$Benchmarking\ the\ Delayed Matrix Stats\ package$

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Chapter 1

Introduction

The *DelayedArray* package defines the *DelayedMatrix* class, for wrapping matrix-like objects to provide a unified interface.

Wrapping an matrix-like object (typically an on-disk object) in a DelayedMatrix object allows one to perform common matrix operations on it without loading the object in memory. In order to reduce memory usage and optimize performance, operations on the object are either delayed or executed using a block processing mechanism (see ?DelayedArray::DelayedMatrix for further details)

A big advantage of this is we can use choose different matrix "backends" for storing the data while preserving a common interface. Examples of backends and data they are tailored towards using are given below:

Class	Package	Type of data	Example
$\begin{array}{c} \hline matrix \\ dgCMatrix \end{array}$	base Matrix	Dense matrix Sparse data	RNA-seq counts matrix Single-cell RNA-seq counts matrix
HDF5Matri	$x\ HDF5Array$	Dense matrix too large for memory	Non-CpG methylation
RleArray	Delayed Array	Data with runs of identical values	Sequencing coverage

1.1 Session info

The R session information when compiling this book is shown below:

```
devtools::session_info()
#> setting value
   version R version 3.4.0 (2017-04-21)
   system x86_64, darwin15.6.0
   ui
            X11
#>
  language (EN)
  collate en_AU.UTF-8
#> tz
            America/New_York
#>
   date
            2017-06-04
#>
#> package
                      * version
                                   date
#> backports
                        1.1.0
                                   2017-05-22
```

base BiocGenerics BiocStyle		3.4.0 0.23.0	2017-04	-21
	*	0 22 0		
BiocStyle		0.23.0	2017-04	-27
200000900		2.5.1	2017-05	
bookdown		0.4	2017-06	
colorspace		1.3-2	2016-12	
compiler		3.4.0	2017-04	-21
datasets	*	3.4.0	2017-04	-21
DelayedArray			2017-06	
${\it DelayedMatrixStats}$	*	0.0.0.9000	2017-05	-28
devtools		1.13.2	2017-06	-02
digest		0.6.12	2017-01	-27
evaluate		0.10	2016-10	-11
fortunes		1.5-4	2016-12	-29
ggplot2		2.2.1	2016-12	-30
graphics	*	3.4.0	2017-04	-21
grDevices			2017-04	
grid		3.4.0	2017-04	
gtable		0.2.0	2016-02	
HDF5Array			2017-05	
•				
knitr				
			2017-03	
-				
= -				
			202. 00	~~
- •				
=				
•				
			•	
•				
_				
			2017-02	
tibble		1.3.3	2017-05	
tools		3.4.0	2017-04	
utils	*	3.4.0	2017-04	-21
withr		1.0.2	2016-06	-20
yaml		2.1.14	2016-11	-12
zlibbioc		1.23.0	2017-04	-27
	datasets DelayedArray DelayedMatrixStats devtools digest evaluate fortunes ggplot2 graphics grDevices grid gtable HDF5Array htmltools IRanges knitr lattice lazyeval magrittr Matrix matrixStats memoise methods microbenchmark munsell parallel plyr profmem Rcpp rhdf5 rlang rmarkdown rprojroot rstudioapi S4Vectors scales stats stats4 stringi stringr tibble tools utils withr yaml	datasets * DelayedArray * DelayedMatrixStats * devtools digest * evaluate fortunes * ggplot2 graphics * grDevices grid * gtable * HDF5Array * htmltools * IRanges * knitr lattice lazyeval magrittr * Matrix * matrixStats * memoise methods * microbenchmark * munsell parallel * plyr profmem * Rcpp rhdf5 * rlang rmarkdown rprojroot rstudioapi * \$\frac{5}{4}\text{Vectors} * \$\frac{5}{4}\text{Stats} * \$\frac{5}{4}\text{Stringi} \$	datasets * 3.4.0 DelayedArray * 0.3.8 DelayedMatrixStats * 0.0.0.9000 devtools 1.13.2 digest 0.6.12 evaluate 0.10 fortunes 1.5-4 ggplot2 2.2.1 graphics * 3.4.0 grid 3.4.0 grid 3.4.0 gtable 0.2.0 HDF5Array * 1.5.8 htmltools 0.3.6 IRanges * 2.11.3 knitr 1.16 lattice 0.20-35 lazyeval 0.2.0 magrittr 1.5 Matrix * 1.2-10 matrixStats * 0.52.2 memoise 1.1.0 methods * 3.4.0 microbenchmark * 1.4-2.1 munsell 0.4.3 parallel * 3.4.0 plyr 1.8.4 profmem * 0.4.0 Rcpp 0.12.11 rhdf5 * 2.21.1 rpojroot 1.5 scal	datasets * 3.4.0 2017-04 DelayedArray * 0.3.8 2017-06 DelayedMatrixStats * 0.0.0.9000 2017-05 devtools 1.13.2 2017-06 digest 0.6.12 2017-01 evaluate 0.10 2016-12 fortunes 1.5-4 2016-12 gpplot2 2.2.1 2016-12 graphics * 3.4.0 2017-04 grid 3.4.0 2017-04 gtable 0.2.0 2016-02 HDF5Array * 1.5.8 2017-05 htmltools 0.3.6 2017-04 IRanges * 2.11.3 2017-05 knitr 1.16 2017-05 lattice 0.20-35 2017-05 lattice 0.20-35 2017-04 methods * 3.4.0 2017-04

