

1 **Vignette for sequential Monte Carlo methods**
2 **for data assimilation problems**

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23 **1 Introduction**

24 Ecological time series data are collected to explain spatio-temporal changes in species distribu-
25 tion. Species distribution models that explain the abundance or occupancy of the species need
26 to be updated and the model parameters updated to reflect the current trends in the species.

27 In recent years, the state space models (SSMs) have become widely used in analyzing such
28 data. These SSMs have been fitted in the Bayesian framework using the Markov chain Monte
29 Carlo approach. This approach can be very computationally expensive and takes a relatively
30 long time to fit. Fitting the SSMs with this approach can be unfeasible in terms of computa-
31 tional load and time needed to run model which increases with data size.

32 A faster approach to fitting the SSMs is using the sequential Monte Carlo (SMC) approach.
33 The SMC uses sequential importance sampling (SIS) to obtain importance weights that are
34 used to generate posterior distributions of latent states at every time step and also update
35 the other parameters in the model (using the particle MCMC approach; Andrieu, Doucet,
36 and Holenstein (2010)). The SMC approaches have been implemented in packages such as
37 `nimbleSMC` (Michaud et al. 2021), and this package will be referred to in this document.

38 This document seeks to demonstrate how once can use MCMC models already fitted to
39 the SSMs and update them using the SMC approach. The bootstrap and auxiliary PFs were

discussed in the main paper, but this document will focus on bootstrap particle filter. The reader is expected to be familiar with the `nimbleSMC` package and its functionalities (the reader is referred to Chapter 8 of de Valpine et al. (2022) and Michaud et al. (2021) for details on how to fit SSMs using SMC approach in NIMBLE). The first part provides a brief introduction to the state space models (SSMs), sequential Monte Carlo (SMC) approaches (specifically the bootstrap particle filter) and the particle MCMC with the necessary changes made to accomodate the updating process when new streams of data are obtained. The next part shows how to fit the model to the simulated data used in Example 1 in the main paper.

2 Examples

In this document, we demonstrate the use of our proposed model framework by applying them to a simulated dataset. The data was simulated from the linear Gaussian state space model in Example 1 of our main paper. The various functions and changes made to the `nimbleSMC` package filtering algorithms and samplers are written in our package `nimMCMCSMCupdates`. The `nimMCMCSMCupdates` package can be installed from github as follows:

```
devtools::install_github("Peprah94/nimMCMCSMCupdates")
```

3 Set-up

Simulating data and loading packages

3.1 Load packages

The following packages are to be loaded for this document to run.

```
library(nimMCMCSMCupdates)
library(nimble)
```

```

library(nimbleSMC)
library(dplyr)
library(ggplot2)
library(ggmcmc)
library(kableExtra)
library(rjags)
library(coda)

```

60

61 3.2 Simulating data

62 We simulate data from the linear Gaussian state space model for $t = 50$ years.

```

#seed seed for reproduceable results

set.seed(1)

nyears = 50 #Number of years
iNodePrev <- 45 # The number of years for reduced model

# function to simulate the data
sim2 <- function(a, b, c, t, mu0){
  x <- y <- numeric(t)
  x[1] <- rnorm(1, mu0, 1 )
  y[1] <- rnorm(1, x[1], 1)

  for(k in 2:t){
    x[k] <- rnorm(1, a*x[k-1] + b, 1)
    y[k] <- rnorm(1, x[k-1]*c, 1)
  }
}

```

63

```

    }
    return(list(x=x, y=y))
  }

# simulating the data
simData <- sim2(a = 0.8,
               b = 1,
               c = 1.5,
               t = nyears,
               mu0 = 0.2)

# Taking a look at the data
str(simData)

```

64

65 List of 2

66 \$ x: num [1:50] -0.426 -0.177 1.188 2.438 3.526 ...

67 \$ y: num [1:50] -0.243 0.956 -1.086 2.52 3.351 ...

68 4 Fitting reduced SSM

69 This tutorial will assumes that the reduced model is fitted to the observations y from time
 70 $t = 1$ to $t = 45$. The reduced SSM is fitted with MCMC using JAGS [cite] and NIMBLE
 71 [cite] and with particle MCMC using [cite]. In this section, we show how the linear Gaussian
 72 state space model is fitted using the these three approaches and the results we need for the
 73 updating process. Specifically, we aim at saving the posterior samples of the latent states x
 74 and top-level parameters a , b , c and μ_0 .

