

PERIDYNAMIC SIMULATION PLATTFORM TO DETERMINE VIRTUAL ALLOWABLES OF MANUFACTURING DEVIATIONS

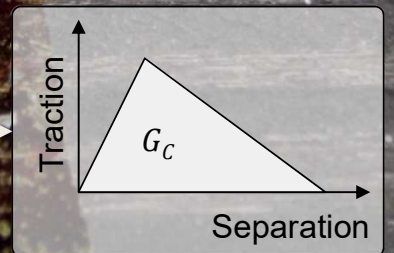
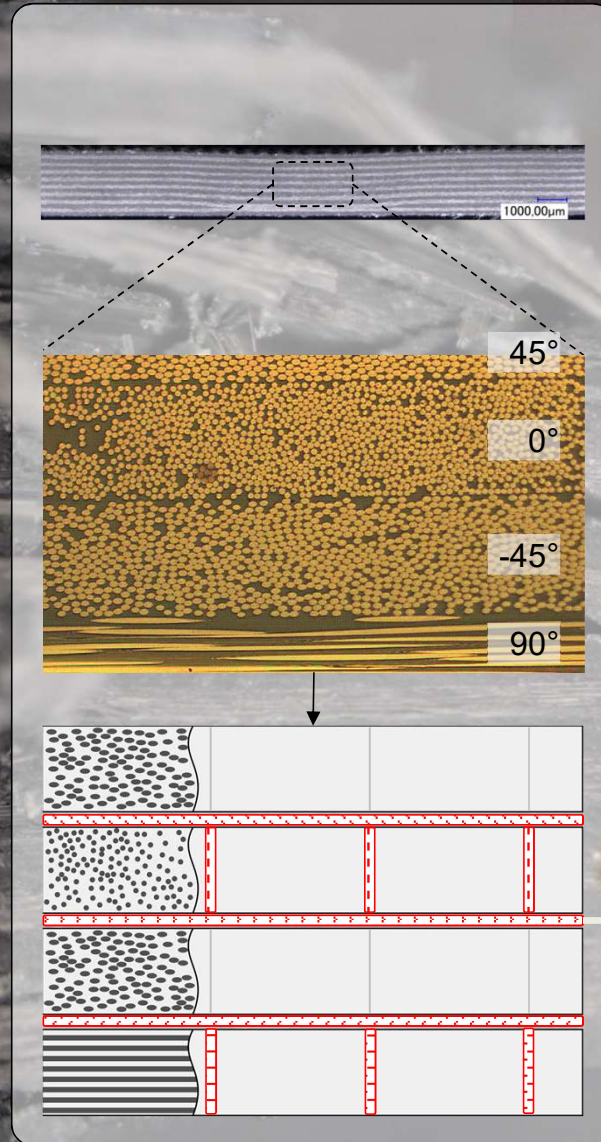
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Knowledge for Tomorrow



Why is modeling damage in FEM so difficult? [1]



Damage – part of the problem or the solution?

Peridynamic mechanics

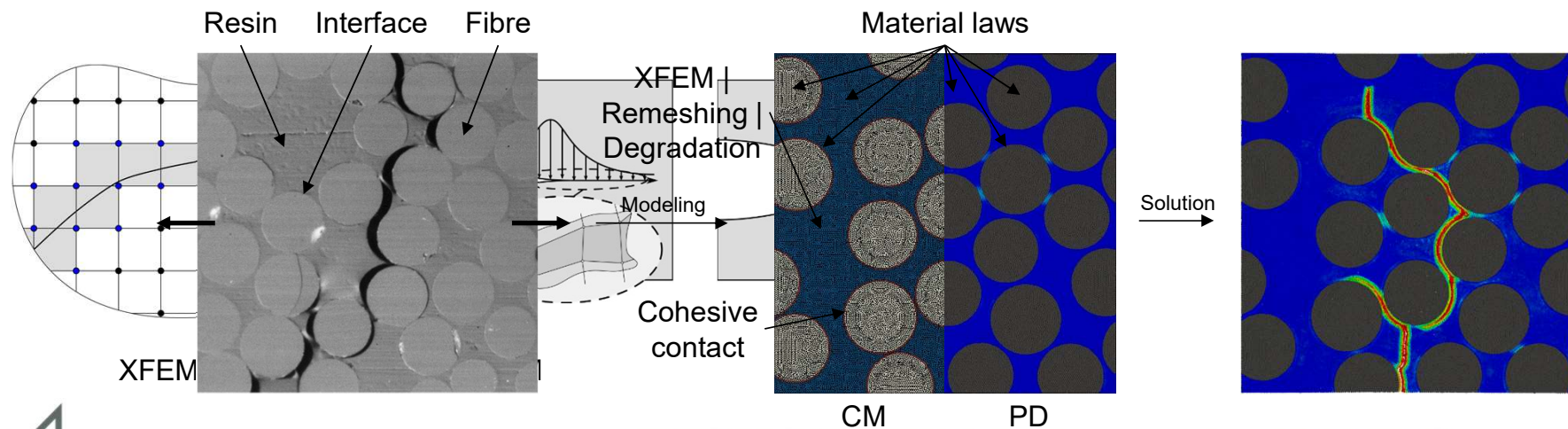
Continuum mechanics (CM) & FEM

- Assumptions:
 - Continuous medium ⚡
 - \mathbf{u} 2x continuously differentiable ⚡
 - Conservation equations satisfied
 - ...
- Momentum conservation: $\nabla \boldsymbol{\sigma} + \mathbf{b} = \rho \ddot{\mathbf{u}}$ ⚡

