MStack Documentation

Release 0.1

Peter C Metz

Contents

Peter C. Metz*

Inamori School of Engineering, Alfred University, 2 Pine St., Alfred, NY 14802

*Contact: pcm1@alfred.edu | (315) 350 1585

Contents 1

2 Contents

CHAPTER 1

Abstract:

In order to refine stacking disorder models in real and reciprocal space, MSTACK has been written to extend two established profile generators: DIFFaX, a reciprocal space intensity distribution calculator built on a stochastic stacking disorder model description; and DiffPy-CMI, a suite of tools including pair distribution function calculators. MSTACK includes tools to expand the stochastic stacking model parameters typical of DIFFaX into supercell models suitable for calculation of stacking disordered pair distribution function data, and to drive refinement of layer structure models from real and reciprocal space data.

MSTACK has been designed with advanced refinement tools in mind. MSTACK is built on the code lmfit which permits the user to include arbitrary constraint equations enabling parametric refinement. Further, MSTACK is designed to be compatible with any minimizer method in the SciPy package, enabling the application of global minimization techniques. Currently implemented minimization methods include the L-BFGS-B non-linear optimization algorithm and the Differential Evolution algorithm. Finally, lmfit and MSTACK enable the user to apply Markov-Chain Monte Carlo analysis, via the package emcee, to the resulting fit. This Bayesian statistical analysis tool has been used predominantly in the astronomical community to interpret data with substantial noise where the error in the data is uncertain. Application of this tool to PDF data suggests many model parameters are not normally distributed- an insight that is expected to have substantial impact on the future of scattering analysis of nanostructured material.

CHAPTER 2

Contents:

background

Created on Thu Mar 30 14:26:43 2017

Background functions for reciprocal-space refinements

@author: Peter C Metz

mstack.background.inv_x_plus_poly3 (x, a, b, c, d, e) define custom fit function 3rd order polynomial + 1/x term

interface

```
Created on Tue Apr 26 13:54:44 2016

@author: Peter C Metz

class mstack.interface.Interface (phases=None, mno=None, debug=False)

Bases: object

Interface DIFFaX-Py object with DiffPy Structure/Calculator objects

_modules return return self.attribute.update({stuff}) and are accessed from interface.attribute

__init__ (phases=None, mno=None, debug=False)

A collection of tools for retreiving values from Phase object(s) in order to construct diffpy.Structure objects and PDF calculations therefrom.

•Phases: (dict | Structure.phase)

•mno: (int, int, int): i.e. (1, 2, 3) a sequence of three integers for supercell expansion

add (attribute, value)

generic method
```

```
expand_supercell (lattice, atoms, trans, dim, label, debug=False)

Expand first unit cell (lattice + atoms) with the transition vectors in trans and the dimension dim

•lattice: diffpy.Structure.Lattice(a, b, c, alpha, beta, gamma)

•atoms: [diffpy.Stucture.Atom(1), ..., Atom(N)]

•trans: Transition.transition(alpij, rx, ry, rz, cijk)

•dim: intintint (i.e. 123) as dim of supercell

•label: label to be applied to supercell

Returns: diffpy.Structure instance of supercell

is_Uiso (atom)

requires atom as Structure.atom as input returns boolean discriminating ADP type

to_cif()

write supercells to supercell.label.cif in cwd

update_phases (phases)
phase updater

mstack.interface.is_dict(d)
returns boolean TIF if d passes type check
```

pairdistributionfunction

Created on Tue Apr 19 13:20:59 2016

Designed to integrate lmfit/scipy differential evolution, existing structure tools, and diffpy PDF generator for global minimization of complex stacking disorered PDF data.

```
@author: Peter C Metz
mstack.pairdistributionfunction.not_implemented(parameter)
    raise exception if
mstack.pairdistributionfunction.name_check(iteritem)
    check if names in iteritem are unique
mstack.pairdistributionfunction.load(filename, subdir=None)
    load a pickled .dat file Note: if all modules needed by the refinement object are not imported at time of
    unpickling, there will likely be AttributeErrors thrown.
```

~! actually, this is problematic. cPickle serializes class by reference, nor definition, so changinging the namespace (e.g. adding or removing modules to this program) will break the pickle.

upgrade to dill which serializes by definition

pairdistributionfunction.PdfData

```
 \begin{array}{c} \textbf{class} \, \texttt{mstack.pairdistributionfunction.PdfData} \, (name=None, \quad data=None, \quad qmax=None, \\ qmin=None, \quad qbroad=None, \quad qdamp=None, \\ scale=None, \quad rmin=None, \quad rmax=None, \\ rstep=None, use=True) \\ \textbf{Bases:} \, mstack.utilities.UpdateMethods, mstack.utilities.MergeParams \\ \end{array}
```

A container for G(r) data which aggregates the miscellaneous necessary values.

__init__ (name=None, data=None, qmax=None, qmin=None, qbroad=None, qdamp=None, scale=None, rmin=None, rmax=None, rstep=None, use=True)

Parameters

- name as string
- data as filepath or (filepath, column) or np.array
- qmax as Å ** -1
- qmin as Å ** -1
- gbroad as Å?? look it up
- qdamp as Å?? look it up
- scale data scale factor
- fit min minimum r value for refinement as Å
- fit_max maximum r value for refinement as Å
- sampling sampling interval as float or 'Nyquist'
- use boolean flag for refinment

update_data (data, column=1)
 add/upate data to data object

Parameters

- data (str / np.array) file path or data array
- column (int) if read, read from column

Returns None

pairdistributionfunction.PdfModel

Bases: mstack.utilities.UpdateMethods, mstack.utilities.MergeParams

A pdf_model is a single structure and the associated envelope parameters. (i.e. scale, Qres, spdiameter, correlated motion delta1|delta2).

