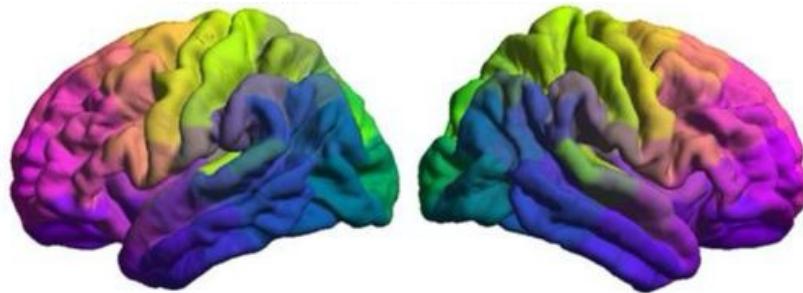


# GRADIENTS OF BRAIN ORGANIZATION: *WHAT, WHY, HOW?*



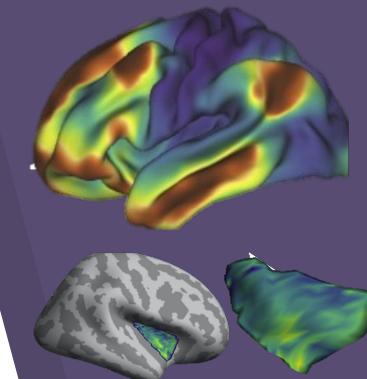
Penn LINC Lab Meeting 9.21.20

# GRADIENTS: *WHAT?*

An axis of continuous feature variation across areas  
of the brain

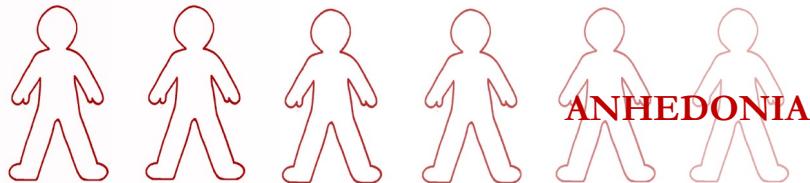
- Can be examined across the cortex or within one structure
- Can be computed at the level of vertices, voxels, or regions
- Can be derived from one metric or multivariate feature matrix

Gradients help us quantify and visualize inter-area  
feature similarity and divergence across the brain



# GRADIENTS:

*WHAT?*

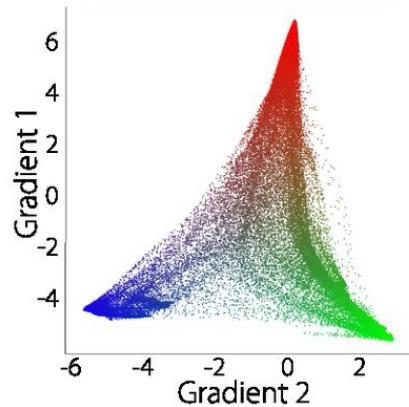
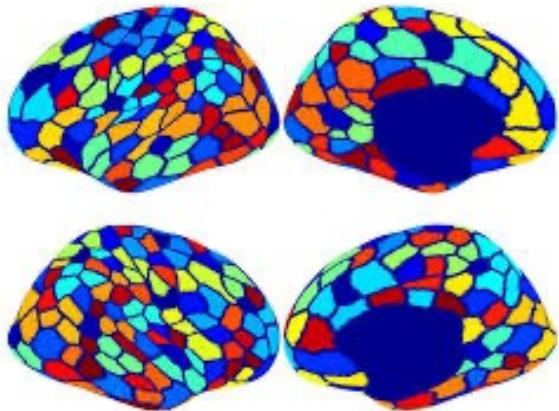


DISCRETE



SPECTRUM

# GRADIENTS: *WHAT?*



DISCRETE

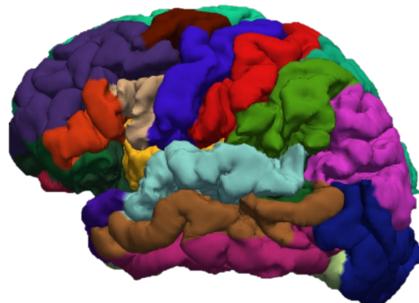
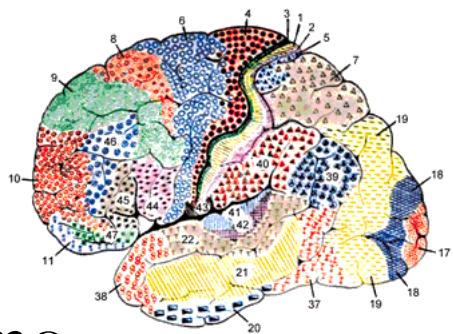