1.1. SESSION INFO

```
#> CRAN (R 3.4.0)
#> local
#> Bioconductor
#> Bioconductor
#> Github (rstudio/bookdown@fdd68e4)
#> CRAN (R 3.4.0)
#> local
#> local
#> Bioconductor
#> local
#> CRAN (R 3.4.0)
#> local
#> local
#> local
#> CRAN (R 3.4.0)
#> Bioconductor
#> CRAN (R 3.4.0)
#> Bioconductor
#> CRAN (R 3.4.0)
#> Github (hadley/memoise@e372cde)
#> local
#> CRAN (R 3.4.0)
#> CRAN (R 3.4.0)
#> local
#> CRAN (R 3.4.0)
#> CRAN (R 3.4.0)
#> CRAN (R 3.4.0)
#> cran (@2.21.1)
#> Github (hadley/rlang@c351186)
#> CRAN (R 3.4.0)
#> CRAN (R 3.4.0)
#> CRAN (R 3.4.0)
#> cran (@0.15.2)
#> CRAN (R 3.4.0)
#> local
#> local
#> CRAN (R 3.4.0)
#> CRAN (R 3.4.0)
#> cran (@1.3.3)
#> local
#> local
#> CRAN (R 3.4.0)
#> CRAN (R 3.4.0)
#> Bioconductor
```

Chapter 2

Test data

We will benchmark the *DelayedMatrixStats* package using different types of matrix-like data:

