

Relief, Stimulus, and Welfare:

Modeling a Cross-sector Scarce Resource Supply Chain Network under Fiscal and Monetary Policies

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November 7-13, 2020



ANNUAL MEETING | 2020 VIRTUAL

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Motivations



A farmer kneeling on his cracked land, Los Angeles, 2014



Congolese soldiers guarding suspected rebel fighters over the conflict of rare earth elements (cobalt, copper, and coltan) near the eastern town of Goma, 2013



Yemenis presenting documents in order to receive food rations provided by a local charity, in Sanaa, Yemmen, 2017



Some empty shelves in a grocery store in the US during COVID-19 pandemic, 2020

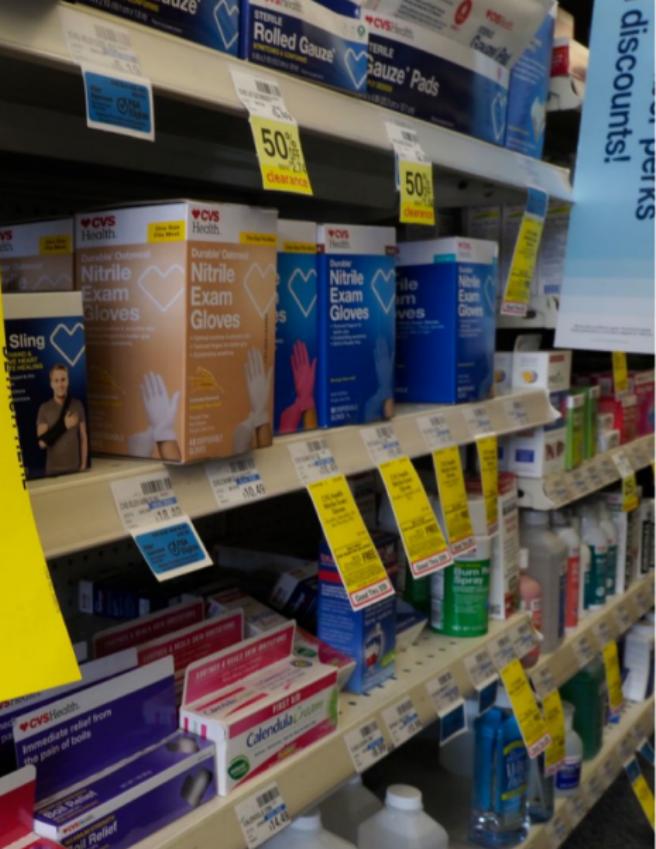
discounts!
PERKS

**Face masks
and gloves
may be
temporarily
unavailable
due to
high
demand.**

Your family's health is our top priority, and we ask for your patience while we work to secure additional supplies as quickly as possible.

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and gloves
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A notice covering an empty shelf at an Oakland CVS store in February, 2020

