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1字符串

2 数学

2.1 GCD & LCM

- require: c++98
- ✓ 封装
- □测试

gcd: 两个整数的最大公因数 (greatest common divisor) lcm: 两个整数的最小公倍数 (least common multiple)

非递归版本参考于GNU __gcd()源码。 递归版本参考于 std::gcd()源码。

相关函数

```
    std::gcd()
    定义在 <numeric>
    require: C++17
    std::lcm()
    定义在 <numeric>
    require: C++17
    _gcd()
    定义在 <algorithm>
    require: C++98, GNU平台
```

2.1.1 非递归 GCD

```
template <typename T> T gcd(T m, T n) {
    while (n != 0) {
        T t = m % n;
        m = n;
        n = t;
    }
    return m;
}
```

2.1.2 递归 GCD

```
template <typename T> T gcd(T m, T n) {
    return m == 0 ? n : n == 0 ? m : gcd(n, m % n);
}
```

2.1.3 LCM

```
template <typename T> T lcm(T m, T n) {
    return (m != 0 && n != 0) ? (m / gcd(m, n)) * n : 0;
}
```

2.2 扩展GCD

3数据结构

3.1 单调队列

- require: C++98
- ✓ 封装
- ☑测试

这个版本相当于是对STL库中 deque 的重写,但引入了比较模板类。实际使用场景比较灵活,可能并不能照搬,但可以作为参考,并在STL的 deque 太慢时作为替换。

```
template <typename T, typename Cmp = less_equal<T> > struct Monoq {
    Cmp comp;
    const static int N = MAXN;
    T q[N];
    int ft, bk;
    inline Monoq() : ft(0), bk(0) {}
    inline bool empty() { return bk - ft <= 0; }</pre>
    inline int size() { return bk - ft; }
    inline T front() { return q[ft]; }
    inline T back() { return q[bk - 1]; }
    inline void push(T x) {
        while (!empty() && comp(x, back()))
            bk--;
        q[bk++] = x;
    inline void pop_back() {
        if (!empty())
            bk--;
    inline void pop_front() {
        if (!empty())
            ft++;
    inline void clear() { ft = 0, bk = 0; }
    inline T *begin() { return q + ft; }
    inline T *end() { return q + bk; }
};
int a[50] = \{3, 6, 7, 5, 3, 5, 6, 2, 9, 1, 2, 7, 0, 9, 3, 6, 0, 6, 2, 6\};
struct MyCmp {
    inline bool operator()(int x, int y) {
        return a[x] <= a[y]; // strict increase monoq</pre>
        // return a[x] >= a[y]; // strict decrease monoq
    }
};
Monoq<int, MyCmp> q;
```

3.2 ZKW线段树

- require: C++98
- HDU1698
- 封装
- ☑测试

区间修改 + 区间查询

```
#include <bits/stdc++.h>
using namespace std;
const int M = 1 \ll 17;
const int INF = 1e9;
int T[M + M + 1], lazy[M + M + 1];
void modify(int 11, int rr, int v) {
    11 += M - 1, rr += M + 1;
    for (int i = 20, l, r; i; i--) {
        l = ll \gg i, r = rr \gg i;
        if (lazy[1]) {
            lazy[1 * 2] = lazy[1 * 2 + 1] = lazy[1];
            T[1 * 2] = T[1 * 2 + 1] = lazy[1] * (1 << (i - 1));
            lazy[1] = 0;
        }
        if (lazy[r]) {
            lazy[r * 2] = lazy[r * 2 + 1] = lazy[r];
            T[r * 2] = T[r * 2 + 1] = lazy[r] * (1 << (i - 1));
            lazy[r] = 0;
        }
    for (int l = ll, r = rr, num = 1; l > 1; l >>= 1, r >>= 1, num <<= 1) {
        if ((1 ^ r ^ 1) > 1) {
            if (~1 & 1)
                lazy[1 ^ 1] = v, T[1 ^ 1] = v * num;
            if (r & 1)
                lazy[r ^ 1] = v, T[r ^ 1] = v * num;
        }
        T[1 >> 1] = T[1] + T[1 ^ 1];
        T[r >> 1] = T[r] + T[r ^ 1];
    }
}
int query(int 1, int r) {
    int ansL = 0, ansR = 0, ln = 0, rn = 0, nn = 1;
    for (1 += M - 1, r += M + 1; 1 ^ r ^ 1; 1 >>= 1, r >>= 1, nn <<= 1) {
        if (lazy[1])
            ansL = lazy[1] * ln;
        if (lazy[r])
            ansR = lazy[r] * rn;
        if (~1 & 1)
```

```
ansL += T[1 ^ 1], ln += nn;
       if (r & 1)
            ansR += T[r ^ 1], rn += nn;
    for (; 1; 1 >>= 1, r >>= 1) {
        if (lazy[1])
            ansL = lazy[1] * ln;
        if (lazy[r])
            ansR = lazy[r] * rn;
    }
    return ansL + ansR;
}
int main() {
    ios::sync_with_stdio(false);
    int t;
    cin >> t;
    for (int ca = 1; ca <= t; ca++) {
        int n, q;
        cin >> n >> q;
       modify(1, n, 1);
        while (q--) {
            int x, y, z;
           cin >> x >> y >> z;
            modify(x, y, z);
        }
        printf("Case %d: The total value of the hook is %d.\n", ca,
               query(1, n));
   }
}
```