75 We proceed by first defining some common parameters that will be used throughout the
 76 process of fitting the reduced SSM. These parameters are the number of MCMC iterations,

77 number of chains, thinning value and the parameters to monitor. For each MCMC or SMC
78 approach to be used in fitting the reduced model, we run the MCMC for 1000 iterations, and
79 use the first 500 samples as burn-in samples with thinning value of 1.

```
nIterations = 10000
nChains = 3
nBurnin = 5000
nParFiltRun = 1000
parametersToMonitor <- c("a", "b", "c", "mu0", "x")
```

80

81 4.1 Fitting reduced model with JAGS

82 We proceed to fit the reduced model with JAGS assuming the reader is familiar with the
83 BUGS language and possible running MCMC with JAGS (Refer to **citation** for tutorials on
84 how to fit the model with JAGS).

85 *Define and set-up JAGS model*

86 To fit the reduced model with JAGS, we first define our JAGS model using the BUGS syntax.
87 We do this by embedding the BUGS model in R.

```
# defining JAGS model in R
cat("model{
  x[1] ~ dnorm(mu0, 1)
  y[1] ~ dnorm(x[1], 1)
  for(i in 2:t){
    x[i] ~ dnorm(x[i-1] * a + b, 1)
    y[i] ~ dnorm(x[i] * c, 1)
  }
  a ~ dunif(0, 1)
  b ~ dnorm(0, 1)
```

88

```

    c ~ dnorm(1,1)
    mu0 ~ dnorm(0, 1)
  }", file="lgssm.txt"
)

#setting the parameters needed to run the MCMC
data <- list(
  y = simData$y[-c((iNodePrev+1):50)],
  t = iNodePrev
)

# Initial values
inits <- list(
  a = 0.1,
  b = 0,
  mu0= 0.2,
  c = 1
)

```

89

90 We then set up the syntax defined above to run in JAGS. We are going to run the model
 91 for 3 chains, with no number of adaptations.

```

jagsModel <- jags.model(file = "lgssm.txt",
                        data = data,
                        inits = inits,
                        n.chains = nChains)

```

92

93 Compiling model graph

94 Resolving undeclared variables

95 Allocating nodes

96 Graph information:

97 Observed stochastic nodes: 45

98 Unobserved stochastic nodes: 49

99 Total graph size: 229

100

101 Initializing model

102 *Run the JAGS model and saving posterior samples*

103 The JAGS model is run and the posterior samples are saved. We run 1000 iterations and
104 use the first 500 samples as burn-in samples.

```
## run JAGS and save posterior samples
```

```
samps <- coda.samples( jagsModel , parametersToMonitor, n.iter= nIterations)
```

```
jagsReducedSamples <- window(samps, start=nBurnin+1)
```

105

106 4.2 Fitting reduced model with NIMBLE

107 We also assume that the user is familiar with the NIMBLE package [cite] and how to fit
108 models with it (See [cite] for details on how to run MCMC with NIMBLE package [cite]).

109 *Defining the NIMBLE model*

110 We first define our nimble model. This process involves writing the BUGS code, defining
111 the data, constant and initial values components of the the nimbleModel function in nimble
112 package. **What does the nimbleModel function do?**

```
lgSSMCode <- nimbleCode({
```

```
  x[1] ~ dnorm(mu0, 1)
```

```
  y[1] ~ dnorm(x[1], 1)
```

113


```

for(i in 2:t){
  x[i] ~ dnorm(x[i-1] * a + b, 1)
  y[i] ~ dnorm(x[i] * c, 1)
}

a ~ dunif(0, 1)
b ~ dnorm(0, 1)
c ~ dnorm(1,1)
mu0 ~ dnorm(0, 1)
})

data <- list(
  y = simData$y[-c((iNodePrev+1):50)]
)

# Defining constants
constants <- list(
  t = iNodePrev
)

# Initial values
inits <- list(
  a = 0.1,
  b = 0,
  mu0= 0.2,
  c = 1
)

# Define the nimbleModel with the various components defined
lgSSModel <- nimbleModel(lgSSMCode,

```

114

```

data = data,
constants = constants,
inits = inits,
check = FALSE)

```

115

116 *Configure, build, compile and run model* We configure the MCMC by adding the parameters
 117 to monitor, build and compile the configured model. The compiled model is then run and the
 118 posterior samples are saved.

```

#Compile model
nMCompile <- compileNimble(lgSSModel)

# configure model
cMCMC <- configureMCMC(lgSSModel, monitors = parametersToMonitor)

#build model
bMCMC <- buildMCMC(cMCMC)

# Compile the model to run in c++
coMCMC <- compileNimble(bMCMC, project = nMCompile)

#runMCMC
mcmc.out <- runMCMC(coMCMC,
                    niter = nIterations,
                    nchains = nChains,
                    nburnin = nBurnin,
                    setSeed = TRUE,