How climate change may impact energy usage: 2080-2099

Projected Changes in Energy Expenditures

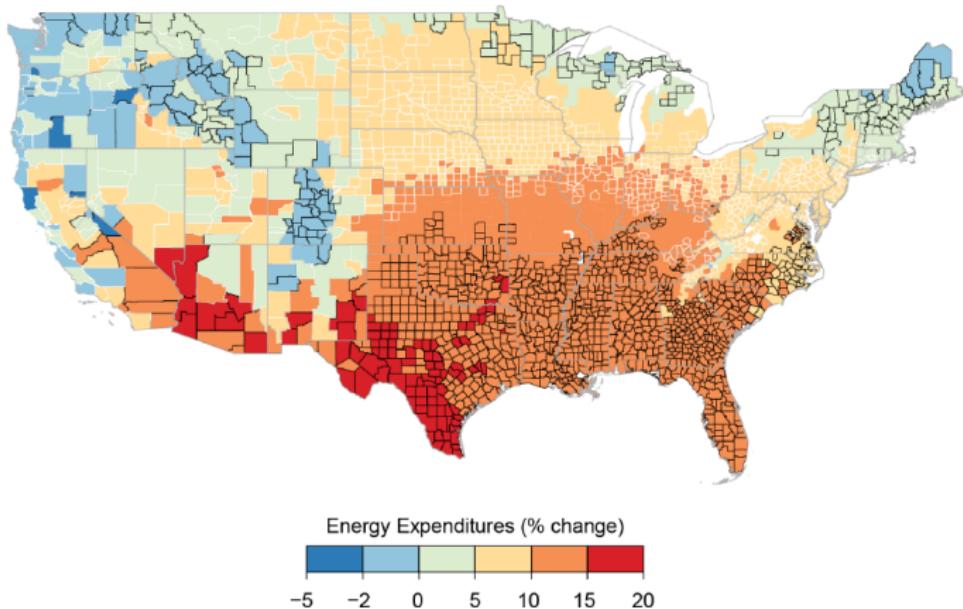


Figure 4.2: This figure shows county-level median projected increases in energy expenditures for average 2080–2099 impacts under the higher scenario (RCP8.5). Impacts are changes relative to no additional change in climate. Color indicates the magnitude of increases in energy expenditures in median projection; outline color indicates level of agreement across model projections (thin white outline, inner 66% of projections disagree in sign; no outline, more than 83% of projections agree in sign; black outline, more than 95% agree in sign; thick gray outline, state borders). Data were unavailable for Alaska, Hawai'i and the U.S.-Affiliated Pacific Islands, and the U.S. Caribbean regions. Source: Hsiang et al. 2017.¹⁴

Background

Scarce Resource

What are considered scarce resources?

(Rosenberg, 1973; Krautkraemer, 2005)

- Natural resources: agricultural crops, fisheries, wildlife, forests, petroleum, metals, minerals, even air, soil, water, etc
- Non-renewable resources: rare earth elements, fossil fuels
- Commodities in high demand during a short period of time: PPE during COVID-19 pandemic.



Resource scarcity: characters and causes

Characters of scarce resource

(Pfeffer and Salancik, 1978; Cannon and Perreault, 1999; Pfeffer and Salancik, 2003; Caniels and Gelderman, 2007; Hunt, 2000)

- Abundance means power
- Heterogeneous demand
- Interdependent with one another

Some causes of resource scarcity or stress

- Growing population and demand
- Climate change
- Geopolitical shift, trade wars
- Rising risk of crises such as pandemics

Laws in resource usage, ownership, and enforcement

Often, the conflicts over scarce resources have been taken to [the courts of law](#).

Some famous resource related supreme court cases

- WYOMING HEREFORD RANCH v. HAMMOND PACKING CO., Supreme court of Wyoming, 1952. (PRIOR APPROPRIATION)
- HARRIS v. BROOKS, Supreme Court of Arkansas 1955. (RIPARIAN RIGHTS)
- COMMONWEALTH OF MASSACHUSETTS et al. v. ENVIRONMENTAL PROTECTION AGENCY, the U.S. Supreme Court, 2007. (EPA's authority on CAA of 1963)



Research Questions

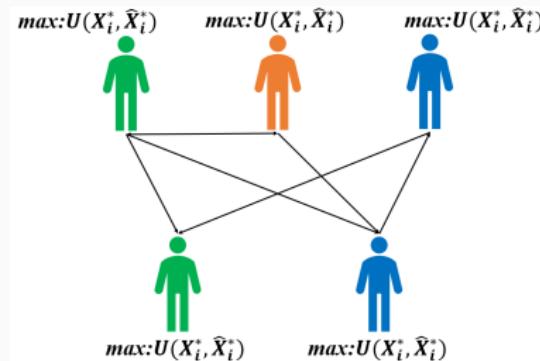
1. How can a scarce resource supply chain be represented by a general network?
2. For **resource producing firms**, how do they benefit from an incentive scheme? How does a specific incentive impact demands, prices, and profits? Under a certain environmental policy, how should firms adjust their business strategies in order to be more profitable and competitive?
3. For **consumers** at different demand markets, how do they benefit from a producer "stimulus package"?
4. For **resources owners**, what happens when conflict emerges? What could alleviate it?
5. For **policy makers**, how does social welfare respond to policy instruments? Who is the winner? During supply chain overload, who should get the stimulus when budget is limited? To relieve a critical resource shortage crisis, what might be a better incentive structure?

Related Literature

Related literature I: network game theories

The theoretical study of network game is a **new avenue** of research. It was revived from the earlier studies that address existence, uniqueness, sensitivity, convergence, and ϵ -approximation, etc.

- Network games theory (existence, uniqueness, sensitivity): Rosen (1965); Jackson and Zenou (2015); Parise and Ozdaglar (2017)
- Emerging trend - scalar quantities (eigenvalues of game Jacobians): Bramoullé et al. (2014); Naghizadeh and Liu (2017); Melo (2018)



- Spatial price equilibrium (SPE) - a transportation network: Enke (1951); Samuelson (1952); Takayama and Judge (1964); Dafermos and Nagurney (1984, 1987)
- General supply chains: Nagurney et al. (2002); Zhang (2006); Nagurney (2006)
- Specialized supply chains: power (Nagurney et al., 2006; Nagurney and Matsypura, 2007; Wu et al., 2006); blood (Nagurney and Dutta, 2019); food (Besik and Nagurney, 2017); drugs (Masoumi et al., 2012).
- Policy intervention: taxation (Wu et al., 2006; Yu et al., 2018); subsidy (Wu et al., 2019)

Related literature III: modeling non-cooperative complex systems

This study is also inherent to the research that aims to understand the interconnected physical resources and their ability to adapt to external stressors in a competitive environment.

