

# Assignment 4

Ozone

February 6, 2018

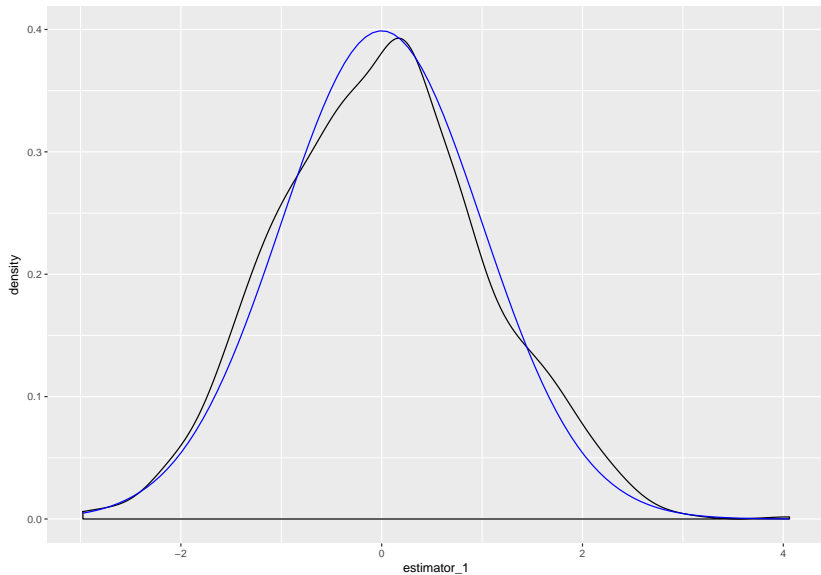
## 1. Explain to your students

$y = 3x + 2 + e$ , where  $x \sim N(1, 1)$ ,  $e \sim \chi^2(2)$

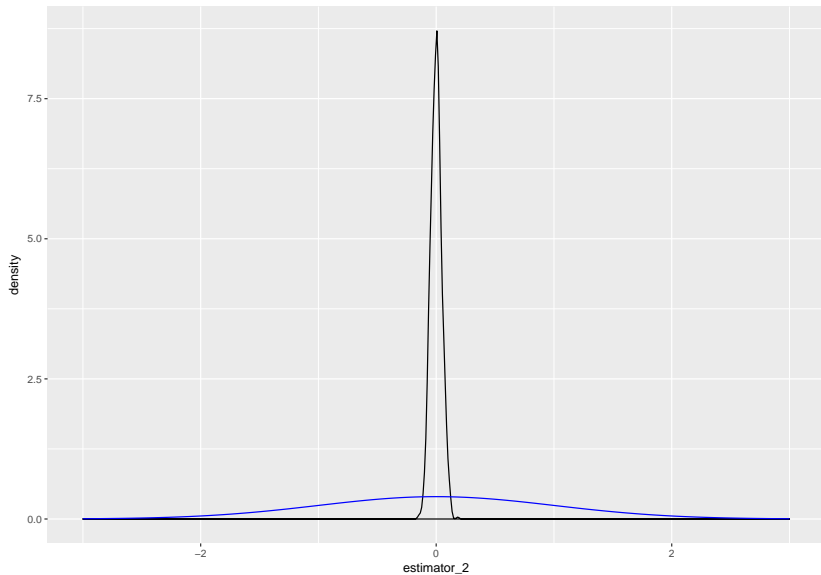
estimator\_1 =  $\frac{\hat{\beta} - \beta}{\text{std.err}(\hat{\beta})}$  is approximately  $N(0, 1)$

estimator\_2 =  $\hat{\beta} - \beta$  converges to 0

# OLS estimator converges to a distribution



## OLS estimator converges to a constant

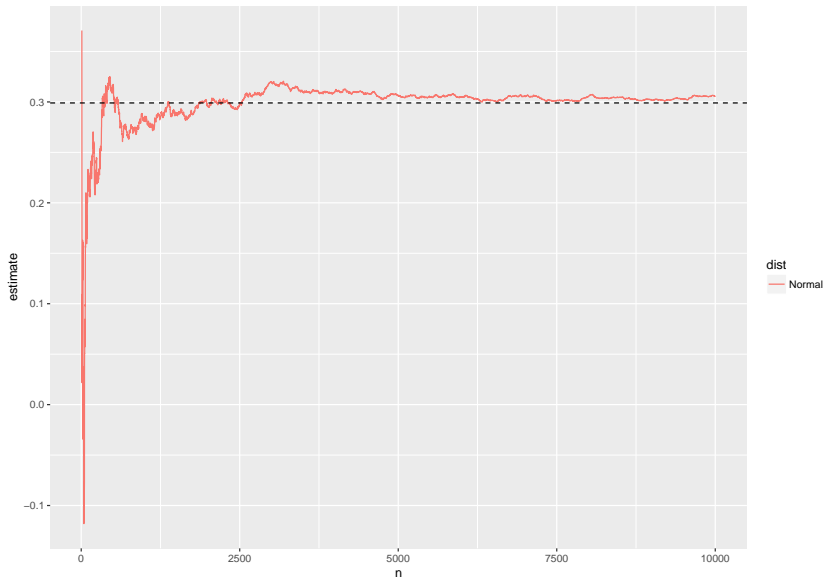


## 2. Augustin-Louis Cauchy

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##
## \begin{table}[!htbp] \centering
##   \caption{Means and sd of the OLS coefficients}
##   \label{}
## \begin{tabular}{@{\extracolsep{5pt}} cccc}
## \ll[-1.8ex]\hline
## \hline \ll[-1.8ex]
##   & dist & means & sd & \ll
## \hline \ll[-1.8ex]
## 1 & Normal & $0.299$ & $0.026$ & \ll
## 2 & Cauchy & $0.352$ & $0.314$ & \ll
## \hline \ll[-1.8ex]
## \end{tabular}
## \end{table}
```

- ▶ In the Normal distribution case, With sample size  $n$  inceasing,  $\hat{\beta}$  converges to the true value  $\beta = 0.3$  as shown in the graph.
- ▶ The Cauchy distribution does not have finite moments of any

# Normal



# Cauchy