4 图论

5 动态规划

6 计算几何

7 其他

7.1 高精度

- require: C++11
- ✓ 封装
- □测试

高精度四则运算。

```
#include <bits/stdc++.h>
typedef long long 11;
using namespace std;
struct Unsigned_BigInt {
    ll k = 10; // base-k positional notation
    vector<ll> a;
    Unsigned_BigInt() {
        a.clear();
        a.push_back(∅);
    Unsigned_BigInt(ll v) {
        a.clear();
        a.push_back(abs(v));
        this->regular();
    }
    Unsigned_BigInt(string s) {
        a.clear();
        for (ll i = s.length() - 1; i >= 0 && s[i] != '-'; i--)
            a.push_back(s[i] - '0');
    void regular() {
        for (ll i = 0; i < a.size(); i++)
            if (a[i] >= k || a[i] < 0) {
                if (i + 1 < a.size())
                    a[i + 1] += (a[i] >= 0 ? a[i] / k : (a[i] + 1) / k - 1);
                else
                    a.push_back(a[i] / k);
                a[i] = (a[i] \% k + k) \% k;
            }
    void give(ll i, ll v) {
        if (i < a.size())</pre>
            a[i] += v;
        else
            a.push_back(v);
    void shrink() {
        for (ll i = a.size() - 1; i >= 0 && a[i] == 0; i--)
            a.pop_back();
```

```
if (a.empty())
        a.push_back(0);
}
bool operator<(const Unsigned_BigInt &b) const {</pre>
    if (a.size() == b.a.size()) {
        ll i = a.size() - 1;
        while (a[i] == b.a[i] \&\& i >= 0)
        return i >= 0 ? a[i] < b.a[i] : false;
    } else
        return a.size() < b.a.size();</pre>
Unsigned_BigInt operator+(const Unsigned_BigInt &b) const {
    Unsigned_BigInt c;
    for (ll i = 0; i < max(a.size(), b.a.size()); i++)
        c.give(i,
               (i < a.size() ? a[i] : 0) + (i < b.a.size() ? b.a[i] : 0));
    c.regular();
    return c;
Unsigned_BigInt operator-(const Unsigned_BigInt &b) const {
    Unsigned_BigInt c;
    bool less = *this < b;</pre>
    for (ll i = 0; i < max(a.size(), b.a.size()); i++) {
        ll temp = (i < a.size() ? a[i] : 0) - (i < b.a.size() ? b.a[i] : 0);
        c.give(i, !less ? temp : -temp);
    c.regular();
    c.shrink();
    return c;
Unsigned BigInt operator*(const 11 &b) const {
    11 bb = abs(b);
    Unsigned_BigInt c;
    for (ll i = 0; i < a.size(); i++)
        c.give(i, a[i] * bb);
    c.regular();
    return c;
Unsigned_BigInt operator*(const Unsigned_BigInt &b) const {
    Unsigned BigInt c;
    for (ll i = 0; i < b.a.size(); i++)
        for (ll j = 0; j < a.size(); j++)
            c.give(j + i, a[j] * b.a[i]);
    c.regular();
    return c;
}
Unsigned_BigInt operator/(const 11 &b) const {
    11 bb = abs(b);
    Unsigned_BigInt c = *this;
    ll dividend = ∅;
    for (ll i = a.size() - 1; i >= 0; i--) {
        dividend = dividend * k + a[i];
        c.a[i] = dividend / bb;
```

```
dividend %= bb;
        }
        c.shrink();
        return c;
    11 operator%(const 11 &b) const {
        11 r = 0;
        for (ll i = a.size() - 1; i >= 0; i--)
            r = ((r * k) % b + a[i]) % b;
        return r;
    }
    void print() {
        for (auto it = a.rbegin(); it != a.rend(); it++)
            // cout << *it;
            printf("%lld", *it);
        // cout << endl;</pre>
        printf("\n");
    }
};
struct BigInt {
    bool sign = false; // 0: +, 1: -
    Unsigned_BigInt num;
    BigInt() : sign(∅), num(Unsigned_BigInt()) {}
    BigInt(ll v) : sign(v < ∅), num(Unsigned_BigInt(v)) {}</pre>
    BigInt(string s) : sign(s[0] == '-'), num(Unsigned_BigInt(s)) {}
    BigInt(Unsigned_BigInt num, bool sign = false) : sign(sign), num(num) {}
    bool operator<(const BigInt &b) const {</pre>
        if (sign ^ b.sign)
            return sign;
        else
            return ((!sign) ? num < b.num : b.num < num);</pre>
    BigInt operator+(const BigInt &b) const {
        if (sign)
            return -(-*this - b); // a + b == -(-a - b)
        if (b.sign)
            return *this - (-b); // a + b == a - (-b)
        return BigInt(num + b.num);
    BigInt operator-() const { return BigInt(num, !sign); }
    BigInt operator-(const BigInt &b) const {
        if (sign)
            return -(-*this + b); // a - b == -(-a + b)
        if (b.sign)
            return *this + (-b); // a - b == a + (-b)
        return BigInt(num - b.num, num < b.num);</pre>
    BigInt operator*(const 11 &b) const {
        return BigInt(num * b, sign ^ b < ∅);
    BigInt operator*(const BigInt &b) const {
        return BigInt(num * b.num, sign ^ b.sign);
    }
```

```
BigInt operator/(const 11 &b) const {
        return BigInt(num / b, sign ^ b < ∅);
    11 operator%(const 11 &b) const { return sign ? -(num % b) : num % b; }
    void print() {
        // cout << (!sign || (num.a.size() == 1 && num.a[0] == 0) ? "" : "-");
        printf(!sign || (num.a.size() == 1 && num.a[0] == 0) ? "" : "-");
        num.print();
    }
};
ostream &operator<<(ostream &os, const Unsigned_BigInt &b) {</pre>
    for (auto it = b.a.rbegin(); it != b.a.rend(); it++)
        os << *it;
    return os;
ostream &operator<<(ostream &os, const BigInt &b) {</pre>
    os << (!b.sign || (b.num.a.size() == 1 && b.num.a[0] == 0) ? "" : "-");
    os << b.num;
    return os;
}
int main() {
    string s1;
    string s2;
    // freopen("./test.in", "r", stdin);
    // freopen("./test.out", "w", stdout);
    while (cin >> s1 >> s2) {
        cout << (BigInt(s1) * BigInt(s2));</pre>
        // (BigInt(s1) * BigInt(s2)).print();
    }
    // fclose(stdin);
    // fclose(stdout);
}
```