- Agriculture and fuels: Wang et al. (2013); Lim and Ouyang (2016); Bai et al. (2016, 2012); Luo and Miller (2013); Bajgiran et al. (2019)
- Energies and water: Zhang and Vesselinov (2016); Hamoud and Jang (2020)
- Water and agriculture: Bakker et al. (2018)

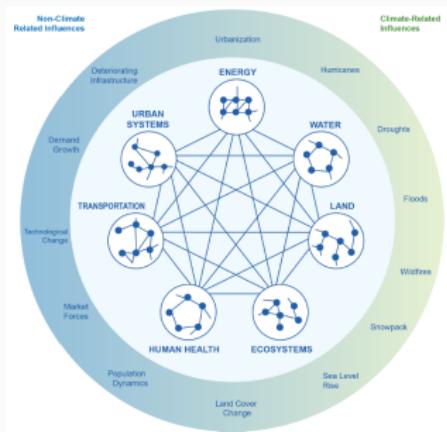


Figure 1: Sources: Pacific Northwest Nat'l Lab, Arizona State, Cornell University

A General Model

The incentivized scarce resource supply chain network

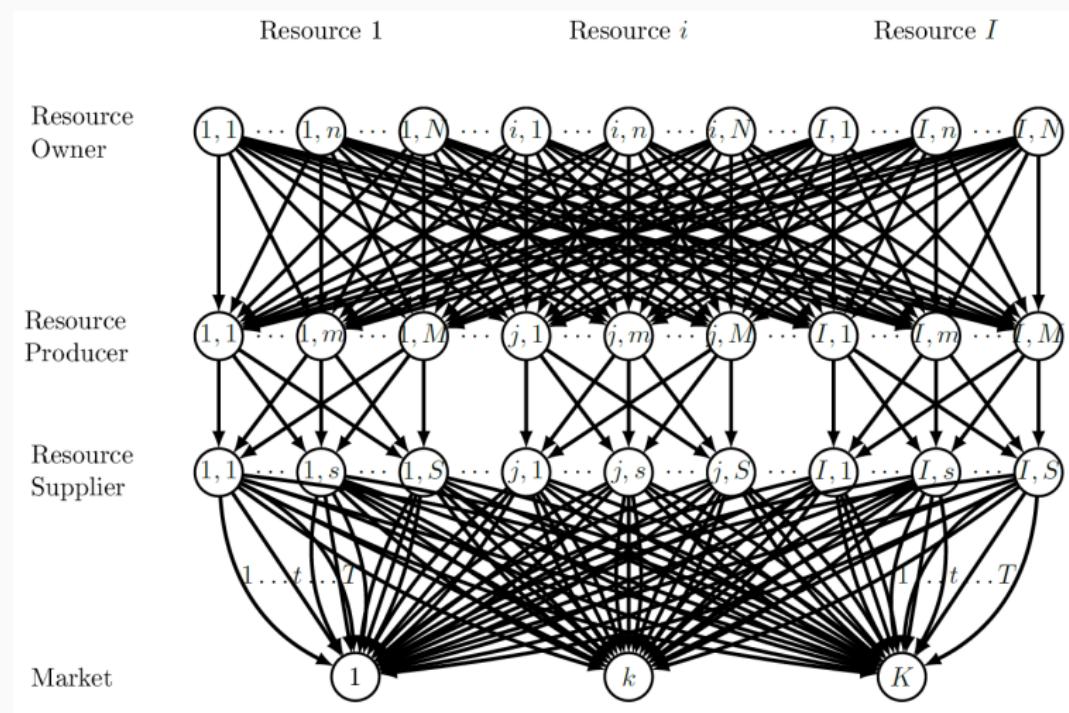


Figure 2: A Scarce Resource Supply Chain Network

The incentive scheme

A_g : cutoff bracket of the incentives, $g = 1, \dots, G$.

δ_g : the excess of output quantity within bracket A_g . Assume linear.

The general incentive payment function

$$\alpha_0(x) + \sum_{g=1}^G \alpha_g(\delta_g), \quad (1)$$

where, $\delta_g = [x - A_g^{in}]_+$, $g = 1, \dots, G$.

Note: this scheme can also be used as a general taxation scheme.

Example: the US Economic Impact Payments of COVID-19 (aka, the stimulus checks) is:

$$\$1200 - \$0.05(\delta_1), \quad (2)$$

where, $\delta_1 = [x - \$75000]_+$, $\delta_2 = [x - \$99000]_+$.

