Lexical Analysis

• Read source program and produce a list of tokens ("linear" analysis)



- The lexical structure is specified using regular expressions
- · Other secondary tasks:
 - (1) get rid of white spaces (e.g., \t, \n, \sp) and comments
 - (2) line numbering

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Lexical Analysis : Page 1 of 40

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The Lexical Structure

Output after the Lexical Analysis ---- token + associated value

LET 51 LPAREN 76 ID(int) 80	FUNCTION 56 ID(a) 77 COMMA 83	ID(do_nothing1) 65 COLON 78 ID(b) 85
COLON 86	ID(string) 88	. ,
EQ 95	ID(do_nothing2)	
LPAREN 110	ID(a) 111	PLUS 112
INT (1) 113	RPAREN 114	FUNCTION 117
<pre>ID(do_nothing2)</pre>	126	LPAREN 137
ID (d) 138	COLON 139	ID (int) 141
RPAREN 144	EQ 146	
<pre>ID(do_nothing1)</pre>	150	LPAREN 161
ID (d) 162	COMMA 163	STRING(str) 165
RPAREN 170	IN 173	
<pre>ID(do_nothing1)</pre>	177	LPAREN 188
INT (0) 189	COMMA 190	STRING(str2) 192
RPAREN 198	END 200	EOF 203

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Example: Source Code

A Sample Toy Program:

What do we really care here?

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Lexical Analysis: Page 2 of 40

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Tokens

• Tokens are the <u>atomic unit</u> of a language, and are usually <u>specific strings</u> or <u>instances</u> of <u>classes</u> of strings.

Tokens	Sample Values	Informal Description
LET	let	keyword LET
END	end	keyword END
PLUS	+	
LPAREN	(
COLON	:	
STRING	"str"	
RPAREN)	
INT	49, 48	integer constants
ID	do_nothing1, a, int, string	letter followed by letters, digits, and under- scores
EQ	=	
EOF		end of file

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Lexical Analysis, How?

• First, write down the <u>lexical specification</u> (how each token is defined?)

using **regular expression** to specify the lexical structure:

```
identifier = letter (letter | digit | underscore)* letter = a | \dots | z | A | \dots | Z digit = 0 | 1 | \dots | 9
```

 Second, based on the above lexical specification, build the lexical analyzer (to recognize tokens) by hand,

Regular Expression Spec ==> NFA ==> DFA ==> Transition Table ==> Lexical Analyzer

• Or just by using lex --- the lexical analyzer generator

Regular Expression Spec (in lex format) ==> feed to lex ==> Lexical Analyzer

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Regular Expressions and Regular Languages

- Given an alphabet Σ , the **regular expressions** over Σ and their corresponding **regular languages** are
 - a) \emptyset denotes \emptyset ; ε , the empty string, denotes the language $\{\varepsilon\}$.
 - b) for each a in Σ , a denotes { a } --- a language with one string.
 - c) if R denotes L_R and S denotes L_S then R / S denotes the language $L_R \cup L_S$, i.e, $\{ x \mid x \in L_R \text{ or } x \in L_S \}$.
 - d) if R denotes L_R and S denotes L_S then RS denotes the language L_RL_S , that is, $\{xy \mid x \in L_R \text{ and } y \in L_S \}$.
 - e) if R denotes L_R then R^* denotes the language L_R^* where L^* is the union of all L^1 (i=0,..., ∞) and L^1 is just $\{x_1x_2...x_i \mid x_1 \in L, ..., x_i \in L\}$.
 - f) if R denotes L_R then (R) denotes the same language L_R

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Regular Expressions

 regular expressions are concise, linguistic characterization of regular languages (regular sets)

- each regular expression define a regular language --- a <u>set of strings</u> over some alphabet, such as ASCII characters; each member of this set is called a sentence, or a word
- · we use regular expressions to define each category of tokens

For example, the above identifier specifies a set of strings that are a sequence of letters, digits, and underscores, starting with a letter.

