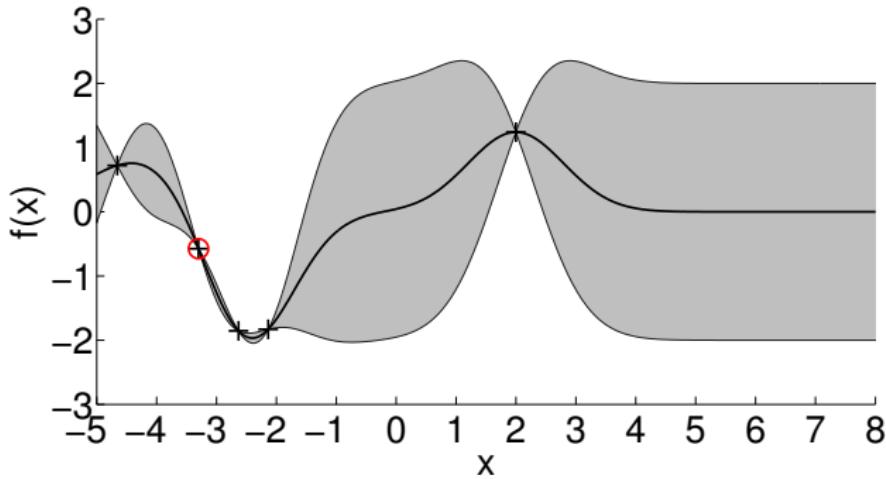


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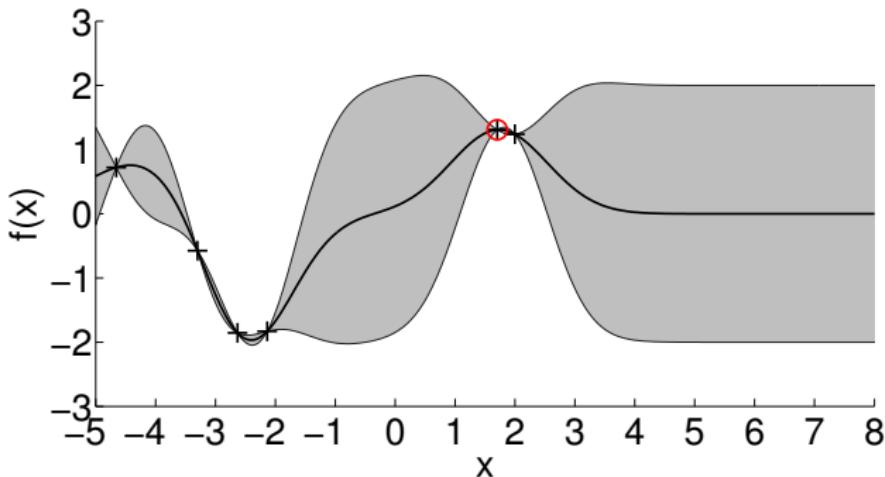


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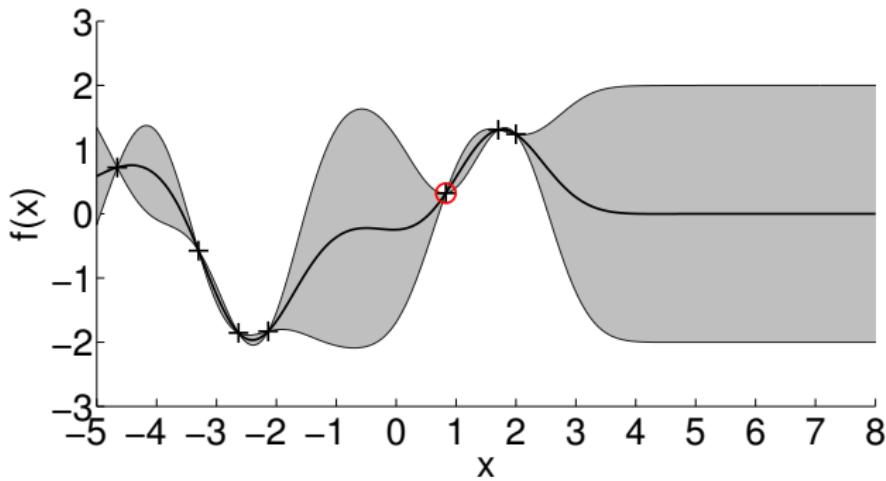


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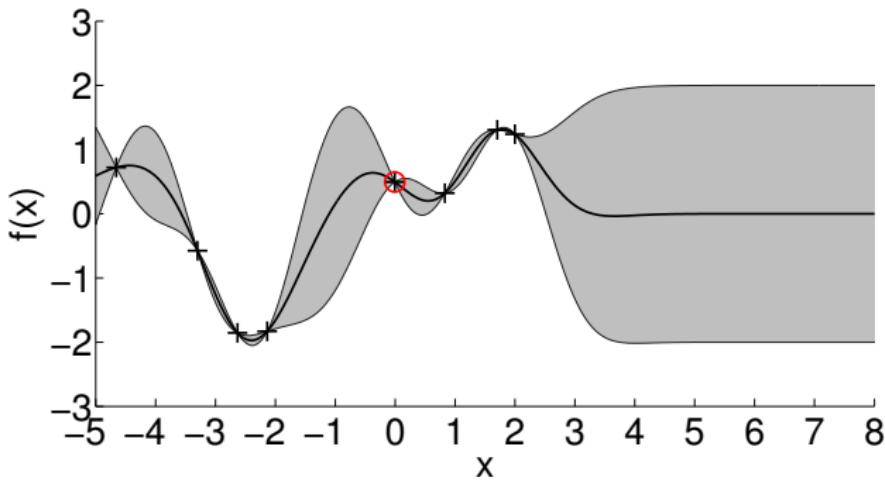


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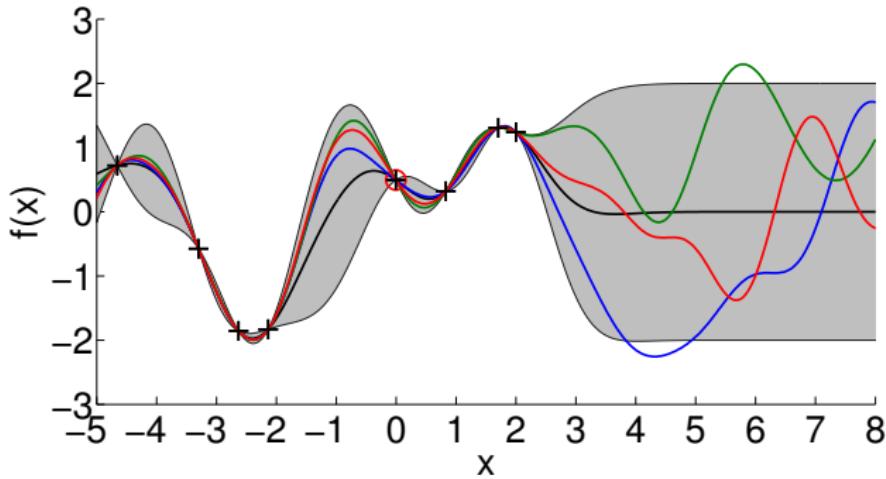


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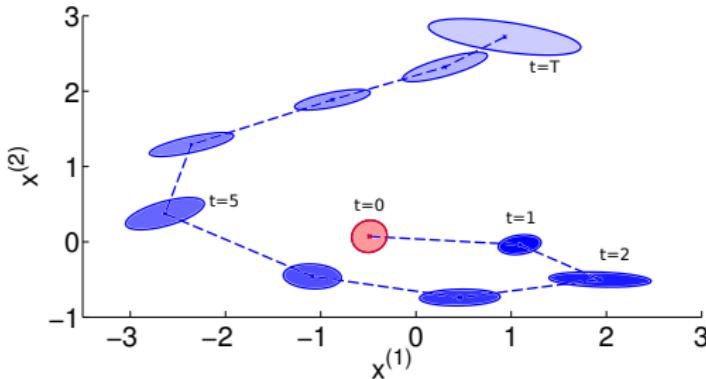
## Objective

Minimize expected long-term cost  $J(\theta) = \sum_t \mathbb{E}[c(x_t)|\theta]$

## PILCO Framework: High-Level Steps

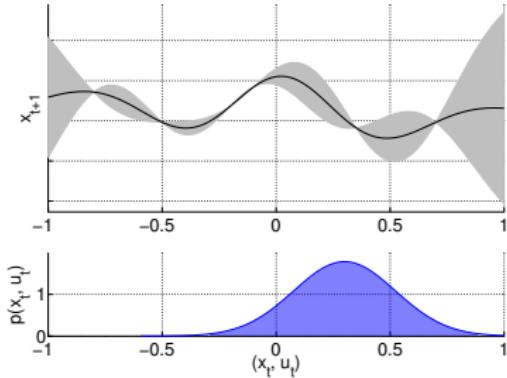
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# Long-Term Predictions