Resource owner's problem (1 of 2)



$$\begin{aligned}
 \max : & \sum_{j=1}^I \sum_{m=1}^M \rho_{0jm}^{in} x_{jm}^{in} - f^{in}(x^{in}) - \sum_{j=1}^I \sum_{m=1}^M c_{jm}^{in}(x_{jm}^{in}) + \alpha_0 \left(\sum_{j=1}^I \sum_{m=1}^M x_{jm}^{in} \right) + \sum_{g=1}^G \alpha_g (\delta_g^{in}) \\
 \text{s.t. :} & \sum_{j=1}^I \sum_{m=1}^M x_{jm}^{in} \leq U_{in}, \\
 & \sum_{j=1}^I \sum_{m=1}^M x_{jm}^{in} - \delta_g^{in} \leq A_g^{in}, \quad \forall g, \\
 & x_{jm}^{in} \geq 0, \quad \forall j, m, \\
 & \delta_g^{in} \geq 0, \quad \forall g.
 \end{aligned}$$

Resource owner's problem (2 of 2)

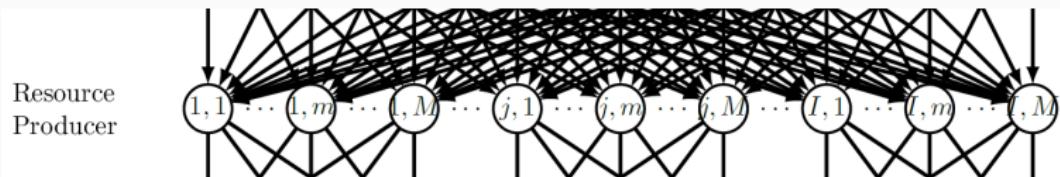
Reformulate the previous optimization problem into VI problem:

Resource owner's optimality condition

$$\begin{aligned}
 & \sum_{i=1}^I \sum_{n=1}^N \sum_{j=1}^J \sum_{m=1}^M \left[\frac{\partial f^{in}(x_j^{in*})}{\partial x_{jm}^{in}} + \frac{\partial c_{jm}^{in}(x_j^{in*})}{\partial x_{jm}^{in}} - \rho_{0jm}^{in*} - \frac{\partial \alpha_0(x_j^{in*})}{\partial x_{jm}^{in}} \right. \\
 & \quad \left. + \lambda_{in}^{0*} + \sum_{g=1}^G \mu_{ing}^{0*} \right] \times (x_{jm}^{in} - x_j^{in*}) \\
 & \quad + \sum_{i=1}^I \sum_{n=1}^N \sum_{g=1}^G \left[-\frac{\partial \alpha_g(\delta_g^{in*})}{\partial \delta_g^{in}} \right] \times (\delta_g^{in} - \delta_g^{in*}) \\
 & \quad + \sum_{i=1}^I \sum_{n=1}^N \left[U_{in} - \sum_{j=1}^J \sum_{m=1}^M x_{jm}^{in*} \right] \times (\lambda_{in}^0 - \lambda_{in}^{0*}) \\
 & \quad + \sum_{i=1}^I \sum_{n=1}^N \sum_{g=1}^G \left[A_g^{in} - \sum_{j=1}^J \sum_{m=1}^M x_{jm}^{in*} + \delta_g^{in*} \right] \times (\mu_{ing}^0 - \mu_{ing}^{0*}) \geq 0, \\
 & \quad \forall (Q^0, \mathfrak{d}^0, \lambda^0, \mu^0) \in \mathcal{K}^1,
 \end{aligned}$$

where, $\mathcal{K}^1 \equiv \{(Q^0, \mathfrak{d}^0, \lambda^0, \mu^0) | (Q^0, \mathfrak{d}^0, \lambda^0, \mu^0) \in R_+^{I^2 MN + 2ING + IN}\}$.

Resource producer's problem (1 of 2)



$$\max : \sum_{s=1}^S \rho_{1s}^{jm*} x_s^{jm} - \sum_{j=1}^I \sum_{n=1}^N \rho_{0jm}^{in*} x_{jm}^{in} - f^{jm}(x_{jm}) - \sum_{s=1}^S c_s^{jm}(x_s^{jm})$$

$$+ \beta_0 \left(\sum_{s=1}^S x_s^{jm} \right) + \sum_{g=1}^G \beta_g (\delta_g^{jm})$$

$$s.t. : \sum_{i=1}^I \sum_{n=1}^N x_{jm}^{in} \cdot \psi_{jm}^{in} \leq \sum_{s=1}^S x_s^{jm},$$

