

To calculate the **Simple Matching Coefficient (SMC)** and **Jaccard Coefficient** between two binary variables P and Q , let's first define how these metrics work.

1. Simple Matching Coefficient (SMC)

The **Simple Matching Coefficient** measures the proportion of matches (both 1s and 0s) between two binary variables.

Formula:

$$\text{SMC} = \frac{(a + d)}{(a + b + c + d)}$$

Where:

- a : The number of times both P and Q are 1 (True Positive)
- d : The number of times both P and Q are 0 (True Negative)
- b : The number of times P is 1 and Q is 0 (False Negative)
- c : The number of times P is 0 and Q is 1 (False Positive)

2. Jaccard Coefficient

The **Jaccard Coefficient** measures the similarity between two sets, focusing only on the 1s.

Formula:

$$\text{Jaccard} = \frac{a}{(a + b + c)}$$

Where:

- a : The number of times both P and Q are 1 (True Positive)
- b : The number of times P is 1 and Q is 0 (False Negative)
- c : The number of times P is 0 and Q is 1 (False Positive)

Values from $P = (1, 1, 1, 1, 0, 1)$ and $Q = (1, 0, 0, 1, 1, 0)$:

P	Q	Matches (1-1 and 0-0)
1	1	$a = 1$
1	0	$b = 1$
1	0	$b = 1$
1	1	$a = 1$
0	1	$c = 1$
1	0	$b = 1$

Counts:

- $a = 2$ (both P and Q are 1)
- $b = 3$ (P is 1, Q is 0)
- $c = 1$ (P is 0, Q is 1)
- $d = 0$ (both P and Q are 0)

Simple Matching Coefficient (SMC):

$$\text{SMC} = \frac{(a + d)}{(a + b + c + d)} = \frac{(2 + 0)}{(2 + 3 + 1 + 0)} = \frac{2}{6} = 0.333$$

Jaccard Coefficient:

$$\text{Jaccard} = \frac{a}{(a + b + c)} = \frac{2}{(2 + 3 + 1)} = \frac{2}{6} = 0.333$$

Conclusion:

- Simple Matching Coefficient (SMC) = 0.333
- Jaccard Coefficient = 0.333

Both coefficients result in the same value in this case because there are no cases where both P and Q are 0, thus no true negatives.