

Somaiya Vidyavihar University
K. J. Somaiya College of Engineering, Mumbai -77
(A Constituent College of Somaiya Vidyavihar University)
DEPARTMENT OF MECHANICAL ENGINEERING

Engineering Mechanics Lab

July - Dec 2023

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1) Problem statement

Given the equation of motion $x = 7t^3 + 3t^2 - 6t + 8$

1. Find the expressions for velocity and acceleration.
2. Plot the graphs of displacement, velocity, and acceleration from $t=0$ to $t=15$ s.

2) Analytical solution of the problem

Given equation of displacement (x)
 $x = 7t^3 + 3t^2 - 6t + 8$

$\frac{dx}{dt} = 21t^2 + 6t - 6$ = velocity

$\frac{d^2x}{dt^2} = 42t + 6$ = acceleration

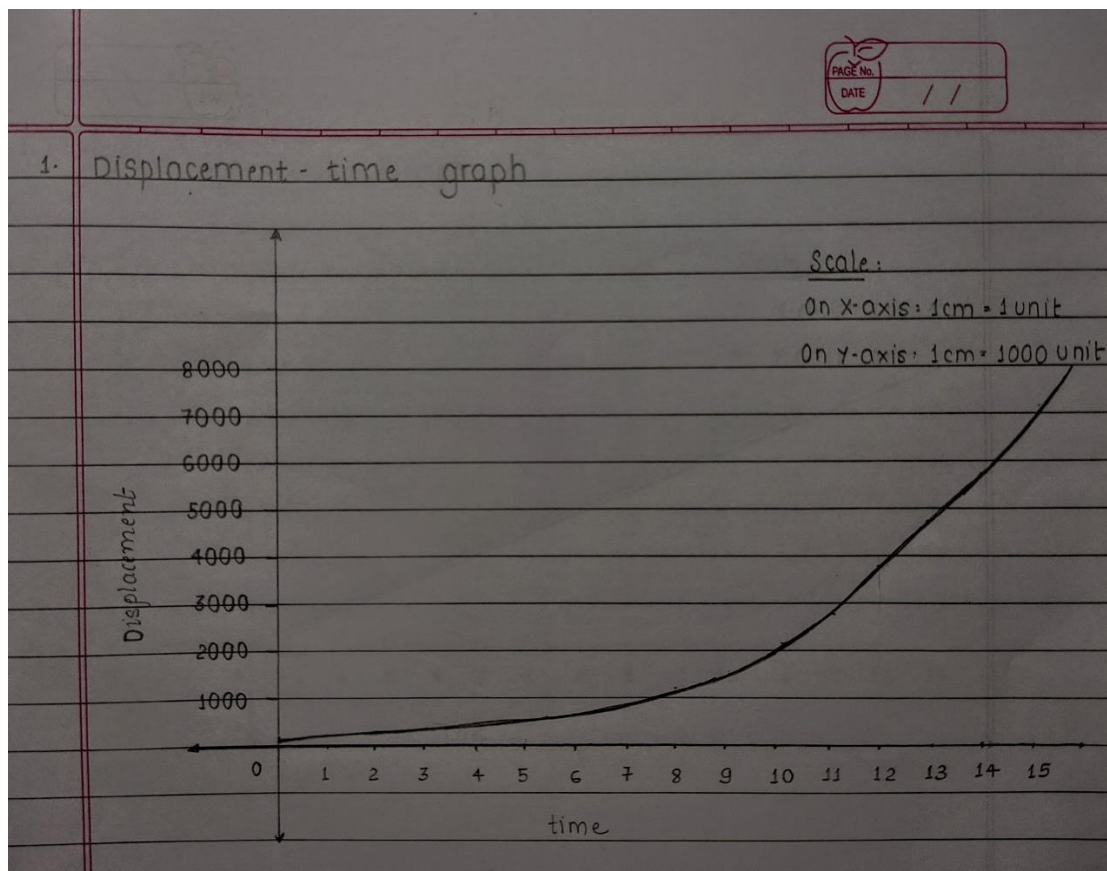
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For the graph,
we substitute the value of time t from
0 to 15s in the three equations,

t	x	v	a
0	8	-6	6
2	46	78	90
4	200	246	174
6	532	486	258
8	1144	798	342
10	2154	1182	426
12	3696	1638	510
14	5880	2166	594
15	7248	2457	636

