

What this is not about

• The usual game and graphics programming math (e.g., linear algebra, transform matrices, quaternions, ballistics, physics simulation...)

Today's goal: Get to know Colab/Jupyter notebooks for game simulations and analytics

- Jupyter notebooks are an easy to use browser-based Python programming environment. Colab is Google's Jupyter service with some UI improvements.
- Python and the Numpy & Scipy packages are perhaps the most popular data science and analytics tools
- No need to install anything, the notebooks can be run on Google's Colab cloud service
- Alternative: Excel / Google sheets. However, many tasks are easier in Python, and Python notebooks are increasingly replacing spreadsheets
- Materials here: https://github.com/PerttuHamalainen/GameAnalysis



Dynamics, again



- Competition is fierce. 1000+ new apps every day.
- Game developers must think statistically and optimize their chances to monetize and stay alive
- Think of chains of random events, e.g., the acquisition and monetization funnel (the *P* denotes probability):

```
P(\text{revenue}) = P(\text{ad eyeballs AND install AND engage AND pay})
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(Simplification, see slide notes)

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\approx P(\text{eyeballs}) P(\text{install}) P(\text{engage}) P(\text{pay})
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At every step of the funnel, you lose a portion of players. For example, optimizing App Store screenshots and icon affects p(install). If you achieve a 10% increase in retention at every step, above, total number of paying customers increases by 46%.



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$$P(revenue) = P(eyeballs) * P(install) * P(engage) * P(pay)$$
 (Simplified, see slide notes)

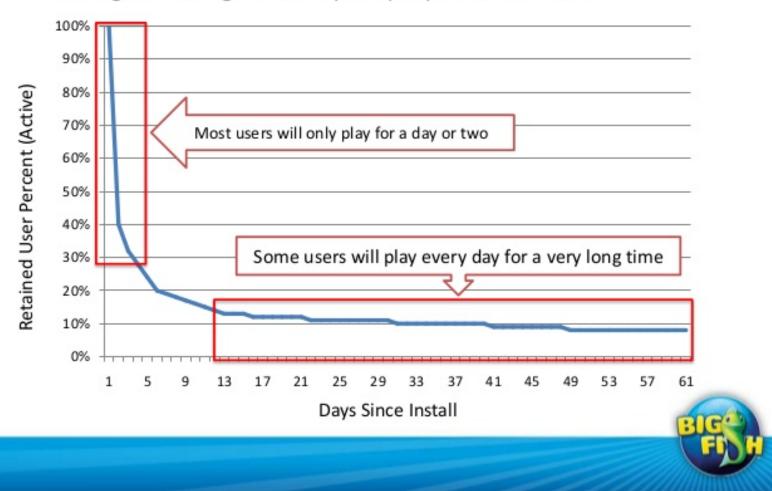
• Total probability is low if even one factor is low. At every step, you lose a portion of players. For example, optimizing App Store screenshots and icon affects p(install). If you achieve a 10% increase in retention at every step, above, total number of paying customers increases by 46%.

Key concept: The power of recursion

- Due to recursive relationships (feedback connections), small changes in attributes (e.g. retention) can have huge impacts (e.g., on long-term revenue)
- Recursion leads to exponential behavior (decay or growth, forms of emergent dynamics)



F2P Retention





Exponential decay: $u(t+1)=u(t) - p_{churn} u(t)$