Peridynamics (PD)

- Assumption:
 - Conservation equations satisfied
- Momentum conservation:

$$\int_{\delta} [\underline{\mathbf{T}}(\mathbf{x}, t) \langle \mathbf{q} - \mathbf{x} \rangle - \underline{\mathbf{T}}(\mathbf{q}, t) \langle \mathbf{x} - \mathbf{q} \rangle dV_{\mathbf{q}}] + \mathbf{b} = \rho \ddot{\mathbf{u}}$$



Modeling

$$\underline{\mathbf{T}}\langle\xi\rangle = \underline{\omega}\langle\xi\rangle \mathbf{P} \mathbf{K}^{-1} \xi$$

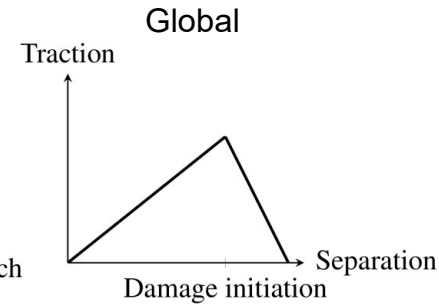
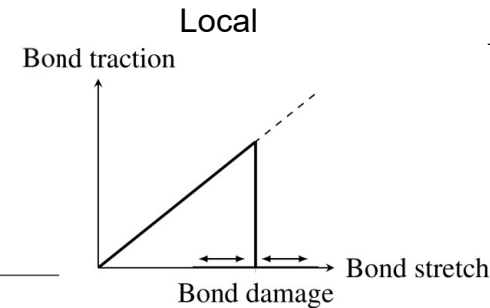
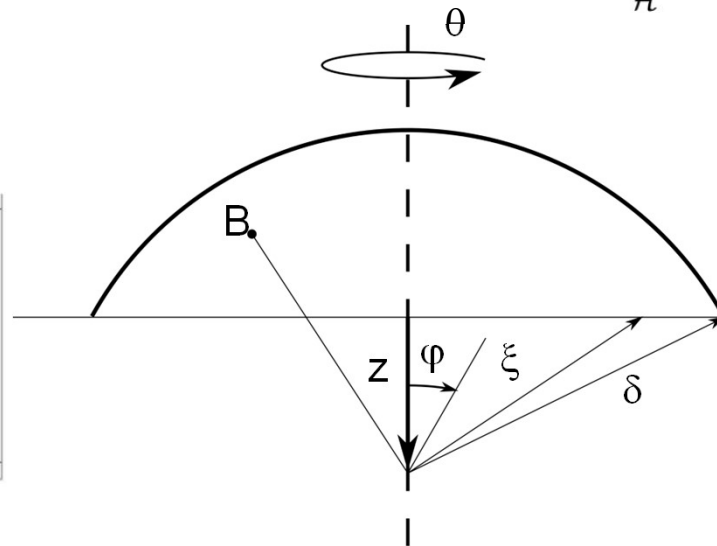
$$\mathbf{P} = \det \mathbf{F} \boldsymbol{\sigma} \mathbf{F}^{-1}$$

$$\mathbf{F} = \left[\int_{\mathcal{H}} \underline{\omega}\langle\xi\rangle \underline{\mathbf{Y}}\langle\xi\rangle \otimes \underline{\mathbf{X}}\langle\xi\rangle dV_x \xi \right] \cdot \mathbf{K}^{-1}$$

$$\mathbf{K} = \int_{\mathcal{H}} \underline{\omega}\langle\xi\rangle \underline{\mathbf{X}}\langle\xi\rangle \otimes \underline{\mathbf{X}}\langle\xi\rangle dV_x \xi$$

$$\boldsymbol{\sigma} = f\left(\frac{\partial \boldsymbol{\sigma}}{\partial \boldsymbol{\varepsilon}}, \boldsymbol{\varepsilon}\right)$$