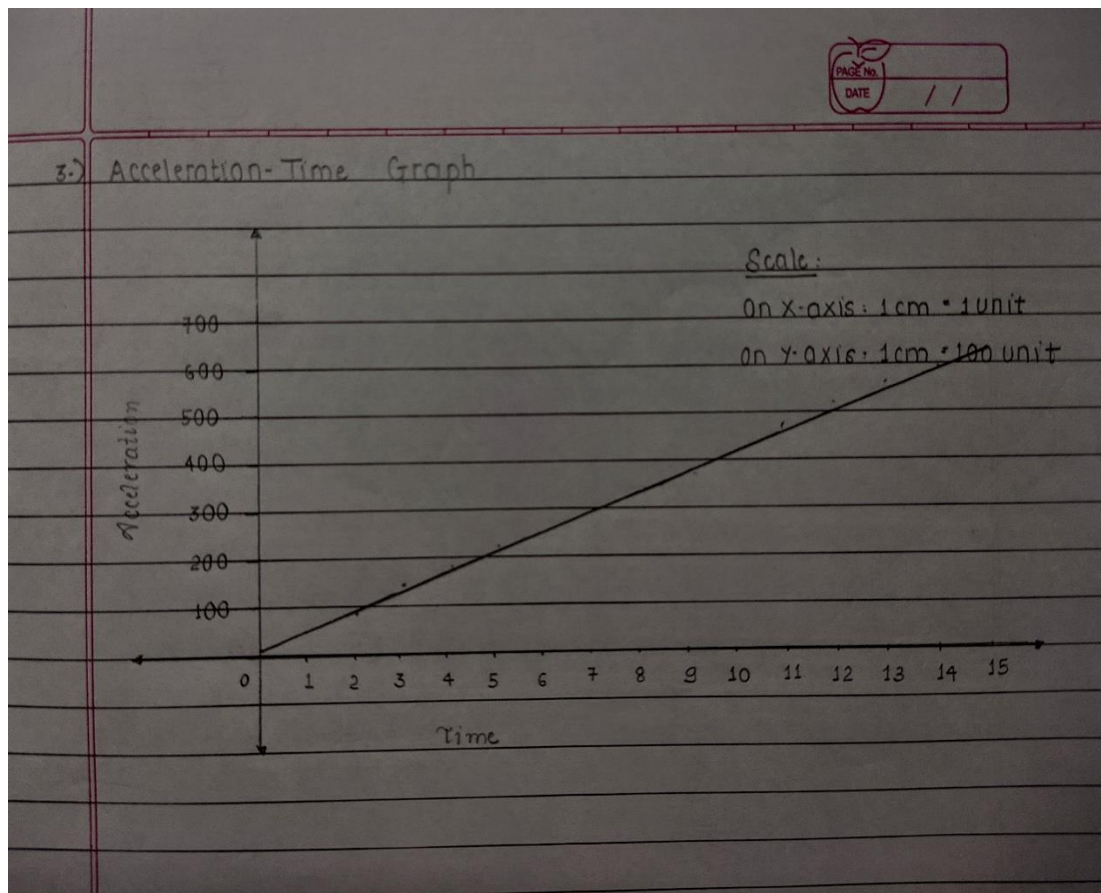