- Iteratively compute  $p(x_1|\theta), \dots, p(x_T|\theta)$

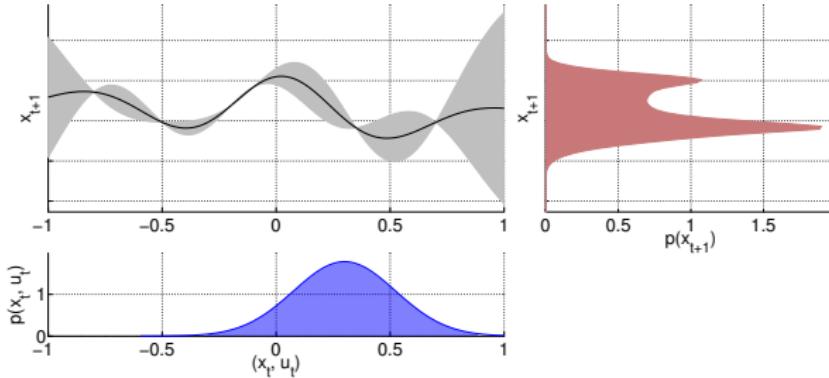
# Long-Term Predictions



- Iteratively compute  $p(x_1|\theta), \dots, p(x_T|\theta)$

$$\underbrace{p(x_{t+1}|x_t, u_t)}_{\text{GP prediction}} \quad \underbrace{p(x_t, u_t|\theta)}_{\mathcal{N}(\mu, \Sigma)}$$

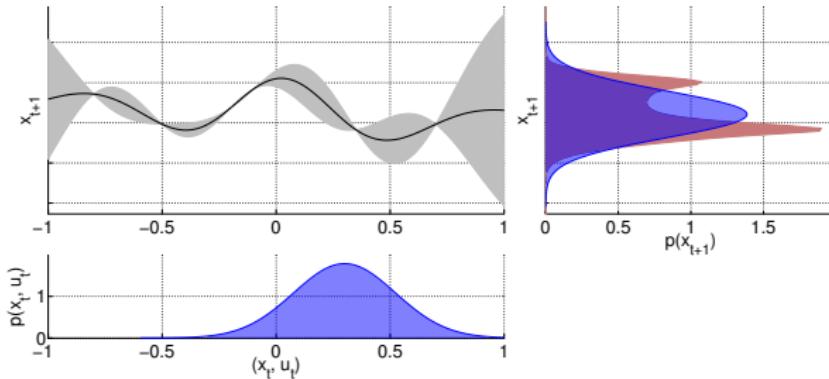
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## ► GP moment matching

(Girard et al., 2002; Quiñonero-Candela et al., 2003)

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  - Compute expected long-term cost  $J(\theta)$
  - Find parameters  $\theta$  that minimize  $J(\theta)$
- 4 Apply controller

## Objective

Minimize expected long-term cost  $J(\theta) = \sum_t \mathbb{E}[c(x_t)|\theta]$

- Know how to predict  $p(x_1|\theta), \dots, p(x_T|\theta)$

## Objective

Minimize expected long-term cost  $J(\boldsymbol{\theta}) = \sum_t \mathbb{E}[c(\mathbf{x}_t) | \boldsymbol{\theta}]$

- Know how to predict  $p(\mathbf{x}_1 | \boldsymbol{\theta}), \dots, p(\mathbf{x}_T | \boldsymbol{\theta})$
- Compute

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and sum them up to obtain  $J(\boldsymbol{\theta})$

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- Analytically compute gradient  $dJ(\boldsymbol{\theta})/d\boldsymbol{\theta}$
- Standard gradient-based optimizer (e.g., BFGS) to find  $\boldsymbol{\theta}^*$

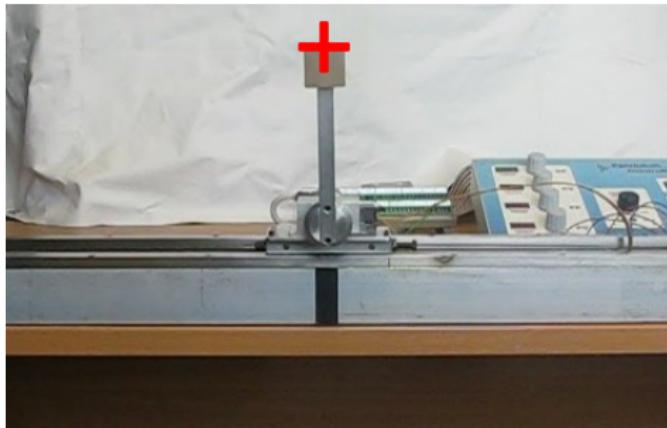
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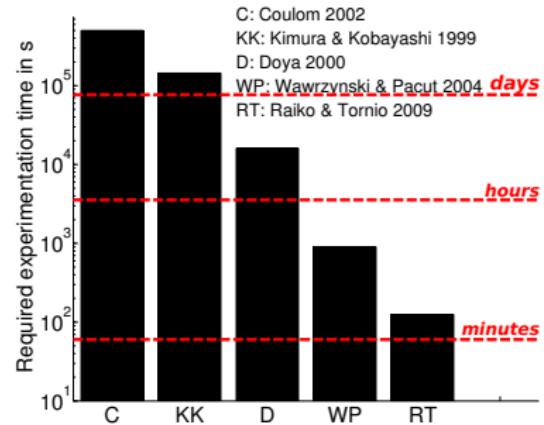
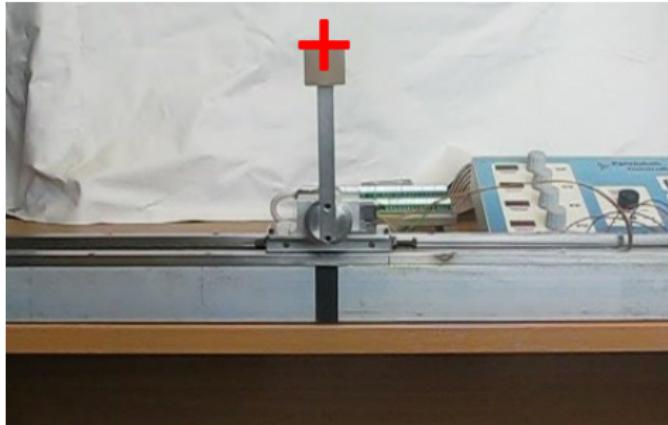
# Standard Benchmark: Cart-Pole Swing-up



- Swing up and balance a freely swinging pendulum on a cart
  - No knowledge about nonlinear dynamics ➤ Learn from scratch
  - Cost function  $c(\mathbf{x}) = 1 - \exp(-\|\mathbf{x} - \mathbf{x}_{\text{target}}\|^2)$
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- Code: <https://github.com/ICL-SML/pilco-matlab>

Deisenroth & Rasmussen (ICML, 2011): PILCO: A Model-based and Data-efficient Approach to Policy Search

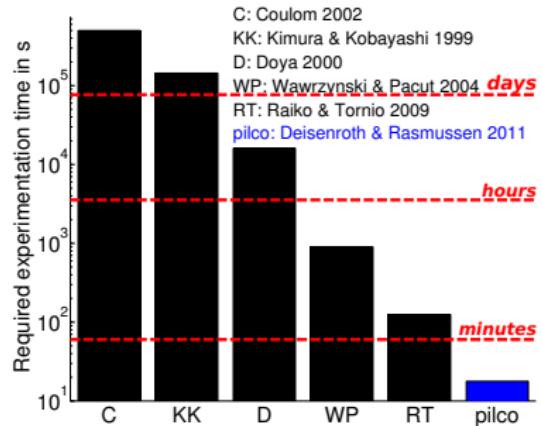
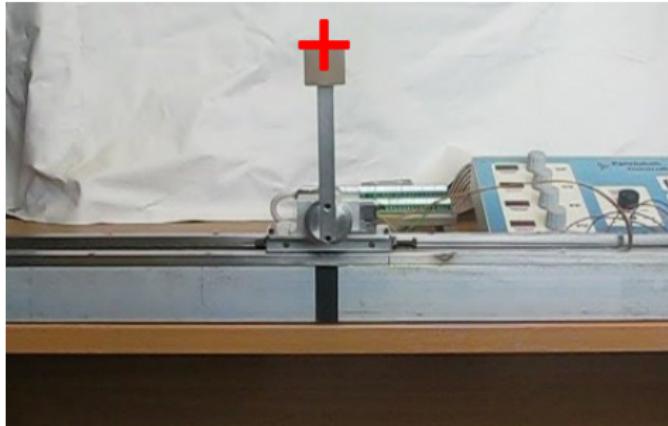
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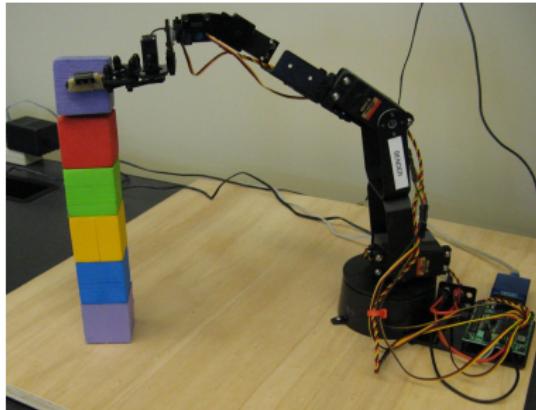
Deisenroth & Rasmussen (ICML, 2011): PILCO: A Model-based and Data-efficient Approach to Policy Search