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Example

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Regular Expression	Explanation	
a*	0 or more a's 1 or more a's	
a ⁺		
(a b)*	all strings of a's and b's (including ε)	
(aa ab ba bb)*	all strings of a's and b's of even length	
[a-zA-Z]	shorthand for "a $ b \dots z A \dots Z"$	
[0-9]	shorthand for "0 1 2 9"	
0([0-9])*0	numbers that start and end with 0	
(ab aab b)*(a aa e)	b)*(a aa e) ?	
? all strings that contain foo as substri		

• the following is **not** a regular expression:

 a^nb^n (n > 0)

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Lexical Analysis : Page 8 of 40

Lexical Specification

Using regular expressions to specify tokens

```
keyword = begin | end | if | then | else
identifier = letter (letter | digit | underscore)*
integer = digit+
relop = < | <= | = | <> | > | >=
letter = a | b | ... | z | A | B | ... | Z
digit = 0 | 1 | 2 | ... | 9
```

- Ambiguity: is "begin" a keyword or an identifier?
- Next step: to construct a token recognizer for languages given by regular expressions --- by using finite automata!

given a string x, the token recognizer says "yes" if x is a sentence of the specified language and says "no" otherwise

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Lexical Analysis : Page 9 of 40

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Transition Diagrams (cont'd)

The token recognizer (for identifiers) based on transition diagrams:

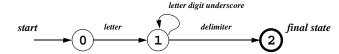
Next: 1. finite automata are generalized transition diagrams! 2. how to build finite automata from regular expressions?

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Transition Diagrams

- Flowchart with states and edges; each edge is labelled with characters; certain subset of states are marked as "final states"
- Transition from state to state proceeds along edges according to the next input character



- Every string that ends up at a final state is accepted
- If get "stuck", there is no transition for a given character, it is an error
- Transition diagrams can be easily translated to programs using case statements (in C).

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Lexical Analysis : Page 10 of 40

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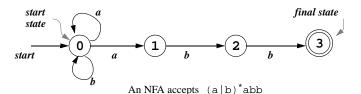
Finite Automata

- Finite Automata are similar to transition diagrams; they have states and labelled edges; there are one unique start state and one or more than one final states
- Nondeterministic Finite Automata (NFA):
 - a) ε can label edges (these edges are called ε -transitions)
 - b) some character can label 2 or more edges out of the same state
- Deterministic Finite Automata (DFA):
 - a) no edges are labelled with ϵ
 - b) each charcter can label at most **one** edge out of the same state
- NFA and DFA accepts string x if there exists a path from the start state to a
 final state labeled with characters in x

NFA: multiple paths **DFA:** one unique path

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Example: NFA

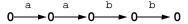


There are many possible moves --- to accept a string, we only need one sequence of moves that lead to a final state.

input string: aabb

One successful sequence: $0 \longrightarrow 0 \longrightarrow 1 \longrightarrow 2 \longrightarrow 1$

Another unsuccessful sequence:



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Lexical Analysis: Page 13 of

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Transition Table

• Finite Automata can also be represented using transition tables

For NFA, each entry is a set of states:

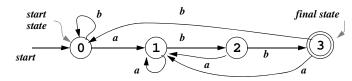
STATE	а	b
0	{0,1}	{0}
1	-	{2}
2	-	{3}
3	-	-

For DFA, each entry is a unique state:

STATE	а	b
0	1	0
1	1	2
2	1	3
3	1	0

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Example: DFA

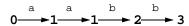


A DFA accepts (a|b)*abb

There is only one possible sequence of moves --- either lead to a final state and accept or the input string is rejected

input string: aabb

The sucessful sequence:



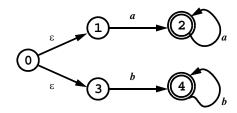
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Lexical Analysis: Page 14 of 40

NFA with ε-transitions

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1. NFA can have ϵ -transitions --- edges labelled with ϵ



accepts the regular language denoted by (aa*|bb*)

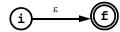
RE -> **NFA** (cont'd)

Regular Expressions -> NFA

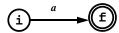
- How to construct NFA (with ε-transitions) from a regular expression?
- Algorithm: apply the following construction rules, use unique names for all the states. (inportant invariant: always one final state!)