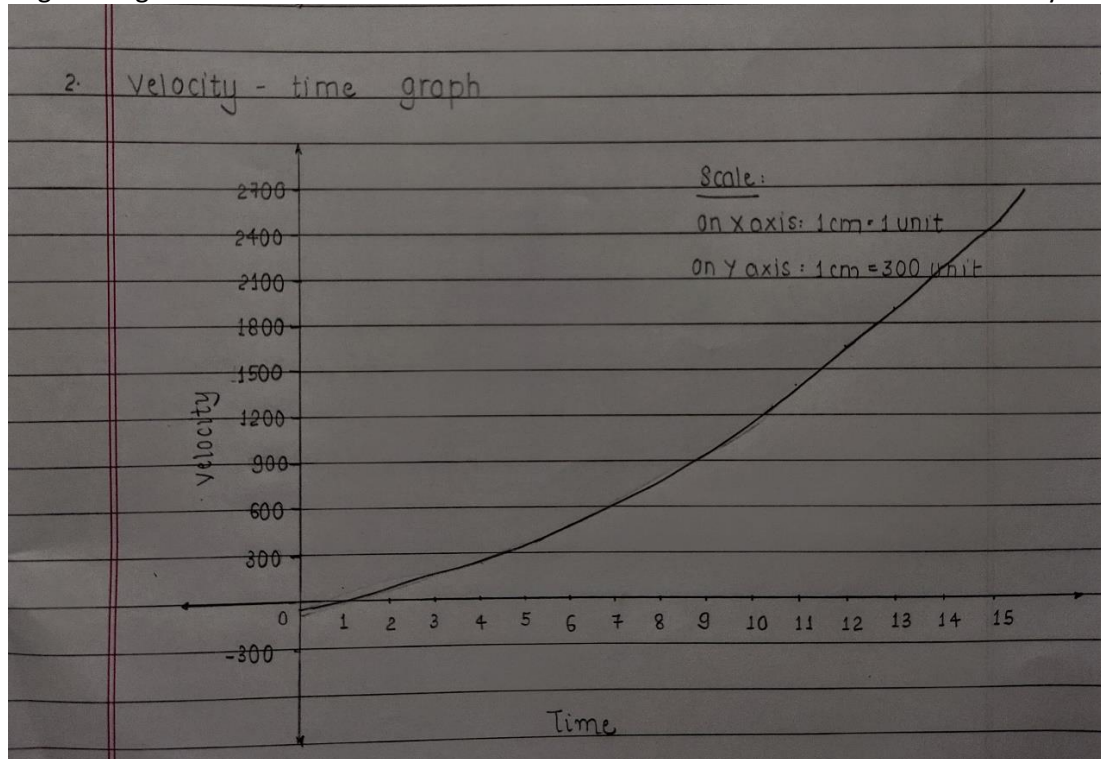


