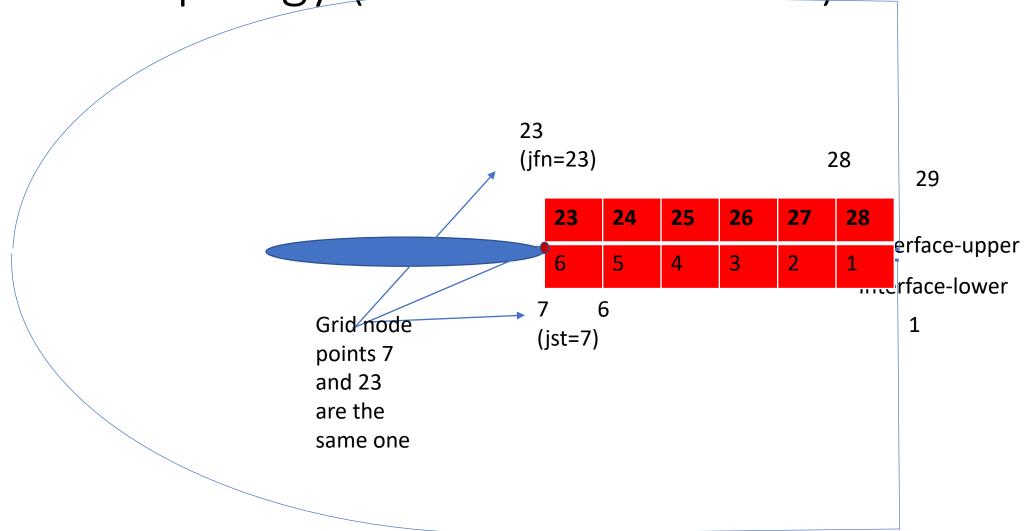


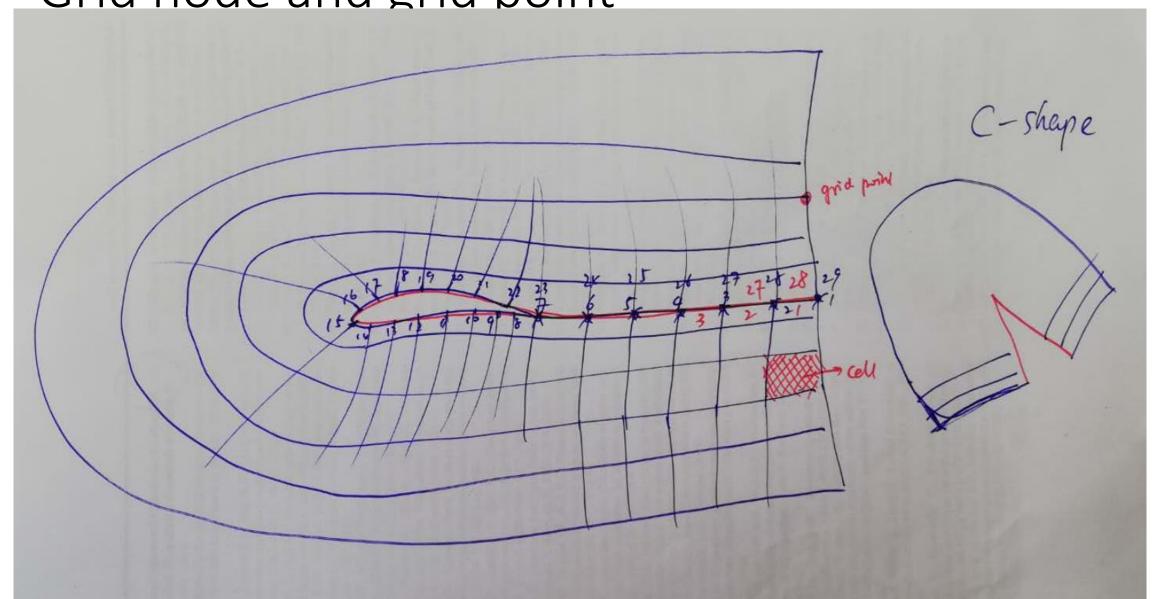
Instruction

Liwei Chen 2023-02-10

Grid Topology (indices start from 1)