7.2 二分答案

- require: C++11
- ✓ 封装
- □测试

对给定函数的 y, 二分查找 x

离散

```
#include <bits/stdc++.h>
using namespace std;

template <typename T> bool dec(T _a, T _b) { return greater<T>()(_a, _b); }
```

```
template <typename T> bool inc(T _a, T _b) { return less<T>()(_a, _b); }
// template <typename T> bool incid(T _a, T _b) {
// return less<T>()(a[_a].id, a[_b].id);
// }
int a[10] = \{7, 5, 5, 5, 3, 3, 3, 1, 1, 1\};
template <typename Tx = int, typename Ty = int>
Tx upperbound(Ty(getval)(Tx), Tx first, Tx last, const Ty &val,
              bool(comp)(Ty, Ty) = inc<Ty>) {
    Tx len = last - first;
    while (len > ∅) {
        Tx half = len >> 1;
        Tx middle = first + half;
        if (comp(val, getval(middle)))
            len = half;
        else {
            first = middle;
            ++first;
            len = len - half - 1;
        }
    return first;
}
template <typename Tx = int, typename Ty = int>
Tx lowerbound(Ty(getval)(Tx), Tx first, Tx last, const Ty &val,
              bool(comp)(Ty, Ty) = inc<Ty>) {
    Tx len = last - first;
    while (len > 0) {
        Tx half = len >> 1;
        Tx middle = first + half;
        if (comp(getval(middle), val)) {
            first = middle;
            first++;
            len = len - half - 1;
        } else
            len = half;
    return first;
}
int geta(int i) { return a[i]; }
int main() { cout << upperbound(geta, 0, 10, 1, dec<int>); }
```