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3) Screenshots of the work done in software showing input parameters, coding, graphs, results etc.

Calculation of velocity and acceleration equations from displacement equations:

```
[3] import matplotlib.pyplot as plt
import numpy as np
from sympy import symbols,diff,lambdify
from sympy.integrals.integrals import integrate

[4] t = symbols('t')

[5] eqn_x = (7*t**3)+(3*t**2)-(6*t)+8

[6] eqn_v = diff(eqn_x,t)
eqn_a = diff(eqn_v,t)

[7] int_v = integrate(eqn_v)
int_a = integrate(eqn_a,t)

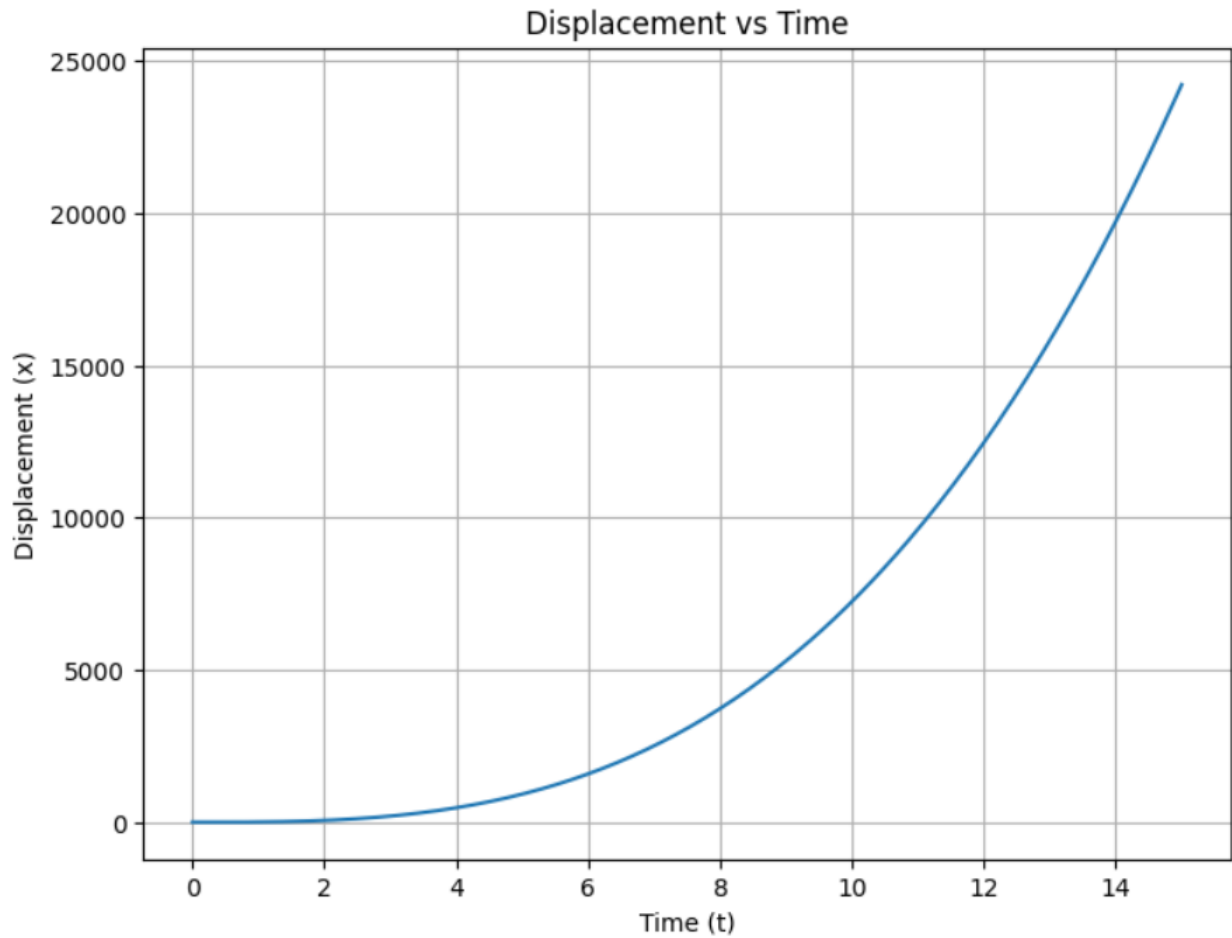
▶ print("Velocity(dx/dt) = ",eqn_v)
print("Acceleration(dv/dt) = ",eqn_a)
print("\n\nIntegration of velocity is displacement= ",int_v)
print("Integration of acceleration is velocity = ",int_a)

Velocity(dx/dt) = 21*t**2 + 6*t - 6
Acceleration(dv/dt) = 42*t + 6

Integration of velocity is displacement= 7*t**3 + 3*t**2 - 6*t
Integration of acceleration is velocity = 21*t**2 + 6*t
```

