2. Method of Variation of Parameters

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METHOD OF VARIATION OF PARAMETERS

· Used for second order LDES only

Consider a second order LDE:

$$\frac{d^2y}{dx^2} + a, \frac{dy}{dx} + a_2 y = \phi(x)$$

det the CF = c, y, + c, y,

Whonskian = $W(y_1, y_2) = |y_1, y_2|$

PI =
$$A(x)y_1 + B(x)y_2$$

where
$$A(x) = -\int \underbrace{y_2 \times \phi(x)}_{W} dx$$

$$B(x) = \int \underbrace{y_1 \times \phi(x)}_{W} dx$$

APPLICATION BASED

Q. A body weighing 10 kg is hung from a spring. A full of 20 kg will stretch the spring to 10 cm. The body is pulled down to 20 cm below the static equilibrium position and released. Find the displacement of the body from equilibrium position at a time 't' seconds, maximum velocity, period of oscillation.

The differential equation governing this principle:

$$\frac{d^2x}{dt^2} + \frac{k}{m}x = 0$$

$$\frac{d^{2}x}{dx^{2}} + \frac{1960}{10} \times = 0$$

$$x = (, us | let + c, sin | let)$$

$$At t = 0, x = 0.2 m$$

$$\frac{dx}{dt} = 0$$

$$C_{1} = 0.2$$

$$C_{2} = 0$$

$$x = 0.2 cos | let)$$

I in series, and the charge q at time t corresponds to the equation:

$$L \frac{d^2q}{dt^2} + R \frac{dq}{dt} + \frac{q}{c} = 0$$

$$L = 0.25 \text{ H} \quad t = 0$$

$$C = 2 \times 10^{-6} \text{ F} \quad q = 0.002 \text{ C}$$

$$R = 250 \Omega \quad dq = 0$$