In the calculation sequence, model+data attributes spawn calculators by passing config dicts (i.e. PDFcalculator(**cfg)) which act on the contained diffpy.Structure to produce a PDF.

pdf_models are subordinate to pdf_phases which are the corresponding object to reciprocal space objects

__init__ (name=None, structure=None, scale=None, delta1=None, delta2=None, spdiameter=None, sthick=None, mno=None, use=True, sratio=None, rcut=None, stepcut=None)

- name (str / None) model name
- structure (diffpy.Structure | None) a supercell generated from interface
- scale (float) scale factor

- **delta1** (float) [Å] component in the broadening equation below
- **delta2** (float) [Å ** 2] component in the broadening equation below
- **spdiameter** (float) [Å] particle diameter in analytic damping function for spherical nanoparticles.
- **sthick** (float) [Å] sheet thickness in analytic damping function (infinite width)
- mno (int, list) [int] (int, int, int) supercell dimensions for expansion of structures
- **use** (bool) include in refinement?
- sratio [-] sigma ratio for bonded atoms- peak sharpening due to correlated motion
- rcut [Å] radius cutoff for application of sratio
- **stepcut** [Å] distance above which G(r) is truncated

Note:

peak width is given by the Jeong peak width model: $\sigma_{ij} = \sigma'_{ij} * \operatorname{sqrt}(1 - \delta_1 / r_{ij} - \delta_2 / r^2_{ij} + Q^2_{\text{broad}} * r^2_{ij})$

pairdistributionfunction.PdfRefinement

Bases: mstack.utilities.UpdateMethods, mstack.utilities.MergeParams

A pdf refinement is comprised of a structure model(s) and data to be fit against

Contains:

- structure_exchange- translate Structure object into diffpy.Structure.Structure object
- generator- subprocess call to diffpy.srreal.pdfcalculator
- residual method- ojective function for minimization
- callback- tasks to be evaluated at each fit call
- lsq_minimize- least squares minimization wrapper for lmfit
- diffev_minimize- differential evolution minimization wrapper for lmfit

___init___ (name=None, data=None, phases=None)

Parameters

- name (str) PdfRefinement name
- data (pairdistributionfunction.PdfData (s)) listlinstance of PdfData
- phases (pairdistributionfunction.PdfPhase(s)) listlinstance of Pdf-Phase

apply_sheetcf(gr, sthick)

Apply sheet cf to a 2xN numpy array containing G(r) in angstroms

- gr (np.array) G(r) data array
- sthick (float) sheet thickness

Returns G(r) data array

Return type np.array

apply_sphericalcf(gr, psize)

apply spherical cf to a Nx2 shape numpy array containing G(r)

Parameters

- gr (np.array) G(r) data array
- psize (float) spherical partical diameter

Returns G(r) data array

Return type np.array

calculator (model, data)

real-space PDF calculation via srreal.pdfcalculator. Calculator built from attributes of model and data.

Parameters

- model (PdfModel) single instance (structure, name=None, scale=None, delta1=None, delta2=None, spdiameter=None, sratio=None, rcut=None, stepcut=None, mno=None)
- data (PdfData) single instance (data, name=None, qmax=None, qmin=None, qbroad=None, qdamp=None, scale=None, rmin=None, rmax=None, rstep=None, use=True)

Returns Calculated (np.array())g(r) scaled by model_scale only

```
Note: Final difference should be calculated from **sum_i**{(data\_scale * data\_i) - **sum_j**{phase\_scale\_j * **sum_k**{g(r)_k}}}
```

Note: No shape function applied to calculator result.

```
callback (params, iter, resid, *args, **kwargs)
```

Add residual point to dynamic plot, model history

Parameters

- params (lmfit.Parameters) -
- iter (int) iteration number
- resid(array) residual array
- **kws** (dict) mostly ignored. use "plot_resid"(bool) to initiate dynamic plot of residual vs. iteration

Returns None

Note: Return type is important in this case. I believe a return type of True causes the minimization to abort.

diffev_minimize (subdir=None, plot_resid=False, sqrt_filter=False, disp=True, popsize=5, tol=0.1, mutation=(0.4, 0.8), recombination=0.8, seed=None, polish=False) Wrapper for lmfit differential_evolution method (global minimization).

- **subdir** (str) directory to stash output files
- plot_resid (bool) plot residual vs. iteration
- sqrt_filter (bool) plot data scaled by (Yobs) ** 1/2
- disp (bool) I forget
- popsize (int) see below
- tol (float) see below
- mutation (tuple) see below
- recombination (float) see below
- seed (Imfit.Parameter?) see below
- polish (bool) follow DIFFEV opt by least squares

Returns

- np.array([sqrt(yo) sqrt(yc)]) if sqrt_filter is True
- np.array([yo-yc]) if sqrt_filter is False

see scipy.optimize.differential_evolution for compete list of minimizer keys & descriptions

Notes

Differential evolution is a stochastic population based method that is useful for global optimization problems. At each pass through the population the algorithm mutates each candidate solution by mixing with other candidate solutions to create a trial candidate. There are several strategies [R141] for creating trial candidates, which suit some problems more than others. The 'best1bin' strategy is a good starting point for many systems. In this strategy two members of the population are randomly chosen. Their difference is used to mutate the best member (the best in best1bin), b0, so far:

```
b' = b0 + mutation (population[rand0] population[rand1])
```

A trial vector is then constructed. Starting with a randomly chosen 'i'th parameter the trial is sequentially filled (in modulo) with parameters from b' or the original candidate. The choice of whether to use b' or the original candidate is made with a binomial distribution (the 'bin' in 'best1bin') - a random number in [0, 1) is generated. If this number is less than the recombination constant then the parameter is loaded from b', otherwise it is loaded from the original candidate. The final parameter is always loaded from b'. Once the trial candidate is built its fitness is assessed. If the trial is better than the original candidate then it takes its place. If it is also better than the best overall candidate it also replaces that. To improve your chances of finding a global minimum use higher popsize values, with higher mutation and (dithering), but lower recombination values. This has the effect of widening the search radius, but slowing convergence.