```

119

```

        samples=TRUE,
        samplesAsCodaMCMC = TRUE,
        summary = TRUE,
        WAIC = FALSE)

    #save posterior samples
    nimbleReducedSamples <- mcmc.out$samples

```

120

121 4.3 Fitting reduced SSM using pMCMC

122 Lastly, we fit the reduced SSM with particle MCMC **cite** using the `nimbleSMC` **[cite]** package.
 123 Similar to the assumptions made for the first two MCMC models fit, we assume that the user
 124 is familiar with the `nimbleSMC` package **[cite]** and how to fit models with it (See **[cite]** for
 125 details on how to run pMCMC with `nimbleSMC` package **[cite]**).

126 *Defining nimble Model* As with the example in the preceeding subsection, we define our
 127 nimble model. We use the same nimble model(`lgSSModel`) used in that section, but we need
 128 to replicate it since it has been compiled for the MCMC run above.

```

    lgSMCmodel <- lgSSModel$newModel(replicate = TRUE)

    #compile nimble model

    clgSMCmodel <- compileNimble(lgSMCmodel)

```

129

130 *configure model and Build Particle filter*

131 After defining our nimble model, we first build a particle to be passed on to the MCMC
 132 part of the pMCMC. In this example, we build a bootstrap particle filter.

```

    mcmcConf <- configureMCMC(lgSMCmodel,

        nodes = NULL,

        monitors = parametersToMonitor)

```

133

```

134 ===== Monitors =====
135 thin = 1: a, b, c, mu0, x
136 ===== Samplers =====
137 (no samplers assigned)
138 ===== Comments =====

particleFilter <- nimbleSMC::buildBootstrapFilter(lgSMCmodel,
                                                nodes = "x", #latent state
                                                control = list(saveAll = TRUE, #save weights and latent states for e
                                                                smoothing = FALSE,
                                                                initModel = FALSE))

#compile particle filter
#compileNimble(lgSMCmodel, particleFilter)
139

140 Build MCMC part of the pMCMC

141 We then use the particle filter defined above to configure our MCMC. The configured model
142 is built, compiled and run to obtain the posterior samples. The posterior samples are saved
143 to be used for the updating process.

#add sampler for pMCMC
mcmcConf$addSampler(target = c("a", "b", "c", "mu0"),
                    type = "RW_PF_block",
                    pf = particleFilter,
                    adaptive = FALSE,
                    pfNparticles = 1000,
                    latents = "x")

```

144

```

#mcmcConf$addMonitors("x")

#building MCMC

bMCMCsmc <- buildMCMC(mcmcConf)

# compile MCMC

cMCMCsmc <- compileNimble(bMCMCsmc,
                           project = lgSMCmodel,
                           resetFunctions = TRUE)

#runMCMC

smcMCMCout <- runMCMC(cMCMCsmc,
                     niter = nIterations,
                     nchains = nChains,
                     nburnin = nBurnin,
                     inits = inits,
                     setSeed = TRUE,
                     samples=TRUE,
                     samplesAsCodaMCMC = TRUE,
                     summary = TRUE,
                     WAIC = FALSE)

#save posterior samples

nimbleSMCReducedSamples <- smcMCMCout$samples

```

145

4.4 Saving all samples

We save all the results from the three fitted reduced SSMs in a list to use in the updating process

```
mcmcSamplesList <- list(jagsReducedSamples = jagsReducedSamples,
                        nimbleReducedSamples = nimbleReducedSamples,
                        nimbleSMCReducedSamples = nimbleSMCReducedSamples)

save(mcmcSamplesList,
     file = "mcmcSample.RData")
```

5 Converting MCMC output for updating process

We load the saved posterior samples for the updating process. It is worth noting that all the samples are `mcmc.list` class, so the procedure we use to prepare the posterior samples from any of these three models can be generalised to any MCMC approach of this class.

```
#load saved that
load("mcmcSample.RData")

#Check the class of each of the returned posterior samples
lapply(mcmcSamplesList, function(x) class(x))
```

```
$jagsReducedSamples
```

```
[1] "mcmc.list"
```

```
$nimbleReducedSamples
```

```
[1] "mcmc.list"
```

```
161 $nimblemcReducedSamples
```

```
162 [1] "mcmc.list"
```