$$\sum_{s=1}^S x_s^{jm} - \delta_g^{jm} \leq B_g^{jm}, \quad \forall g,$$

$$x_s^{jm} \geq 0, \quad \forall s,$$

$$\delta_g^{jm} \geq 0, \quad \forall g.$$

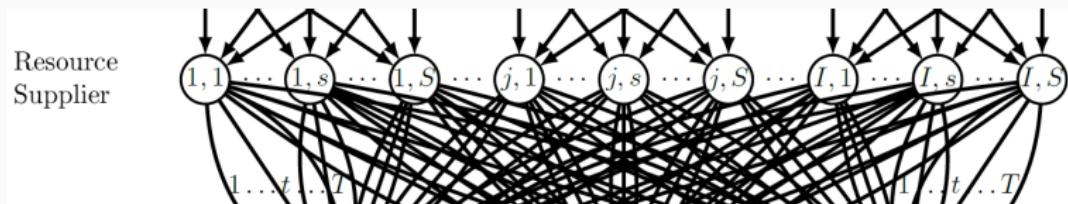
Resource producer's problem (2 of 2)

Resource producer's optimality condition

$$\begin{aligned}
& \sum_{i=1}^I \sum_{n=1}^N \sum_{j=1}^I \sum_{m=1}^M \left[\frac{\partial f^{jm}(x_{jm}^*)}{\partial x_{jm}^{in}} + \rho_{0jm}^{in*} + \psi_{jm}^{in} \lambda_{jm}^{1*} \right] \times (x_{jm}^{in} - x_{jm}^{in*}) \\
& + \sum_{j=1}^I \sum_{m=1}^M \sum_{s=1}^S \left[\frac{\partial c_s^{jm}(x_s^{jm*})}{\partial x_s^{jm}} - \rho_{1s}^{jm*} - \frac{\partial \beta_0(x_s^{jm*})}{\partial x_s^{jm}} - \lambda_{jm}^{1*} + \sum_{g=1}^G \mu_{jmg}^{1*} \right] \times (x_s^{jm} - x_s^{jm*}) \\
& \quad + \sum_{j=1}^I \sum_{m=1}^M \sum_{g=1}^G \left[- \frac{\partial \beta_g(\delta_g^{jm*})}{\partial \delta_g^{jm}} \right] \times (\delta_g^{jm} - \delta_g^{jm*}) \\
& + \sum_{j=1}^I \sum_{m=1}^M \left[\sum_{s=1}^S x_s^{jm*} - \sum_{i=1}^I \sum_{n=1}^N x_{jm}^{in*} \cdot \psi_{jm}^{in} \right] \times (\lambda_{jm}^1 - \lambda_{jm}^{1*}) \\
& + \sum_{j=1}^I \sum_{m=1}^M \sum_{g=1}^G \left[B_g^{jm} - \sum_{s=1}^S x_s^{jm*} + \delta_g^{jm*} \right] \times (\mu_{jmg}^1 - \mu_{jmg}^{1*}) \geq 0, \\
& \quad \forall (Q^0, Q^1, \delta^1, \lambda^1, \mu^1) \in \mathcal{K}^2,
\end{aligned}$$

where, $\mathcal{K}^2 \equiv \{(Q^0, Q^1, \delta^1, \lambda^1, \mu^1) | (Q^0, Q^1, \delta^1, \lambda^1, \mu^1) \in R_+^{I^2 MN + IMS + 2IMG + IM}\}$.

Resource supplier's problem (1 of 2)



$$\max : \sum_{t=1}^T \sum_{k=1}^K \rho_{2tk}^{js*} x_{tk}^{js} - \sum_{j=1}^I \sum_{m=1}^M \rho_{1s}^{jm*} x_s^{jm} - f^{js}(x^{js}) - \sum_{t=1}^T \sum_{k=1}^K c_{tk}^{js}(x_{tk}^{js})$$

$$S.t. : \sum_{k=1}^K \sum_{t=1}^T x_{tk}^{js} \leq \sum_{m=1}^M x_s^{jm},$$

$$x_{tk}^{js} \geq 0, \quad \forall t, k.$$

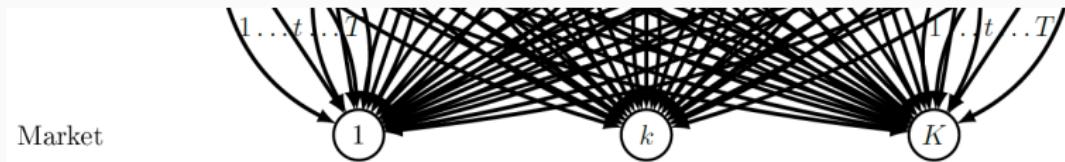
Resource supplier's problem (2 of 2)