[R140]: Storn, R and Price, K, "Differential Evolution - a Simple and Efficient Heuristic for Global Optimization over Continuous Spaces," *Journal of Global Optimization* 11, 341 - 359 (1997).

```
dim_check (calc_data, exp_data)
```

Returns len(calc_data) == len(exp_data)

Return type bool

```
filter_report (variable=True, constrained=False)
```

print a limited portion of the lmfit minimizer fit report ~! moved to utilities

generic_update (params)

generic update method passes parameters to subordinate objects

Parameters params (lmfit.Parameters) -

Returns True

Return type bool

lsq_minimize (subdir=None, plot_resid=False, epsfcn=None, xtol=None, sqrt_filter=False, method='leastsq', minkws=None)

Wrapper for lmfit least_squares method (Levenberg-Marquardt)

Parameters

- **subdir** (*str*) directory to put the DIFFaX input/output into.
- plot_resid (bool) toggle dynamic plotting of R vs. iter.
- **epsfcn** (float) (default = 1e-02) if step-length is too small the minimizer may not progress as no Jacobian is calculated.
- **xtol** (float) (default = 1e-04) convergence criterion for the approximate solution.
- **method** (str) (default = leastsq) optimizer method (i.e. leastsq, nelder, lbfgsb)

Returns np.array([(yo-yc)])

Note: See the SciPy minimizer documentation for full list of minimizer methods.

map_exp_calc (exp_data, calc_data, rmin, rmax)

map exp data, calc data onto same array dim and stride

Parameters

- exp_data (list array) experimental data
- calc_data (list array) calculated data
- rmin (float) min real space radius
- rmax (float) max real space radius

Returns exp_data, (np.array)calc_data

Return type np.array

 $merge_add(A1, A2)$

Add A1 and A2, merging length to longest vector if unequal

Parameters A2 (A1,) -

Returns np.array

model_composite(phase, data)

Populate dict of model components for (PdfPhase)phase and (PdfData)data: Model components: self.gr: {data_1: {phase_1: {model_1: $g(r)_1, ...}, ...}, ...}$

Parameters

- phase (pairdistributionfunction.PdfPhase) -
- data (pairdistributionfunction.PdfPhase) -

Returns phase_scale * sum_i{gr_i} | dtype=float

```
objective_function(params, **kwargs)
```

Note: individual residuals aren't returned for each data set. I'm not sure how to introduce a weighting scheme yet (all data equally weighted).

Parameters

- params (lmfit.Parameters) -
- kwargs see below

kwargs: -subdir: subdirectory -plot_resid: real-time residual plotting (pass thru to callback)

Returns: **sum_i**{residual_i} for i in phases

phase_composite (phases, data, recalc=True)

Get sum of scaled model gr for data. We need to wade through three levels to get to comprable patterns:

- •Model components: self.gr: {data_1: {phase_1: {model_1: g(r)_1, ...}, ...}, ...}
- •Phase components: self.GR: {data_1: {phase_1: $G(r)_1, ...$ }, ...}
- •Phase composite: self.composite: {data_1: G(r)_1, ...}

Parameters

- phases (dict) PdfPhases
- data (pairdistributionfunction.PdfData) pdf data
- recalc (bool) not implemented

Note:

```
•phases -> dict({phase.name: phase}) (plural)
```

- •data -> (PdfData) (singular)
- •shape function applied to each model_composite G(r)
- •recalc(default=True) passed in | determined at objective function

Returns: None

plot_min_result (data, fontsize=12)

Plot the calculated, observed, background and difference curves of the last computation. Executed at end of every minimization.

Parameters

- sqrt_filter (bool) plot data scaled by (Yobs) ** 1/2
- fontsize (float) font size

Returns matplotlib.Figure

report_refined(tabulate=True)

report parameters with attribute vary == True ~! moved to utilities

```
reset()
     use self.original to reset refined parameters to previous values
residual method(data)
     For each phase in refinement, get DIFFaX pattern and calculate residual
         Parameters
             • params (lmfit.Parameters) -
             • kws - see below
     kws: subdir: subdirectory plot_resid: real-time residual plotting (pass thru to callback) sqrt_filter: sounds
         silly, actually just compare sqrt intensities
         Returns residual with length of data
         Return type np.array
revert()
     use self.backup to revert Parameters instance to last minimizer call
rwp()
     calculate rwp for the refinement (utilities method) .. note:: ~! not suitable for multiple data
save (filename=None, subdir=None)
     Create a pickled save state of the refinement.
         Parameters
             • filename (str) – filename.pkl or some such
             • subdir (str) – directory
         Returns None
update_data(data)
     update data dictionary
         Parameters data (list?) -
update_phases (phases)
     update structure dict
         Parameters phases (pairdistribution function. PdfPhase) – layer phases
         Returns None
```

validate diffev()

Differential evolution requires min/max values to be supplied for all variables, not just those that are refined.

This function coerces min/max values from supplied information if none are given by the user.

Returns True

refinement

Created on Thu Dec 03 09:24:07 2015

Designed to integrate lmfit/scipy differential evolution, existing structure tools, and DIFFaX I(Q) generator for global minimization of complex stacking disorered powder diffraction data

2.4. refinement 13

@author: Peter C Metz

mstack.refinement.load (filename, subdir=None)
load a pickled .dat file

Parameters

- **filename** (str) file to load
- **subdir** (str | None) directory

Note: !!!!!!! EXTREMELY IMPORTANT !!!!!!!!! cPickle saves dependencies by reference. If the source code changes between execution, save state, and loading, the save state WILL NOT LOAD. THIS WILL MAKE YOU VERY SAD.

The next step is to switch from pickle to dill, which saves dependencies by definition. This should make save files compatible across development.

If all modules needed by the refinement object are note imported at time of unpickling, there will likely be AttributeErrors thrown.

refinement.Refinement

Bases: mstack.utilities.MergeParams, mstack.utilities.UpdateMethods

hierarchy of refinement objects:

- refinement: contains experiment (data, parameters) + phase(s) + weights (normalized to 100%)
- phase: described by a structure + transitions
- · transitions: holds stacking disorder parameters
- structure: holds asymmetric unit and cell parameters
- atoms: holds coordinates and isotropic thermal displacement parameters

Note: Specific ref_to_phase and phase_to_ref methods are depricated by the UpdateMethods in the utilities module.

