

PES Institute of Technology, Bangalore (Autonomous Institute under VTU, Belgaum)

12MA151

End semester assesment(ESA) B. E. I SEMESTER - November- 2015 ENGINEERING MATHEMATICS-II (Fast track)

Tiı	me:3	Hrs Answer All Questions Max Marks: 10	0
1.	a)	Solve _a linear differential equation of the form $\frac{dy}{dx} + y \cot x = \cos x$.	7
	b)	Solve $(x^2 - 4xy - 2y^2)dx + (y^2 - 4xy - 2x^2)dy = 0$	7
	c)	Find orthogonal trajectories of family of circles $x^2 + y^2 = c^2$.	6
2.	a)	Solve $y'' + 4y' + 4y = 0$	7
	b)	Solve $y'' - 5y' + 6y = e^{4x} + 3$	7
	c)	Find Laplace transform of $e^{-3t}\cos^2 2t$	6
3.	a)	Find $L[t^2 \sin at]$	7
	b)	Find Laplace transform of $\frac{1-e^{at}}{t}$	7
	c)	. Find inverse Laplace transform of $\frac{s^2+s-2}{s\left(s+3\right)\left(s-2\right)}$	6
4	The particle moves along the curve $x = 2t^2$, $y = t^2 - 4t$, $z = 3t - 5$, where t is time. Find the component of		
-	a)	velocity and acceleration at t=1,in the direction $\hat{i}+3\hat{j}+2\hat{k}$	7
	b)	Find the values of a, b, & c if $\hat{F} = (3x+3y+az)\hat{i} + (bx+2y-4z)\hat{j} + (2x+cy+z)\hat{k}$ is Irrotational.	7
	c)	Find the directional derivative of $\phi = xy^2 + yz^3$ at $(2,-1,1)$ in the direction $2\hat{i} + \hat{j} + 2\hat{k}$	6
5.	a)	Find the unit normal to the surface $x^3 + y^3 + 3xyz = 3$ at $(1,2,-1)$.	7
	b)		7
	,	Prove that $J_{1/2}(x) = \sqrt{\frac{2}{\pi x}} \sin x$	
	c)	By using Rodrigue's formula ,prove that $P_n'(x) = x P_{n-1}'(x) + n P_{n-1}(x)$.	6