User Material



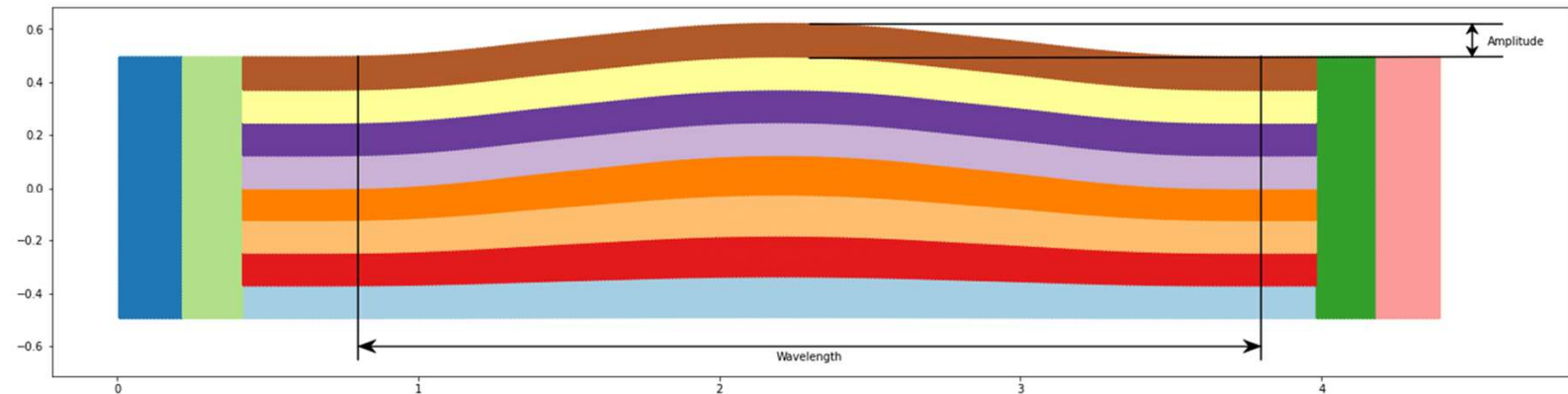
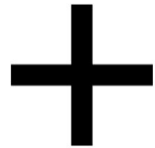
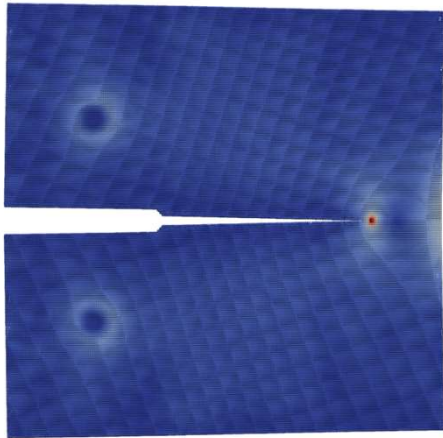
$$G = 2 \int_0^\delta \int_{H_r} w_b dV_\xi$$

$$w_b = \frac{4G}{\pi\delta^4}$$