I haven't tested the code since replacing the depricated method here.

If this is problematic replace refinement_to_phase and phase_to_refinement methods before __init__ and uncomment the appropriate lines (indicated with in line comments).

```
__init__ (wavelength=None, exp_data=None, t_range=None, broadening=None, background=None, phases=None, weights=None, global_scale=None, lateral_broadening=None, phase_params=None, name=None)
```

- wavelength (*) experimental radiation in angstrom
- **exp_data** (*) array like [(x1, y1), ..., (xn, yn)]
- t range (*) 2-theta range like [2T min, 2T max, 2T step]

- broadening (*) [gau] gaussian FWHM or [u, v, w, sigma] pseudo-voight parameters
- background (*) list of coefficients to yb = A/x + B + C*x + D*x**2 + E*x**2
- **phases** (*) list of phase instance(s) like [<phase_1>, ... <phase_N>]
- weights (*) dictionary of weight percents like {phase_1.name: weight_1, ..., phase_N.name, weight_N}
- global_scale (*) global scale factor (float)
- lateral_broadening (*) lateral dimension in Angstroms, per DIFFaX Manual (float)
- **phase_params** (*) dict of {'phase_name': <lmfit.Parameters>}
- name (\star) a string to identify the refinement instance

callback (params, iter, resid, **kws)

Add residual point to dynamic plot, model history

Parameters

- params (lmfit.Parameters) -
- iter (int) iteration number
- resid (array) residual array
- **kws** (dict) mostly ignored. use "plot_resid"(bool) to initiate dynamic plot of residual vs. iteration

Returns None

Note: Return type is important in this case. I believe a return type of True causes the minimization to abort.

diffev_minimize (subdir=None, plot_resid=False, sqrt_filter=False, disp=True, popsize=5, tol=0.1, mutation=(0.4, 0.8), recombination=0.8, seed=None, polish=False) Wrapper for lmfit differential_evolution method (global minimization).

Parameters

- **subdir** (str) directory to stash output files
- plot resid (bool) plot residual vs. iteration
- sqrt_filter (bool) plot data scaled by (Yobs) ** 1/2
- disp(bool) I forget
- popsize (int) see below
- tol (float) see below
- mutation (tuple) see below
- recombination (float) see below
- seed (lmfit.Parameter?) see below
- polish (bool) follow DIFFEV opt by least squares

Returns

• np.array([sqrt(yo) - sqrt(yc)]) if sqrt_filter is True

2.4. refinement 15

• np.array([yo-yc]) if sqrt_filter is False

see scipy.optimize.differential_evolution for compete list of minimizer keys & descriptions

Notes

Differential evolution is a stochastic population based method that is useful for global optimization problems. At each pass through the population the algorithm mutates each candidate solution by mixing with other candidate solutions to create a trial candidate. There are several strategies [R141] for creating trial candidates, which suit some problems more than others. The 'best1bin' strategy is a good starting point for many systems. In this strategy two members of the population are randomly chosen. Their difference is used to mutate the best member (the best in best1bin), b0, so far:

b' = b0 + mutation (population[rand0] population[rand1])

A trial vector is then constructed. Starting with a randomly chosen 'i'th parameter the trial is sequentially filled (in modulo) with parameters from b' or the original candidate. The choice of whether to use b' or the original candidate is made with a binomial distribution (the 'bin' in 'best1bin') - a random number in [0, 1) is generated. If this number is less than the recombination constant then the parameter is loaded from b', otherwise it is loaded from the original candidate. The final parameter is always loaded from b'. Once the trial candidate is built its fitness is assessed. If the trial is better than the original candidate then it takes its place. If it is also better than the best overall candidate it also replaces that. To improve your chances of finding a global minimum use higher popsize values, with higher mutation and (dithering), but lower recombination values. This has the effect of widening the search radius, but slowing convergence.

[R140]: Storn, R and Price, K, "Differential Evolution - a Simple and Efficient Heuristic for Global Optimization over Continuous Spaces," *Journal of Global Optimization* 11, 341 - 359 (1997).

```
filter_report (variable=True, constrained=False)
```

print a limited portion of the lmfit minimizer fit report ~! moved to utilities

flag (true=None, false=None)

Toggle elements of each list TruelFalse respectively

Parameters

- true (list) parameter name strings
- **false** (list) parameter name strings

Returns None

generic_update(params)

generic update method passes parameters to subordinate objects

Parameters params (lmfit.Parameters) -

Returns True

Return type bool

lsq_minimize (subdir=None, plot_resid=False, epsfcn=None, xtol=None, sqrt_filter=False, method='leastsq', minkws=None)

Wrapper for lmfit least_squares method (Levenberg-Marquardt)

- **subdir** (str) directory to put the DIFFaX input/output into.
- plot_resid (bool) toggle dynamic plotting of R vs. iter.
- **epsfcn** (float) (default = 1e-02) if step-length is too small the minimizer may not progress as no Jacobian is calculated.

- **xtol** (float) (default = 1e-04) convergence criterion for the approximate solution.
- **method** (str) (default = leastsq) optimizer method (i.e. leastsq, nelder, lbfgsb)

Returns np.array([(yo-yc)])

Note: See the SciPy minimizer documentation for full list of minimizer methods.

map_calc_exp_background(calc_data)

Map calc, exp, background data onto same array dim and stride

```
Parameters calc_data (list) - [(x1, y1), ..., ]
```

Returns [(x1, y1), ...]

Return type list

plot_min_result (sqrt_filter=False, fontsize=12)

Plot the calculated, observed, background and difference curves of the last computation. Executed at end of every minimization.

