

# Implementation of the exponential function

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## Abstract

We show some basic capabilities of the LaTeX system: math, figures, references, sections...

## 1 The Exponential Function

The natural exponential function is defined as the function which is given as

$$f(x) = e^x \quad \text{where } e = 2.71828... \quad (1)$$

This function is its own derivative:

$$\frac{d}{dx}e^x = e^x \log_e e = e^x \quad (2)$$

In a plot, the exponential function looks as shown on Figure 1.

## 2 Approximations

As was shown from Figure 1, the exponential function is positive for all  $x \in \mathcal{R}$ . To describe the function at  $x < 0$  we see that we should converge towards 0 for  $x \rightarrow -\infty$ . A function that does exactly that is  $1/-x$ , which ensures a positive sign while the fraction ensures the convergence towards 0.

When looking at the values of  $x > 0$  we see that the function behaves as a parabolic function therefore making it tempting to approximate by  $x^2$ .

When  $x$  is around origin, we can use a power expansion on the exponential function which can be shown to give

$$e^x = \sum_n \frac{x^n}{n!} = 1 + x \left( 1 + \frac{1}{2}x \left( 1 + \frac{1}{3}x (...) \right) \right) \quad (3)$$

Plotting the approximate exponential function on top of the real, we acquire figure 2

