

# STL and templates

Paolo Joseph Baioni

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## Exercise 1 - What is a sparse matrix?

- ▶ A  $N \times N$  sparse matrix is a matrix whose number of non-zero elements  $N_{\text{nz}}$  is  $O(N)$ .
- ▶ The average number  $m$  of non-zero elements per row (or column) is constant w.r.t. the matrix size.
- ▶ If the majority of matrix entries is 0, *i.e.* if  $m \ll N$  it is convenient to store only the non-zero elements.
- ▶ The matrix-vector product (which is the basic ingredient of Krylov solvers) is  $O(N)$  rather than  $O(N^2)$ .

## Exercise 1 - Sparse matrix formats

Some (slightly revisited) classical data structures for sparse matrices

$$A = \begin{bmatrix} 4 & -1 & 0 & 0 \\ -1 & 4 & -1 & 0 \\ 0 & -1 & 4 & -1 \\ 0 & 0 & -1 & 4 \end{bmatrix}$$

COO (coordinates) or AIJ:

```
std::vector<double> A{4, -1, -1, ...};  
std::vector<int>    I{0, 0, 1, ...};  
std::vector<int>    J{0, 1, 0, ...};
```

triplet vector:

```
std::vector<std::tuple<int, int, double>>  
t{{0, 0, 4}, {0, 1, -1}, {1, 0, -1}, ...};
```

CSR (Compressed Sparse Row) or CRS (Compr. Row Storage) or Yale:

```
std::vector<double> val{4, -1, -1, 4, -1, -1, 4, -1, -1, 4};  
std::vector<int>    col_idx{0, 1, 0, 1, 2, 1, 2, 3, 2, 3};  
std::vector<int>    row_ptr{0, 2, 5, 8, 10}; // One entry per row.
```

# Exercise 1 - Typical operations with sparse matrices

- ▶ Insertion:

```
A[i][j] = x;
```

- ▶ Deletion:

```
A[i].erase(j);
```

- ▶ Random access:

```
x = A[i][j]; A[i][j] += y;
```

- ▶ Sequential traversing:

```
for (row : A)
{
    for (column : row)
        std::cout << column.value << " ";
    std::cout << std::endl;
}
```

- ▶ Matrix-vector multiplication:

```
std::vector<double> y = A * x;
```

## Exercise 1 - Inheriting from STL containers

- ▶ The C++ standard leaves a lot of freedom for implementation of containers.
- ▶ STL containers have non-virtual destructors.
- ▶ C.35: A base class destructor should be either public and virtual, or protected and non-virtual.

```
class Base {  
public:  
    ~Base { do_something(); }; // Non-virtual.  
}
```

```
class Derived : public Base {  
public:  
    MyComplexType member;  
    ~Derived { member.clear(); ... }  
}
```

```
Base *var = new Derived;  
delete var; // Calls var::~~Base() but not var::~~Derived()!
```

## Exercise 1 - Sparse matrix class

- ▶ Implement a C++ class to represent a sparse matrix based on STL containers.
- ▶ Simplify random access, allocation, entry increment, sequential traversing.

## Exercise 1 - Sparse matrix class

Implement the following methods:

*/// Convert row-oriented sparse matrix to AIJ format.*

**void**

```
aij(std::vector<double> &a,  
    std::vector<int> & i ,  
    std::vector<int> & j );
```

*/// Convert row-oriented sparse matrix to CSR format.*

```
void csr(std::vector<double> &a,  
         std::vector<int> & col_ind ,  
         std::vector<int> & row_ptr);
```

*/// Stream operator.*

```
friend std::ostream &  
operator<<(std::ostream &stream ,  
           sparse_matrix &M);
```

*/// Sparse matrix increment.*

```
void sparse_matrix::operator+=(sparse_matrix &other);
```

*/// Compute matrix-vector product.*

```
friend std::vector<double>  
operator*(sparse_matrix &M,  
          const std::vector<double> &x);
```

## Exercise 2 - Templates

Generalise the sparse matrix class using templates, to make it able to store any custom type instead of doubles only