163 Creating model values from saved posterior samples

164 The posterior samples need to be stored in as ModelValues to be used for updating the SSM
165 (see Chapter 15 of [cite nimble manual] for details on modelValues definition). To do this,
166 we need to re-define our model as we used JAGS as a nimble model, or use our reduced model
167 from the MCMC with nimble and pMCMC with nimbleMCMC. In this example, we re-define
168 the JAGS model as a nimble model. We do this by copying the text file into a nimbleCode
169 and then we can define the nimbleModel as we did for the two examples.

```
jagsToNimbleCode <- nimbleCode({  
  x[1] ~ dnorm(mu0, 1)  
  y[1] ~ dnorm(x[1], 1)  
  for(i in 2:t){  
    x[i] ~ dnorm(x[i-1] * a + b, 1)  
    y[i] ~ dnorm(x[i] * c, 1)  
  }  
  a ~ dunif(0, 1)  
  b ~ dnorm(0, 1)  
  c ~ dnorm(1,1)  
  mu0 ~ dnorm(0, 1)  
})  
  
data <- list(  
  y = simData$y[-c((iNodePrev+1):50)]  
)  
# Defining constants
```

```
170
```

```

constants <- list(
  t = iNodePrev
)
# Initial values
inits <- list(
  a = 0.1,
  b = 0,
  mu0 = 0.2,
  c = 1
)
# Define the nimbleModel with the various components defined
jagsToNimbleModel <- nimbleModel(jagsToNimbleCode,
                                data = data,
                                constants = constants,
                                inits = inits,
                                check = FALSE)

```

171

172 After defining the nimble model, we can create the modelValues object. The modelValue
 173 object is created for each MCMC chain. In this example, we show how to do it for the first
 174 chain.

```

# Define latent states and top-level parameters
latent = "x"
target = c("a", "b", "c", "mu0")

# Expand the node names for the latent variables
latentNodes <- jagsToNimbleModel$expandNodeNames(latent)

```

175


```

# Find all the latent nodes

# Function in nimbleSMC

nodes <- findLatentNodes(jagsToNimbleModel,
                        latent,
                        timeIndex = 1)

#find the dimension of the nodes

dims <- lapply(nodes, function(n) nimDim(jagsToNimbleModel[[n]]))

if(length(unique(dims)) > 1)
  stop('sizes or dimensions of latent states varies')

# create a vars vector that contains the names of the latent nodes and top-level parameters
vars <- c(jagsToNimbleModel$getVarNames(nodes = nodes), target)

#create a list of model objects to store the variable values
modelSymbolObjects <- jagsToNimbleModel$getSymbolTable()$getSymbolObjects()[vars]

# retrun the names, type and size components for the modelValues.
# These are the essential components needed to create modelValues
names <- sapply(modelSymbolObjects, function(x) return(x$name))
type <- sapply(modelSymbolObjects, function(x) return(x$type))
size <- lapply(modelSymbolObjects, function(x){
  y <- x$size
  #Make sure variables with nDim= 0 will have size of 1
  t <- length(y)

```

```

    rr <- c()
    if(t > 1){
rr <- y
    }else{
        if(length(y)>0){
            rr <- y
        }else{
rr <- 1}
        }
    return(rr)
}
)

#create ModelValues object
mvSamplesEst <- modelValues(modelValuesConf(vars = names,
                                             types = type,
                                             sizes = size))

#let's check the mvSamplesEst
print(mvSamplesEst)

```

177

178 modelValues object with variables: x, a, b, c, mu0.

```

# The modelValue object created has size of 1.
mvSamplesEst$getSize()

```

179

180 [1] 1

```

# resize the modelValues object created to be equal to (number of iterations - burnin samp
mcmcSampleSize = (nIterations - nBurnin)
resize(mvSamplesEst, mcmcSampleSize)

# check size now
mvSamplesEst$getSize()
181

[1] 5000
182

# retrieve posterior samples for the first chain
mcmcOut <- mcmcSamplesList$jagsReducedSamples[[1]]

#create mvEst for the first chain
for(iter in 1:mcmcSampleSize ){
  for(j in 1:length(names)){
    if(names[j] == latent & length(size[[1]]) > 1){
      mvSamplesEst[[names[j]]][[iter]] <- matrix(mcmcOut[iter, jagsToNimbleModel$expandNodeN
    }else{
      mvSamplesEst[[names[j]]][[iter]] <- mcmcOut[iter, jagsToNimbleModel$expandNodeNames
    }
  }
}
183