Parameters

- sqrt_filter (bool) plot data scaled by (Yobs) ** 1/2
- fontsize (float) font size

Returns matplotlib. Figure

preview (subdir=None, sqrt filter=False)

get peak at first calculated state

pub_control (subdir=None, path='/media/sf_Dropbox/Thesis/MStack/mstack_0.1/doc')

Publish control file for all structures in self.phases Control.dif written in working directory Path as os.path.join(*[k for k in [subdir, phase] if k is not None])

Parameters

- **subdir** (str) directory in which to write
- path (str) directory in which to write

Returns None

pub_input (subdir=None, path='/media/sf_Dropbox/Thesis/MStack/mstack_0.1/doc')

Raises method of phase to refinement level Passes dictionary of ancillary information (info) to phase.pub_input to maintain backwards compatibility with DIFFEV/old input methods Default behavior is to publish control file for all structures in self.phase Path as os.path.join(*[k for k in [subdir, phase] if k is not None])

Parameters

- **subdir** (str) directory in which to write
- path (str) directory in which to write

Returns None

report_constrained(tabulate=False)

report parameters with attribute expr != None

report_refined (tabulate=False)

report parameters with attribute vary == True ~! moved to utilities

2.4. refinement 17

```
reset()
     use self.original to reset refined parameters to previous values
residual method (params, **kws)
     For each phase in refinement, get DIFFaX pattern and calculate residual
         Parameters
             • params (lmfit.Parameters) -
             • kws - see below
     kws: subdir: subdirectory plot_resid: real-time residual plotting (pass thru to callback) sqrt_filter: sounds
         silly, actually just compare sqrt intensities
         Returns residual with length of data
         Return type np.array
revert()
     use self.backup to revert Parameters instance to last minimizer call
rwp (weight=None)
     calculate rwp for the model: Rwp = \{sum_m(w_m * (Y_{0,m} - Y_{c,m}) ** 2) / sum_m(w_m * Y_{0,m}) ** 2\}
         ** 1/2 wm = 1 / sigma ** 2
     weight (length == data) defalut weight: (Y_0, m^{**} 1/2)^{**} - 2
save (filename=None, subdir=None)
     Create a pickled save state of the refinement.
         Parameters
             • filename (str) – filename.pkl or some such
             • subdir (str) – directory
         Returns None
update_background (background_coefficients=None, params=None)
     update background from list of coefficients or parameters instances assumes a functional form vbg = A/x
     + B + C * x + D * x **2 + E * x **3
         Parameters
             • background_coefficients(list | None)-
             • params (lmfit.Parameters | None) -
         Returns None
update_broadening(broadening)
     update empirical instrumental broadening parameters from list gaussian broadening: [FWHM] length 1
     argument pseudo-voight: [u, v, w, sigma] length 4 argument
         Parameters broadening (list) -
         Returns None
```

update_phase (phases)

add phases to refinement.Phase(s) dict

update_phase_params (phase_params)

updatelinitialize phase_params

```
Parameters phase_params (dict) - {'phase_name': <lmfit.Parameters>}
```

Returns None

update_theta_range (theta_range)

Update the refined data range

Parameters theta_range (1ist) - [min, max, stride] in units of 2 theta

Returns None

update_weights (weights)

Update weights.

Parameters weights (dict) – {phase name: weight}

Note: weights are automatically normalized to 1

Returns None

validate_diffev()

Differential evolution requires min/max values to be supplied for all variables, not just those that are refined.

This function coerces min/max values from supplied information if none are given by the user.

Returns True

```
weighted_composite(subdir=None,
```

individual=False,

column=2.

path='/media/sf_Dropbox/Thesis/MStack/mstack_0.1/doc')

Return composite of patterns generated by phases & associated weighting factors. looks for phase_name.spc in pathsubdir

Args:

Returns all weighted components individual is False (list | default): [(x1, y1), ...]

Return type individual is True (dict)

structure

A structure contains atoms (x ,y, z, occ, type, ADP), and a structure contains a unit cell (a, b, c, α , β , γ) and asymmetric unit (list of atoms).

A phase contains layer structures as well as transitions to propagate the layer motif in along the perpendicular vector. The stacking vector is always taken as parallel to **c**. Created on Fri Oct 16 16:37:48 2015

A structure is a essentially an enhanced dictionary that contains lattice parameters and atom instances.

@author: Peter C Metz

mstack.structure.build_cif(filename, structure_name=None, layer_number=1, path=None)

Use PyCifRW to parse a .cif file and output a Structure instance.

Args:

- filename (str): pathfilname.extension
- structure_name (str): name for Structure intsance

2.5. structure 19

- layer_number (int): layer number
- path (strlNone): directory

•currently required site labels as "TypeNumber"; i.e. Mn1, O5000, Uuo195

Note: There appears to be an error with parsing a filename containing a complete path. i.e. C:Path1Path2...

ilename.cif is interpreted as a URL for some dumb reason. The current use of ReadCif simply strips the mount point of your disk drive, which seems to work so long as the current working directory is on the same disk as your .cif file.

structure.Atom

an atom instance contains its type (name) and number (of its kind) which define a unique label (i.e. O1, Nb5). x, y, & z are float fractional coordinates and Uiso is the thermal displacement parameter (Biso = 8*pi**2*<u**2> = 8*pi**2*Uiso)

Parameters

- atom_name (*) atom name
- number (*) site number
- x, y, z (*) fractional coordinates
- **Uiso_or_equiv** (*) isotropic thermal displacement parameter
- occ (*) occupancy fractional
- disp_type (*) 'Biso' or 'Uiso'

__init__ (atom_name, number, x, y, z, Uiso_or_equiv, occ, disp_type='Uiso')

Parameters

- atom_name (*) atom name
- number (*) site number
- \mathbf{x} , \mathbf{y} , \mathbf{z} (\star) fractional coordinates
- Uiso_or_equiv (*) isotropic thermal displacement parameter
- occ (*) occupancy fractional
- disp_type (*) 'Biso' or 'Uiso'

structure.Structure

```
 \begin{array}{c} \textbf{class} \; \texttt{mstack.structure.Structure} \; (\textit{name}, \; a, \; b, \; c, \; alp = 90, \; bet = 90, \; gam = 90, \; atoms = None, \; number = 1) \\ \textbf{Bases:} \; \textit{mstack.utilities.UpdateMethods}, \; \textit{mstack.utilities.MergeParams} \end{array}
```