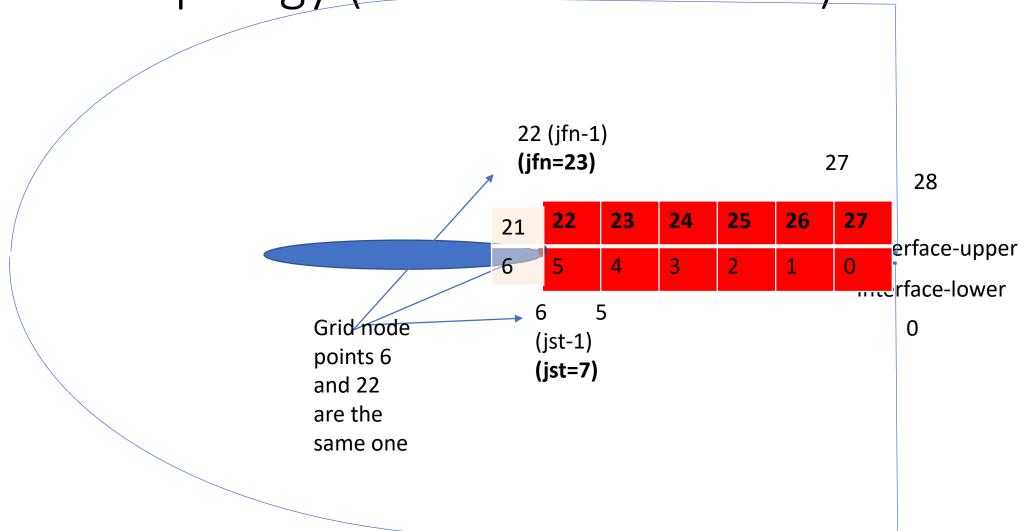
Grid node and grid point



Some notes

- Grid node file is under the folder: train_mesh_point (129 x 129 grid points)
- Grid cell file in the folder: train_mesh (128 x 128 cells)
- All the flowfield variables are defined on grid cell: 128 x 128. Files are under the folder "train"
- At the moment, I only provide you three airfoils

Grid Topology (indices start from 0)

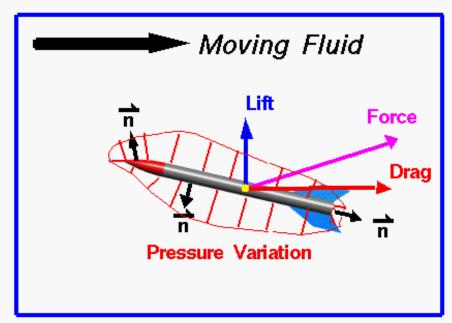


How to calculate Force-X and Force-Y



Aerodynamic Forces





Pressure forces act normal (perpendicular) to surface. Force on the body is the vector sum of the pressure x area around the entire solid body.

$$\vec{F} = \sum_{\text{surface}} p \vec{n} A = \oint p \vec{n} dA$$
Lift = F_{normal}
Drag = F_{stream}

Calculate "Cl, Cd" w/ Differentiable Functions

Liwei Chen

2023-02-22

Differentiable Metrics

- Implemented and tested the calculation of Cl and Cd using differentiable functions.
- Here we provide some example codes for the caluclation of metrics using differentiable operators (in pytorch).
- We are currently developing it for complex cases, such as "differentiable solver + NN", learned simulator for unsteady aerodynamics with mesh deformations (we will publish it in the near future).