Notation:

u(t) Number of players at time t

p_{churn} Probability of player quitting (percentage of churned players divided by 100)

F2P Retention





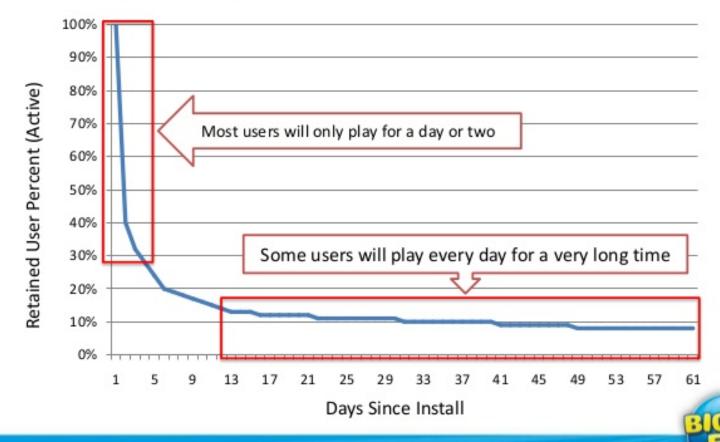
Exponential decay: $u(t+1)=u(t) - p_{churn} u(t)$

Alternatively:

$$u(t+1)=p_{retention} u(t)$$
,

$$p_{retention} = 1 - p_{churn}$$

F2P Retention





Exponential decay: $u(t+1)=u(t) - p_{churn} u(t)$

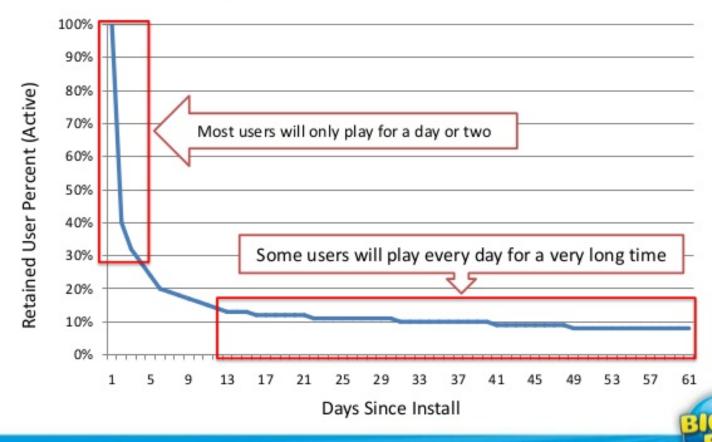
Alternatively:

$$u(t+1)=p_{retention} u(t)$$
,

$$p_{retention} = 1 - p_{churn}$$

Nonlinear because the number of players depends on itself recursively and *multiplicatively,* instead of, say, u(t+1)=u(t)-1

F2P Retention





Exponential decay model's accuracy?

- In real games, churn is often higher for the first day
- Bad tutorial/onboarding can easily make you lose most of your players
- On the other hand, the more time one has already invested in a game, the more committed one might be to continue, provided that the game provides meaningful progress
- If you use this kind of model for making predictions based on your initial player data, measure the churn rate over multiple days, maybe without taking the first few days into account.



Retention outside free-to-play

F2P player churn is dramatic: With zero initial investment, players can easily switch to another game.

Data from paid games can be quite different.

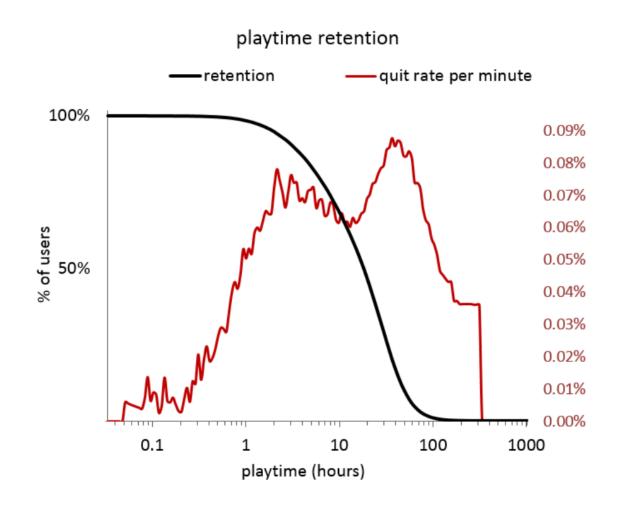


Fig. 4. Far Cry 4 retention in black and quit rate in red.

https://hal.archives-ouvertes.fr/hal-02436692/document

Notable churn/retention research

- Viljanen, Markus, et al. "Modelling user retention in mobile games." 2016 IEEE Conference on Computational Intelligence and Games (CIG). IEEE, 2016.
- Allart, Thibault, et al. "Design influence on player retention: A method based on time varying survival analysis." 2016 IEEE Conference on Computational Intelligence and Games (CIG). IEEE, 2016.
- Periáñez, África, et al. "Churn prediction in mobile social games: Towards a complete assessment using survival ensembles." 2016 IEEE International Conference on Data Science and Advanced Analytics (DSAA). IEEE, 2016.
- Demediuk, Simon, et al. "Player retention in league of legends: a study using survival analysis." *Proceedings of the Australasian Computer Science Week Multiconference*. 2018.
- Roohi, Shaghayegh, et al. "Predicting Game Difficulty and Churn Without Players." *Proceedings of the Annual Symposium on Computer-Human Interaction in Play.* 2020.