# Standard Benchmark: Cart-Pole Swing-up



- Swing up and balance a freely swinging pendulum on a cart
- No knowledge about nonlinear dynamics ➤ Learn from scratch
- Cost function  $c(x) = 1 - \exp(-\|x - x_{\text{target}}\|^2)$
- **Unprecedented learning speed** compared to state-of-the-art
- Code: <https://github.com/ICL-SML/pilco-matlab>

Deisenroth & Rasmussen (ICML, 2011): PILCO: A Model-based and Data-efficient Approach to Policy Search



- Autonomously learn block-stacking with a low-cost robot
- Kinect camera as only sensor
- Robot very noisy
- Learn forward model and controller **from scratch**
- Small number of interactions: **Robot wears out quickly**

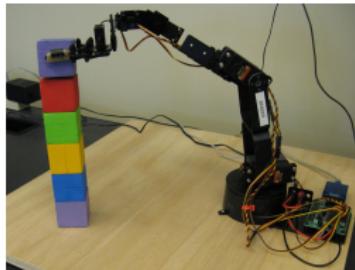
Deisenroth et al. (RSS, 2011): *Learning to Control a Low-Cost Manipulator using Data-efficient Reinforcement Learning*

# Learning to Pick up Objects

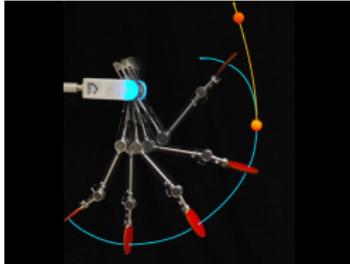


- Robotino XT (compliant behavior)
- Omnidirectional platform with pneumatic arm/trunk
- Motion capture
- 9D states, 9D actions

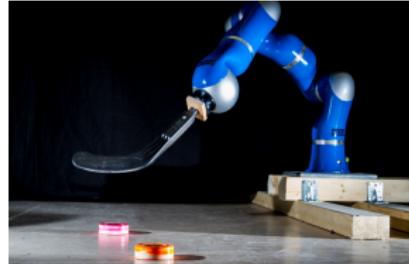
# Wide Applicability



with D Fox



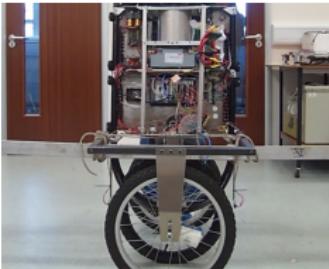
with P Englert, A Paraschos, J Peters



with A Kupcsik, J Peters, G Neumann



B Bischoff (Bosch), ESANN 2013



A McHutchon (U Cambridge)



B Bischoff (Bosch), ECML 2013

## ► Application to a wide range of robotic systems

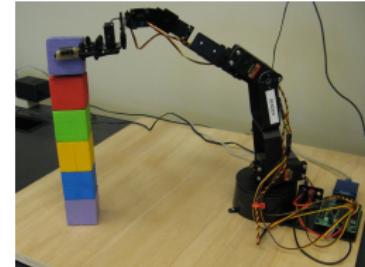
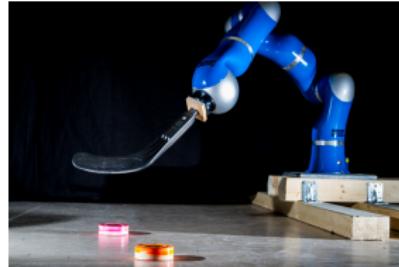
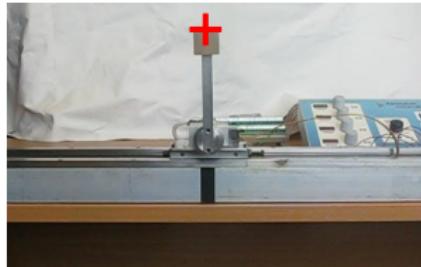
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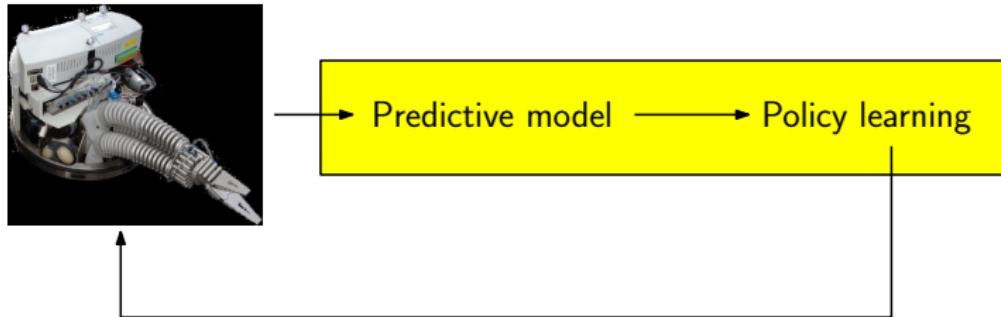
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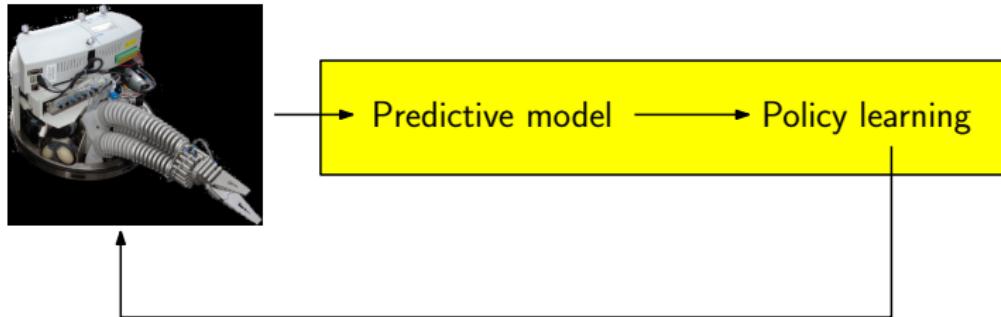
# Summary (1)



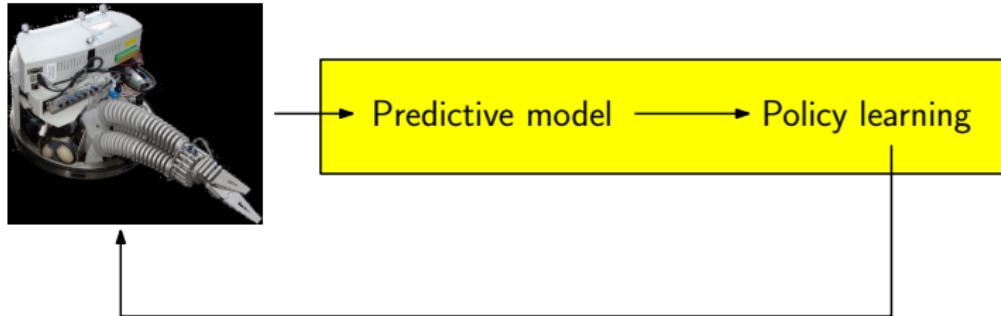
- In robotics, **data-efficient** learning is critical
- Probabilistic, model-based RL approach
  - Reduce model bias
  - Unprecedented learning speed
  - Wide applicability



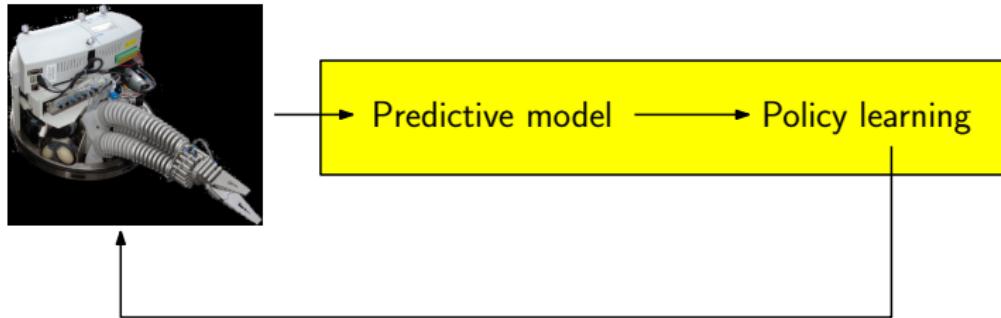
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- Sometimes this assumption is unrealistic
- Alternative approach to data-efficient controller learning



- Learning forward models is not always easy
- E.g., Ground contacts in legged locomotion

## Objective

Find parameters  $\theta$  of controller  $\pi(\theta)$



- Learning forward models is not always easy
- E.g., Ground contacts in legged locomotion

## Objective

Find parameters  $\theta$  of controller  $\pi(\theta)$

## Challenges:

- No forward model
  - No analytic cost function, no demonstrations
  - Still need to be data efficient (fragile robot)
  - Manual parameter search can be tedious
- Bayesian optimization (e.g., Jones 1998; Osborne et al., 2009)

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Minimize an objective function  $g$ , which is very expensive to evaluate

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- 1 Build a model  $\tilde{g}$  of the true objective function  $g$
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## Objective (Bayesian Optimization)