1. Basic Construction

• ε



• $a \in \Sigma$



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Lexical Analysis: Page 17 of 40

: Page 17 of 40

• $R_1 \mid R_2$ i ϵ o N_1 o N_2 : NFA for R_2 the new and unique final state for N_1 and N_2 • $R_1 R_2$ merge: final state of N_1 and initial state of N_2

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2. "Inductive" Construction

Lexical Analysis : Page 18 of 40

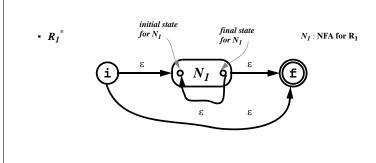
final state

 N_I : NFA for R_1

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RE -> **NFA** (cont'd)

2. "Inductive" Construction (cont'd)

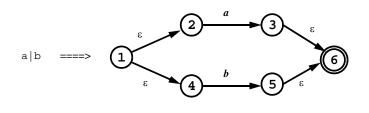


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Example: RE -> NFA

Converting the regular expression: (a|b)*abb

$$(in \ a|b) = 3$$



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Example : RE -> NFA (cont'd)

Converting the regular expression: (a|b) *abb

(a|b)*abb ====>

Example : RE -> NFA (cont'd)

Converting the regular expression: (a|b)*abb

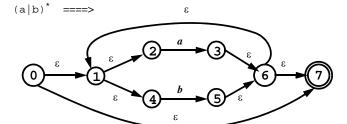
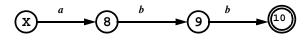


abb ====> (several steps are omitted)



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Lexical Analysis : Page 21 of 40

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Lexical Analysis : Page 22 of 40

$C\ S\ 4\ 2\ 1 \quad C\ O\ M\ P\ I\ L\ E\ R\ S \quad A\ N\ D \quad I\ N\ T\ E\ R\ P\ R\ E\ T\ E\ R\ S$

$NFA \rightarrow DFA$

- NFA are non-deterministic; need DFA in order to write a deterministic prorgam!
- There exists an algorithm ("subset construction") to convert any NFA to a DFA that accepts the same language
- States in DFA are sets of states from NFA; DFA simulates "in parallel" all possible moves of NFA on given input.
- Definition: for each state s in NFA,

 ε -CLOSURE(\mathbf{s}) = { \mathbf{s} } \cup { \mathbf{t} | \mathbf{s} can reach \mathbf{t} via ε -transitions }

• **Definition:** for each set of states **S** in NFA,

 ε -CLOSURE(S) = $\bigcup_i \varepsilon$ -CLOSURE(s) for all s_i in S

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NFA -> DFA (cont'd)

- each DFA-state is a **set** of NFA-states
- suppose the start state of the NFA is s, then the start state for its DFA is ε-CLOSURE(s); the final states of the DFA are those that include a NFA-final-state
- Algorithm: converting an NFA N into a DFA D----

```
Dstates = {e-CLOSURE(s<sub>0</sub>),s<sub>0</sub> is N's start state}
Dstates are initially "unmarked"
while there is an unmarked D-state X do {
    mark X
    for each a in S do {
        T = {states reached from any s<sub>i</sub> in X via a}
        Y = e-CLOSURE(T)
        if Y not in Dstates then add Y to Dstates "unmarked"
        add transition from X to Y, labelled with a
        }
}
```

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Lexical Analysis : Page 24 of 40

Example: NFA -> DFA

• converting NFA for (a|b) *abb to a DFA -----

The start state $A = \varepsilon$ -CLOSURE(0) = {0, 1, 2, 4, 7}; **Dstates**={A}

1st iteration: A is unmarked; mark A now; a-transitions: $T = \{3, 8\}$ a new state $B = \epsilon$ -CLOSURE(3) \cup ϵ -CLOSURE(8) $= \{3, 6, 1, 2, 4, 7\} \cup \{8\} = \{1, 2, 3, 4, 6, 7, 8\}$ add a transition from A to B labelled with a

b-transitions: $T = \{5\}$ a new state $C = \epsilon\text{-CLOSURE}(5) = \{1, 2, 4, 5, 6, 7\}$ add a transition from A to C labelled with b $\textbf{Dstates} = \{A, B, C\}$

2nd iteration: B, C are unmarked; we pick B and mark B first; $B = \{1, 2, 3, 4, 6, 7, 8\}$ B's a-transitions: T = $\{3, 8\}$; T's \$\varepsilon\$-CLOSURE is B itself. add a transition from B to B labelled with a

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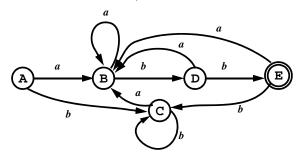
Lexical Analysis : Page 25 of 40

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Example : NFA -> DFA (cont'd)

E's a-transitions: $T = \{3, 8\}$; its ϵ -CLOSURE is B. add a transition from E to B labelled with a E's b-transitions: $T = \{5\}$; its ϵ -CLOSURE is C itself. add a transition from E to C labelled with b

all states in **Dstates** are marked, the DFA is constructed!