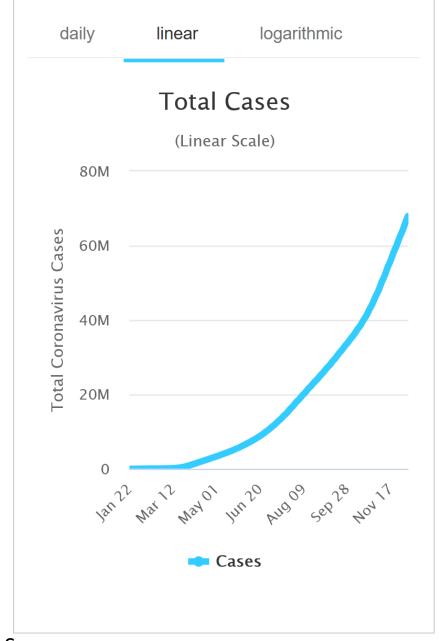
Exponential (viral) growth

- Every coronavirus case infects a number of new cases
- Organic growth of games: Portion of players share on social media or show a game to their friends at school etc.

Equation:

$$u(t+1) = u(t) + vu(t),$$

where v is "virality", i.e., how many new players each player "infects" per day



Source:

https://www.worldometers.info/coronavirus/?

Another source of exponential growth in games as a service

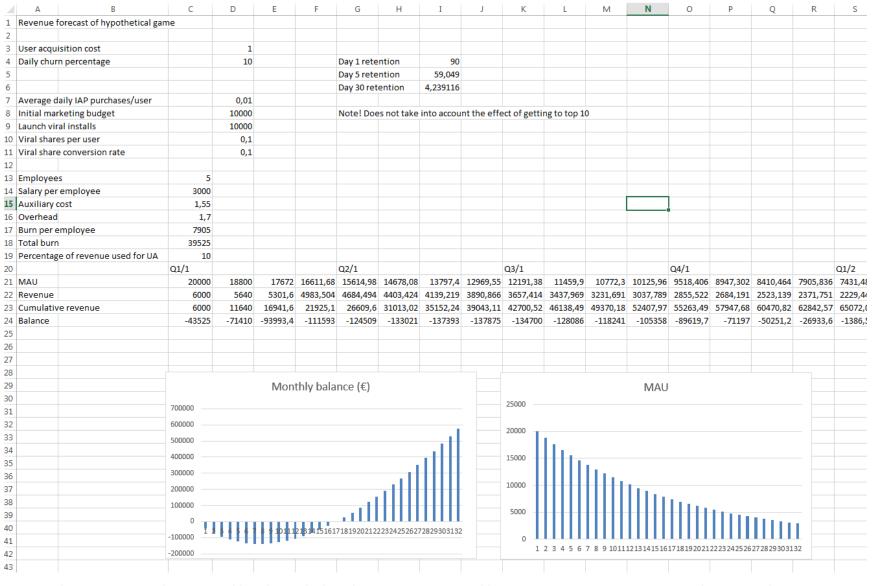
- Achieving high virality is hard.
- Combining the following can also produce exponential growth:
 - 1. Achive good retention and monetization: At least some players keep playing for a long time and provide a steady revenue stream (e.g., season passes)
 - 2. Invest a portion of the revenue in acquiring new players



Why does the math matter?

- You can measure parameters like p_{churn} from your player data
- Using the parameters, you can make predictions about your playerbase and company cashflow
- Soft launch: A business practice where you launch the game on a limited market to measure, make predictions, and iterate so that your parameters improve.
- Successful soft launch: Your data and predictions indicate good ROI (Return On Investment) for global launch (marketing, servers, support staff...)

Exercise: Cashflow prediction



Tweak the values in the cells highlighted in yellow. Try to complete the exercises at the bottom of the sheet.