Example Codes

tfi_torch.py

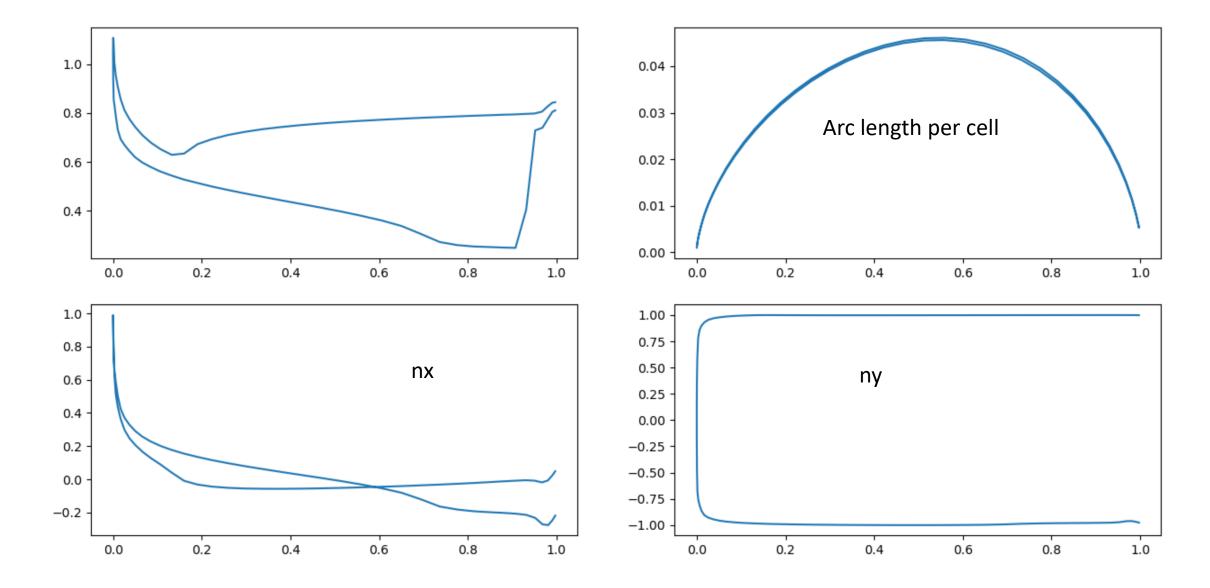
readnpz_and_mesh--Torch.py

global_variables.py

readnpz_and_mesh--Torch.py

```
(base) liwei@PC05:~/Codes/coord-trans-encoding_inv/BASIC_simulations_inv$ python readnpz and mesh--Torch.py
Enter the file name: ah63k127 80 125 1000.npz
ah63k127
0.8 1.25 1.0
Successfully read grid file train mesh point/ah63k127.p3d
torch.Size([1, 1, 128, 129])
jst-2 tensor(0.0053, device='cuda:0')
jfn-1 tensor(0.0053, device='cuda:0')
wake lower jfn - 1 tensor(3.5774, device='cuda:0')
wake upper jfn - 2 tensor(3.5774, device='cuda:0')
jst-1 tensor(0.0053, device='cuda:0')
jfn-2 tensor(0.0053, device='cuda:0')
ist-1 1.0 0.0
jfn-1 1.0 0.0
(128, 128) (128, 128)
torch.Size([128, 128])
tensor([0.9476], device='cuda:0') tensor([0.1344], device='cuda:0') tensor([2.0387], device='cuda:0')
```

Cl, Cd from the ref. CFD: 0.9476330E+00 0.1343771E+00



```
#imax, jmax, kmax, xc, yc, threed = read_grid("train_mesh/"+basename+".p3d")
_, _, _, xp, yp, threed = read_grid("train_mesh_point/"+basename+".p3d")
xc, yc = convert_center(xp, yp)
x_current, y_current = torch.from_numpy(xp).cuda(), torch.from_numpy(yp).cuda()
x_current = x_current.view(batch_size,1,idim,jdim).type(torch.cuda.DoubleTensor)
y_current = y_current.view(batch_size,1,idim,jdim).type(torch.cuda.DoubleTensor)
 now calculate the coordinate transformation metrics according to the paper Comput and Fluids
 ideally this should be done with "cell-point-type" grid files.
#dx_i, dy_i, ds_i, dx_j, dy_j, ds_j, area = calcMetrics(xp, yp)
dx_i, dy_i, ds_i, dx_j, dy_j, ds_j = calculateMetrics(x_current, y_current)
#pressure_center = calculateCellCenter(dynamics[:,istep,3], x_current, y_current)
# dx i: the x-component of the unit normal-wise vector of i-face
# dy_i: the y-component of the unit normal-wise vector of i-face
# ds i: the arc length of the cell along-i (circumferential)
# note: the face norm vec of i-face points into the airfoil (into the object)
# dx j: the x-component of the unit normal-wise vector of j-face
# dy j: the y-component of the unit normal-wise vector of j-face
ds j: the arc length of the cell along-j (normal)
note: the face norm vec of j-face points clock-wise direction
x, y = xc, yc
# data[0] - xmach # in our current case,
 data[1] - aoa # these three numbers are the
 data[3] - rho ... density
 data[4] - rho*u ... density times X-velocity
 data[5] - rho*v ... density times Y-velocity
 data[6] - rho*E ... density times total energy (it is complex, but below you will see how I calculate pressure)
rint(ds_i.shape)
```