SPECTRUM

# GRADIENTS: WHY?

Vogt  
Brodmann  
Von Economo

FreeSurfer  
Schaefer  
Atlases *etc.*



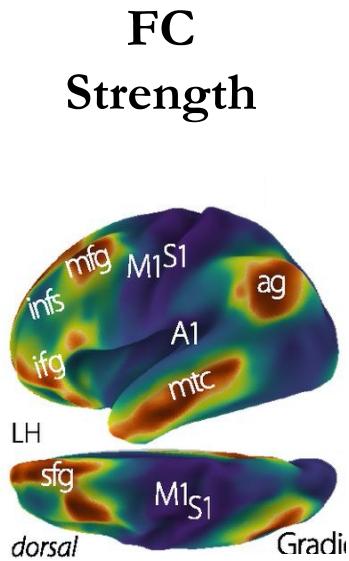
Bailey and von Bonin (1951):  
Drawing of sharp areal boundaries is  
a fundamental defect of most maps

Elkhonon Goldberg (1989):  
Gradiental approach to neocortical  
functional organization

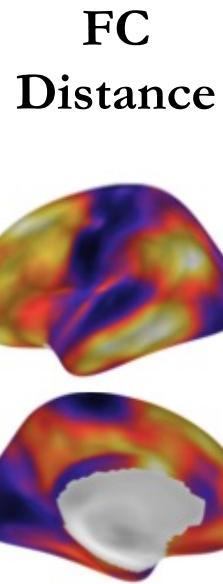
Mesulam (1998):  
From sensation to cognition