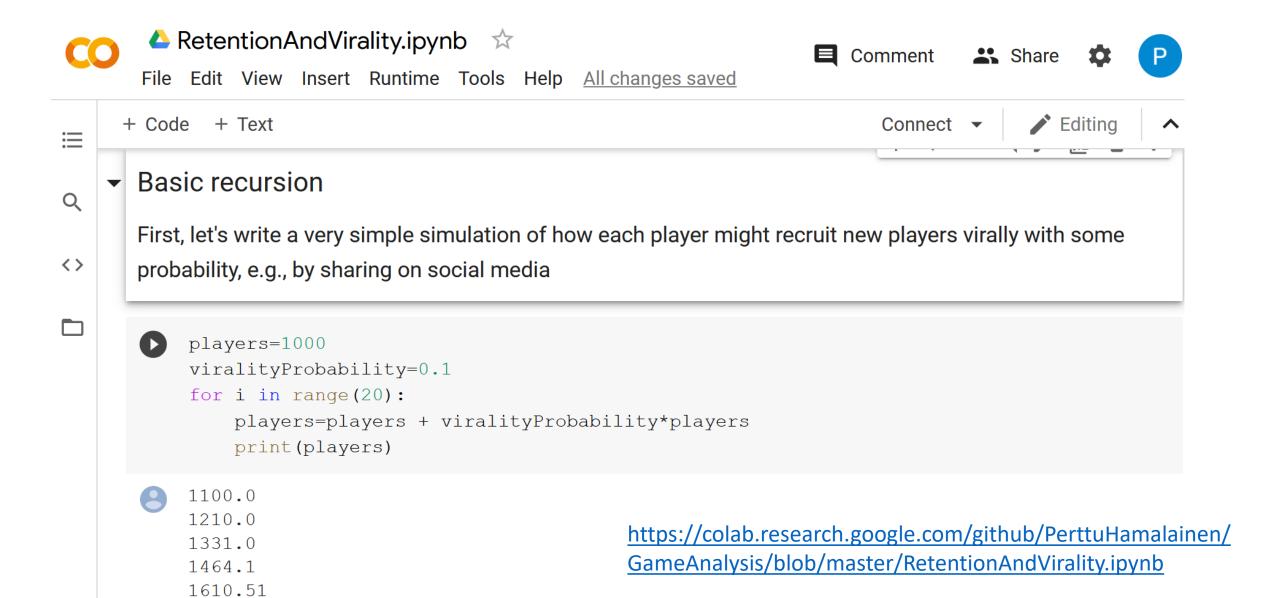
Spreadsheets vs. Python notebooks

- Spreadsheet formulas be very hard to understand for someone who didn't create it. Python code uses human-readable variable names.
- Simple things might be easier in Excel, but Python scales better to complex simulations

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Α	В	C	D E
MAU		20000	emiai sti
Revenue		30000	
UA spend		21000	
UA new use	ers	21000	
Cumulative revenue		30000	
Cumulative burn		46575	
Balance		-16575	



Same in Python



This is the first Python simulation in the RetentionAndVirality notebook. Let's investigate it to learn Python syntax, assuming that you're only familiar with Unity C#...

```
#Simulation parameters
#You can choose these as you like.
players=1000
virality=0.1
#Simulation loop
for i in range (20):
    players=players + virality*players
    print(players)
```

means that the rest of the line is comments that explain the code. The computer running the code ignores these.

```
#Simulation parameters
#You can choose these as you like.
players=1000
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#Simulation loop
for i in range (20):
    players=players + virality*players
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```

This introduces a variable called "players" and sets its value to 1000. Python does not need type specifiers like C#'s "int players=1000"

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```

In Python, you don't need to add the ";" at the end of a line.

```
#Simulation parameters
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players=1000
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for i in range (20):
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```

This declares a loop: All code inside the loop is run for 20 times. In C#, this would be "for (int i=0; i<20; i++)"

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For loop declaration ends with ":"

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Everything after the ":" that is intended belongs inside the loop. In C#, the loop contents would be inside curly brackets.

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This assigns the variable "players" a new value based on its old value and the virality parameter. Mathematical expressions follow standard rules: Multiplication is executed before addition.

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The print function prints things into the Colab output. In Python, print usually works no matter the variable type.

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Combining spreadsheets and Python/Colab

- Many data scientists do some quick visualization and manipulation of data in Excel
- More detailed analyses in Python or R.