- dense_matrix: A dense matrix with 600 columns and 20000 rows (91.6 Mb)
- sparse_matrix: A sparse dgcMatrix with 600 columns and 20000 rows where 60% of entries are zero (54.9 Mb)
- rle_matrix: An run-length encoded column RleMatrix with 6 columns and 2000000 rows (0.5 Mb)

```
library(DelayedMatrixStats)
library(Matrix)
library(HDF5Array)
# Dense matrix
dense_matrix <- DelayedArray(matrix(runif(20000 * 600), nrow = 20000,</pre>
                                 ncol = 600)
dense matrix
#> DelayedMatrix object of 20000 x 600 doubles:
                                                   [,599]
                 [,1]
                            [,2]
                                       [,3] ...
                                                              [,600]
#>
       [1,] 0.56211049 0.06052366 0.38033128 . 0.87799385 0.84693600
      [2,] 0.96372515 0.83906637 0.62496370 . 0.87406395 0.06190513
#>
#>
      [3,] 0.18319063 0.81058923 0.63978155 . 0.73985395 0.30726775
                                            . 0.19136272 0.37044424
#>
      [4,] 0.67745600 0.75232175 0.34283933
#>
      [5,] 0.82650284 0.29491392 0.09360019 . 0.86290053 0.63351816
#>
#> [19996,] 0.94517978 0.95109336 0.88648460 . 0.07201023 0.48243563
#> [19997,] 0.99308461 0.85953562 0.78748557 . 0.17937134 0.31886901
#> [19998,] 0.55040209 0.64421003 0.02668481    . 0.77054324 0.27607450
#> [19999,] 0.97592622 0.48989835 0.79181370 . 0.22407128 0.64161406
# 60% zero elements
sparse_matrix <- seed(dense_matrix)</pre>
zero_idx <- sample(length(sparse_matrix), 0.6 * length(sparse_matrix))</pre>
sparse_matrix[zero_idx] <- 0</pre>
sparse_matrix <- DelayedArray(Matrix::Matrix(sparse_matrix, sparse = TRUE))</pre>
sparse_matrix
#> DelayedMatrix object of 20000 x 600 doubles:
#>
                 [,1]
                            [,2]
                                       [,3] ...
                                                   [,599]
                                                              [,600]
#>
       [1,] 0.00000000 0.06052366 0.00000000 . 0.0000000 0.0000000
      [2,] 0.00000000 0.83906637 0.62496370 . 0.0000000 0.0000000
```

```
#>
      [3,] 0.18319063 0.81058923 0.63978155 . 0.7398540 0.0000000
#>
      [4,] 0.67745600 0.00000000 0.34283933
                                             0.1913627 0.3704442
      [5,] 0.00000000 0.29491392 0.00000000 .
                                             0.8629005 0.0000000
#>
#>
#> [19996,] 0.9451798 0.0000000 0.0000000 . 0.07201023 0.00000000
#> [19998,] 0.5504021 0.0000000 0.0000000 . 0.00000000 0.27607450
#> [19999,] 0.0000000 0.0000000 0.0000000 . 0.22407128 0.64161406
                                           . 0.00000000 0.00000000
#> [20000,] 0.6349679 0.0000000 0.0000000
# HDF5-backed dense matrix
# hdf5_matrix <- as(dense_matrix, "HDF5Array")</pre>
# Run-length encoded column matrix
rle_matrix <- RleArray(Rle(sample(2L, 200000 * 6 / 10, replace = TRUE), 100),</pre>
                     \dim = c(2000000, 6))
rle_matrix
#> RleMatrix object of 2000000 x 6 integers:
#>
            [,1] [,2] [,3] [,4] [,5] [,6]
#>
        [1,]
                  1
                        2
                             2
                                 1
#>
        [2,]
               2
                    1
                        2
                             2
                                 1
                                      1
                                1
#>
        [3,]
              2
                  1
                        2
                             2
                                      1
#>
        [4,]
             2
                  1
                        2 2
#>
        [5,]
             2
                        2
                             2
                                 1
                  1
                                      1
#>
#> [1999996,]
              1
                   1
                             1
                                 1
                                      2
                        1
#> [1999997,]
                   1
              1
                        1
                             1
                                 1
                                      2
#> [1999998,]
              1
                    1
                        1
                             1
                                 1
                                      2
#> [1999999,]
               1
                    1
                        1
                             1
                                 1
                                      2
#> [2000000,]
                                      2
               1
                                 1
```

Obviously, this is not a comprehensive set of inputs. Rather, it chosen to be somewhat representative of some typical genomics data.

2.1 Measuring performance

Timings are measured using the *microbenchmark* package using 10 repetitions (times). Memory allocations are reported using the *profmem* package.

```
library(microbenchmark)
library(profmem)
times <- 10</pre>
```

Chapter 3

colSums2()

We compare the DelayedArray::colSums() method, which uses the block-processing algorithm, to the DelayedMatrixStats::colSums2() method, which uses tailored algorithms depending on the seed of the DelayedMatrix and to the DelayedMatrixStats:::.colSums2() method that acts directly on the seed of the DelayedMatrix object¹