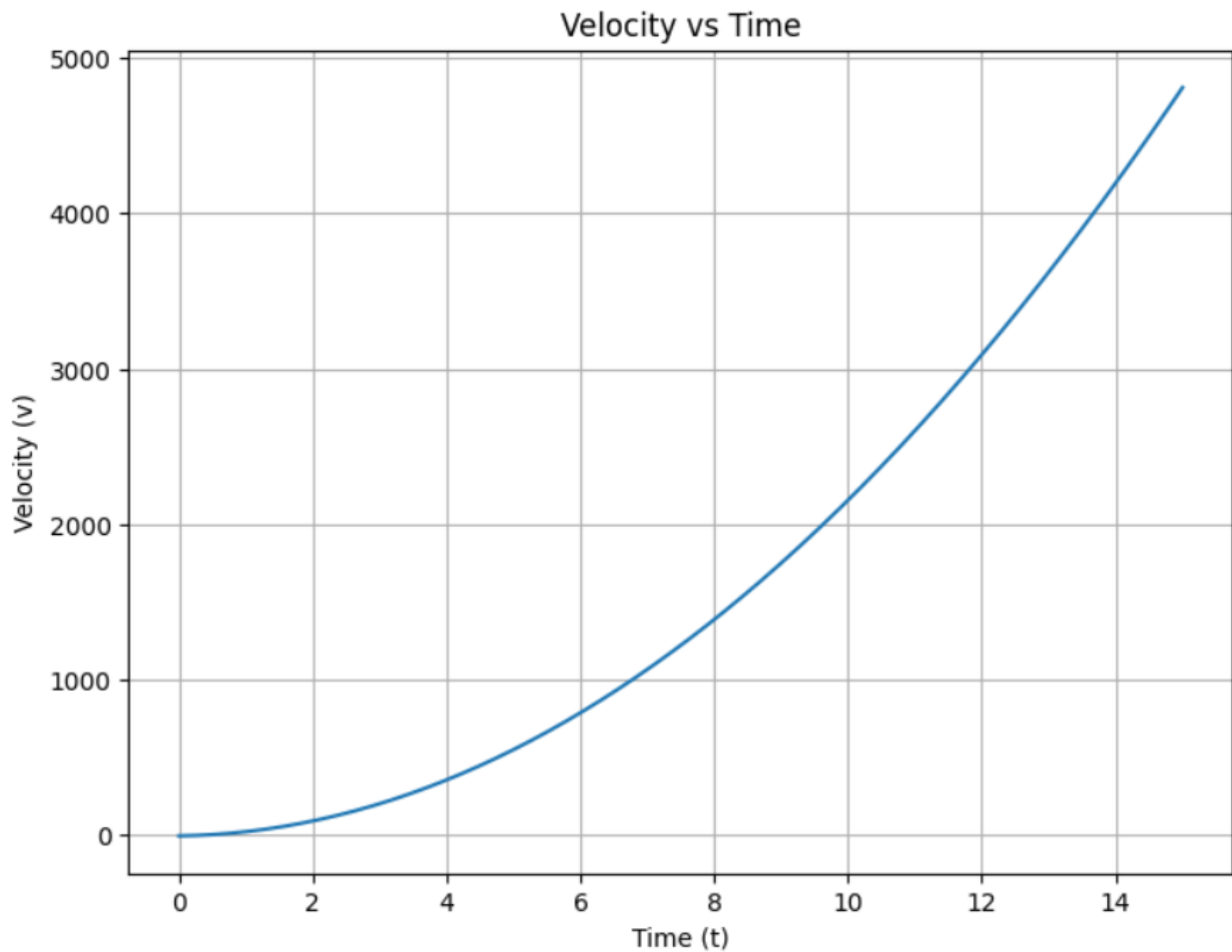
1)Graph of displacement(x):

```
▶ eq_fn = lambdify(t, eqn_x, modules='numpy')
tvalue = np.linspace(0,15,400)
xvalue = eq_fn(tvalue)
fig = plt.figure(figsize = (8,6))
plt.plot(tvalue,xvalue)
plt.xlabel('Time (t)')
plt.ylabel('Displacement (x)')
plt.title('Displacement vs Time')
plt.grid(True)
plt.show()
```