$$w_b > w_{critical}$$



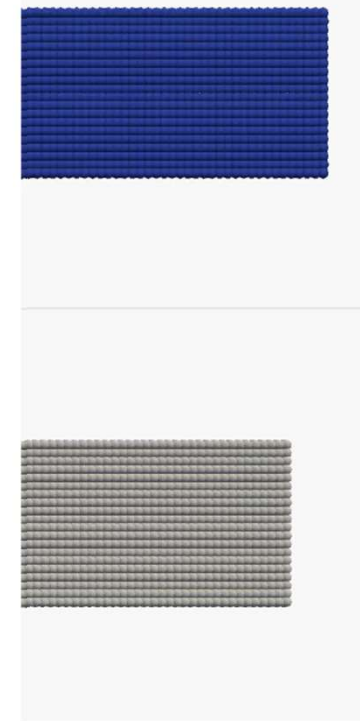
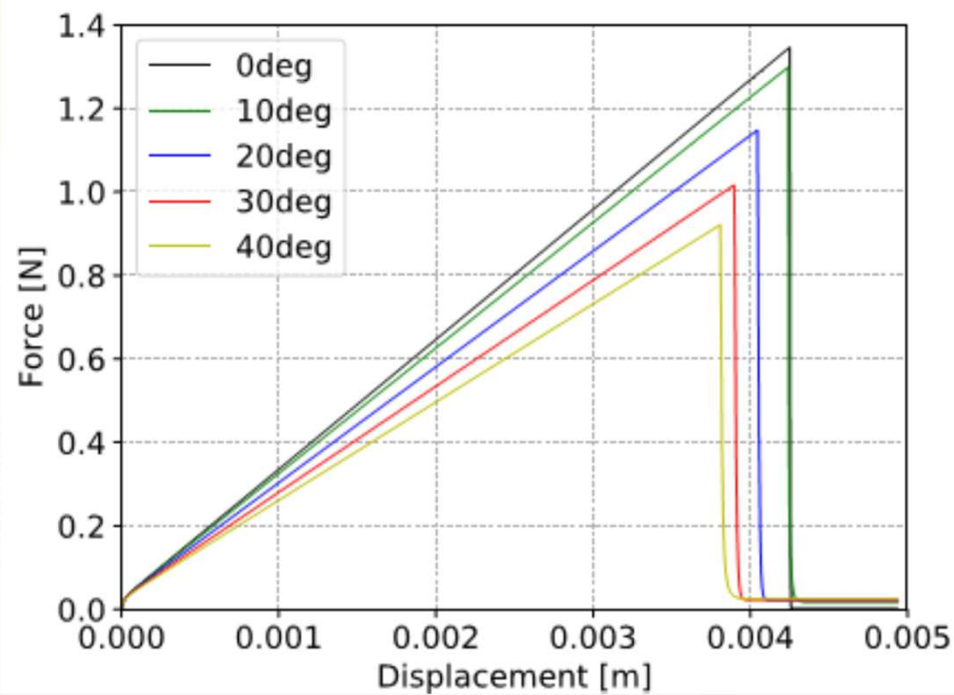
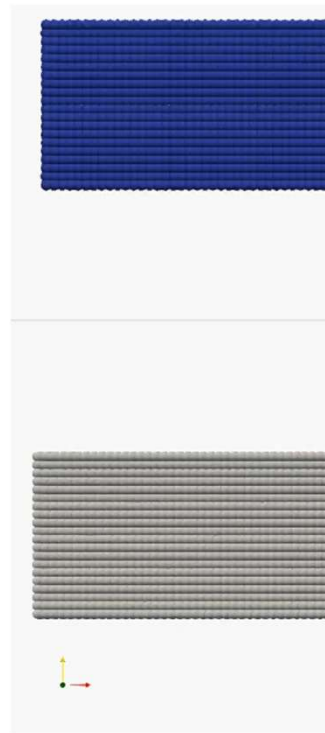
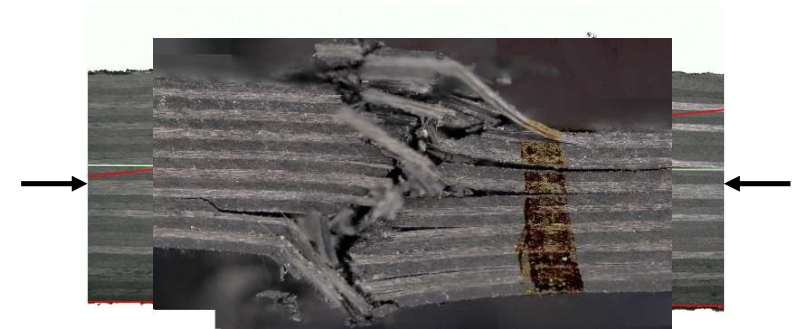
Virtual Testing