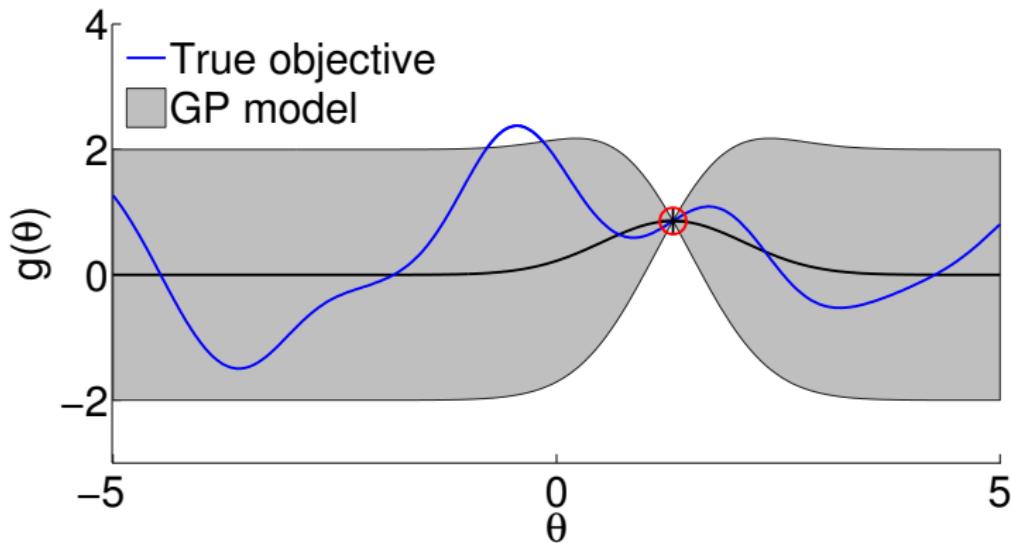
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- Standard model  $\tilde{g}$  is a Gaussian process

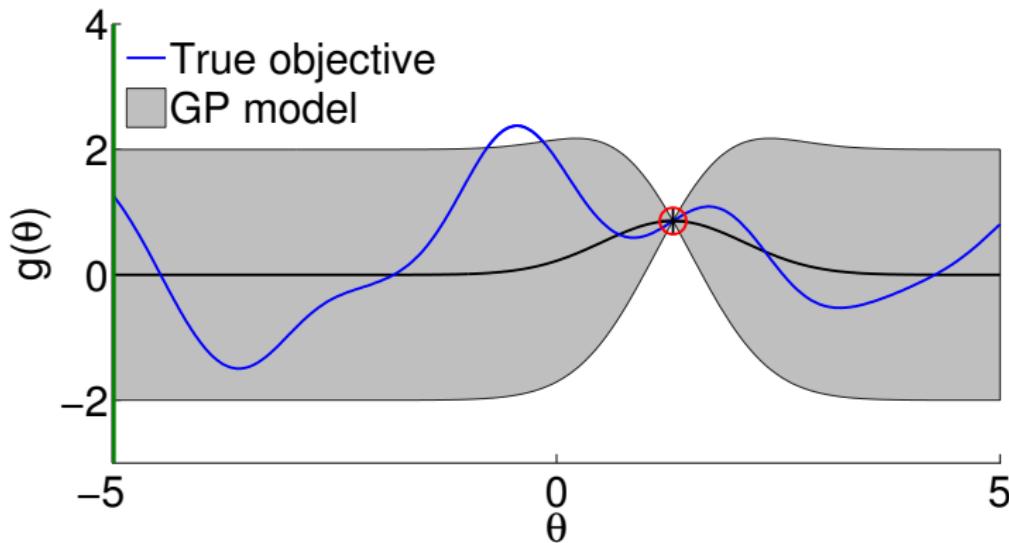
# Bayesian Optimization: Illustration



- Upper-Confidence-Bound (UCB) criterion to select next point

$$\theta^* \in \arg \min_{\theta} \quad \mathbb{E}[\tilde{g}(\theta)] - 2\sqrt{\text{V}[\tilde{g}(\theta)]}$$

