

1. Solve:  $(D^2 - DD' - 2D'^2 + 2D + 2D')z = e^{2x+3y} + \sin(2x + y) + xy.$

**Ans:**  $z = f_1(x - y) + e^y f_2(2x + y) - \frac{1}{10} e^{2x+3y} - \frac{1}{6} \cos(2x + y) + \frac{x}{24} (6xy - 6y + 9x - 2x^2 - 12)$

2. Solve:  $(D^2 - D'^2 + D - D')z = e^{2x+3y}$

**Ans:**  $z = f_1(y + x) + e^{-x} f_2(y - x) - \frac{1}{6} e^{2x+3y}$

3. Solve:  $(D - D' - 1)(D - D' - 2)z = \sin(2x + 3y)$

**Ans:**  $z = e^x f_1(y + x) + e^{2x} f_2(y + x) + \frac{1}{10} [\sin(2x + 3y) - 3\cos(2x + 3y)]$

4. Solve:  $(DD' + D - D' - 1)z = xy$

**Ans:**  $z = f_1(y) + e^{-x} f_2(y + x) + x$