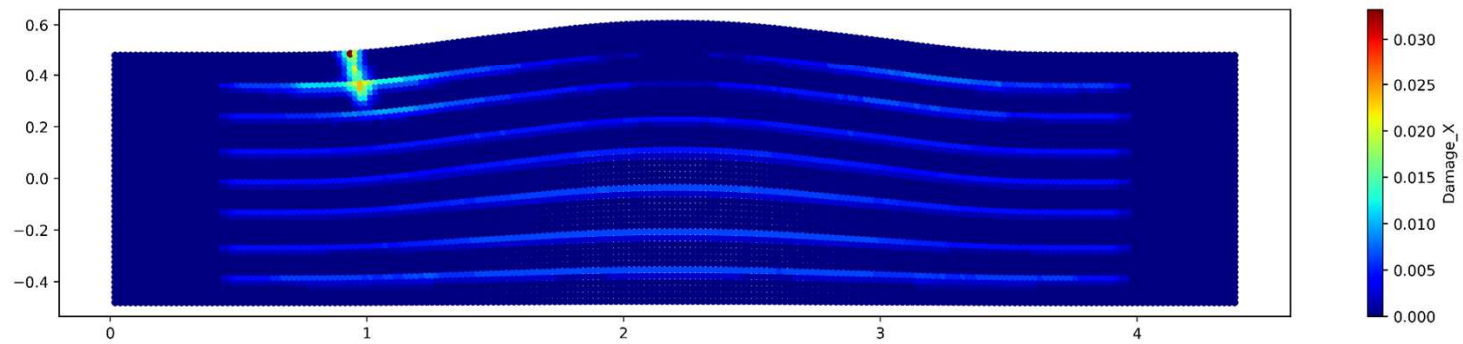
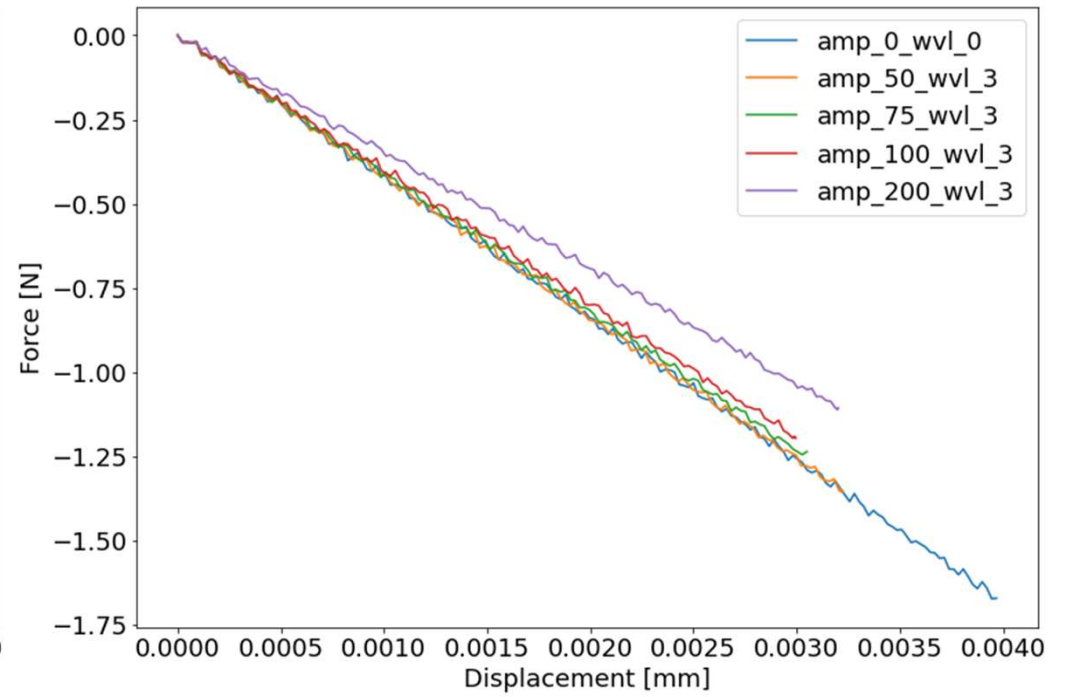
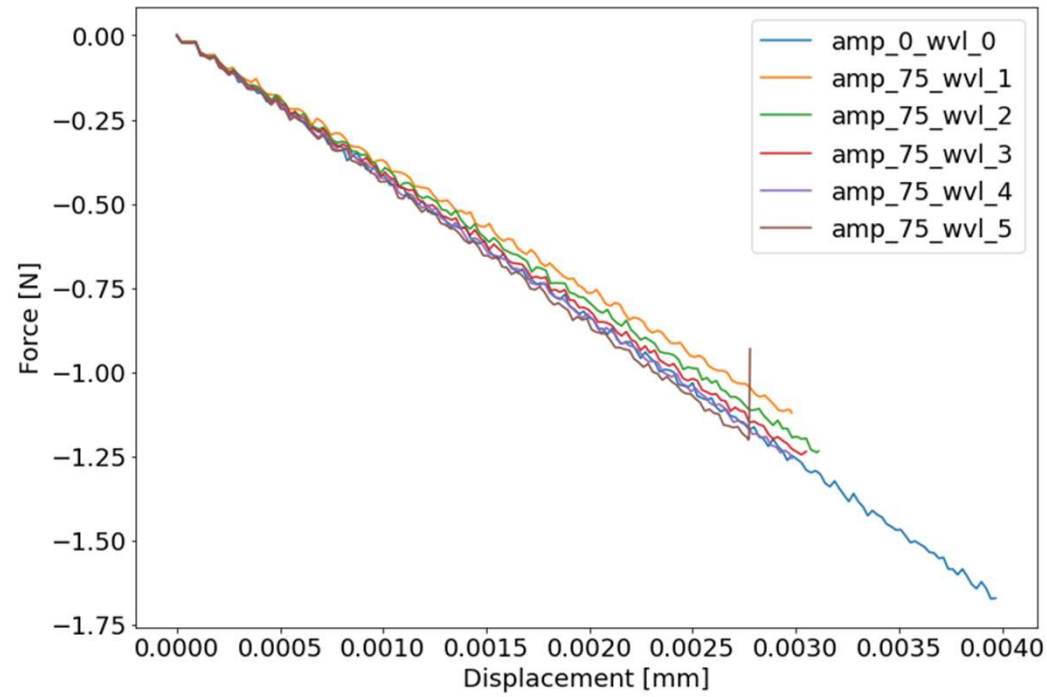