- The Pandas Python package allows one to load, manipulate, and save spreadsheets (we use this in the Clash Royale notebook)
- Python can also directly manipulate Google Sheets using the Google Sheets API:

https://developers.google.com/sheets/api/quickstart/python



Rest of today: Work on the Colab notebook

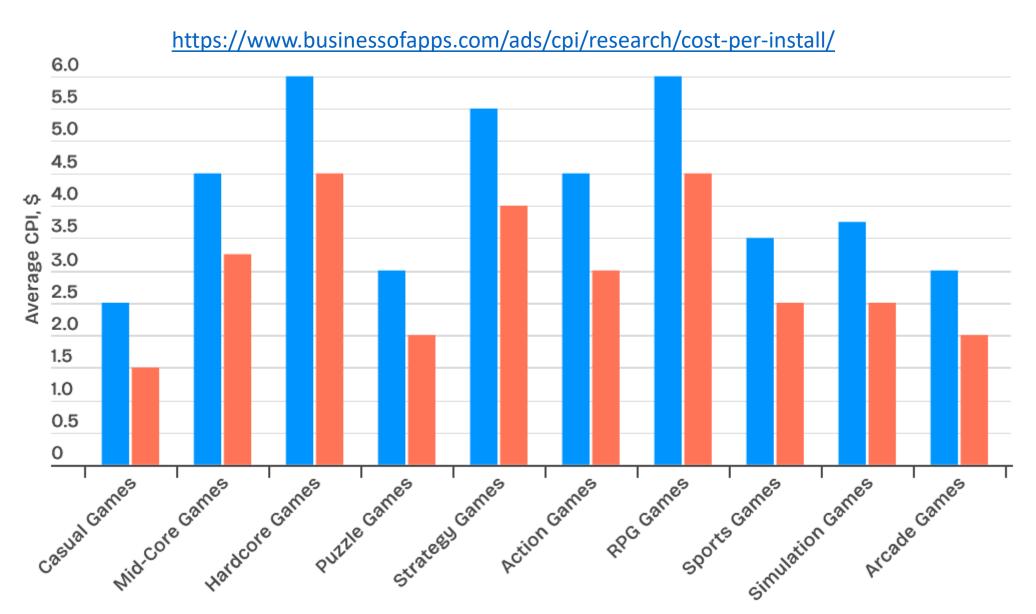
- Everyone goes through the virality and retention Colab in their own pace.
- Go for a break when you feel like it
- If you complete the notebook, you can already proceed to the Clash royale balancing one
- Note: Kaggle is another notebook service that currently provides more free compute than Colab (including high-memory GPU:s for Al training), but this course's notebooks haven't been tested in the Kaggle environment.

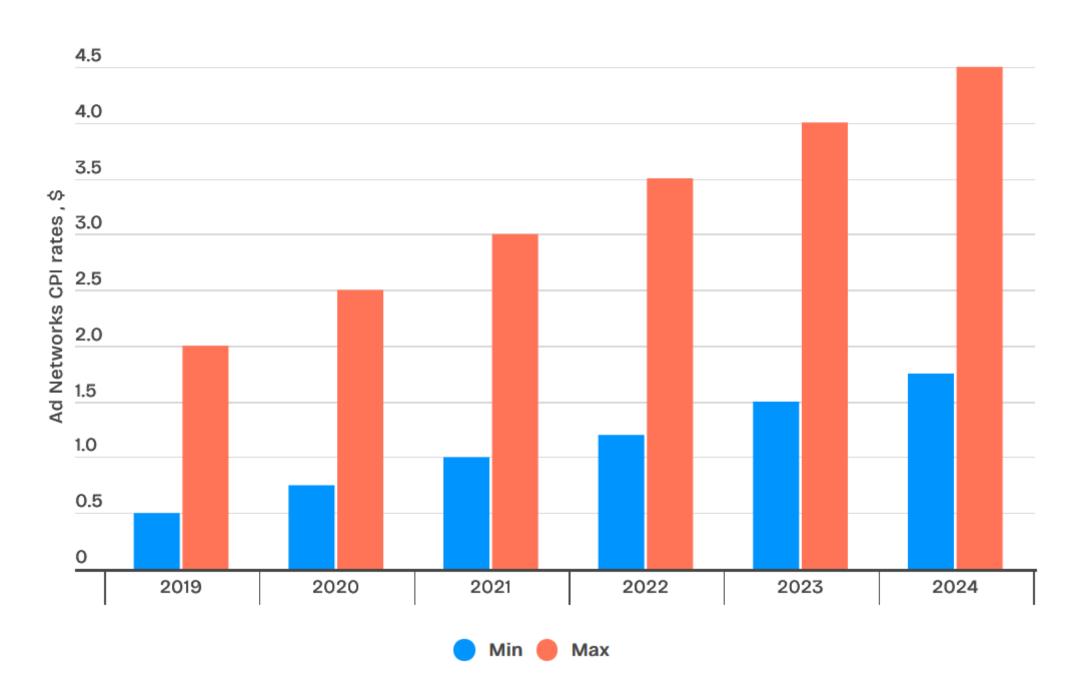
Lesson learned: To make it with a small initial budget, one needs to...