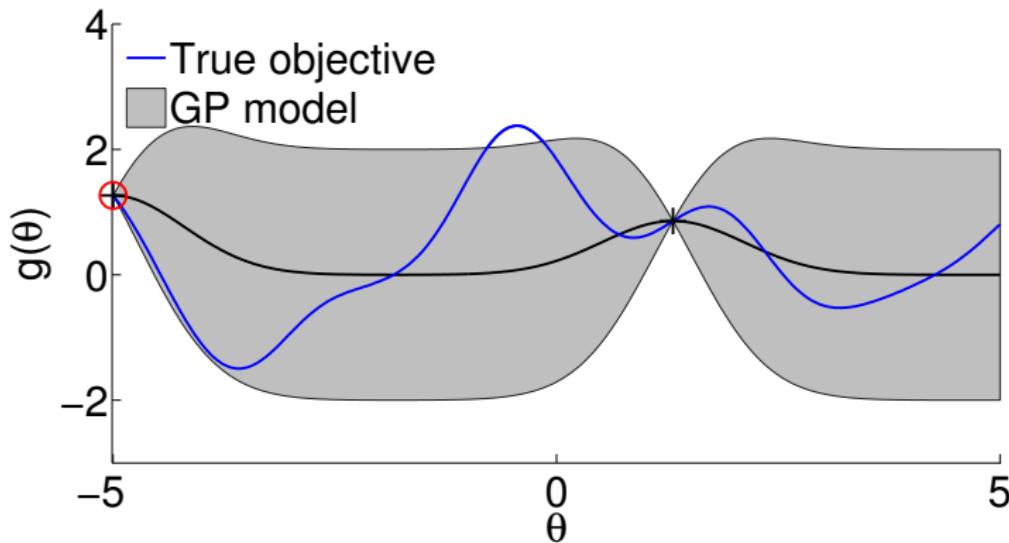
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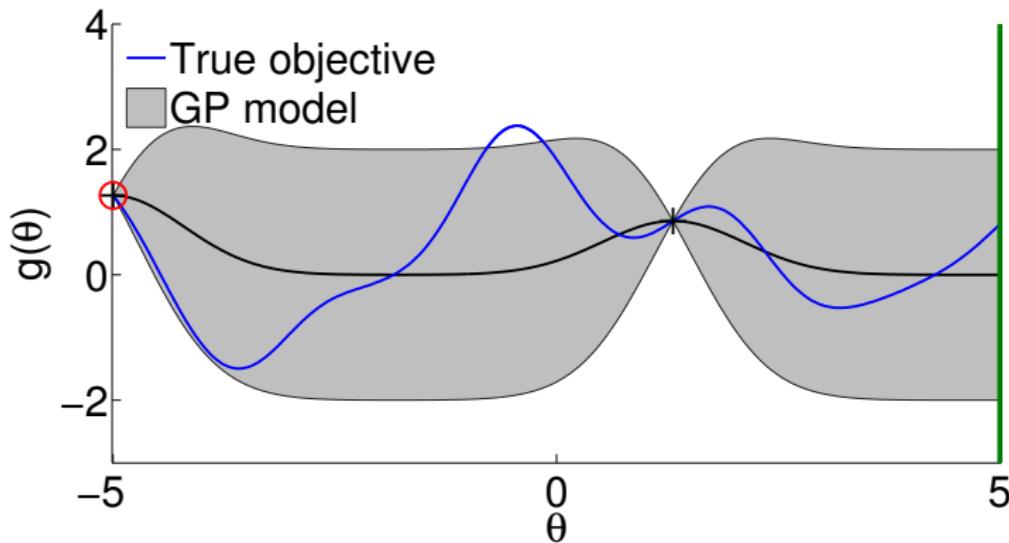
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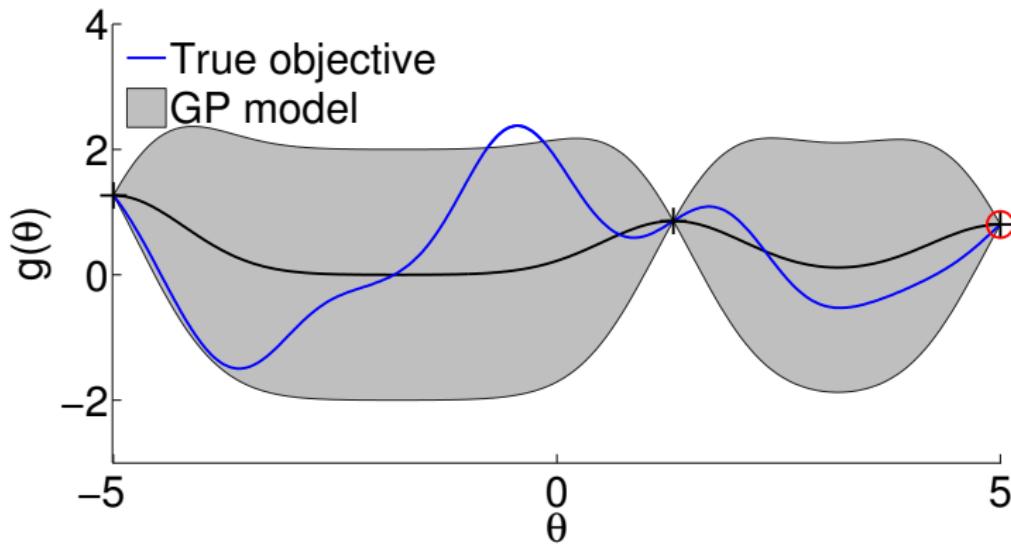
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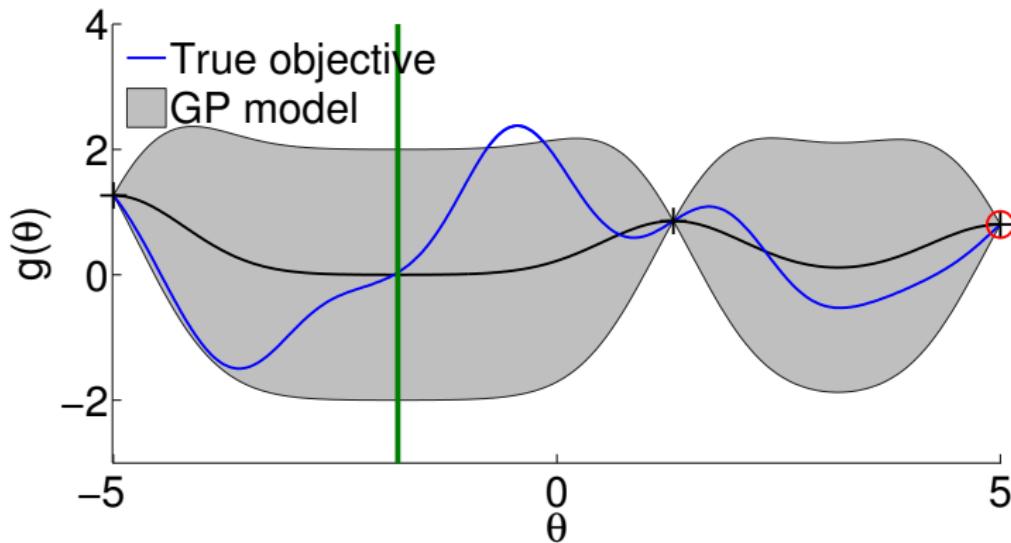
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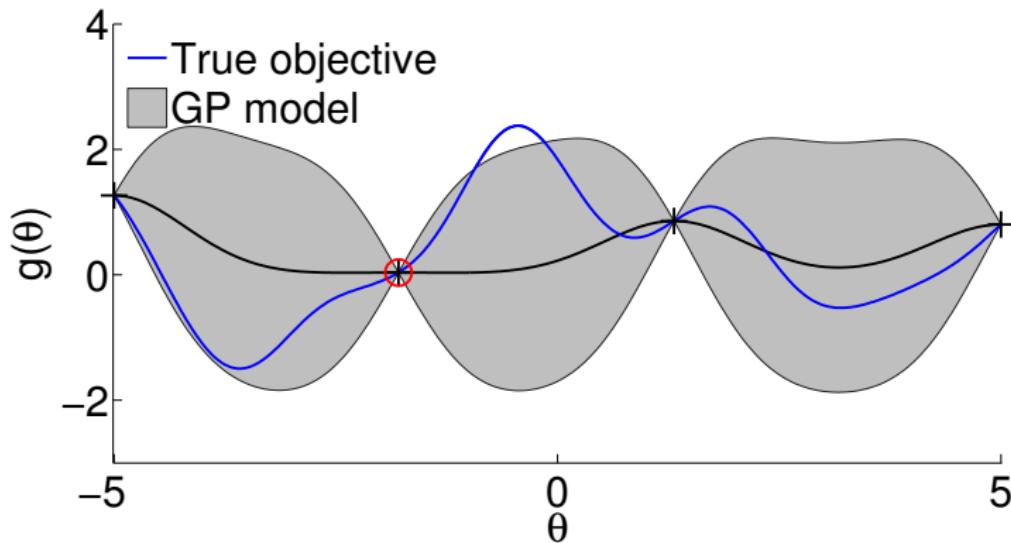
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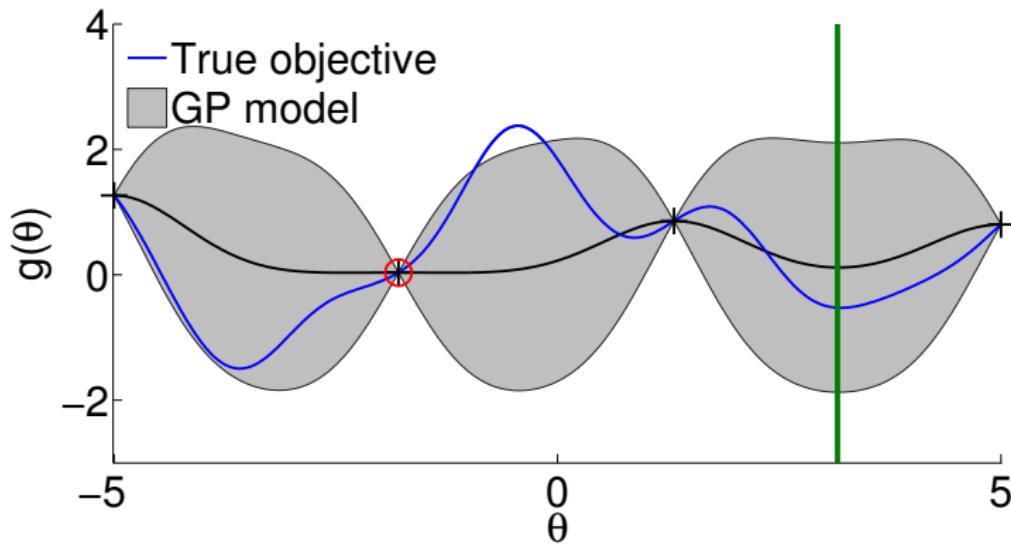
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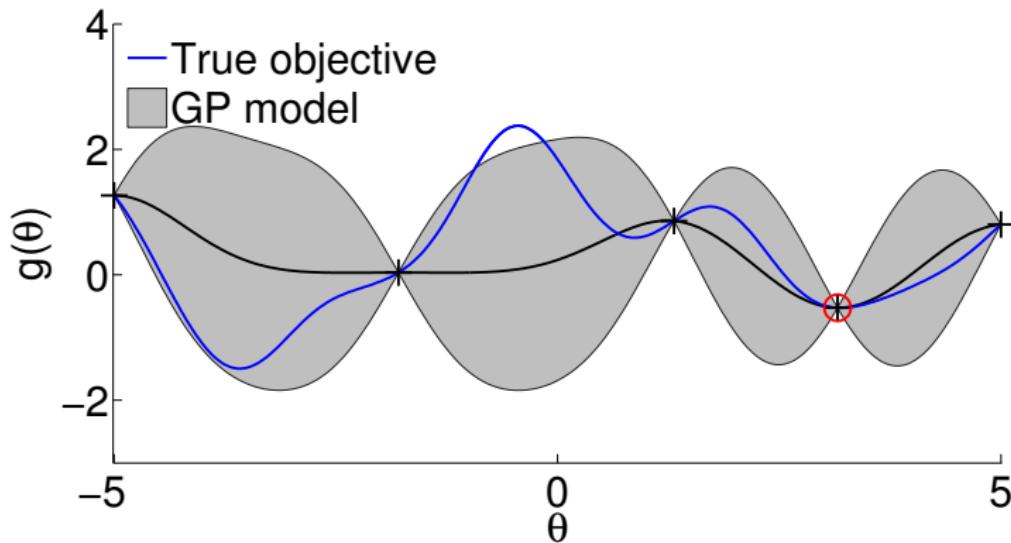