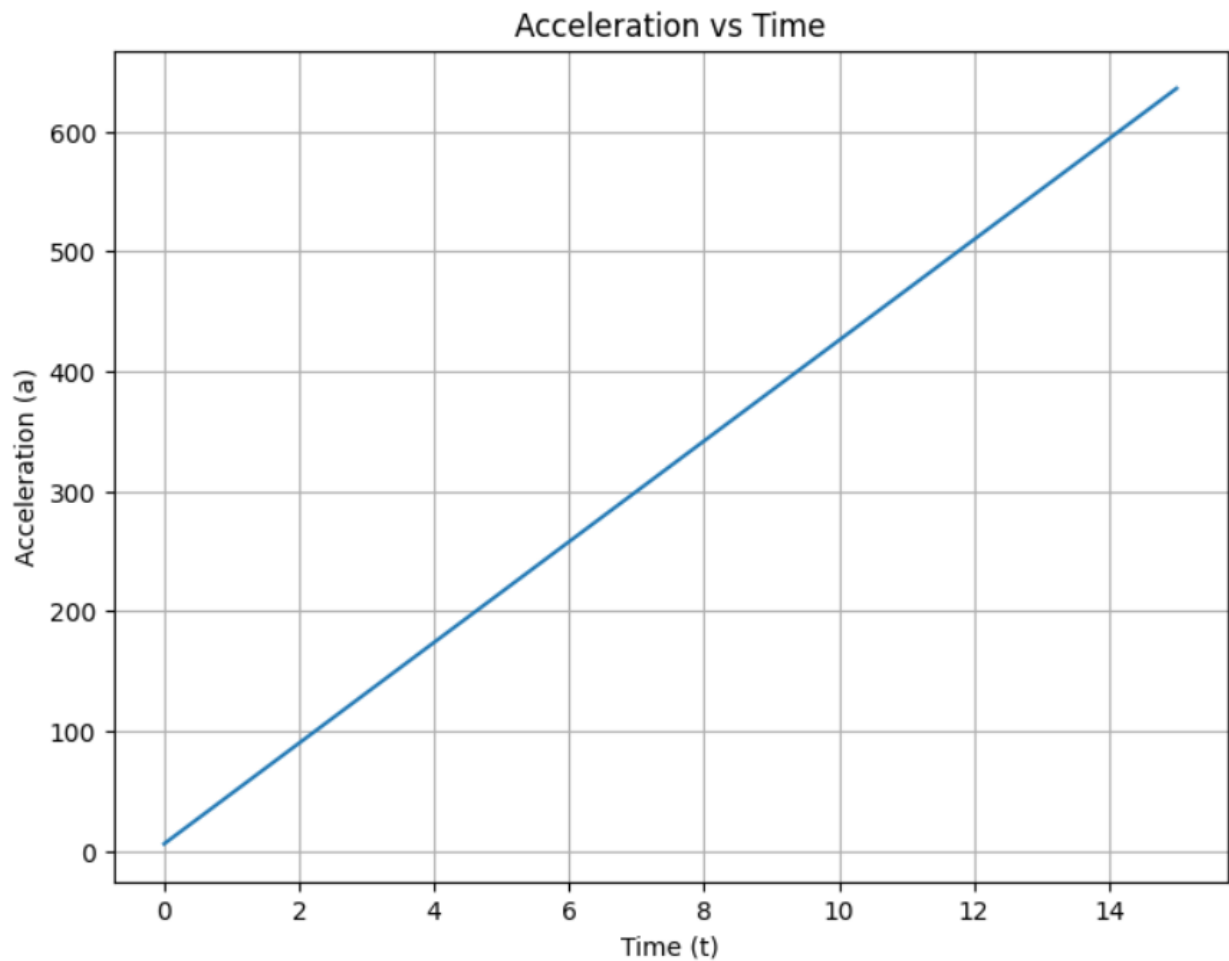
2) Graph of velocity(v):

```
eq_fn = lambdify(t, eqn_v, modules='numpy')
tvalue = np.linspace(0,15,400)
xvalue = eq_fn(tvalue)
fig = plt.figure(figsize = (8,6))
plt.plot(tvalue,xvalue)
plt.xlabel('Time (t)')
plt.ylabel('Velocity (v)')
plt.title('Velocity vs Time')
plt.grid(True)
plt.show()
```



3) Graph of acceleration(a):

```
eq_fn = lambda t, eqn_a, modules='numpy':  
tvalue = np.linspace(0,15,400)  
xvalue = eq_fn(tvalue)  
fig = plt.figure(figsize = (8,6))  
plt.plot(tvalue,xvalue)  
plt.xlabel('Time (t)')  
plt.ylabel('Acceleration (a)')  
plt.title('Acceleration vs Time')  
plt.grid(True)  
plt.show()
```



4) Result

The velocity(v) is equal to $21t^2+6t-6$ and the acceleration(a) is equal to $42t+6$.

The graph of Displacement(x) vs Time(t) is of 3rd order, the graph of Velocity(v) vs Time(t) is of 2nd order & the graph Acceleration(a) vs Time(t) is linear.

5) Conclusion

We solved an Engineering Mechanics problem using both analytical methods and computational tools. Through mathematical derivations and expressions, we'll solve it analytically. Furthermore, Python will aid in graphical analysis, providing visual and numerical insights.