Peridynamics

Numerical prediction of phenomena

- Example: Waviness
- Modeled by local variation of material orientation





Conclusion

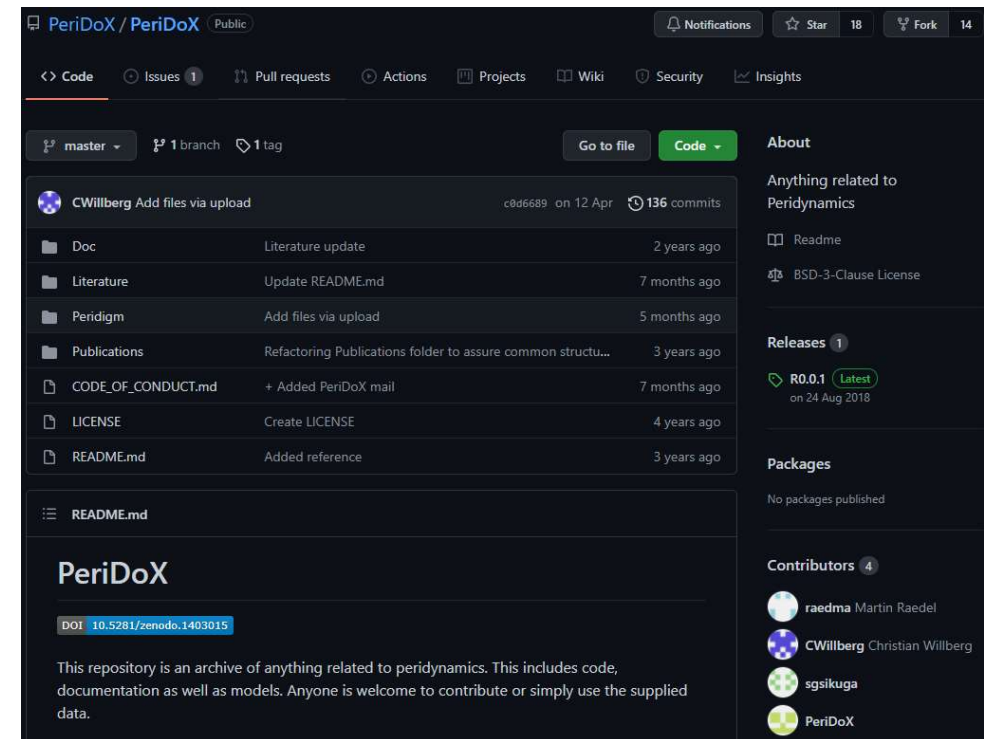
- Ondulations have significant influence in load carrying capacity
- Virtual testing helps to catch a wide variety of scenarios
- Peridynamics is a good method to describe the progressive failure
- Next steps
 - Analysis of a wide range of parameters and sensitivity analysis
 - Validation of the process