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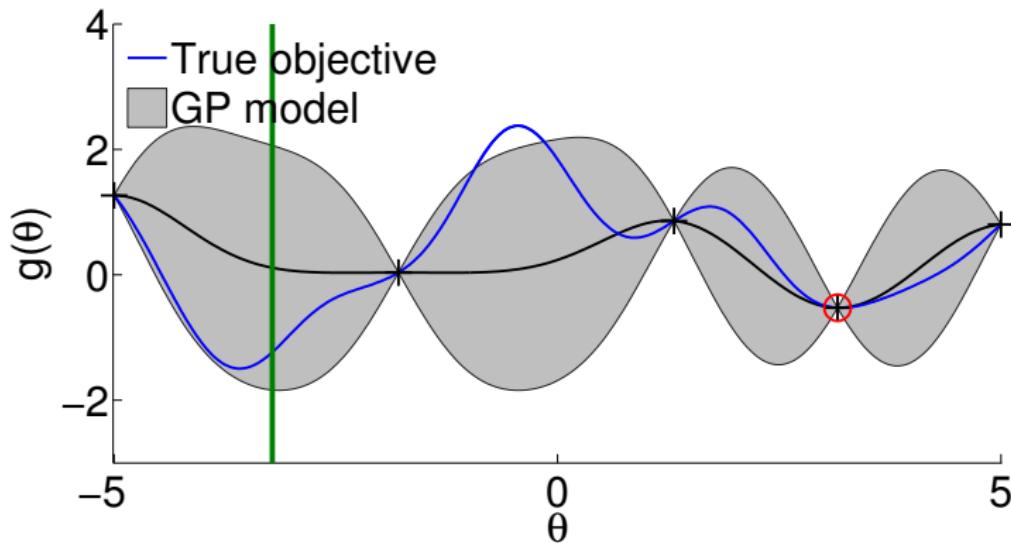
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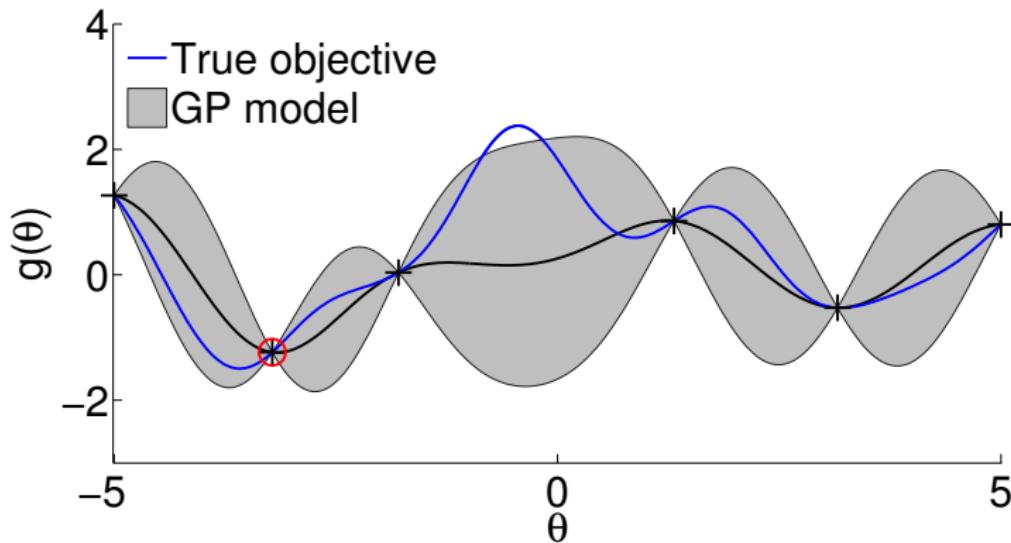
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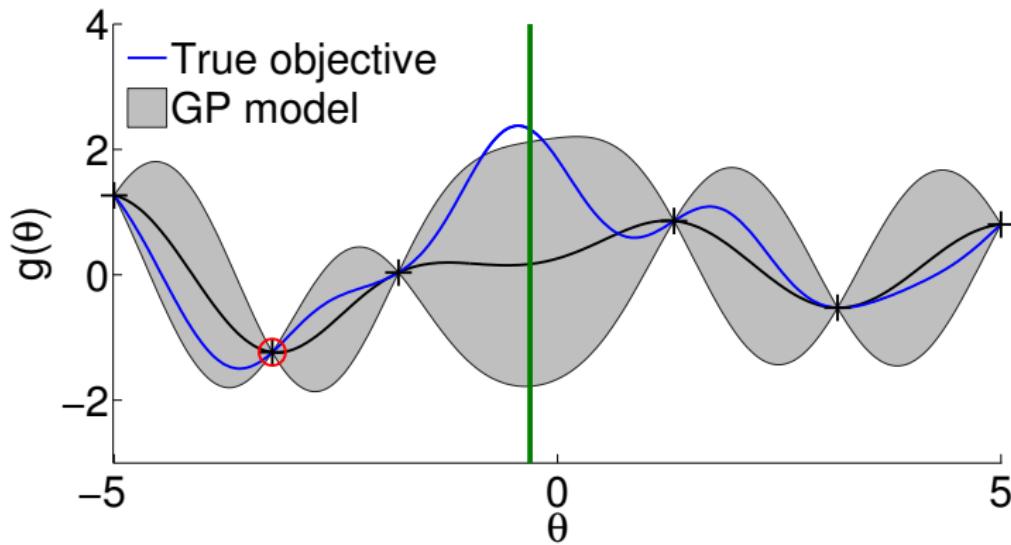
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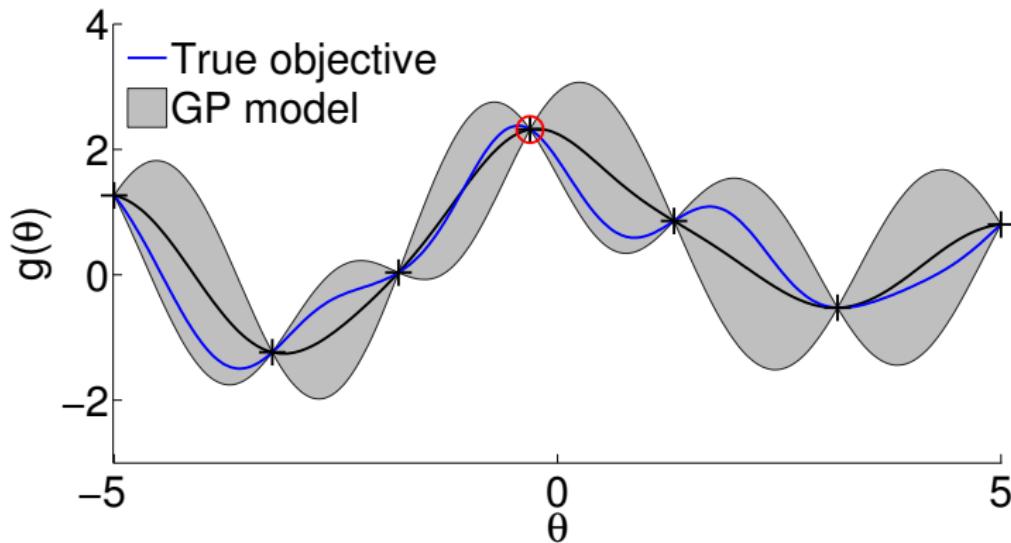
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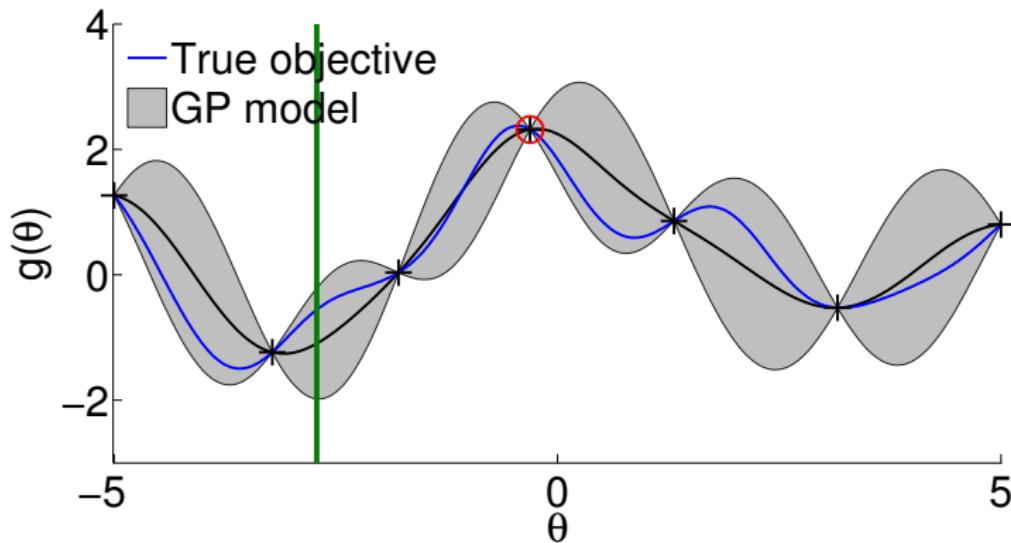
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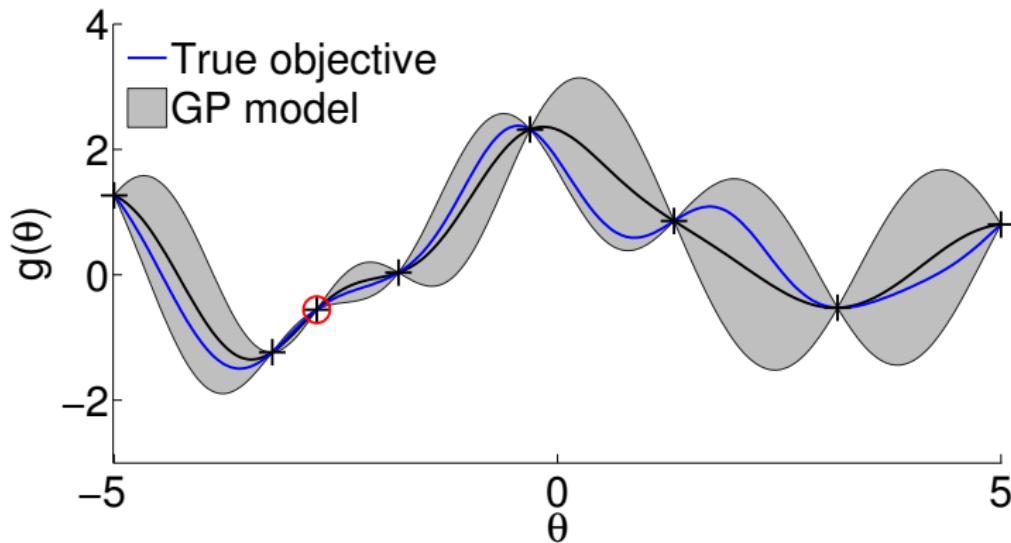
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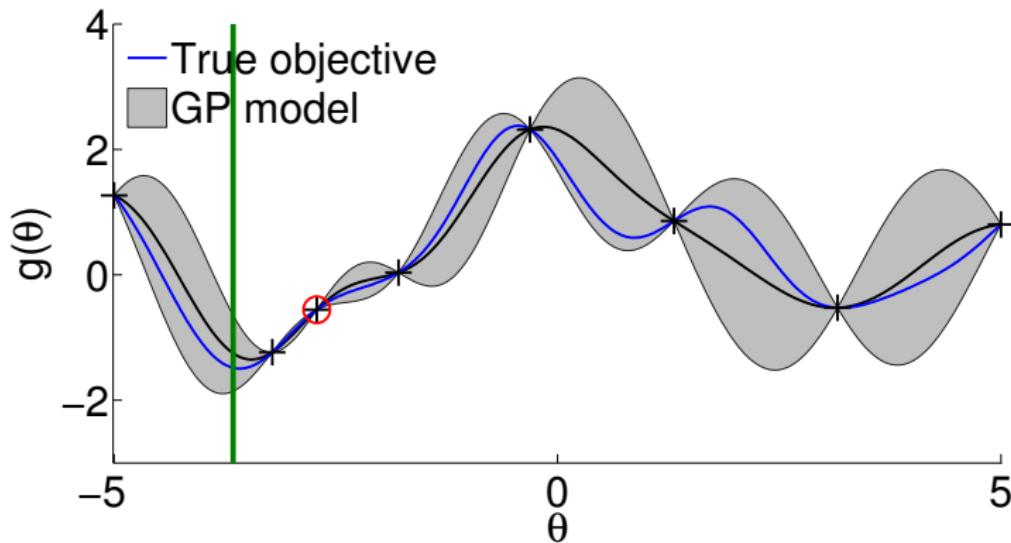