Resource supplier's optimality condition

$$\begin{aligned} & \sum_{j=1}^I \sum_{s=1}^S \sum_{t=1}^T \sum_{k=1}^K \left[\frac{\partial f^{js}(x^{js*})}{\partial x_{tk}^{js}} + \frac{\partial c_{tk}^{js}(x_{tk}^{js*})}{\partial x_{tk}^{js}} - \rho_{2tk}^{js*} + \lambda_{js}^{2*} \right] \times (x_{tk}^{js} - x_{tk}^{js*}) \\ & + \sum_{j=1}^I \sum_{m=1}^M \sum_{s=1}^S \left[\rho_{1s}^{jm*} - \lambda_{js}^{2*} \right] \times (x_s^{jm} - x_s^{jm*}) \\ & + \sum_{j=1}^I \sum_{s=1}^S \left[\sum_{m=1}^M x_s^{jm*} - \sum_{k=1}^K \sum_{t=1}^T x_{tk}^{js*} \right] \times (\lambda_{js}^2 - \lambda_{js}^{2*}) \geq 0, \\ & \forall (Q^1, Q^2, \lambda^2) \in \mathcal{K}^3, \end{aligned}$$

where, $\mathcal{K}^3 \equiv \{(Q^1, Q^2, \lambda^2) | (Q^1, Q^2, \lambda^2) \in R_+^{IMS+ISTK+IS}\}.$

Demand market's problem (1 of 2)



The spatial price equilibrium condition is given by

$$\rho_{2tk}^{js*} + \hat{c}_{tk}^{js*}(x_{tk}^{js*}) \begin{cases} = \rho_{3k}^j(d^*) & \text{if } x_{tk}^{js*} > 0 \\ > \rho_{3k}^j(d^*) & \text{if } x_{tk}^{js*} = 0 \end{cases} \quad \forall j, s, t, k.$$

Demand market's problem (2 of 2)

Demand market's optimality condition

$$\sum_{j=1}^I \sum_{s=1}^S \sum_{t=1}^T \sum_{k=1}^K [\rho_{2tk}^{js*} + \hat{c}_{tk}^{js}(x_{tk}^{js*})] \times (x_{tk}^{js} - x_{tk}^{js*}) - \sum_{j=1}^I \sum_{k=1}^K \rho_{3k}^j(d^*) \times (d - d^*) \geq 0,$$
$$\forall (Q^2, d) \in \mathcal{K}^4,$$

where, $\mathcal{K}^4 \equiv \{(Q^2, d) | Q^2 \in R_+^{ISTK}, d \in R_+^{IK}\}$.

The equilibrium

$$\begin{aligned}
& \sum_{i=1}^I \sum_{n=1}^N \sum_{j=1}^I \sum_{m=1}^M \left[\frac{\partial f^{in}(x_j^{in*})}{\partial x_{jm}^{in}} + \frac{\partial f^{jm}(x_{jm}^{in*})}{\partial x_{jm}^{in}} + \frac{\partial c_{jm}^{in}(x_{jm}^{in*})}{\partial x_{jm}^{in}} - \frac{\partial \alpha_0(x_{jm}^{in*})}{\partial x_{jm}^{in}} + \lambda_{in}^0 + \psi_{jm}^{in} \lambda_{jm}^1 + \sum_{g=1}^G \mu_{ing}^0 \right] \times (x_{jm}^{in} - x_{jm}^{in*}) \\
& + \sum_{j=1}^I \sum_{m=1}^M \sum_{s=1}^S \left[\frac{\partial c_s^{jm}(x_s^{jm*})}{\partial x_s^{jm}} - \frac{\partial \beta_0(x_s^{jm*})}{\partial x_s^{jm}} - \lambda_{jm}^1 - \lambda_{js}^2 + \sum_{g=1}^G \mu_{jmg}^1 \right] \times (x_s^{jm} - x_s^{jm*}) \\
& + \sum_{j=I}^I \sum_{s=1}^S \sum_{t=1}^T \sum_{k=1}^K \left[\frac{\partial f^{js}(x_{tk}^{js*})}{\partial x_{tk}^{js}} + \frac{\partial c_{tk}^{js}(x_{tk}^{js*})}{\partial x_{tk}^{js}} + \hat{c}_{tk}^{js}(x_{tk}^{js*}) + \lambda_{js}^2 \right] \times (x_{tk}^{js} - x_{tk}^{js*}) \\
& - \sum_{i=1}^I \sum_{n=1}^N \sum_{g=1}^G \frac{\partial \alpha_g(\delta_g^{in*})}{\partial \delta_g^{in}} \times (\delta_g^{in} - \delta_g^{in*}) - \sum_{j=1}^I \sum_{m=1}^M \sum_{g=1}^G \frac{\partial \beta_g(\delta_g^{jm*})}{\partial \delta_g^{jm}} \times (\delta_g^{jm} - \delta_g^{jm*}) \\
& - \sum_{j=1}^I \sum_{k=1}^K \rho_{3k}^j(d^*) \times (d - d^*) + \sum_{i=1}^I \sum_{n=1}^N \left[U_{in} - \sum_{j=1}^I \sum_{m=1}^M x_{jm}^{in*} \right] \times (\lambda_{in}^0 - \lambda_{in}^0) \\
& + \sum_{j=1}^I \sum_{m=1}^M \left[\sum_{s=1}^S x_s^{jm*} - \sum_{i=1}^I \sum_{n=1}^N x_{jm}^{in*} \cdot \psi_{jm}^{in} \right] \times (\lambda_{jm}^1 - \lambda_{jm}^1) + \sum_{j=I}^I \sum_{s=1}^S \left[\sum_{m=1}^M x_s^{jm*} - \sum_{k=1}^K \sum_{t=1}^T x_{tk}^{js*} \right] \times (\lambda_{js}^2 - \lambda_{js}^2) \\
& + \sum_{i=1}^I \sum_{n=1}^N \sum_{g=1}^G \left[A_g^{in} - \sum_{j=1}^I \sum_{m=1}^M x_{jm}^{in*} + \delta_g^{in*} \right] \times (\mu_{ing}^0 - \mu_{ing}^0) \\
& + \sum_{j=1}^I \sum_{m=1}^M \sum_{g=1}^G \left[B_g^{jm} - \sum_{s=1}^S x_s^{jm*} + \delta_g^{jm*} \right] \times (\mu_{jmg}^1 - \mu_{jmg}^1) \geq 0,
\end{aligned}$$

