



1.	a)	Solve, differential equation of the form $\frac{dy}{dx} + y \cot x = \cos x$ .	7
	b)	Solve $(x^2 - 4xy - 2y^2)dx + (y^2 - 4xy - 2x^2)dy = 0$	7
	c)	Find orthogonal trajectories of family of circles $x^2 + y^2 = c^2$ .	6
2.	a)	Solve $y'' + 4y' + 4y = 0$	7
	b)	Solve $y'' - 5y' + 6y = e^{4x} + 3$	7
	c)	Find Laplace transform of $e^{-3t} \cos^2 2t$	6
3.	a)	Find $L[t^2 \sin at]$	7
	b)	Find Laplace transform of $\frac{1 - e^{at}}{t}$	7
	c)	Find inverse Laplace transform of $\frac{s^2 + s - 2}{s(s+3)(s-2)}$	6
4.	a)	The particle moves along the curve $x = 2t^2, y = t^2 - 4t, z = 3t - 5$ , where $t$ is time. Find the component of velocity and acceleration at $t=1$ , in the direction $\hat{i} + 3\hat{j} + 2\hat{k}$	7
	b)	Find the values of $a, b$ , & $c$ if $\vec{F} = (3x + 3y + az)\hat{i} + (bx + 2y - 4z)\hat{j} + (2x + cy + z)\hat{k}$ is Irrotational.	7
	c)	Find the directional derivative of $\phi = xy^2 + yz^3$ at $(2, -1, 1)$ in the direction $2\hat{i} + \hat{j} + 2\hat{k}$	6
5.	a)	Find the unit normal to the surface $x^3 + y^3 + 3xyz = 3$ at $(1, 2, -1)$ .	7
	b)	Prove that $J_{1/2}(x) = \sqrt{\frac{2}{\pi x}} \sin x$	7
	c)	By using Rodrigue's formula, prove that $P_n'(x) = x P_{n-1}'(x) + n P_{n-1}(x)$ .	6