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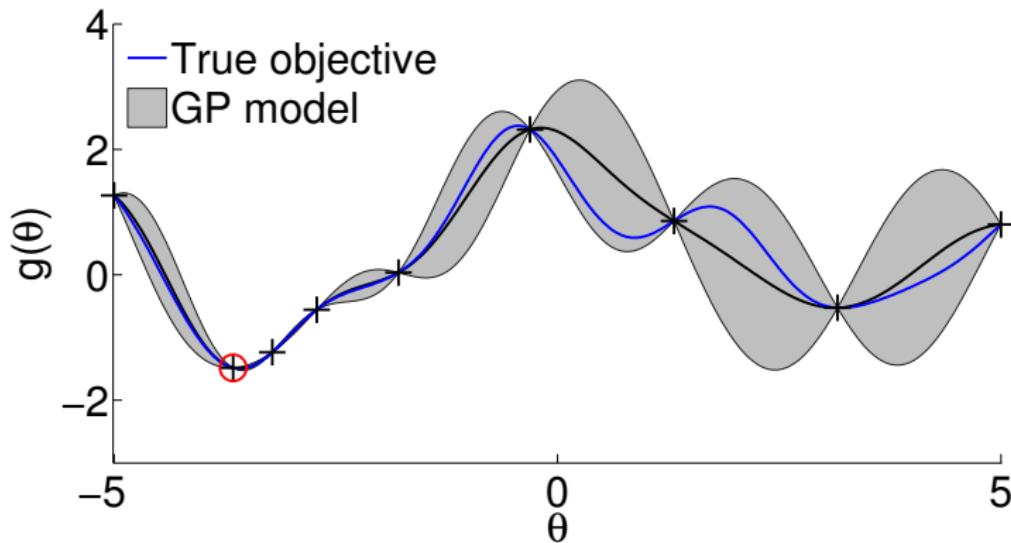
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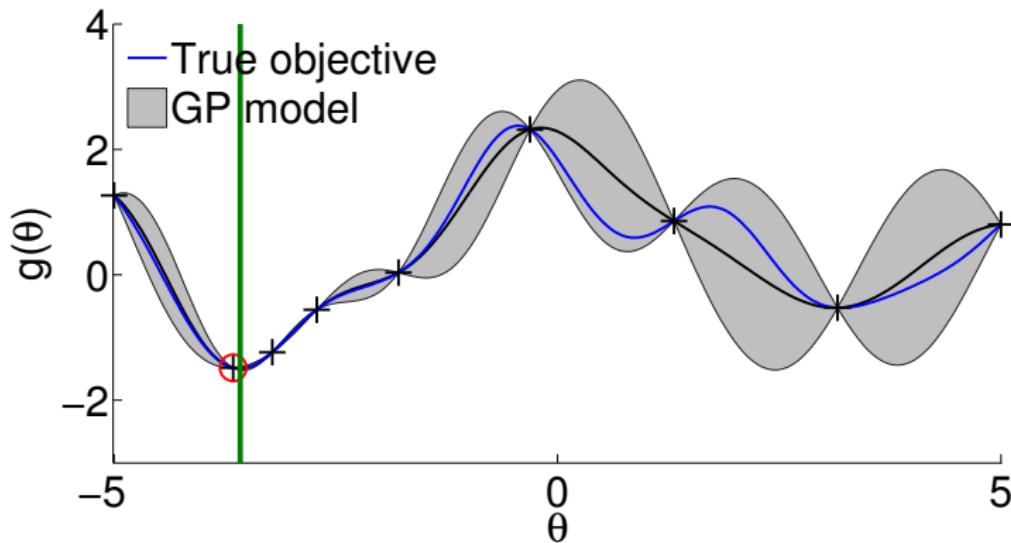
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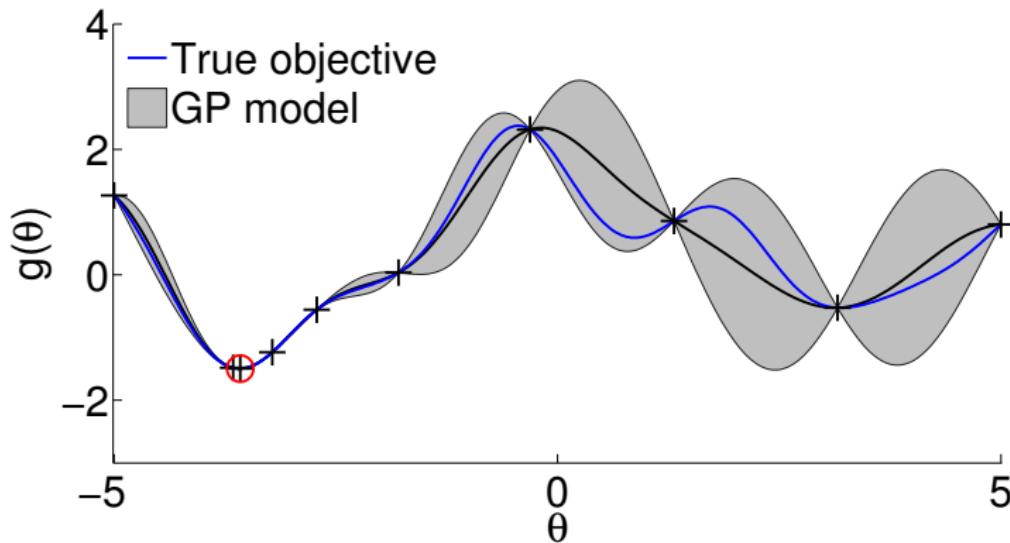
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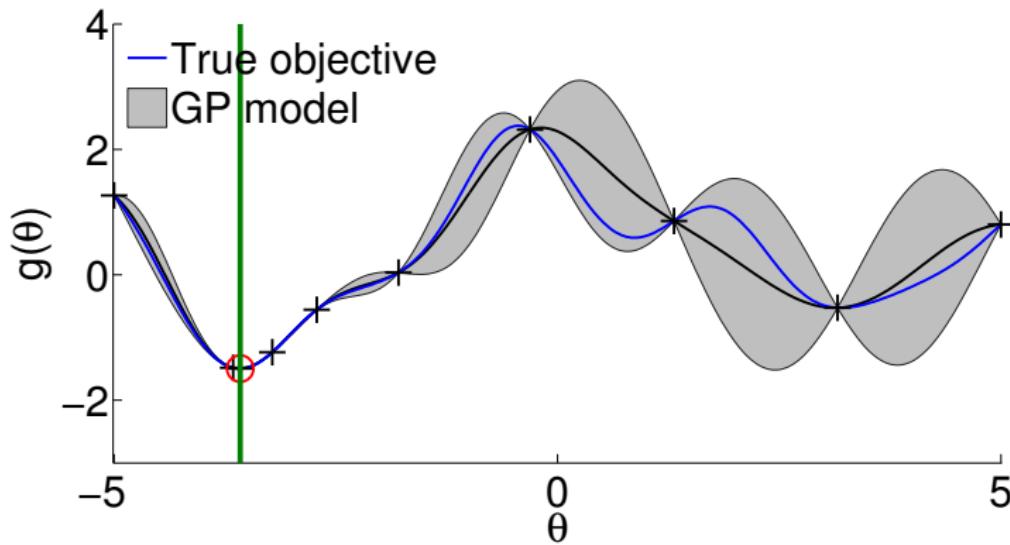
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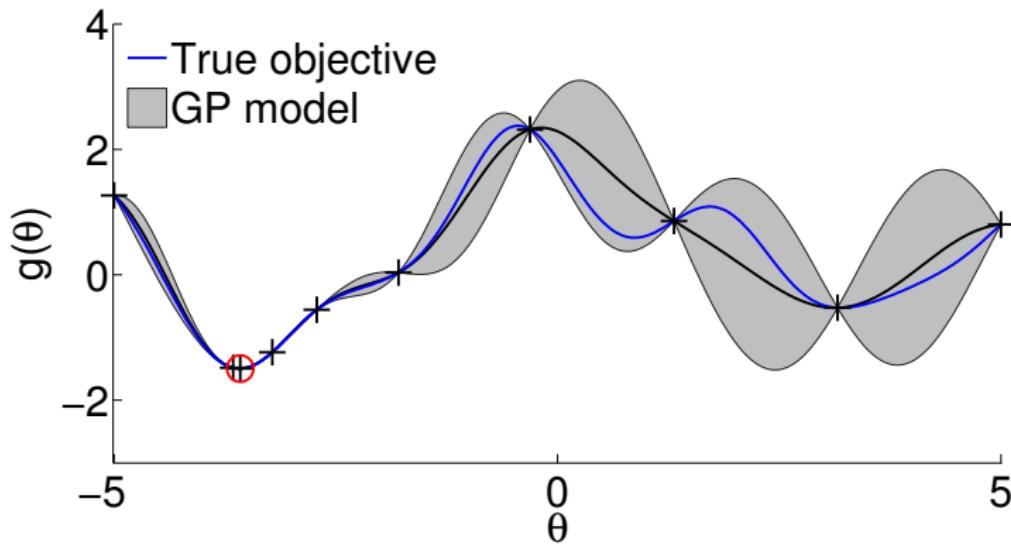
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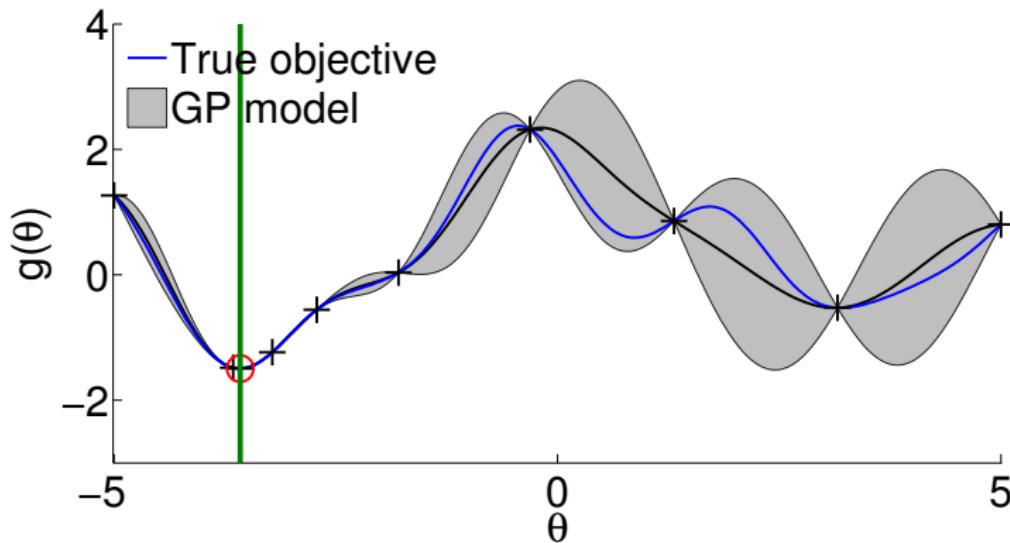
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- Global minimum found after 10 function evaluations