A structure instance contains the lattice and asymmetric unit, presently limited only to P1 symmetry, of a layer structure.

```
__init__ (name, a, b, c, alp=90, bet=90, gam=90, atoms=None, number=1)
```

Parameters

- **a** (*) lattice parameter a [Å]
- **b** (*) lattice parameter b [Å]
- c (*) lattice parameter c [Å]
- alp (*) lattice parameter alpha [°] default = 90
- **bet** (*) lattice parameter beta [°] *default* = 90
- $gam(\star)$ lattice parameter gamma [°] default = 90
- atoms (*) list of atom instances default = None
- number (*) layer number [integer] used to index layer when building transition matrix

Note: In DIFFaX alpha and beta are constrained to 90°- only gamma may vary. These are presently included as a formality.

```
get_all_par()
```

returns dictionary of all paramters stored in structure, e.g.:

- lattice parameters (vector magnitudes and angles)
- atom parameters (x, y, z, occ, Uiso)

```
Returns {[atom.label]_[par]: value, ...}
```

Return type dict

```
get_atom_par(par)
```

return atom par(str) with keys label_par (dict)

lattice_angles()

return lattice angles as variables (dict)

lattice_params()

return lattice parameters as variables (dict)

merge_adp (atoms)

get list of atom ADPS in common ADP type (Biso)

Parameters atoms (*) – list of atom instances

```
parameters (*valid keys)
```

Creates a lmfit Parameters instance from the contents of structure.

All pars come fixed by default- user will flag enteries for refinment using the Parameters method in-stance['parname'].vary=Boolean.

If a list of keywords is passed, parameters() will attempt to assemble a Parameters instance using the valid keys and reporting the invalid keys (i.e. ['a', 'b', 'c', 'Ox']... returned params.keys()= 'a', 'b', 'c'): invalid key 'ox'.)

Parameters valid_keys (str, list) – parameter keys

Returns instance containing *valid_keys

Return type lmfit.Parameters

2.5. structure 21

structure.Phase

```
class mstack.structure.Phase (name,
                                               transitions=None.
                                                                     structures=None,
                                                                                           parame-
                                                  redchi=None,
                                   ters=None,
                                                                   broadening=None,
                                                                                        mcl=None,
                                   path='/media/sf_Dropbox/Thesis/MStack/mstack_0.1/doc')
     Bases: mstack.utilities.MergeParams, mstack.utilities.UpdateMethods
     A Phase contains the layer structure and transition(s) to be expanded into a refinable supercell model.
     Multiple Phase objects can be fed to the Refinement object to accout for polytypism or multiphase data, etc.
     init (name, transitions=None, structures=None, parameters=None, redchi=None, broaden-
                 ing=None, mcl=None, path='/media/sf_Dropbox/Thesis/MStack/mstack_0.1/doc')
              Parameters
                  • transitions- transitions instance (*)-
                  • structures- list of structure instances (*)-
                  • parameters- lmfit parameters instance (*)-
                  • redchi - reduced chi value of last iteration (*) -
                  • broadening -[FWHM] | [u, v, w, sigma] (*) -
                  • mcl - mean column length (*) -
                  • path (*) – directory path
     initialize_structure_params (stru)
          initialize structure parameters as lmfit parameters for stru(s)
              Parameters stru(*)-
     pub control (info, inputname='diffax in.dat', path='/media/sf Dropbox/Thesis/MStack/mstack 0.1/doc',
          write control file for single file inputname.dat supply T min, T max T step as info ~! this will change
          at some point
              Parameters
                  • info (*) – theta information (min, max, step)
                  • inputname (*) – .dat file for DIFFaX to munch crunch upon
                  • path (*) – directory
                  • subdir (*) – more directory info... probably scrap this
              Returns
                  • None
     pub_input (info, inputname='diffax_in', path='/media/sf_Dropbox/Thesis/MStack/mstack_0.1/doc',
                   subdir=None)
          Distill phase into diffax input file inputname.dat.
          At the moment, ancillary information is not stored in model- i.e. radiation type, 2-theta limits, etc... needs
          to be passed in needed (key):
             •wavelength (wvl)
             •broadening parameters (gau) ~! only gaussian implimented right now!
             •lateral braodening (lat) – this is optional
```

•Mean Column Length (MCL)

Parameters

- info (*) indicated above
- inputname (*) fname

Returns

• None

```
report_refined()
    returns dict of items with self.params[item].vary == True
toggle(flags=None)
    set refinement_flags to refine
    flags (str): parameter names to togggle vary - True
update_mcl(mcl)
```

Create mean column length and MCL/1022 variabels. DIFFaX interprets mcl >= 1022 as infinite crystallites, hence the normalization.

Parameters mcl (\star) – 1 <= mean column length <= 1022

```
update_structures (stru)
```

add/update structure to/in model

```
Parameters stru (*) -
```

$update_transitions(T)$

add/update transition to/in model

Parameters T (transition.Transitions) -

supercell

Created on Wed Mar 02 11:34:35 2016

quick script to translate Structure instances into supercells -copy/shift asymmetric unit according to single vector - accept user dimension (N-units along c-vector) or default to MCL -dump .xyz file and/or .cif (P1) file for visualization and supercell PDF

```
* pub_cif
```

- * pub_xyz
- * supercell

@author: Peter C. Metz

mstack.supercell.pub_cif (a, b, c, gam, asym, path, filename) publish a structure in .cif format.

Parameters

- b, c, $gam(a_1)$ lattice parameters
- asym (list) list of structure. Atoms
- path (str) directory of file.cif
- **filename** (*str*) filname for dump (omit .cif)

2.6. supercell 23

```
mstack.supercell.pub_xyz (a, b, c, gam, asym, path, filename) write .xyz as <N atoms> <comment line> < atom> <x> <y> <z>
```

Parameters

- b, c, $gam(a_1)$ lattice parameters
- asym (list) list of structure. Atoms
- path (str) directory of file.xyz
- **filename** (str) filname for dump (omit .xyz)

@!!!!!! Orthogonal vector space conversion is broken

```
mstack.supercell.supercell(struct, vector, N=None, cif=True, xyz=False, path=None, file-name=None, debug=False)
```

Dump a supercell model for input structure and vector with dim 1x1xN.

