



K. J. Somaiya College of Engineering, Mumbai-77
(A Constituent College of Somaiya Vidyavihar University)
Department of Computer Engineering

Batch: E-2 Roll No.: 16010123325

Experiment No. __2__

Grade: AA / AB / BB / BC / CC / CD / DD

Signature of the Staff In-charge with date

Title: Study, Implementation, and Comparative Analysis of Strassen's matrix multiplication.

Objective: To learn the divide and conquer strategy of solving the problems of different types

CO to be achieved:

CO 2 Describe various algorithm design strategies to solve different problems and analyse Complexity.

Books/ Journals/ Websites referred:

1. Ellis horowitz, Sarataj Sahni, S.Rajsekaran," Fundamentals of computer algorithm", University Press
2. T.H.Cormen ,C.E.Leiserson,R.L.Rivest and C.Stein," Introduction to algortihms",2nd Edition ,MIT press/McGraw Hill,2001
3. http://en.wikipedia.org/wiki/Binary_search_algorithm
4. https://www.princeton.edu/~achaney/tmve/wiki100k/docs/Binary_search_algorithm.html
5. <http://video.franklin.edu/Franklin/Math/170/common/mod01/binarySearchAlg.html>
6. <http://xlinux.nist.gov/dads/HTML/binarySearch.html>
7. <https://www.cs.auckland.ac.nz/software/AlgAnim/searching.html>

Pre Lab/ Prior Concepts:

Data structures

Historical Profile:

Strassen's Algorithm is a groundbreaking algorithm in computer science and mathematics that introduced a faster method for matrix multiplication compared to the traditional method. It has a rich history, being one of the first major breakthroughs in computational complexity for matrix operations. Matrix multiplication is a fundamental operation in linear algebra with



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applications in computer graphics, scientific computing, machine learning, and more. Strassen's algorithm is an advanced technique for matrix multiplication, introduced by Volker Strassen in 1969, which significantly improves the time complexity of traditional matrix multiplication algorithms.

Traditional Matrix Multiplication:

Complexity: $O(n^3)$ for multiplying two $n \times n$ matrices using the standard algorithm.

Strassen's Matrix Multiplication: Reduces the number of multiplications required in the divide-and-conquer approach from 8 to 7. Complexity: Approximately $O(n^{2.81})$.

New Concepts to be learned:

Number of comparisons, Application of algorithmic design strategy to any problem, Classical problem solving Vs Divide-and-Conquer problem solving.

Algorithm :

Input : Two $n \times n$ matrices A and B, where n is a power of 2 (if not, pad the matrices with zeros).

Step 1: Divide the Matrices

$A = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix}$,

$B = \begin{bmatrix} B_{11} & B_{12} \\ B_{21} & B_{22} \end{bmatrix}$

Step 2: Compute Seven Intermediate Products

Define seven products based on specific combinations of additions and subtractions of submatrices:

1. $M_1 = (A_{11} + A_{22}) * (B_{11} + B_{22})$
2. $M_2 = (A_{21} + A_{22}) * B_{11}$
3. $M_3 = A_{11} * (B_{12} - B_{22})$
4. $M_4 = A_{22} * (B_{21} - B_{11})$
5. $M_5 = (A_{11} + A_{12}) * B_{22}$
6. $M_6 = (A_{21} - A_{11}) * (B_{11} + B_{12})$
7. $M_7 = (A_{12} - A_{22}) * (B_{21} + B_{22})$

Step 3: Combine Results. (Use the seven intermediate products to compute the resulting matrix C)

$C = \begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix}$ where:



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- $C_{11} = M_1 + M_4$
- $C_{12} = M_3 + M_5$
- $C_{21} = M_2 + M_4$
- $C_{22} = M_1 - M_2 + M_3 + M_6$

Implementation-

Strassen's Matrix Multiplication

Page No.:
Date:

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{bmatrix} \quad A \Rightarrow A_{11} A_{12} A_{21} A_{22}$$
$$B = \begin{bmatrix} b_{11} & b_{12} & b_{13} & b_{14} \\ b_{21} & b_{22} & b_{23} & b_{24} \\ b_{31} & b_{32} & b_{33} & b_{34} \\ b_{41} & b_{42} & b_{43} & b_{44} \end{bmatrix} \quad B \Rightarrow B_{11} B_{12} B_{21} B_{22}$$
$$\begin{aligned} C_{11} &= A_{11} \times B_{11} + A_{12} \times B_{21} \\ C_{12} &= A_{11} \times B_{12} + A_{12} \times B_{22} \\ C_{21} &= A_{21} \times B_{11} + A_{22} \times B_{21} \\ C_{22} &= A_{21} \times B_{12} + A_{22} \times B_{22} \end{aligned}$$
$$TC: T(n) = 7(n/2) + O(n^2)$$
$$\begin{aligned} &= O(n^{\log_2 7}) \\ &= O(n^{2.81}) \end{aligned}$$

Sc: $O(n^2)$

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Code-

```
import java.util.Scanner;

public class Strassens {
    public static void main(String[] args) {
        Scanner scanner = new Scanner(System.in);
        int[][] x = new int[2][2];
        int[][] y = new int[2][2];
        int[][] z = new int[2][2];

        System.out.println("Enter elements for the first 2x2 matrix:");
        for(int i = 0; i < 2; i++) {
            for(int j = 0; j < 2; j++) {
                x[i][j] = scanner.nextInt();
            }
        }

        System.out.println("Enter elements for the second 2x2 matrix:");
        for(int i = 0; i < 2; i++) {
            for(int j = 0; j < 2; j++) {
                y[i][j] = scanner.nextInt();
            }
        }

        int m1 = (x[0][0] + x[1][1]) * (y[0][0] + y[1][1]);
        int m2 = (x[1][0] + x[1][1]) * y[0][0];
        int m3 = x[0][0] * (y[0][1] - y[1][1]);
        int m4 = x[1][1] * (y[1][0] - y[0][0]);
        int m5 = (x[0][0] + x[0][1]) * y[1][1];
        int m6 = (x[1][0] - x[0][0]) * (y[0][0] + y[0][1]);
        int m7 = (x[0][1] - x[1][1]) * (y[1][0] + y[1][1]);

        z[0][0] = m1 + m4 - m5 + m7;
        z[0][1] = m3 + m5;
        z[1][0] = m2 + m4;
        z[1][1] = m1 - m2 + m3 + m6;

        System.out.println("\nProduct achieved using Strassen's algorithm:");
        for(int i = 0; i < 2; i++) {
            for(int j = 0; j < 2; j++) {
                System.out.print(z[i][j] + "\t");
            }
            System.out.println();
        }
        scanner.close();
    }
}
```



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Output-

```
Enter elements for the first 2x2 matrix:
1 2
3 4
Enter elements for the second 2x2 matrix:
9 8
7 6

Product achieved using Strassen's algorithm:
23    20
55    48
```

The space complexity:

Space Complexity : $O(n^2)$

The Time complexity:

Time Complexity : $O(n^{2.81})$

CONCLUSION:

The above experiment highlights implementation of Strassen's multiplication in Java to reduce the complexity from n^3 to $n^{2.81}$.