3.1 Pristine DelayedMatrix

```
microbenchmark(DelayedArray::colSums(dense_matrix),
               DelayedMatrixStats::colSums2(dense_matrix),
               DelayedMatrixStats:::.colSums2(seed(dense_matrix)),
               times = times)
#> Unit: milliseconds
#>
#>
                   DelayedArray::colSums(dense_matrix) 1237.05967 1286.72366
#>
            DelayedMatrixStats::colSums2(dense matrix)
                                                          13.75110
                                                                     14.48974
   DelayedMatrixStats:::.colSums2(seed(dense_matrix))
#>
                                                          12.24977
                                                                     12.52132
#>
                   median
                                  uq
#>
   1338.77309 1313.47916 1425.51354 1472.51304
                 14.89400
                           16.46142
                                       19.15365
      15.43412
                                                    10
                 12.83785
      13.46753
                            13.45714
                                       17.22766
                                                    10
total(profmem(DelayedArray::colSums(dense_matrix)))
#> [1] 2498171088
total(profmem(DelayedMatrixStats::colSums2(dense_matrix)))
#> [1] 165512
microbenchmark(DelayedArray::colSums(sparse_matrix),
               DelayedMatrixStats::colSums2(sparse_matrix),
               DelayedMatrixStats:::.colSums2(seed(sparse_matrix)),
               Matrix::colSums(seed(sparse_matrix)),
               times = times)
#> Unit: milliseconds
#>
#>
                   DelayedArray::colSums(sparse_matrix) 1263.948627
            DelayedMatrixStats::colSums2(sparse_matrix)
                                                           11.125717
```

¹DelayedMatrixStats:::.colSums2() shouldn't be called by the user because it does not realise delayed operations. It is used here for demonstration purposes on a "pristine" DelayedMatrix to measure the additional overhead of S4 methods

```
DelayedMatrixStats:::.colSums2(seed(sparse_matrix)) 9.694688
#>
#>
                  Matrix::colSums(seed(sparse_matrix))
                                                         9.831111
#>
                     mean median
                                                      max neval
            lq
                                           uq
#>
   1277.792760 1354.97051 1345.26165 1409.33254 1478.01487 10
#>
     11.321978 13.61341 12.38058 14.26526 24.21124
                                                             10
#>
      9.737193 11.27165
                            10.42035
                                       11.44131
                                                  15.96811
      10.428975 11.36380 10.85824
                                       12.76856
                                                  13.00290
                                                             10
#>
total(profmem(DelayedArray::colSums(sparse_matrix)))
#> [1] 1709267496
total(profmem(DelayedMatrixStats::colSums2(sparse_matrix)))
#> [1] 5464
microbenchmark(DelayedArray::colSums(rle_matrix),
              DelayedMatrixStats::colSums2(rle_matrix),
              DelayedMatrixStats:::.colSums2(seed(rle_matrix)),
              times = times)
#> Unit: milliseconds
#>
                                                                        lq
                                               expr
                                                           min
#>
                  DelayedArray::colSums(rle_matrix) 2480.267737 2522.151174
#>
           DelayedMatrixStats::colSums2(rle_matrix)
                                                      3.846588
                                                                  4.031420
  DelayedMatrixStats:::.colSums2(seed(rle_matrix))
                                                       2.660000
                                                                  2.794059
#>
                    median
          mean
                                    uq
                                               max neval
#> 2564.381064 2555.504718 2616.171735 2646.783855
      4.632065
                  4.457076 4.814034
                                                     10
#>
                                        6.303599
       7.772226
                  3.021242
                              3.113427
                                        50.727535
total(profmem(DelayedArray::colSums(rle_matrix)))
#> [1] 787403608
total(profmem(DelayedMatrixStats::colSums2(rle_matrix)))
#> [1] 1872
```