Parameters

- **struct** (structure. Structure) layer structure
- vector (list, dict) layer vector in fractional values
- N (bool | None) supercell dimension
- cif (bool / True) output cif?
- xyz (bool | False) output xyz?
- path (str/None) directory
- filename (str/None) filename
- **debug** (bool | False) return expanded asymmetric unit

Returns None

transition

transition.Transition

```
class mstack.transition.Transition (i, j, alpij=None, vector=None, cij=None)
Bases: object
```

instantiate a transition to create empty variables that satisfy the program requirements of DIFFaX. Parameters include transition index n, transition probability alphaij, vector R, and uncertainty cij

- * generic
- * scale_cij
- * update_cij
- * update_alpij
- * update vector

```
__init__(i, j, alpij=None, vector=None, cij=None)

Announce components of the nth transition. Defaults = 0.0.
```

```
• vector (dict) - {'rx': float, 'ry': float 'rz': float}
                   • cij (dict) - {'c11': float, 'c22': float, 'c33': float, 'c12': float, 'c13': float, 'c23':
                     float}
           Note: Pass additional information as tuple, e.g. (value [, TruelFalse [, min, max]])
     generic (generic, name, min0=0.0, max0=1.0)
           Method for updating params.
               Parameters
                   • generic (dict) - {key: (value [, TruelFalse [, min, max]]), ...} optional vary boolean,
                     min, max as positional args
                   • name (str) – alpijlcijlvector
               Returns sets parameter and updates appropriate attribute
     scale_cij (force=False)
           scale cij by smaller corresponding cii to satisfy requirement that cij <= cii
               Parameters force (bool) – executes scaling whether or not self.scaled is True
               Returns True
               Return type bool
     update_alpij (alpij)
           initialize/update transition probabilities (dim(n))
     update_cij(cij)
           initialize/update cij (fractions) and scaled_cij (appropriately scaled copy)
     update_vector(vector)
           initialize/update vector
transition.Transitions
class mstack.transition.Transitions (nlayers=None, transitions=None)
     Bases: object
     Container for all the transitions specifying a stacking disorder problem.
      * pub trans
           method to publish transitions block in DIFFaX format. I.e.: {alpij Rxj Ryj Rzj (clm)} 1.00000000000
           0.3550\ 0.3550\ 1.0000\ (10.0000\ 10.0000\ 2.0000\ 0.0000\ 0.0000\ 0.0000\ )\{1-1\}\dots
               \{N-N\}
      * row_normal
      * todict
      * update_transitions
     * validate_transitions
     __init__ (nlayers=None, transitions=None)
               Parameters
```

• alpij (dict) - {'alpn1': float, ..., 'alpnN': float} dim(n_layers)

2.7. transition 25

```
• transitions (list) – list containing transition instances
                   • nlayers (int) – number of layer types (N)
     pub_trans()
           publish the transition information in DIFFaX suitable format, e.g. alpij Rx Ry Rz (Cijk) {i-j}
               Returns list of transitions in DIFFaX format (string lists) (0th element always empty)
     row normal(row=0)
           row normalize entries in alpij
     todict()
           map numpy array as dict
     update_transitions (transitions)
           initialize/update dictionary of transitions
     validate_transitions (force=False)
           Note: Because empty fields are initialized with appropriate values except for probabilities, we really just
           need to confirm the user supplied probabilities and that they:
              1.are row normalized.
             2.of uniform dimension (N x N)
           These conditions are enforced (transitions are operated on) if not correct
               Parameters force (bool | False) - recompute scaled cij whether or not trans.scaled is
                   True
               Returns TruelFalse
               Return type Boolean
utilities
Created on Thu Dec 03 13:28:46 2015
Common utility classes and functions for MStack.
@author: Peter C Metz
class mstack.utilities.DynamicPlot (fontsize=14)
     Bases: object
     Plotting utility used to create output for itterative function. Called in minimizer callback function to create Rwp
     vs. iter Reserves plot number 100 for this purpose.
     call signiture: DynamicPlot(xdata, ydata) -> appended point to plot
     __init__ (fontsize=14)
     on_launch()
           set up plot
     on_running (new_x, new_y)
```

update plot

class mstack.utilities.MergeParams

Bases: object

Tools to merge Parmeters instances between objects containing them while maintaining unique parameter names.

The result is an lmfit.Parameters object on the top class with the name 'params' (so call your lmfit.Parameters instance params if you want this to work smoothly) Although the specification of lmfit.Parameters attributes as other names works with specifier

add_set_params (name=None, value=None, vary=None, min=None, max=None, expr=None)
add/set parameter in refinement parameters

for list of supported mathematics, see: http://lmfit.github.io/lmfit-py/constraints.html# supported-operators-functions-and-constants

Parameters

- name (str) parameter name
- value (float) parameter value
- **vary** (bool) vary in refinement?
- min (float) minimum bound
- max (float) maximum bound
- **expr** (str) constrain expression.

Returns None

exists (attribute, value=None)

check if attribute exists in object | create with value(None) else

```
lower_to_upper (top_attribute, specifier=None)
```

When merging lmfit.Parameters instances belonging to different constituent refinement objects, we run into an issue of unique variable naming (x occurs for each atom coodinate, i.e.)