- readnpz_and_mesh--Torch.py
- global_variables.py

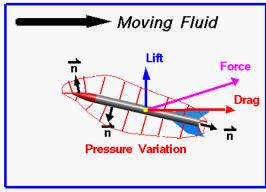
```
def calculateMetrics(x, y):
      bs = x.shape[0]
      kernel_i = torch.Tensor( [[-1.0], [1.0]]).cuda().type(torch.cuda.DoubleTensor) # 2x1
kernel_j = torch.Tensor( [[-1.0, 1.0]] ).cuda().type(torch.cuda.DoubleTensor) # 1x2
kernel_i = kernel_i.vtew((1,1,2,1))
      kernel_j = kernel_j.view((1,1,1,2))
# the first dim: # of input channels
       # the second dim: # of output channels
       # the thrid and fourth dims: kernel size
       # calculate tangential direction
      ti1 = F.conv2d(x, kernel_i, padding=0) # dx/di (or dx/dxi)
ti2 = F.conv2d(y, kernel_i, padding=0) # dy/di (or dy/dxi)
       #print(ti1.shape, ti2.shape)
       ds_i = ((ti1)**2 + (ti2)**2)**0.5
       ## normalize
      #dx i = torch.div(ti1, ds i)
       # rotate -90deg to get normal, i.e. *(0 - 1*j)
       #dx i = torch.div(-ti2, ds i)
       #dy i = torch.div( ti1, ds i)
      dx_i = ti2/ds_i
       dy_i = -ti1/ds_i
       #print(dx_i.shape, dy_i.shape)
      tj1 = F.conv2d(x, kernel_j, padding=0)
tj2 = F.conv2d(y, kernel_j, padding=0)
       ds_j = ((tj1)**2 + (tj2)**2)**0.5
       ## normalize
       #dy_j = torch.div(tj2, ds_j)
       # rotate -90deg to get normal, i.e. *(0 - 1*j)
       #dx_j = torch.div( tj2, ds_j)
      #dy_j = torch.div(-tj1, ds_j)
dx_j = tj2/ds_j
       dy_j = -tj1/ds_j
```

How to calculate Force-X and Force-Y



Aerodynamic Forces





Pressure forces act normal (perpendicular) to surface.

Force on the body is the vector sum of the pressure x area around the entire solid body.

$$\vec{F} = \sum_{\text{surface}} \vec{p} \cdot \vec{n} \cdot A = \oint \vec{p} \cdot \vec{n} \cdot dA$$
Lift = F_{normal}
Drag = F_{strean}