```

184 This process of converting MCMC posterior samples to modelValues that can be used by
185 **nimbleSMC** is written in **updateUtils** function in our **nimbleMCMCSMC** package. It takes as
186 input the reduced model, the MCMC samples, latent state, target vectors, the MCMC sample
187 size, the timeIndes for the **findLatentNodes** function. The code delow show produce the
188 same results as above.

```

updateVars <- updateUtils(model = jagsToNimbleModel,
                           mcmcOut = mcmcSamplesList$jagsReducedSamples[[1]],
                           latent = latent,
                           target = target,
                           n.iter = mcmcSampleSize ,
                           m = nParFiltRun,
                           timeIndex = 1)

```

189

6 Updating process using nimbleSMC

190

After saving posterior samples as `modelValues`, we then proceed to fit the updated SSM. We modified the bootstrap and auxiliary particle filter algorithms as well as the MCMC samplers in the `nimbleSMC` package. We use the modified functions, which can be found in our `nimbleMCMCSMC` package, to illustrate the updating process. Note that the entire process defined here has to be repeated for number of chains times.

196

Re-defining the `nimbleModel`

197

The reduced SSM needs to be updated with the observation from time $t = 46$ to $t = 50$. To do this, we change the data and constant components of our reduced model and create a new nimble model.

199

```

data <- list(
  y = simData$y
)
# Defining constants
constants <- list(
  t = nyyears
)

```

200

```

# Initial values
inits <- list(
  a = 0.1,
  b = 0,
  mu0= 0.2,
  c = 1
)

# Define the nimbleModel with the various components defined
lgSSMUpdated <- nimbleModel(lgSSMCode,
                             data = data,
                             constants = constants,
                             inits = inits,
                             check = FALSE)
201

202 Build updated particle filter and set up MCMC configuration

    modelMCMCconf <- nimble::configureMCMC(lgSSMUpdated,
                                             nodes = NULL,
                                             monitors = parametersToMonitor)
203

204 ===== Monitors =====
205 thin = 1: a, b, c, mu0, x
206 ===== Samplers =====
207 (no samplers assigned)
208 ===== Comments =====

# Define control element
    pfControl = list(saveAll = TRUE,
209

```

```

        smoothing = FALSE,
        M = nyears - iNodePrev,
        iNodePrev = iNodePrev)

# Build particle filter
particleFilter <- nimMCMCSCMCupdates::buildBootstrapFilterUpdate(model = lgSSMUpdated ,
nodes = latent,
mvSamplesEst = mvSamplesEst,
target = target,
control = pfControl)

```

210

211 Build, compile and run MCMC

```

pfTypeUpdate = 'bootstrapUpdate'

#Add RW_blockUpdate sampler
modelMCMCconf$addSampler(target = target,
                          type = 'RW_PF_blockUpdate',
                          control = list(latents = latent,
                                         target = target,
                                         adaptInterval = mcmcSampleSize,
                                         pfControl = list(saveAll = TRUE,
                                                         M = nyears - iNodePrev,
                                                         iNodePrev = iNodePrev),
                                         pfNparticles = nParFiltRun,
                                         pfType = pfTypeUpdate,
                                         mvSamplesEst = mvSamplesEst,

```

212

```

logLikeVals = NA))

#Check if we are getting the variables we want to monitor
modelMCMCconf$printMonitors()

#build MCMC
modelMCMC <- buildMCMC(modelMCMCconf)

#compile MCMC
compiledList <- nimble::compileNimble(lgSSMUpdated,
                                     modelMCMC,
                                     resetFunctions = TRUE)

#run MCMC
mcmc.out <- nimble::runMCMC(compiledList$modelMCMC,
                            niter = mcmcSampleSize,
                            nchains = 1,
                            nburnin = 0,
                            setSeed = TRUE,
                            samples=TRUE,
                            samplesAsCodaMCMC = TRUE,
                            summary = TRUE,
                            WAIC = FALSE)

#check the output
head(mcmc.out$summary)