3.2 With row subsetting

```
i <- sample(nrow(dense_matrix), nrow(dense_matrix) / 10)</pre>
microbenchmark(DelayedArray::colSums(dense_matrix[i, ]),
               DelayedMatrixStats::colSums2(dense_matrix, rows = i),
               times = times)
#> Unit: milliseconds
#>
                                                    expr
                                                               min
                DelayedArray::colSums(dense_matrix[i, ]) 150.12124 177.85944
#>
\# DelayedMatrixStats::colSums2(dense_matrix, rows = i) 14.09315 14.59356
                                        max neval
                median
                              uq
#> 198.11233 192.73521 226.85481 240.19939
                                               10
   15.12774 14.92626 15.38786 17.04865
total(profmem(DelayedArray::colSums(dense_matrix[i, ])))
#> [1] 326614368
total(profmem(DelayedMatrixStats::colSums2(dense_matrix, rows = i)))
#> [1] 21512
microbenchmark(DelayedArray::colSums(sparse matrix[i, ]),
               DelayedMatrixStats::colSums2(sparse_matrix, rows = i),
```

```
times = times)
#> Unit: milliseconds
#>
                                                    expr
#>
               DelayedArray::colSums(sparse_matrix[i, ]) 181.0150 185.5543
#> DelayedMatrixStats::colSums2(sparse_matrix, rows = i) 43.4571 46.1228
        mean median
                              uq
                                       max neval
#> 241.06562 214.46952 260.04889 403.65730
#> 47.23405 47.07576 48.33854 51.88142
total(profmem(DelayedArray::colSums(sparse_matrix[i, ])))
#> [1] 217297184
total(profmem(DelayedMatrixStats::colSums2(sparse_matrix, rows = i)))
#> [1] 5805384
i <- sample(nrow(rle_matrix), nrow(rle_matrix) / 10)</pre>
microbenchmark(DelayedArray::colSums(rle_matrix[i, ]),
              DelayedMatrixStats::colSums2(rle_matrix, rows = i),
              times = times)
#> Unit: milliseconds
#>
                                                 expr
                                                            min
               DelayedArray::colSums(rle_matrix[i, ]) 266.4322 282.946
#>
\# DelayedMatrixStats::colSums2(rle_matrix, rows = i) 2509.9470 2536.812
#>
              median
                                      max neval
        mean
                              uq
   288.4523 285.5148 287.8931 342.1545
#>
#> 2565.2083 2557.8006 2567.9954 2645.7166
total(profmem(DelayedArray::colSums(rle_matrix[i, ])))
#> [1] 86579640
total(profmem(DelayedMatrixStats::colSums2(rle_matrix, rows = i)))
#> [1] 99980704
```

3.3 With column subsetting

```
j <- sample(ncol(dense_matrix), ncol(dense_matrix) / 10)</pre>
microbenchmark(DelayedArray::colSums(dense matrix[, j]),
              DelayedMatrixStats::colSums2(dense_matrix, cols = j),
              times = times)
#> Unit: milliseconds
#>
                                                   expr
#>
               DelayedArray::colSums(dense_matrix[, j]) 130.822413
#> DelayedMatrixStats::colSums2(dense_matrix, cols = j)
                                                          2.954383
#>
                                          uq
           lq
                  mean
                            median
#> 185.368641 192.741377 199.560679 204.350156 217.700374
                                                             10
     3.031592 3.534314 3.402916 3.717595 5.269981
                                                             10
total(profmem(DelayedArray::colSums(dense_matrix[, j])))
total(profmem(DelayedMatrixStats::colSums2(dense_matrix, cols = j)))
#> [1] 161192
microbenchmark(DelayedArray::colSums(sparse matrix[, j]),
              DelayedMatrixStats::colSums2(sparse_matrix, cols = j),
              times = times)
#> Unit: milliseconds
```

```
#>
                                                   expr min
               DelayedArray::colSums(sparse_matrix[, j]) 145.41955 151.62413
#>
#> DelayedMatrixStats::colSums2(sparse_matrix, cols = j) 12.24748 12.81168
                                    max neval
    mean median
#>
                            uq
#> 187.63815 182.46718 222.64284 240.3814
   25.01388 14.35228 14.91043 124.2795
total(profmem(DelayedArray::colSums(sparse_matrix[, j])))
#> [1] 217156704
total(profmem(DelayedMatrixStats::colSums2(sparse_matrix, cols = j)))
#> [1] 5755072
j <- sample(ncol(rle_matrix), ncol(rle_matrix) / 2)</pre>
microbenchmark(DelayedArray::colSums(rle_matrix[, j]),
              DelayedMatrixStats::colSums2(rle_matrix, cols = j),
              times = times)
#> Unit: milliseconds
#>
                                                expr
               DelayedArray::colSums(rle_matrix[, j]) 1204.439061 1265.87484
#>
#> DelayedMatrixStats::colSums2(rle_matrix, cols = j)
                                                        3.645216
#>
        mean
                 median
                                 uq
                                            max neval
#> 1280.29217 1287.497136 1296.26175 1336.682742 10
      4.20517
                4.107648
                          4.52946
                                     4.896633
total(profmem(DelayedArray::colSums(rle_matrix[, j])))
#> [1] 401705608
total(profmem(DelayedMatrixStats::colSums2(rle_matrix, cols = j)))
#> [1] 1872
```