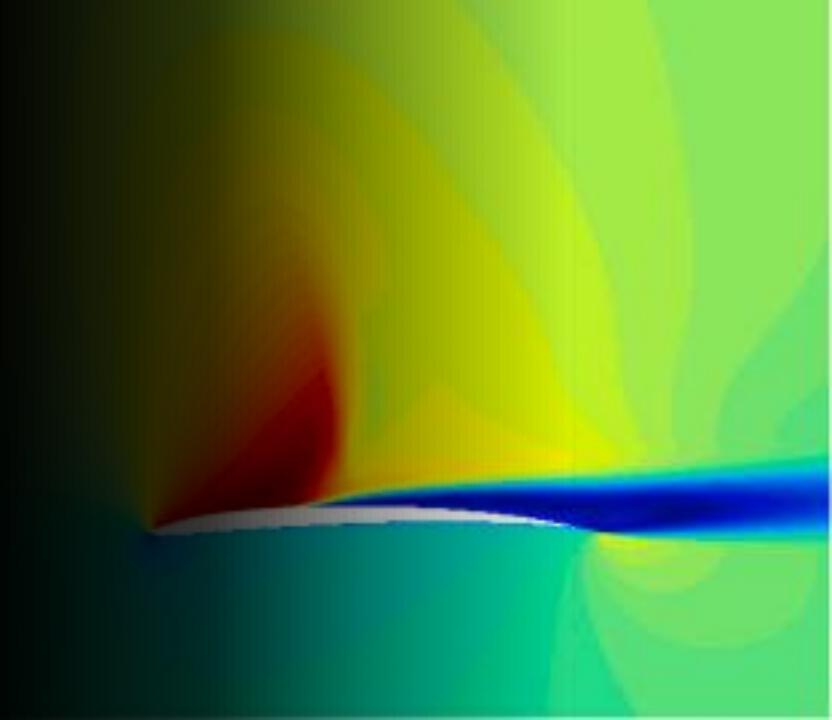
Project fx, fy onto the fluid-moving direction, so we need angle of attack.

```
294 angle_of_attack = 1.25 #degree
295 angle_of_attack = angle_of_attack / 180. * np.pi
296 cosDir = np.cos(angle_of_attack)
297 sinDir = np.sin(angle of attack)
300 pressure center = torch.from numpy(p).cuda().type(torch.cuda.DoubleTensor)
301 #pressure_farfield_boundary = torch.from_numpy(p[:,-1]).cuda().type(torch.cuda.DoubleTensor)
302 #pressure farfield boundary = pressure farfield boundary.view(imax,1)
303 #print(pressure farfield boundary.shape)
 04 #pressure_center = torch.cat((pressure_center, pressure_farfield_boundary), dim=1) # just make sure it has the same shape as ds and dx
 05 print(pressure_center.shape)
 07 xc_cuda = torch.from_numpy(xc).cuda().type(torch.cuda.DoubleTensor)
 08 #yc_cuda = torch.from_numpy(yc).cuda().type(torch.cuda.DoubleTensor)
 09 pressure_surface = torch.masked_select( pressure_center, cellcenterMask ).view(1,-1)
 10 xc surface
                    = torch.masked_select( xc_cuda,
                                                             cellcenterMask ).view(1,-1)
311 arcLength_surface = torch.masked_select( ds_i,
                                                             segmentMask ).view(1,-1)
312 nx surface = torch.masked select( dx i,
                                                      segmentMask ).view(1,-1)
313 ny surface = torch.masked select( dy i,
                                                      segmentMask ).view(1,-1)
315 #print("inner_x:", inner_x.shape) # inner_x: torch.Size([5, 1, 256, 129])
316 #print("segmentMask:", segmentMask.shape) # segmentMask: torch.Size([5, 256, 129])
317 #print("mode_1a:",mode_1a.shape)
318 #print("test mask:",torch.masked_select(inner_x,segmentMask).view(batch_size,-1).shape)
                   torch.sum( torch.masked_select(inner_x,segmentMask).view(batch_size,-1), dim=1 ) #*mode_1a
319 #f pred 1 =
                  torch.sum( torch.masked select(inner y,segmentMask).view(batch size,-1), dim=1 ) #*mode 2a
 21 #print(f pred 1, f pred 2)
323 #plt.figure()
324 fig, axs = plt.subplots(2, 2)
325 axs[0,0].plot(xc_surface[0].cpu().detach().numpy(), pressure_surface[0].cpu().detach().numpy())
326 axs[0,1].plot(xc_surface[0].cpu().detach().numpy(), arcLength_surface[0].cpu().detach().numpy())
327 axs[1,0].plot(xc_surface[0].cpu().detach().numpy(), nx_surface[0].cpu().detach().numpy())
328 axs[1,1].plot(xc_surface[0].cpu().detach().numpy(), ny_surface[0].cpu().detach().numpy())
329 plt.show()
333 dfx = (1.4*pressure surface-1)*arcLength surface*nx surface/(0.5*0.8**2*1.4)
334 dfy = (1.4*pressure surface-1)*arcLength surface*ny surface/(0.5*0.8**2*1.4)
            torch.sum( dfx, dim=1 )
            torch.sum( dfy, dim=1 )
 38 # for sanity check, calculate the wet surface, theoretically it should 2.0
 39 wet_surface = torch.sum( arcLength_surface, dim=1 )
 41 Cd = fx*cosDir + fy*sinDir
 42 Cl =-fx*sinDir + fy*cosDir
 #5 print(Cl, Cd, wet surface)
```