$$\forall (Q^0, Q^1, Q^2, \mathfrak{d}^0, \mathfrak{d}^1, d, \lambda^0, \lambda^1, \lambda^2, \mu^0, \mu^1) \in R_+^{(I^2MN+ING+IMG+IMS+ISTK)+I(N+M+S+K)}, \quad (3)$$

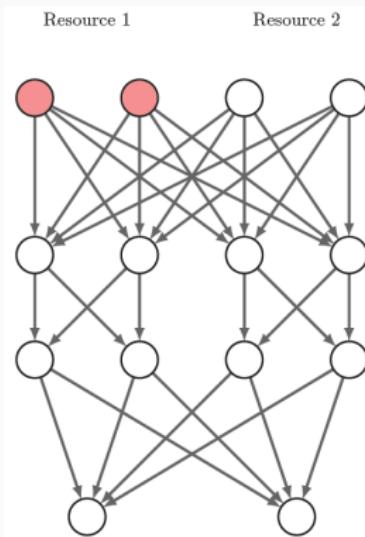
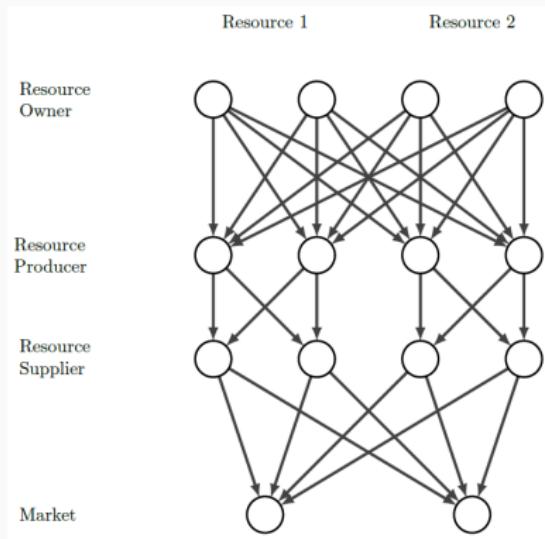
Algorithms that solve variational inequalities

- Lemke-Howson algorithm (Lemke and Howson Jr, 1964; Eaves, 1978)
- Newton-based (Newton, Quasi-Newton, linearized Jacobi, projection) methods (Cottle, 1966; Korpelevich, 1976; Pang and Chan, 1982)
- Fixed-point method (Scarf, 1967)
- Euler method (Dupuis and Nagurney, 1993; Zhang and Nagurney, 1995).

Small Scale Examples

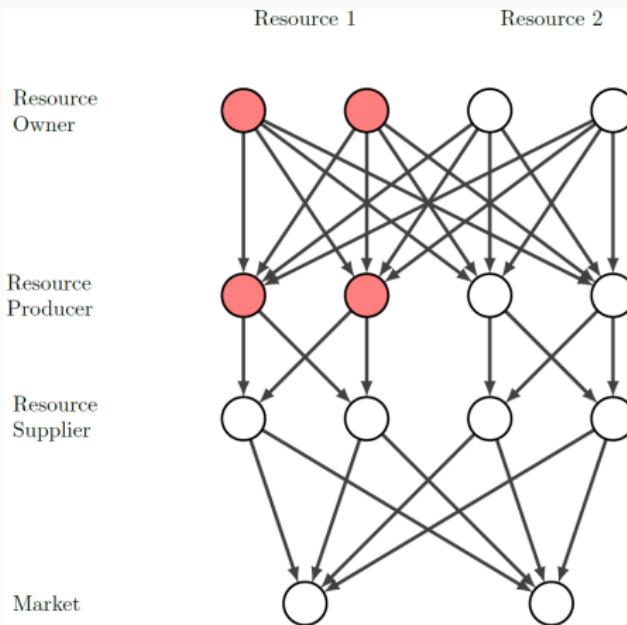
Example 1: un-incentivized v.s. incentivized network