- Minimize burn
- Invest revenue in user acquisition
- Maximize odds of virality and free exposure => create something that's both unique and can be communicated in a social media GIF or video
- For example: Is your game unique and innovative enough to, e.g., get to GDC Experimental Gameplay Workshop or shortlisted for Independent Games Festival? Check the games featured there in previous years.



Cost per install (CPI, user acquisition cost)

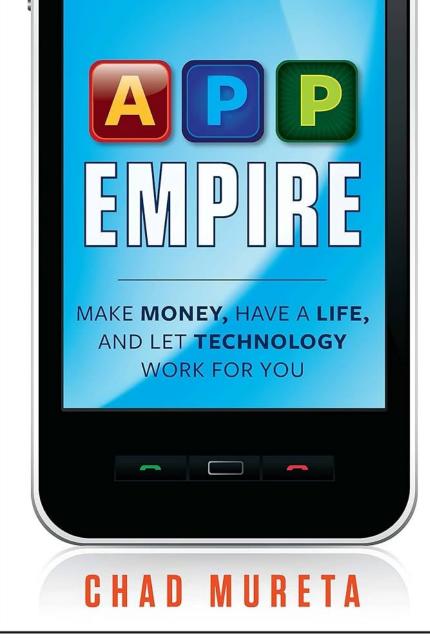






Hypercasual games

- Highly viral: low user acquisition cost and strong organic growth
- Virality is unpredictable, but as Voodoo has shown, one can mitigate this by stealing ideas that others have tested to work.
- Low production cost and short production cycle: Can launch multiple games
- An "app empire" of multiple games provides an ad network that can feed players to new games, further lowering the user acquisition cost

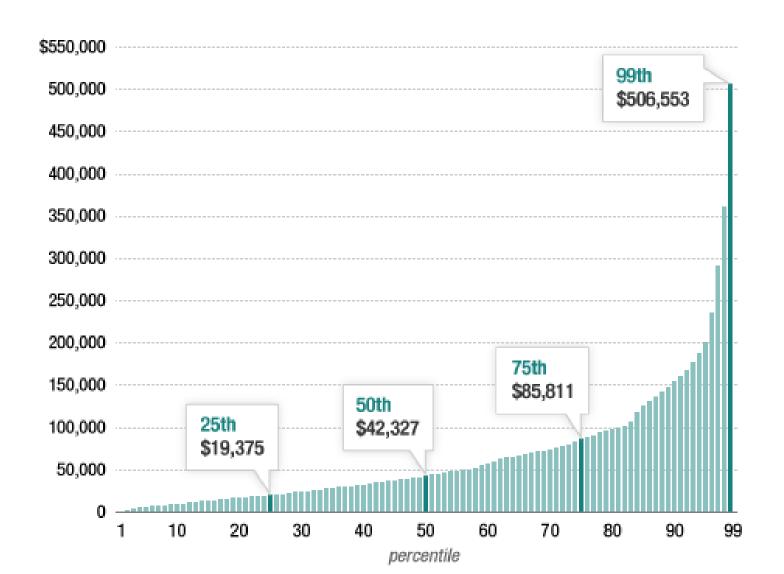


https://www.amazon.com/App-Empire-Make-Money-Technology/dp/111810787X

More on "power law" relations

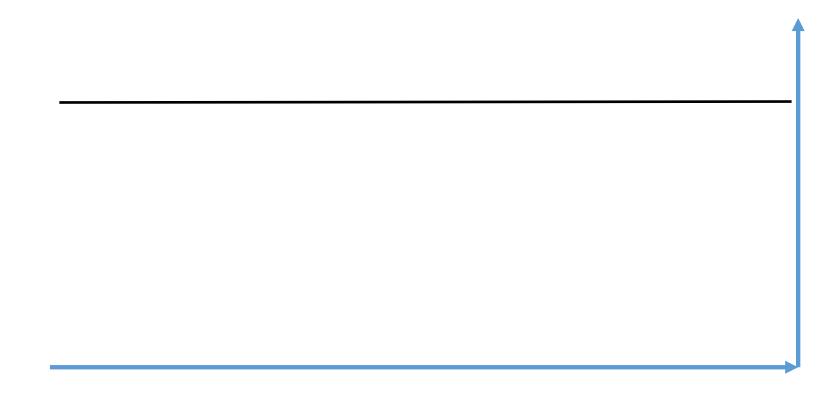


Income distribution looks like a power law. Is there a recursion?

