

PES UNIVERSITY, BANGALORE

(Established under Karnataka Act 16 of 2013)

Department of Science and Humanities

B Tech First Semester

Session: Aug-Dec 2023

Subject Name: Engineering Mathematics I (4-0-0-4-4)

Subject Code: UE23MA141A

Self-learning component

Unit 1:

1. In estimating the cost of a pile of bricks measured as 2m x 15m x 1.2m, the tape is stretched 1% beyond the standard length. If the count is 450 bricks to 1 cu. m. and bricks costs Rs. 530 per 1000, find the approximate error in the cost. **Ans: 257.58**
2. The diameter and height of a right circular cylinder are measured to be 5 and 8 inches respectively. If each of these dimensions may be in error by ± 0.1 inch, find the relative percentage error in volume of the cylinder.
Ans: ± 0.0525

Unit 2:

3. Solve: $yp^2 - 2xp + y = 0$. **Ans: $y^2 = 2cx - c^2$**
4. Solve: $xp^2 - yp - y = 0$. **Ans: $x = c(1 + p)$; $y = p^2 e^{pc}$**

Unit 3:

5. Solve the differential equation: $x^2 \frac{d^2y}{dx^2} - 4x \frac{dy}{dx} + 6y = x^4 \sin x$
Ans: $y = c_1 x^2 + c_2 x^3 - x^2 \sin x$
6. Solve the differential equation: $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} - y = \frac{x^3}{1+x^2}$
Ans: $y = c_1 x + \frac{c_2}{x} + \frac{1}{4} \left(x + \frac{1}{x} \right) \log(1 + x^2) - \frac{x}{4}$

Unit 4:

7. Form the PDE of the family of all the spheres whose centres lie on the xy-plane and have the constant radius r. **Ans: $z^2(p^2 + q^2 + 1) = r^2$**
8. Form the PDE by eliminating the arbitrary functions from $z = (x + y)\phi(x^2 - y^2)$. **Ans: $py + qz = z$**