7.3 Berlekamp-Massey

- require:
- ✓ 封装
- ■测试

```
#include <bits/stdc++.h>
using namespace std;
#define rep(i,a,n) for (long long i=a;i<n;i++)</pre>
#define per(i,a,n) for (long long i=n-1;i>=a;i--)
#define pb push_back
#define mp make_pair
#define all(x) (x).begin(),(x).end()
#define fi first
#define se second
#define SZ(x) ((long long)(x).size())
typedef vector<long long> VI;
typedef long long 11;
typedef pair<long long,long long> PII;
const 11 \mod = 1e9+7;
11 powmod(11 a, 11 b) {11 res=1; a\%=mod; assert(b>=0); for(;b;b>>=1)
{if(b&1)res=res*a%mod;a=a*a%mod;}return res;}
// head
long long n;
namespace linear_seq
    const long long N=10010;
    11 res[N],base[N],_c[N],_md[N];
    vector<long long> Md;
    void mul(l1 *a,l1 *b,long long k)
    {
        rep(i,0,k+k) _c[i]=0;
        rep(i,0,k) if (a[i]) rep(j,0,k)
            _c[i+j]=(_c[i+j]+a[i]*b[j])%mod;
        for (long long i=k+k-1; i>=k; i--) if (_{c}[i])
            rep(j,0,SZ(Md)) _c[i-k+Md[j]]=(_c[i-k+Md[j]]-_c[i]*_md[Md[j]])%mod;
        rep(i,0,k) a[i]=_c[i];
    long long solve(ll n, VI a, VI b)
    { // a 系数 b 初值 b[n+1]=a[0]*b[n]+...
//
          printf("%d\n",SZ(b));
        11 ans=0,pnt=0;
        long long k=SZ(a);
        assert(SZ(a)==SZ(b));
        rep(i,0,k) _md[k-1-i]=-a[i];_md[k]=1;
        Md.clear();
        rep(i,0,k) if (\_md[i]!=0) Md.push_back(i);
        rep(i,0,k) res[i]=base[i]=0;
        res[0]=1;
        while ((111<<pnt)<=n) pnt++;</pre>
        for (long long p=pnt;p>=0;p--)
            mul(res,res,k);
            if ((n>>p)&1)
```

```
{
                for (long long i=k-1;i>=0;i--) res[i+1]=res[i];res[0]=0;
                 rep(j,0,SZ(Md)) res[Md[j]]=(res[Md[j]]-res[k]*_md[Md[j]])%mod;
            }
        }
        rep(i,0,k) ans=(ans+res[i]*b[i])%mod;
        if (ans<0) ans+=mod;
        return ans;
    VI BM(VI s)
    {
        VI C(1,1), B(1,1);
        long long L=0, m=1, b=1;
        rep(n,0,SZ(s))
        {
            11 d=0;
            rep(i, 0, L+1) d=(d+(l1)C[i]*s[n-i])%mod;
            if (d==0) ++m;
            else if (2*L <= n)
            {
                VI T=C;
                11 c=mod-d*powmod(b,mod-2)%mod;
                while (SZ(C) < SZ(B) + m) C.pb(0);
                rep(i,0,SZ(B)) C[i+m]=(C[i+m]+c*B[i])%mod;
                L=n+1-L; B=T; b=d; m=1;
            }
            else
            {
                11 c=mod-d*powmod(b,mod-2)%mod;
                 while (SZ(C) < SZ(B) + m) C.pb(0);
                 rep(i, 0, SZ(B)) C[i+m] = (C[i+m] + c*B[i]) mod;
                ++m;
            }
        }
        return C;
    }
    long long gao(VI a,ll n)
    {
        VI c=BM(a);
        c.erase(c.begin());
        rep(i, 0, SZ(c)) c[i] = (mod - c[i]) mod;
        return solve(n,c,VI(a.begin(),a.begin()+SZ(c)));
    }
};
int main()
{
    while(~scanf("%I64d", &n))
    { printf("%I64d\n",linear_seq::gao(VI{1,5,11,36,95,281,781,2245,6336,18061,
51205},n-1));
    }
}
```