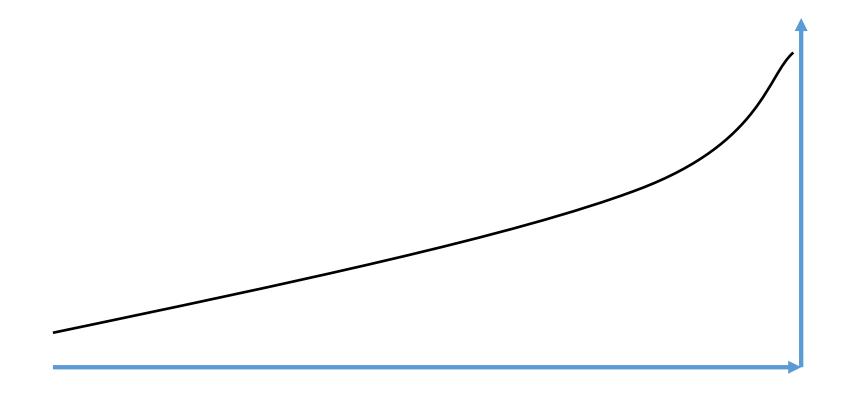




Distribution of wealth through recursion in Monopoly (game start)



Distribution of wealth through recursion in Monopoly (game progresses)



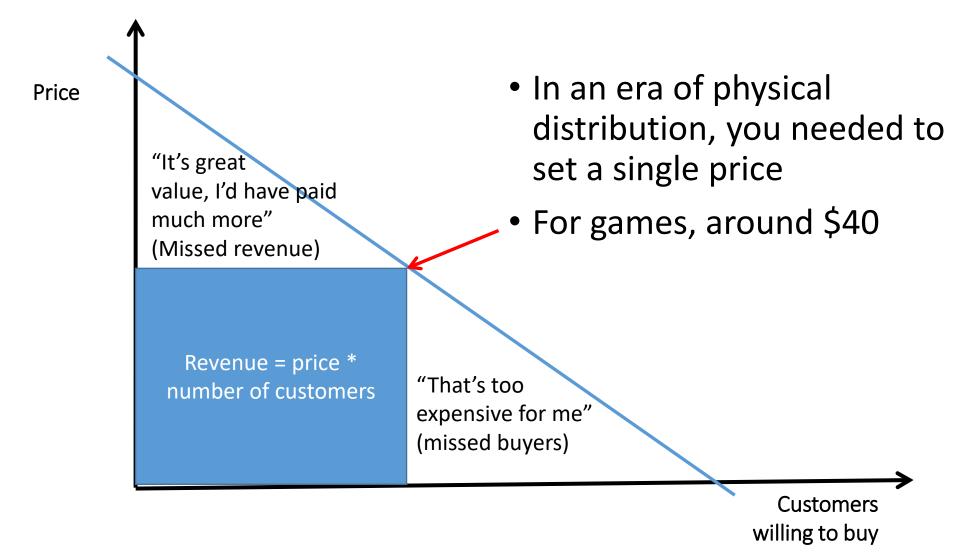


Distribution of wealth through recursion in Monopoly (game progresses)

The connection to game monetization



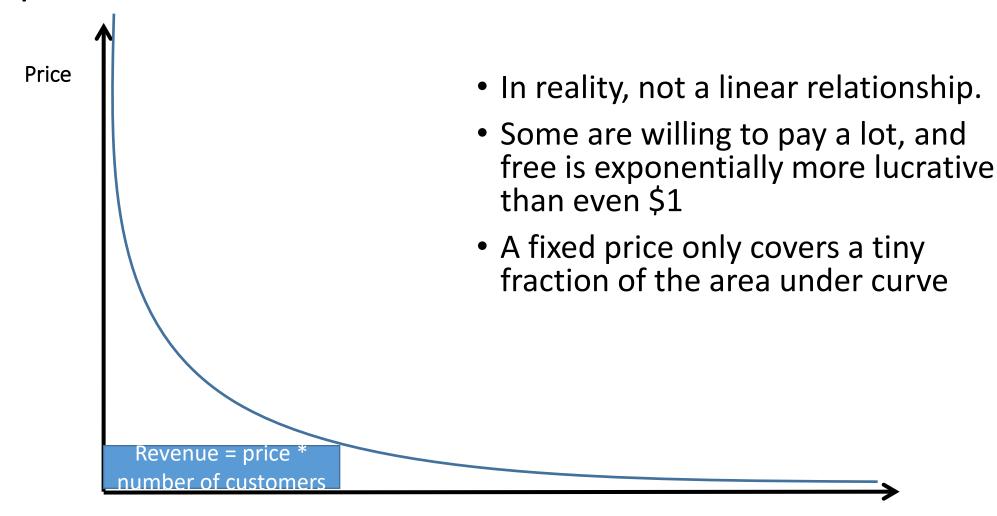
The price/demand curve



http://www.slideshare.net/nicholaslovell/whales-power-laws-and-the-future-of-media



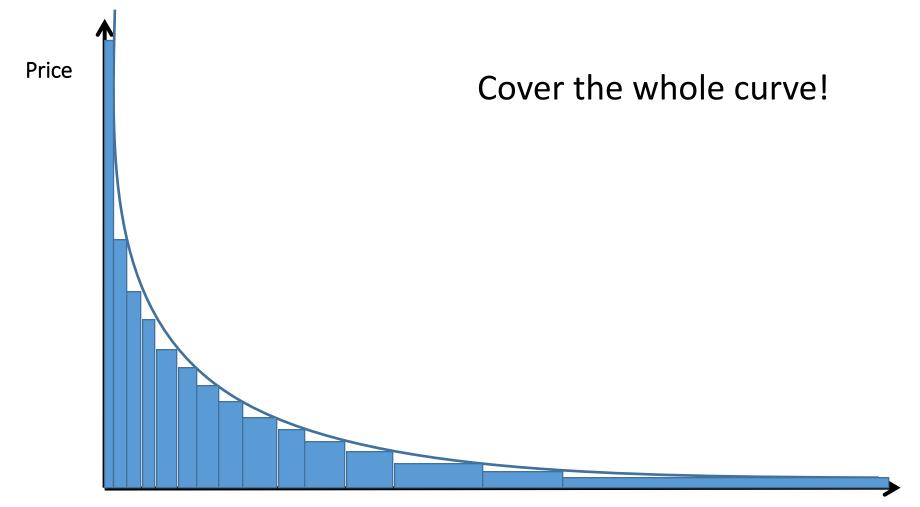
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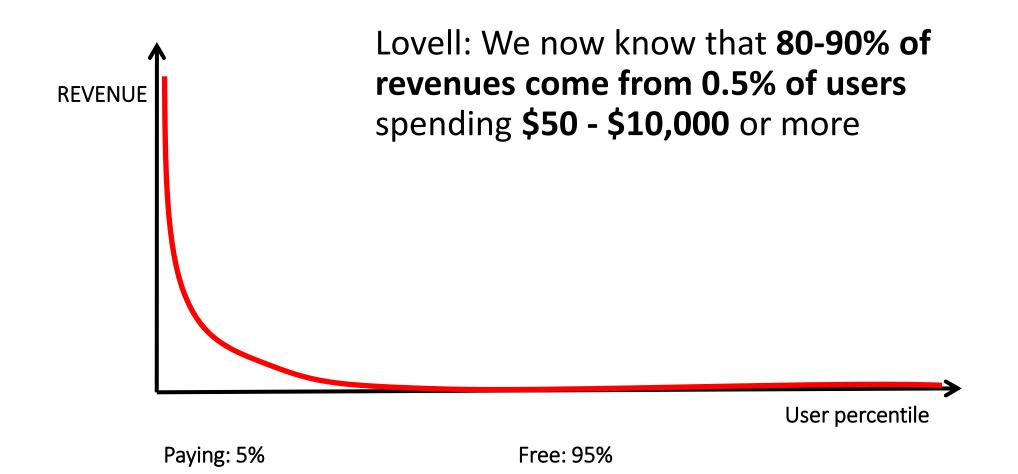
Customers willing to buy



F2P: Allowing users to choose how much to pay



F2P: Allowing users to choose how little to pay



Huge differences in players is not news

- 90% of gamers don't finish a game
- Only <10% of purchasers participate in online discussion forums



Other explanation: addiction

- Free-to-play games utilize principles that lead to gambling addiction with some people (more of that in upcoming weeks)
- Combining ethics and economics: Limit player spending, just don't set the limit too low.

Summary

- Power laws and exponential growth or decay caused by recursion are common in game economics
- Tipping points: sometimes small changes have huge effects, e.g., change behavior from exponential decay to exponential growth
- Retention, virality (organic growth), and investing revenue for continuous user acquisition are crucial