Daniel Margulies,  
Boris Bernhardt

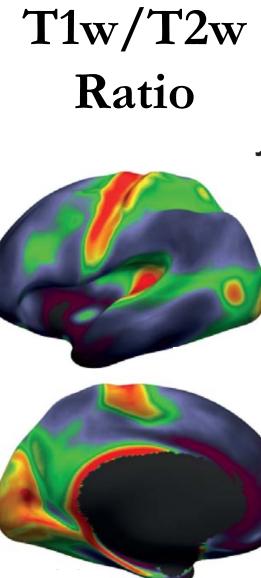
# GRADIENTS: *WHY?*



*Margulies et al. 2016*



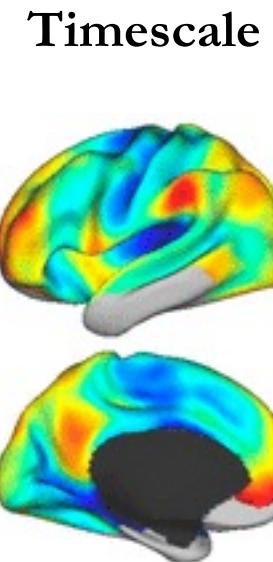
*Oligschläger et al. 2017*



*Wang et al. 2019*

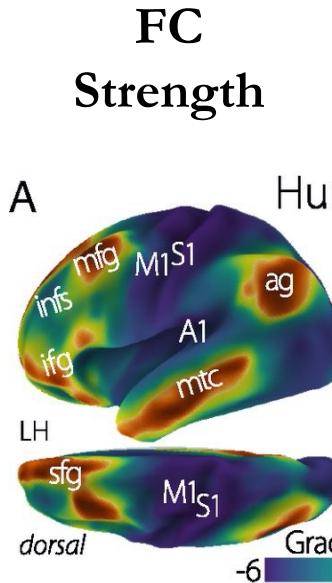


*Burt et al. 2018*

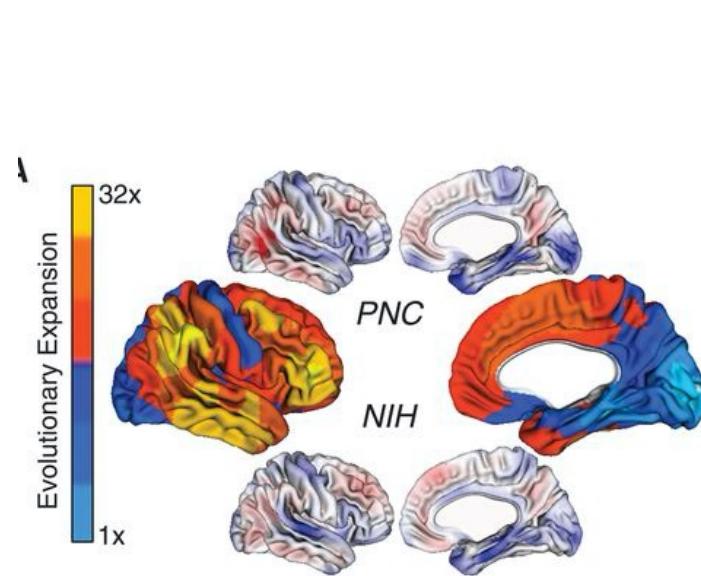
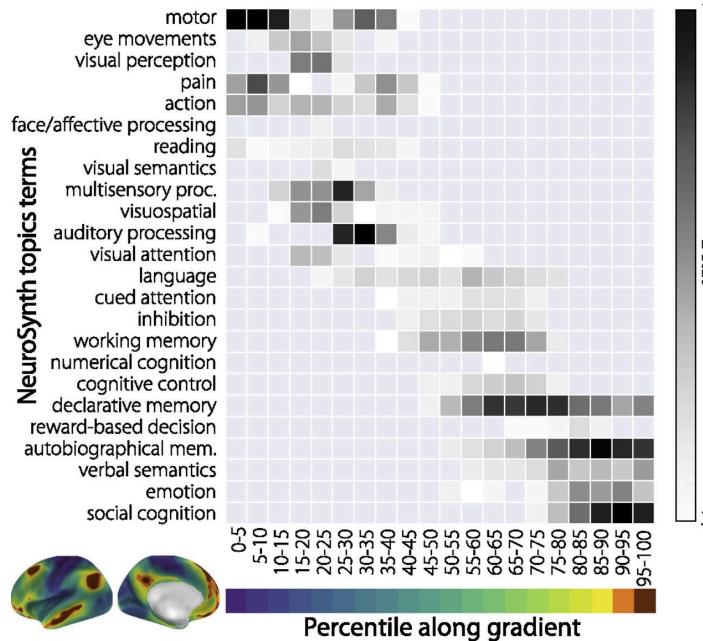


*Raut et al. 2020*

# GRADIENTS: *WHY?*



Margulies et al. 2016



Hill et al. 2010  
Reardon et al. 2018

**Sensory-association gradient: a natural, hierarchical axis of cortical organization with evolutionary origins**

# A molecular gradient along the longitudinal axis of the human hippocampus informs large-scale behavioral systems

Jacob W. Vogel , Renaud La Joie, Michel J. Grothe, Alexandr Diaz-Papkovich, Andrew Doyle, Etienne Vachon-Presseau, Claude Lepage, Reinder Vos de Wael, Rhalena A. Thomas, Yasser Iturria-Medina, Boris Bernhardt, Gil D. Rabinovici & Alan C. Evans 

*Nature Communications* 11, Article number: 960 (2020) | [Cite this article](#)



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Dispersion of functional gradients across the adult lifespan

Richard A.I. Bethlehem <sup>a,b,1,\*</sup>, Casey Paquola <sup>c,1</sup>, Jakob Seidlitz <sup>d,e</sup>, Lisa Ronan <sup>f</sup>, Boris Bernhardt <sup>c</sup>, Cam-CAN Consortium <sup>g</sup>, Kamen A. Tsvetanov <sup>h,i</sup>





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# Gradients in brain organization

Edited by Daniel Margulies, Boris Bernhardt, Jonathan Smallwood, Sheila Keilholz

Last update 11 September 2020

Complementary to mapping discrete regional boundaries, recent years have seen a rise of new methods and applications to study smooth spatial transitions — or gradients — in numerous aspects of brain organization. Already recognized in early post-mortem histological work, r...