```

214 The entire process described above is written up in the **spartaNimUpdates** function in
215 our **nimMCMCSMCupdates** package. We use this function to run the updated model for all the
216 three chains.

```
# Replicate the updated and reduced models
newModelReduced <- jagsToNimbleModel$newModel(replicate = TRUE)
newModelUpdated <- lgSSMUpdated$newModel(replicate = TRUE)

#reduced model list
mcmcList <- list()
mcmcList$samples <- mcmcSamplesList$jagsReducedSamples
mcmcList$summary <- NULL

lgSSMUpdatedResults <- nimMCMCSMCupdates::spartaNimUpdates(
  model = newModelUpdated, #nimble model
  reducedModel = newModelReduced, # reduced nimbleModel
  latent = "x", #latent variable
  pfType = "bootstrap", # type of SMC
  MCMCconfiguration = list(target = c('a', 'b', 'c', 'mu0'), #top-level parameters
    additionalPars = "x", #additional parameters to monitor
    n.iter = mcmcSampleSize, #number of iterations
    n.chains = nChains, # number of chains
    n.burnin = 0, # number of burnin samples
    n.thin = 1), # number of thinning samples
  postReducedMCMC = mcmcList, # MCMC posterior samples from reduced SSM
  pfControl = list(saveAll = TRUE,
    smoothing = FALSE,
```

217


```

        M = nyears - iNodePrev,
        iNodePrev = iNodePrev)
    )

    save(lgSSMUpdatedResults, file = "lgSSMUpdatedResults.RData")

```

The **spartaNimUpdates** function returns the posterior samples, summary of the posterior samples and the timeRun

```
data("lgssmUpdated") # load results
```

Warning in data("lgssmUpdated"): data set 'lgssmUpdated' not found

```
#str(example1UpdatedModel)
```

6.1 Comparing the various models fit

Our package provides functions to compare the reduced and updated SSM fitted in this document.

6.1.1 Comparing individual model parameters

The *compareModelsIndividualPars* function compares a list of SSM models fit with our package. It returns the efficiency, effective sample size (ESS), time run, and Monte Carlo standard error of the individual models provided in the function. We present the efficiency of the reduced and updated SSM fitted in this document in Table ??

```

target = c('a', 'b', 'c', 'mu0')

models <- list(example1ReducedModel,
               example1UpdatedModel)

results <- compareModelsIndividualPars(models = models,

```

```

n.chains = 2,
nodes = target,
modelName = c("reducedModel", "updatedModel"))

# Return efficiency
results$efficiency%>%
  do.call("rbind", .)%>%
  mutate(model = c(rep("reduced Model", length(target)),
                    rep("updated Model", length(target))))%>%
  kbl() %>%
  kable_material(c("striped", "hover"))

```

233

234 6.1.2 Comparison plots for selected parameters

235 The *compareModelsPlots* function also compares a list of SSM models fit with our package. It
 236 returns a plot of the efficiency, effective sample size (ESS), time run, and Monte Carlo standard
 237 error of the individual models provided in the function. We present the plot of the efficiency
 238 of the reduced and updated SSM fitted in this document as shown in Figure ??.

```

ret <- compareModelsPlots(models = models,
                          modelName = c("reduced model", "updated Model"),
                          n.chains = 2,
                          nodes = target)

# return efficiency
ret$efficiencyPlot

```

239

240 6.1.3 Posterior summaries for models

241 We also provide a function that returns the posterior mean of parameters of interest and the
242 credible intervals around the estimates.

```
ret <- compareModelsMeanPlots(models = models,  
                              modelNames = c("reduced model", "updated Model"),  
                              fullModel = stateSpaceModel,  
                              nodes = target)  
  
#return confint plot  
ret$confintPlot
```

243

244 6.1.4 Run baseline model

245 7 References

- 246 Andrieu, Christophe, Arnaud Doucet, and Roman Holenstein. 2010. "Particle Markov Chain
247 Monte Carlo Methods." *Journal of the Royal Statistical Society: Series B (Statistical
248 Methodology)* 72 (3): 269–342.
- 249 de Valpine, Perry, Christopher Paciorek, Daniel Turek, Nick Michaud, Cliff Anderson-Bergman,
250 Fritz Obermeyer, Claudia Wehrhahn Cortes, Abel Rodríguez, Duncan Temple Lang, and
251 Sally Paganin. 2022. *NIMBLE User Manual* (version 0.13.1). [https://doi.org/10.5281/ze
252 nodo.1211190](https://doi.org/10.5281/zenodo.1211190).
- 253 Michaud, Nicholas, Perry de Valpine, Daniel Turek, Christopher J Paciorek, and Dao Nguyen.
254 2021. "Sequential Monte Carlo Methods in the Nimble and nimbleSMC r Packages." *Jour-
255 nal of Statistical Software* 100: 1–39.