3.4 With row and column subsetting

```
i <- sample(nrow(dense_matrix), nrow(dense_matrix) / 10)</pre>
j <- sample(ncol(dense_matrix), ncol(dense_matrix) / 10)</pre>
microbenchmark(DelayedArray::colSums(dense_matrix[i, j]),
              DelayedMatrixStats::colSums2(dense matrix, rows = i, cols = j),
              times = times)
#> Unit: milliseconds
#>
                                                             expr
#>
                        DelayedArray::colSums(dense_matrix[i, j]) 38.678242
\# DelayedMatrixStats::colSums2(dense_matrix, rows = i, cols = j) 2.471122
          lq
                                                 max neval
#>
                 mean median
                                      uq
#> 40.658299 63.969289 67.446417 71.177195 103.697163
   2.514982 2.757317 2.719349 2.876589 3.446033
microbenchmark(DelayedArray::colSums(sparse_matrix[i, j]),
              DelayedMatrixStats::colSums2(sparse_matrix, rows = i, cols = j),
              times = times)
#> Unit: milliseconds
#>
#>
                        DelayedArray::colSums(sparse_matrix[i, j]) 58.16497
\# DelayedMatrixStats::colSums2(sparse_matrix, rows = i, cols = j) 44.19810
                                           max neval
         lq mean median
                                   uq
#> 61.23579 72.97175 64.44056 68.37965 156.5290
#> 45.33201 47.71227 47.05405 50.12441 52.1516
```

```
i <- sample(nrow(rle_matrix), nrow(rle_matrix) / 10)</pre>
j <- sample(ncol(rle_matrix), ncol(rle_matrix) / 2)</pre>
microbenchmark(DelayedArray::colSums(rle_matrix[i, j]),
               DelayedMatrixStats::colSums2(rle_matrix, rows = i, cols = j),
               times = times)
#> Unit: milliseconds
#>
                                                            expr
                                                                       min
                        DelayedArray::colSums(rle_matrix[i, j]) 144.6618
#>
#> DelayedMatrixStats::colSums2(rle_matrix, rows = i, cols = j) 1227.4698
          lq mean median
#>
                                      uq
                                                max neval
  146.4575 150.6922 147.420 148.844 179.0782
#>
#> 1245.4921 1263.5119 1253.124 1269.115 1353.0914
```

3.5 With delayed ops

```
microbenchmark(DelayedArray::colSums(dense_matrix ^ 2),
              DelayedMatrixStats::colSums2(dense_matrix ^ 2),
              times = times)
#> Unit: milliseconds
#>
                                           expr
#>
          DelayedArray::colSums(dense matrix~2) 1326.8490 1431.4468
#> DelayedMatrixStats::colSums2(dense_matrix^2) 246.0587 266.2838
       mean median
                            uq
                                      max neval
#> 1484.4255 1496.4808 1545.328 1591.2768
   302.2183 299.9772 310.943 413.7981
microbenchmark(DelayedArray::colSums(sparse_matrix ^ 2),
              DelayedMatrixStats::colSums2(sparse_matrix ^ 2),
              times = times)
#> Unit: milliseconds
#>
                                             expr
                                                       min
#>
          DelayedArray::colSums(sparse_matrix^2) 1368.0792 1402.4556
  DelayedMatrixStats::colSums2(sparse_matrix^2) 531.5231 567.5002
#>
#>
        mean
                median
                                       max neval
                              uq
#> 1486.7550 1466.0952 1545.2155 1652.8075
   582.7944 587.3182 602.8364 621.8481
microbenchmark(DelayedArray::colSums(rle_matrix ^ 2),
              DelayedMatrixStats::colSums2(rle_matrix ^ 2),
              times = times)
#> Unit: seconds
#>
                                         expr
                                                   min
                                                             lq
#>
          DelayedArray::colSums(rle_matrix^2) 2.617288 2.673016 2.765875
#> DelayedMatrixStats::colSums2(rle_matrix^2) 2.330117 2.380350 2.441969
#>
     median
                  uq
                          max neval
#> 2.715906 2.887769 2.987700
#> 2.418112 2.530877 2.547293
```

3.6 Summary

Bibliography