The transmogrifier appends the top_attribute.name to the bottom_attribute.Parameter.name attribute to construct a unique variable label. This change is propagated to variables in the instance's constraint expression to maintain validity.

i.e top_attribute = (attribute as str) indicating dictionary of subordinate objects bottom_attribute = params instance subordinate object

```
{\tt param\_finder} \ (bottom\_attribute, specifier)
```

get parameter instance from subordinate object

upper to lower (top attribute, specifier=None, debug=False)

•top_attribute: attribute name for dict of subordinate objects i.e. 'phases' -> refinement.phases = {'phase_1': <PairDistributionFunction.PdfPhase>}

•specifier: name of parameters instance in subordinate object

class mstack.utilities.UpdateMethods

Bases: object

Generic update methods for the data types dealt with in pdf refinement objects

- •initialize: set attribute for class if it doesn't exist, add Parameter instance
- •update: update an initialized parameter with appropriate method
- •update_with_limits: update when value received as (value, min, max)

2.8. utilities 27

```
•update with lmfit: update when value received as lmfit.Parameter instance
     initialize (attribute, value=None)
          default variable initialization
     update (attribute, value=None)
          default update mode
     update_with_limits (attribute, tup)
          allow args passed as (value, min, max)
     update_with_lmfit (attribute, parameter)
          update self.params with Parameter instance
mstack.utilities.attributegetter(items)
     Return a callable object that retrieves named attributes from its operand using the objects __getattribute__()
     method. This is analogous to the built-in operator operator.itemgetter.
          Parameters items (str, list) – attribute names
          Returns callable object that retreives attribute values from the operand
mstack.utilities.checkequal(iterator)
     Check if subsequent iterables are equivilant used only in Structure.pub input
          Parameters iterator (iterable) -
          Returns bool
mstack.utilities.filter report(refinement, variable=True, constrained=False, print=True,
                                           text=False)
     print a limited portion of the lmfit minimizer fit report.
          Parameters
                 • refinement (Refinement instance) - Pdf or I(Q) Refinement instance
                 • variable (bool | True) - report refined variables
                 • constrained (bool | False) - report constrained variables
                 • _print (bool | True) - print output
                 • _text (bool | False) - list output
          Returns list of lines of output text
          Return type list
mstack.utilities.flatten(iterable)
     flatten list of lists with N-recursion depth
mstack.utilities.interpolate_data(Array1, Array2, *mesh)
     Map Array1 onto Array2 if Array 2 specified Else, map Array1 onto user defined mesh(float)
          Parameters
                 • Array1 (list, np.array) - (x, y) data
                 • Array2 (list, np.array) – (x, y) data
                 • mesh (float) – stride for interpolation if Array2 absent
          Returns [(x1, y1), ..., (xn, yn)]
```

Return type list

```
mstack.utilities.isfinite (value)
    test if value is infinite
```

mstack.utilities.not_header(line, override=False)

Check line in input file for # or text Override used for debugging only

Returns True if data, False if header

Return type bool

```
mstack.utilities.plot(*Array, **kwargs)
```

Takes a list of tuples [(x1,y1),...,(xn,yn)] and plots with line format

~! bug: axis determined on last loaded plot (could lead to truncation)

Parameters

- Array (list, np.array) array(s) with shape (N,2)
- kwargs accepts xmin, xmax, ymin, ymax as key word args

Returns matplotlib plot object

mstack.utilities.print_table(dictionary=None, table=None, key=None, headers=None)
pretty print wrapper of tabulate.

Parameters

- dictionary (dict | None) dictionary of table content
- table (list | None) list format of table
- **key** (sort key | None) last operation is list.sort(key=key)
- headers (list | None) list of headers for columns ['string', ...'Nstring']

Returns prints table, returns True if no exception raised

Return type bool

```
mstack.utilities.read_data(filename, column=1, lam=None, q=False, override=True)
```

Reads data from space delimited format. Default assumption is that (x, y) are in the first and second column, respectively. Use column argument to change elsewise. use argument 'q' if data is a function of scattering vector rather than 2theta.

Parameters

- filename [str] path/filename.extension
- column [int] location of f(x), x being the 0th column
- lam [float] wavelength of experimental radiation
- q [bool] whether data is a function of scattering vector q
- override [bool] skip stripping header operation if output is unacceptable

Returns (x,y) array of data like [(x1, y1), ..., (xn, yn)]

Return type list

mstack.utilities.report_refined(minimizer_results_object_params, tabulate=False)
report values of parameters object with attribute vary=True

Parameters

- result (lmfit.result) fit result object
- tabulate (bool | False) print or return table

2.8. utilities 29

```
Returns if tabulate is False print: if tabulate is True
           Return type dict
mstack.utilities.rwp (PDF_refinement, weight=None)
     returns the pattern weighted residual for a single data set refinement e.g.
           (sum(weight * diff ** 2) / sum(weight * ref.yo ** 2)) ** 0.5
           Parameters
                 • PDF_refinement – [PdfRefinement instance]
                 • weight – [np.array] with same shape as observed data vector Yo
           Returns Rwp value
           Return type float
utilities.DynamicPlot
class mstack.utilities.DynamicPlot (fontsize=14)
     Bases: object
     Plotting utility used to create output for itterative function. Called in minimizer callback function to create Rwp
     vs. iter Reserves plot number 100 for this purpose.
     call signiture: DynamicPlot(xdata, ydata) -> appended point to plot
     __init__ (fontsize=14)
     on_launch()
           set up plot
     on_running(new_x, new_y)
           update plot
utilities.MergeParams
class mstack.utilities.DynamicPlot (fontsize=14)
     Bases: object
     Plotting utility used to create output for itterative function. Called in minimizer callback function to create Rwp
     vs. iter Reserves plot number 100 for this purpose.
     call signiture: DynamicPlot(xdata, ydata) -> appended point to plot
     __init__ (fontsize=14)
     on_launch()
           set up plot
     on_running(new_x, new_y)
           update plot
```

utilities.UpdateMethods

```
class mstack.utilities.DynamicPlot (fontsize=14)
    Bases: object
```

Plotting utility used to create output for itterative function. Called in minimizer callback function to create Rwp vs. iter Reserves plot number 100 for this purpose.

call signiture: DynamicPlot(xdata, ydata) -> appended point to plot

```
__init__ (fontsize=14)
on_launch()
    set up plot
on_running (new_x, new_y)
    update plot
```

2.8. utilities 31

$\mathsf{CHAPTER}\,3$

Indices and tables

- genindex
- modindex
- search

Python Module Index

m

```
mstack.background, ??
mstack.interface, ??
mstack.pairdistributionfunction, ??
mstack.refinement, ??
mstack.structure, ??
mstack.supercell, ??
mstack.utilities, ??
```