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Example : NFA -> DFA (cont'd)

B's b-transitions: $T = \{5, 9\}$; a new state $D = \epsilon$ -CLOSURE($\{5, 9\}$) = $\{1, 2, 4, 5, 6, 7, 9\}$ add a transition from B to D labelled with b **Dstates** = $\{A, B, C, D\}$

then we pick C, and mark C

C's a-transitions: $T = \{3, 8\}$; its ϵ -CLOSURE is B. add a transition from C to B labelled with a C's b-transitions: $T = \{5\}$; its ϵ -CLOSURE is C itself. add a transition from C to C labelled with b

next we pick D, and mark D

D's a-transitions: $T = \{3, 8\}$; its ϵ -CLOSURE is B. add a transition from D to B labelled with a D's b-transitions: $T = \{5, 10\}$; a new state $E = \epsilon$ -CLOSURE($\{5, 10\}$) = $\{1, 2, 4, 5, 6, 7, 10\}$ **Dstates** = $\{A, B, C, D, E\}$; E is a **final state** since it has 10;

next we pick E, and mark E

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Lexical Analysis : Page 26 of 40

Other Algorithms

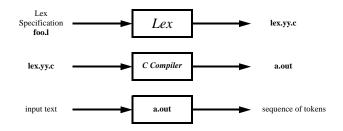
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- How to minimize a DFA? (see Dragon Book 3.9, pp141)
- How to convert RE to DFA directly? (see Dragon Book 3.9, pp135)
- How to prove two Regular Expressions are equivalent? (see Dragon Book pp150, Exercise 3.22)

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Lex

• Lex is a program generator ----- it takes lexical specification as input, and produces a lexical processor written in C.



• Implementation of Lex:

Lex Spec -> NFA -> DFA -> Transition Tables + Actions -> yylex()

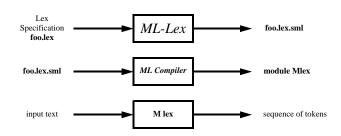
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Lexical Analysis : Page 29 of 40

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ML-Lex

• ML-Lex is like Lex ------ it takes lexical specification as input, and produces a lexical processor written in Standard ML.



• Implementation of ML-Lex is similar to implementation of Lex

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Lex Specification

- expression is a regular expression; action is a piece of C program;
- for details, read the **Lesk&Schmidt** paper

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Lexical Analysis : Page 30 of 40

 $C\ S\ 4\ 2\ 1 \quad C\ O\ M\ P\ I\ L\ E\ R\ S \quad A\ N\ D \quad I\ N\ T\ E\ R\ P\ R\ E\ T\ E\ R\ S$

ML-Lex Specification

```
type pos = int
                                         user's ML
val lineNum = ...
                                        declarations
val lexresult = ....
%%
%s COMMENT STRING;
SPACE=[ \t n\012];
                                    ml-lex definitions
DIGITS=[0-9];
%%
expression => (action);
                                      translation rules
integer
            => (print("INT"));
            => (...lineNum...);
                                       can call the above
                                       ML declarations
```

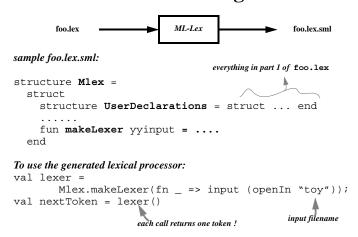
• <u>expression</u> is a regular expression; <u>action</u> is a piece of ML program; when the input matches the <u>expression</u>, the <u>action</u> is executed, the text matched is placed in the variable <u>yytext</u>.

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Lexical Analysis : Page 32 of 40

What does ML-Lex generate?



