A complete Newton solver using Eigen

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Newton solver

This example (a simplified version of Examples/src/NewtonSolver) is about a set of tools that implement generic Newton or quasi-Newton methods to determine the zero of a system of non-linear equations, based on the Eigen library.

The code structure is the following:

- NewtonTraits contains the definition of the types used by the main classes, to guarantee uniformity.
- ▶ JacobianBase is a base class which implements the action of a quasi-Jacobian: the user may choose among FullJacobian where the actual Jacobian (or an approximation of it) must be specified by the user, and DiscreteJacobian, that approximates the Jacobian via finite differences.
- JacobianFactory instantiates a concrete derived class of JacobianBase family on the fly.
- Newton applies the Newton method, given the non-linear system and a JacobianBase.
- ▶ NewtonOptions and NewtonResults encapsulate the input options and the output results.