# GRADIENTS: *WHY?*

- Help identify intrinsic patterns of cortical organization
- Allow us to relate multifaceted feature similarity across measures and across species
- Provide an underutilized framework for studying how gradients change in development, aging, and illness

# GRADIENTS: *HOW?*

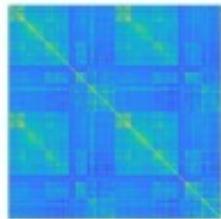
1. Obtain input feature matrix from neuroimaging data
2. Calculate affinity (feature similarity) matrix
3. Embed the affinity matrix in low dimensional space

“Core to these techniques is the computation of an affinity matrix that captures inter-area similarity of a given feature followed by the application of dimensionality reduction techniques to identify a gradual ordering of the input matrix in a lower dimensional manifold space”-  
Vos de Wael, 2020, Communications Biology, BrainSpace

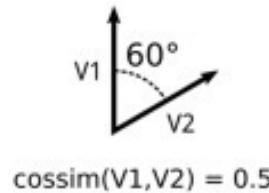
# GRADIENTS: *HOW?*

1. Obtain input feature matrix from neuroimaging data
2. Calculate affinity (feature similarity) matrix
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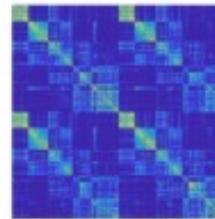
Functional  
Connectivity Matrix



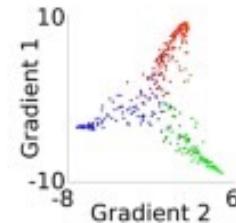
Affinity Computation  
(Cosine Similarity)



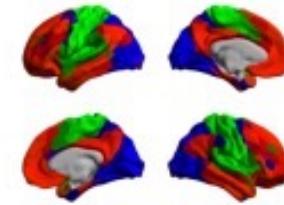
Affinity Matrix



First Components



Gradients on  
Cortical Surface



# GRADIENTS: *HOW?*

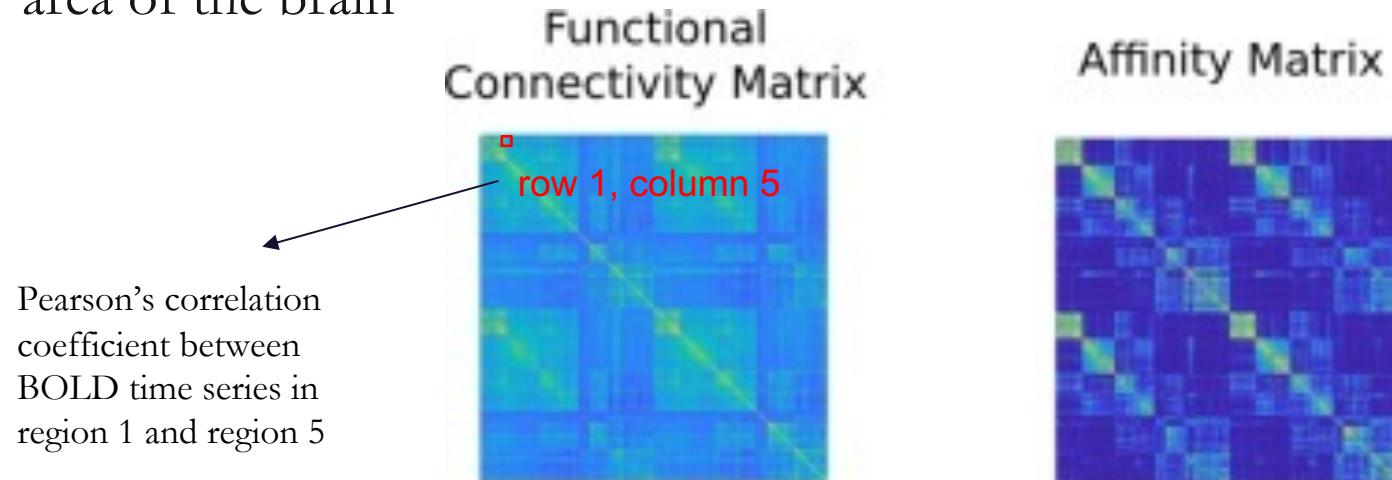
Vogt-Bailey Index  
BrainSpace  
LittleBrain

1. Obtain input feature matrix from neuroimaging data

# GRADIENTS: *HOW?*

## 2. Calculate affinity (feature similarity) matrix

An affinity matrix contains information about how similar each area (vertex, voxel, ROI) of the brain is to every other area of the brain