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 $C\ S\ 4\ 2\ 1 \quad C\ O\ M\ P\ I\ L\ E\ R\ S \quad A\ N\ D \quad I\ N\ T\ E\ R\ P\ R\ E\ T\ E\ R\ S$

ML-Lex Translation Rules

• Each translation rule (3rd part) are in the form

```
<start-state-list> regular expression => (action);
```

• Valid ML-Lex regular expressions: (see ML-Lex-manual pp 4-6)

a character stands for itself except for the reserved chars:

? * + | () ^ \$ / ; . = < > [{ " \
to use these chars, use backslash! for example, \\\" represents
the string \"

using square brackets to enclose a set of characters (\ - ^ are reserved)

```
[abc] char a, or b, or c
[^abc] all chars except a, b, c
[a-z] all chars from a to z
[\n\t\b] new line, tab, or backspace
[-abc] char - or a or b or c
```

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ML-Lex Definitions

• Things you can write inside the "ml-lex definitions" section (2nd part):

%reject REJECT() to reject a match
%count count the line number
%structure {identifier} the resulting structure name

(the default is Mlex)

define new start states

(hint: you probably don't need use %reject, %count,or %structure for assignment 2.)

<u>Definition of named regular expressions:</u>

<u>identifier</u> = <u>regular</u> <u>expression</u>

```
SPACE=[ \t n\012]
IDCHAR=[ a-zA-z0-9]
```

%s COMMENT STRING

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Lexical Analysis : Page 34 of 40

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ML-Lex Translation Rules (cont'd)

• Valid ML-Lex regular expressions: (cont'd)

escape sequences: (can be used inside or outside square brackets)

\b backspace \n newline \t tab

ddd any ascii char (ddd is 3 digit decimal)

any char except newline (equivalent to [^\n])

"x" match string x exactly even if it contains reserved chars

x? an optional x x* 0 or more x's x+ 1 or more x's

x | y x or y

^x if at the beginning, match at the beginning of a line only {x} substitute definition x (defined in the lex definition section)

(x) same as regular expression x

 $x\{n\}$ repeating x for n times

 $x\{m-n\}$ repeating x from m to n times

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Lexical Analysis : Page 33 of 40

ML-Lex Translation Rules (cont'd)

what are valid actions?

- Actions are basically ML code (with the following extensions)
- All actions in a lex file must return values of the same type
- Use yytext to refer to the current string

```
[a-z]+ => (print yytext);
[0-9]{3} => (print (Char.ord(sub(yytext,0))));
```

- Can refer to anything defined in the ML-Declaration section (1st part)
- YYBEGIN $\underline{\mathtt{start-state}}$ ----- enter into another start state
- lex() and continue() to reinvoking the lexing function
- yypos --- refer to the current position

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Lexical Analysis: Page 37 of 40

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Start States (or Start Conditions)

- <u>start states</u> permit multiple lexical analyzers to run together.
- each <u>translation rule</u> can be prefixed with <start-state>
- the lexer is initially in a predefined start stae called **INITIAL**
- define new start states (in ml-lex-definitions): %s COMMENT STRING
- to switch to another start states (in action):
 YYBEGIN COMMENT
- example: multi-line comments in C

```
%%
%s COMMENT
%%
<INITIAL>"/*" => (YYBEGIN COMMENT; continue());
<COMMENT>"*/" => (YYBEGIN INITIAL; continue());
<COMMENT>.|"\n" => (continue());
<INITIAL>......
```

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Ambiguity

- what if more than one translation rules matches?
 - A. <u>longest</u> match is preferred
 - B. among rules which matched the same number of characters, the rule given <u>first</u> is preferred

```
%%
%%
1 while => (Tokens.WHILE(...));
2 [a-zA-Z][a-zA-Z0-9_]* => (Tokens.ID(yytext,...));
3 "<" => (Tokens.LESS(...));
4 "<=" => (Tokens.LE(yypos,...));
```

```
input "while" matches rule 1 according B above
input "<=" matches rule 4 according A above</pre>
```

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Lexical Analysis : Page 38 of 40

Implementation of Lex

- construct NFA for <u>sum</u> of Lex translation rules (regexp/action);
- convert NFA to DFA, then minimize the DFA
- to recognize the input, simulate DFA to termination; find the <u>last</u> DFA state that includes NFA final state, execute associated action (this pickes longest match).
 If the last DFA state has >1 NFA final states, pick one for rule that appears first
- how to represent DFA, the transition table:

```
2D array indexed by state and input-character too big!
each state has a linked list of (char, next-state) pairs too slow!
hybrid scheme is the best
```

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