Bibliography

Raffael Bogenfeld, Janko Kreikemeier, and Tobias Wille. “Review and benchmark study on the analysis of low-velocity impact on composite laminates”. In: Engineering Failure Analysis 86 (2018), pp. 72–99. ISSN : 1350-6307. DOI : [10.1016/j.engfailanal.2017.12.019](https://doi.org/10.1016/j.engfailanal.2017.12.019)

[2] Daniel Krause. “Micromechanics of the fatigue behaviour of polymers”. DLR Report 2016-26. PhD Thesis. Technical University Braunschweig, 2016.



<https://github.com/PeriDoX/PeriDoX>



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The work was done in German Research Foundation funded project: “Gekoppelte Peridynamik-Finite-Elemente-Simulationen zur Schädigungsanalyse von Faserverbundstrukturen”

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Thank you!

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Rädel, M. & Willberg, C. PeriDoX Repository

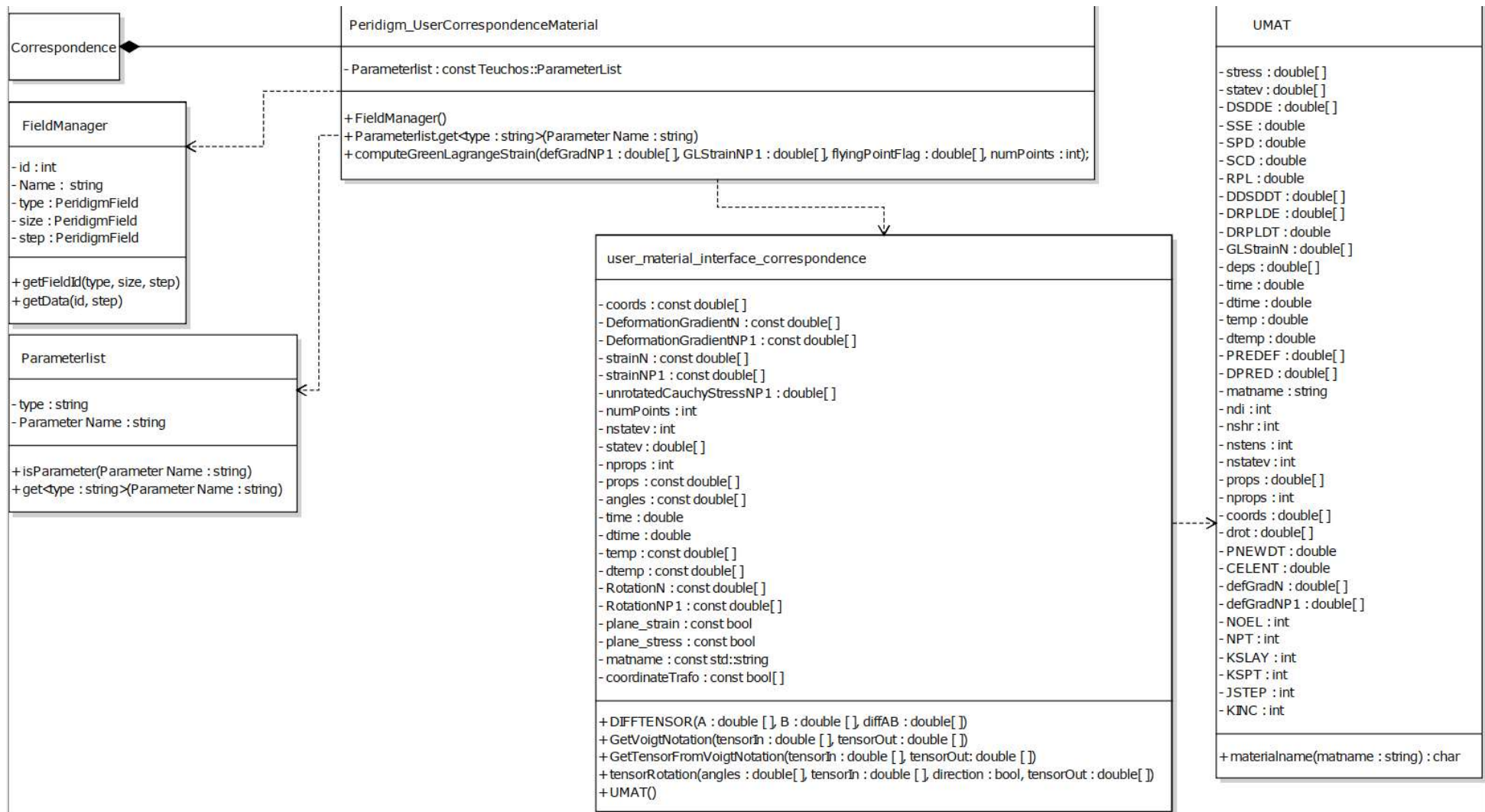
<https://github.com/PeriDoX/PeriDoX>

Doi: 10.5281/zenodo.1403015



Knowledge for Tomorrow

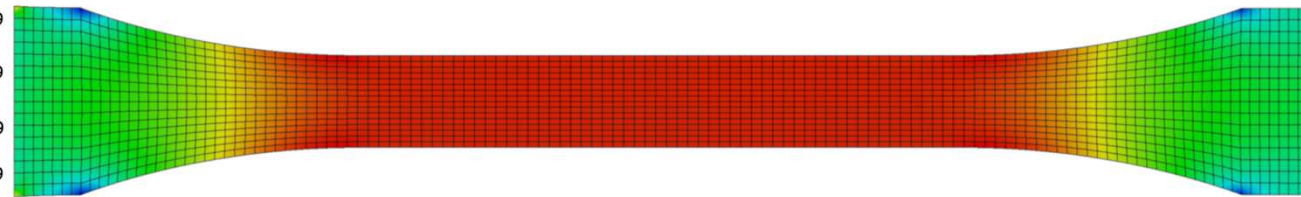
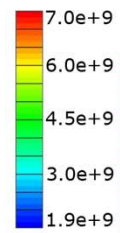




Verification

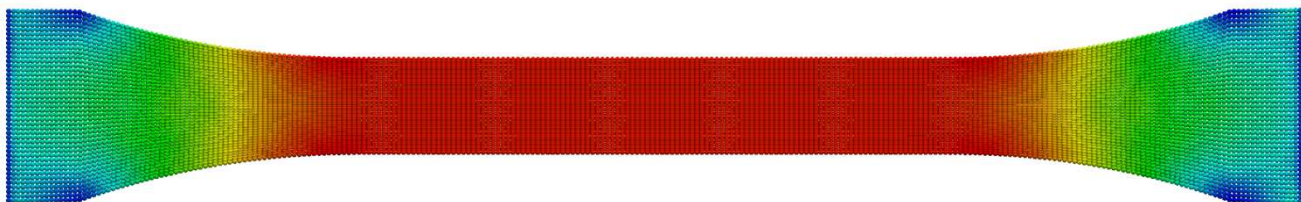
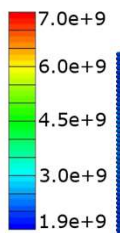
Abaqus