# Bayesian Gait Optimization for Legged Robots



- Fragile biped
  - ▶ Only few experiments feasible
- Maximize robustness and walking speed
- 4 motors:
  - 2 actuated hips + 2 actuated knees
- Controller implemented as a finite-state-machine (8 parameters)



Calandra et al. (LION, 2014): *Bayesian Gait Optimization for Bipedal Locomotion*

Calandra et al. (ICRA, 2014): *An Experimental Evaluation of Bayesian Optimization on Bipedal Locomotion*

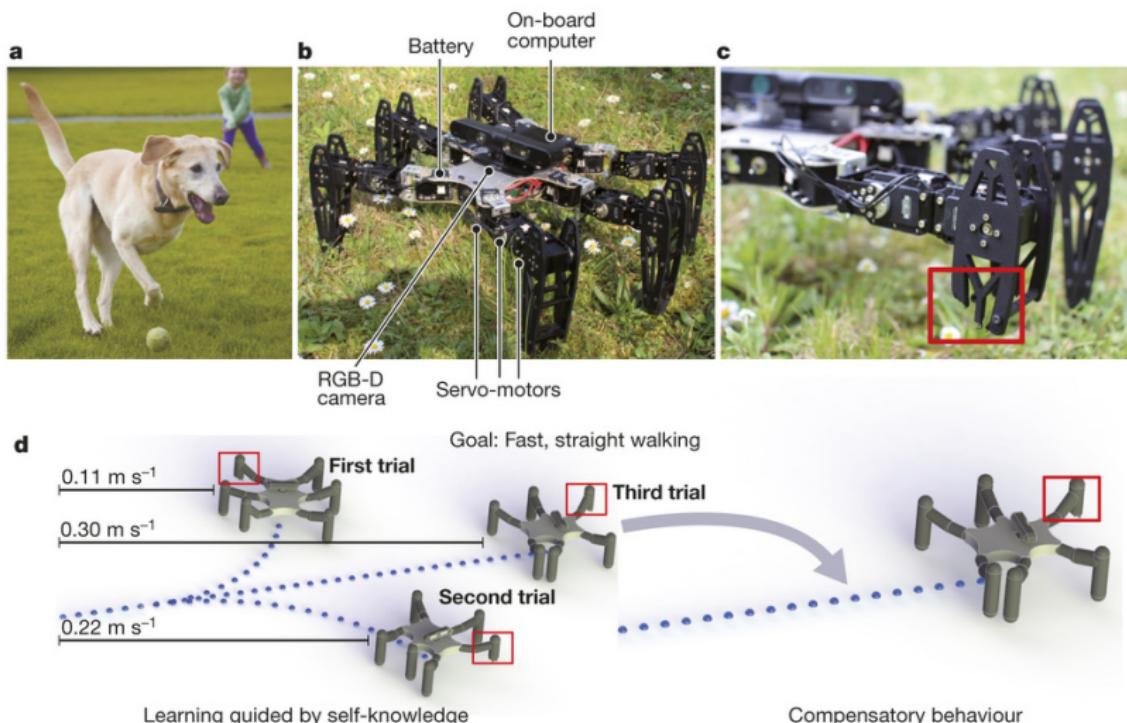
- Fragile biped
  - ▶ Only few experiments feasible
- Maximize robustness and walking speed
- 4 motors:
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- Controller implemented as a finite-state-machine (8 parameters)
- Good parameters found after 80–100 experiments
- Substantial speed-up compared to manual parameter search



Calandra et al. (LION, 2014): *Bayesian Gait Optimization for Bipedal Locomotion*

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# Robots That Learn to Recover from Damage



Cully et al. (2015)

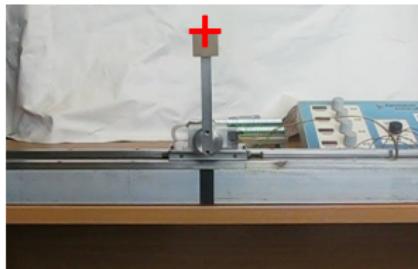


## Bayesian Optimization for Control

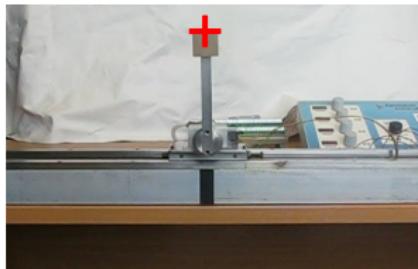
- ▶ Bayesian optimization for learning controllers in a few experiments
- ▶ General framework:  
No assumptions on dynamics, no explicit cost required
- ▶ Limited to few parameters ( $\approx 10\text{--}20$ )

	Cost	Dynamics model	Policy learning	# Parameters
RL	✓	✓	✓	$\leq 10,000$
BO	✗	✗	✓	$\leq 20$

- If a **good dynamics model can be learned** and a cost function can be defined, RL-based methods provide **more flexibility**
- Bayesian optimization is a **more general/easier** framework for learning a few parameters, but it **does not scale to many parameters**



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- In robotics, **data-efficient** learning is critical
- Controller learning based using machine learning
  - Reinforcement Learning
  - Bayesian optimization
- **Key to success:** Uncertainty modeling and exploitation



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**Thank you for your attention**

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