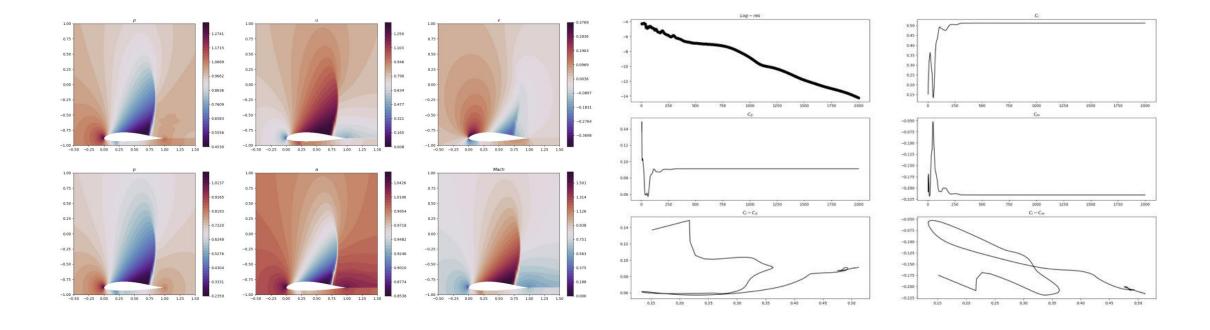
In Progress: Surrogate Model

 https://github.com/tumpbs/coord-trans-encoding

• Now we directly calculate metrics information by python script. No need Fortran solver anymore.

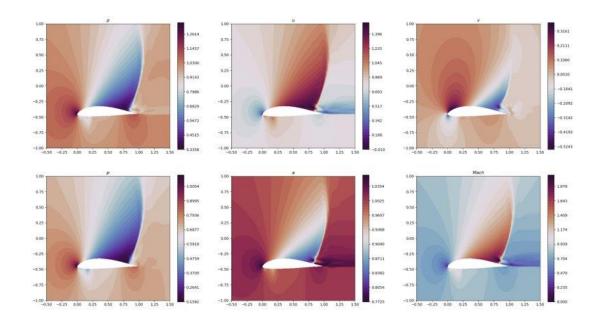


0.283, 0.087, -0.062



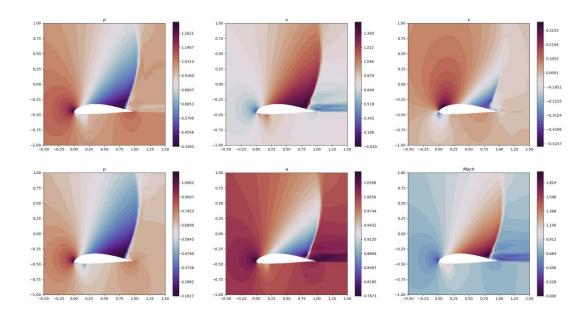
Cl =0.5123548E+00 Cd=0.9131187E-01 Cm=-0.2159179E+00

0.639, 0.043, -0.127



Cl = 0.8308828E+00 Cd = 0.1734693E+00 Cm = -0.3984813E+00

0.692, 0.162, -0.283



Cl = 0.8255088E+00 Cd = 0.1721221E+00 Cm = -0.3907791E+00