Partial StressX X

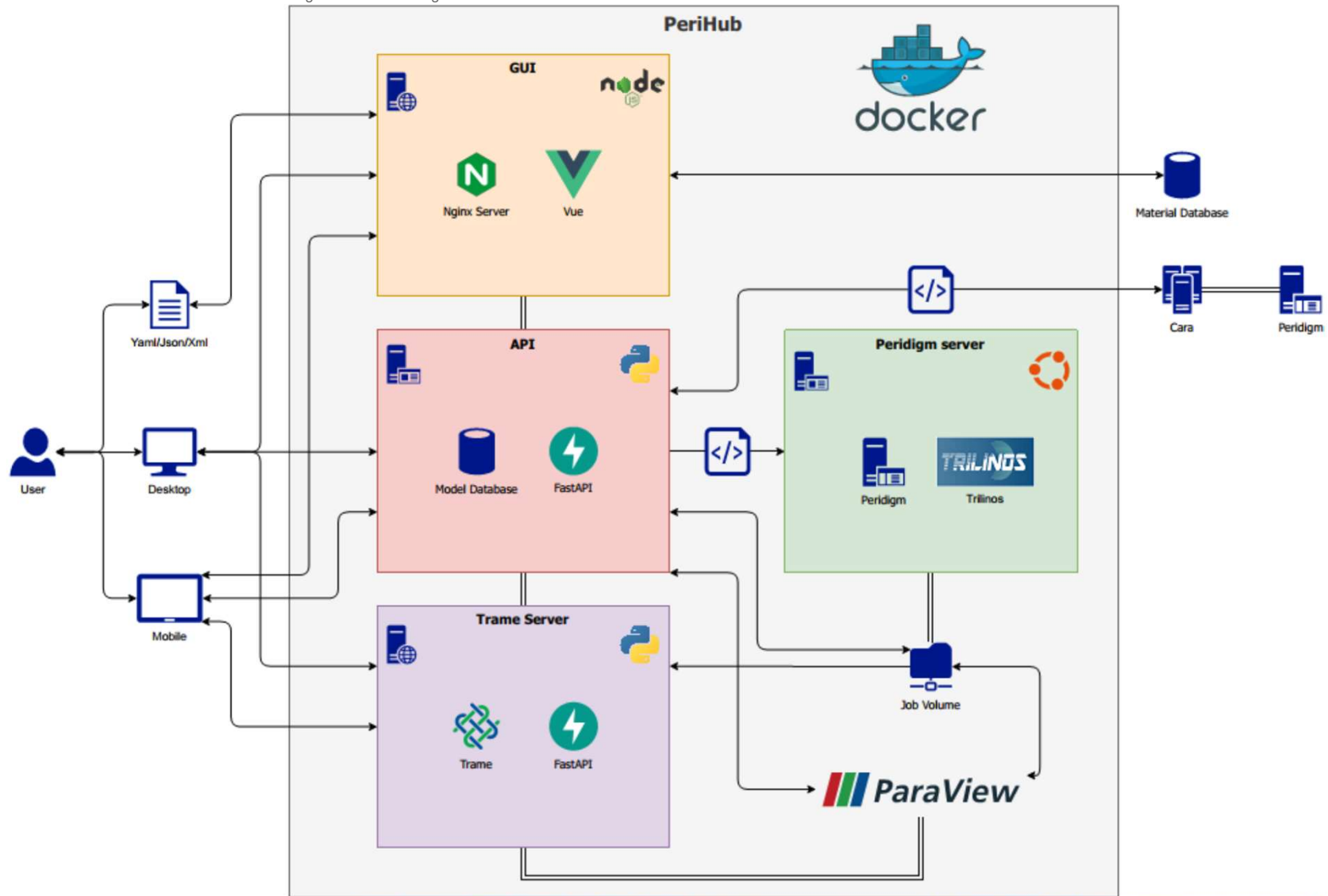


Peridigm

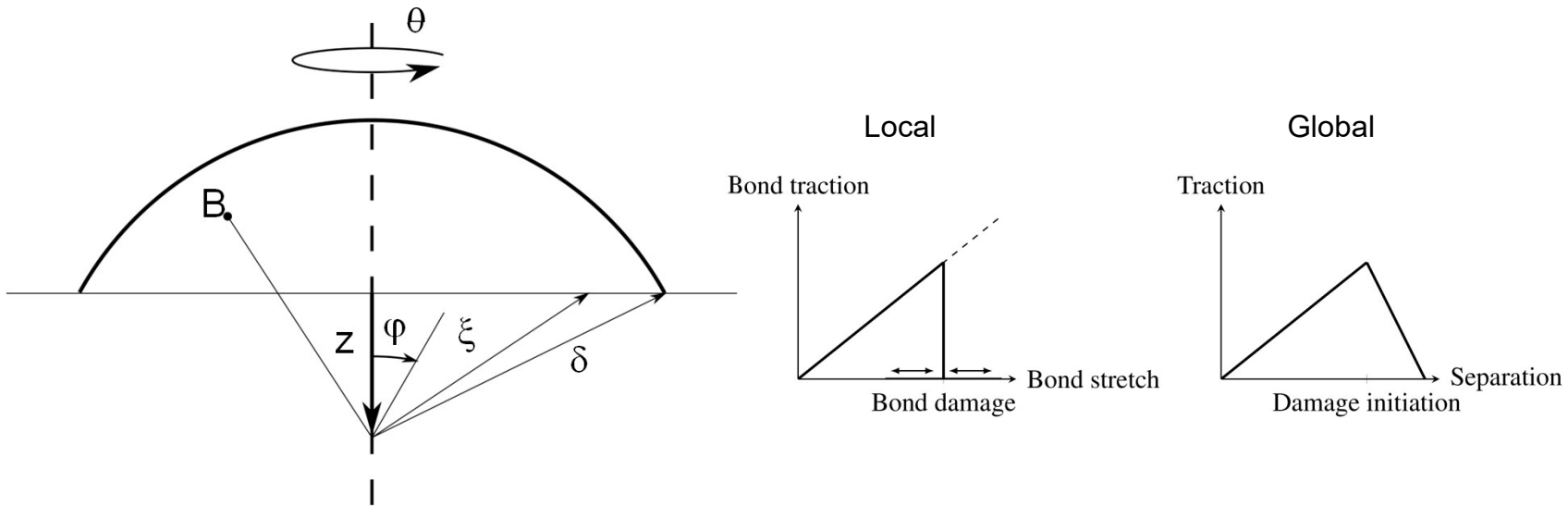
Partial StressX X



Usability



Modeling



$$G = 2 \int_0^\delta \int_{H_r} w_c dV_\xi \quad G = \int_0^\delta \int_0^{2\pi} \int_z^\delta \int_0^{\cos^{-1} z/\xi} w_c \xi^2 \sin \varphi d\varphi d\xi d\theta dz \quad w_c = \frac{4G}{\pi\delta^4}$$