In this example, we examine the output quantities of firms, market prices, and welfare estimates between the following two networks.



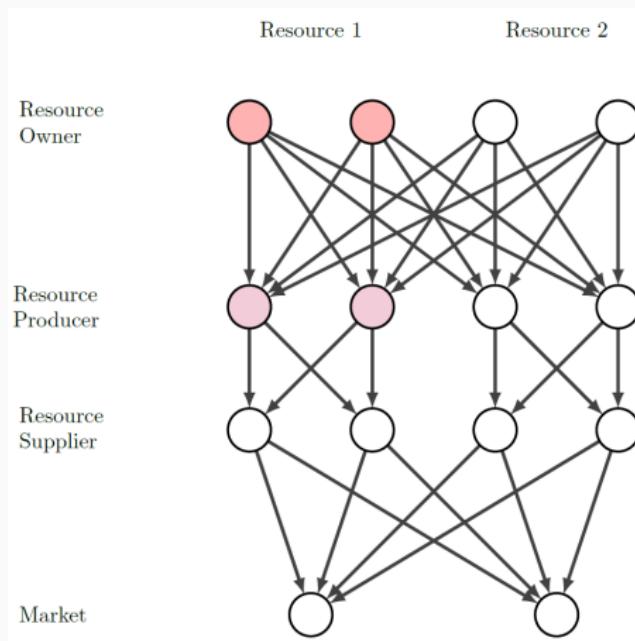
Example 2: Critical resource shortage relief

In this example, resource 1 emerges to be a critical shortage in supplies. To relieve such distress, both resource owner and producer of resource 1 receive flat-rate incentives.



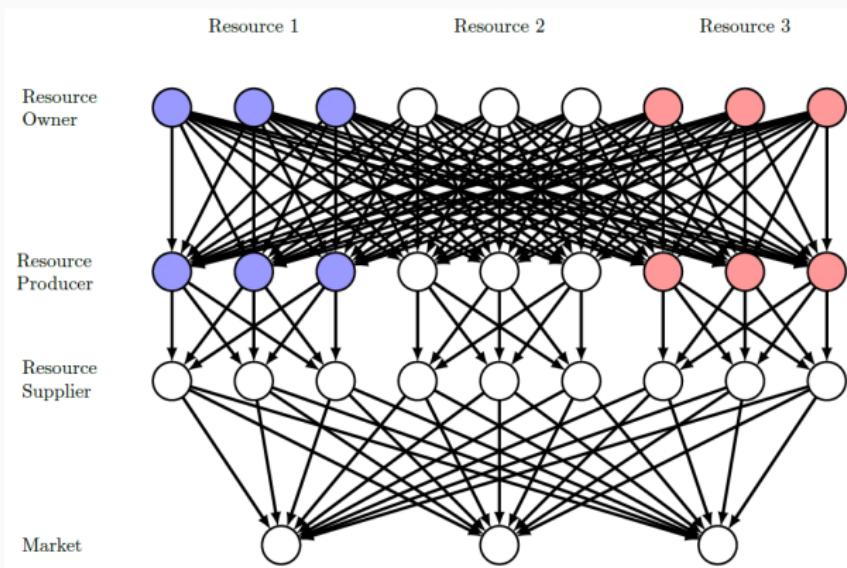
Example 3: Monetary policies with limited budget

In this example, a government has limited budget on the total of incentives. This example gives insight to who should get the stimulus. Owners or producers?



Example 4: a balanced monetary-fiscal policy with taxation and incentive

We examine a monetary-fiscal policy by which a tax scheme is applied to an undesired resource (e.g., a conventional energy with adverse environmental effect), and an incentive scheme is applied to a desired resource (e.g., a new clean energy). In this example, resource 1 is taxed, while resource 3 is incentivized.



In this ongoing research:

1. We construct a general scarce resource supply chain network equilibrium model under fiscal/monetary policies.
2. The model is formulated in variational inequalities; the optimality conditions for the resource representatives of the network are derived.
3. Small scale examples are furnished to demonstrate the application of the model.

Thank you!
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