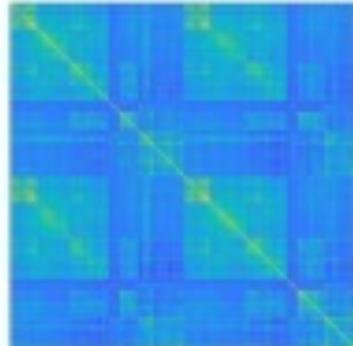


# GRADIENTS: *HOW?*

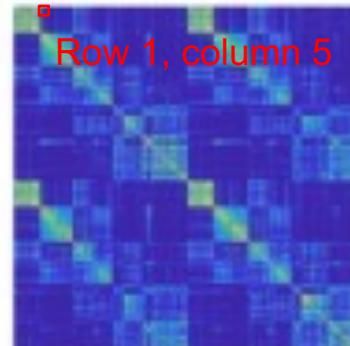
## 2. Calculate affinity (feature similarity) matrix

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Functional  
Connectivity Matrix



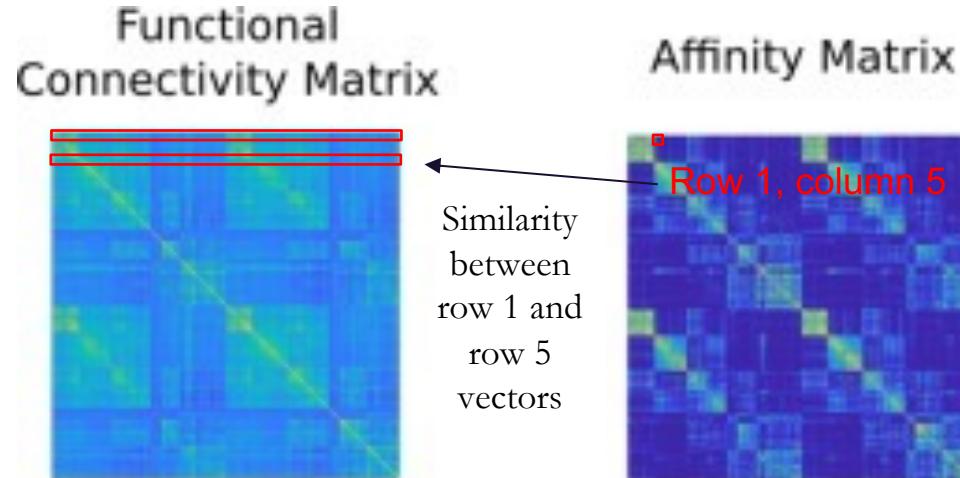
Affinity Matrix



# GRADIENTS: *HOW?*

## 2. Calculate affinity (feature similarity) matrix

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# GRADIENTS: *HOW?*

## 2. Calculate affinity (feature similarity) matrix

An affinity matrix contains information about how similar each area (vertex, voxel, ROI) of the brain is to every other area of the brain

Computing feature similarity:

- **Cosine similarity** (centered data)
- **Normalized angle similarity** (arccosine, normalized by 90 degrees)
- **Pearson's** and **Spearman's** rank correlations

# GRADIENTS: *HOW?*

## 2. Calculate affinity (feature similarity) matrix

*Considerations:*

- Input matrix values must be non-negative → drop negative values or add a scalar constant
- Can use entire input matrix or zero out values that fall below a given threshold (mitigate noise, sparsify matrix)

# GRADIENTS: *HOW?*

## 3. Embed the affinity matrix in low dimensional space

The goal of this step is to create a one-dimensional ordering of brain areas based on how similar they are to one another. We penalize putting long distances between brain areas with high affinity, and find a final positioning where the sum of distance penalties amongst all areas is minimized

Linear dimensionality reduction methods: **PCA**

Non-linear dimensionality reduction methods: **Diffusion map embedding, Laplacian Eigenmaps**

# GRADIENTS: *Vogt-Bailey Index*

The VB index: Is the transition between one brain area to another in low dimensional space gradual/continuous or sharp/discrete?

- Based on a measure of algebraic connectivity (second smallest Laplacian eigenvalue). Higher connectivity = more continuous; Low connectivity indicates potential clusters with discrete boundaries
- 1. Compute a whole brain, single gradient VB index
- 2. Compute an ROI-specific gradient and VB index (e.g. VB index within each functional network)
- 3. Identify boundaries via a vertex-wide searchlight (edge detection)