

- **Course Title:** Engineering Cost Analysis & Economy (ENGR 222)
- **Session:** Fall 2024
- **Instructor:** Sudipta Chowdhury  
([chowdhurys@marshall.edu](mailto:chowdhurys@marshall.edu))
- **Class Time:** TR 9.30 AM-10.15 AM
- **Office hours:** TR 1.00 PM-2.30 PM



# **Independent Projects with Budget Limitation**

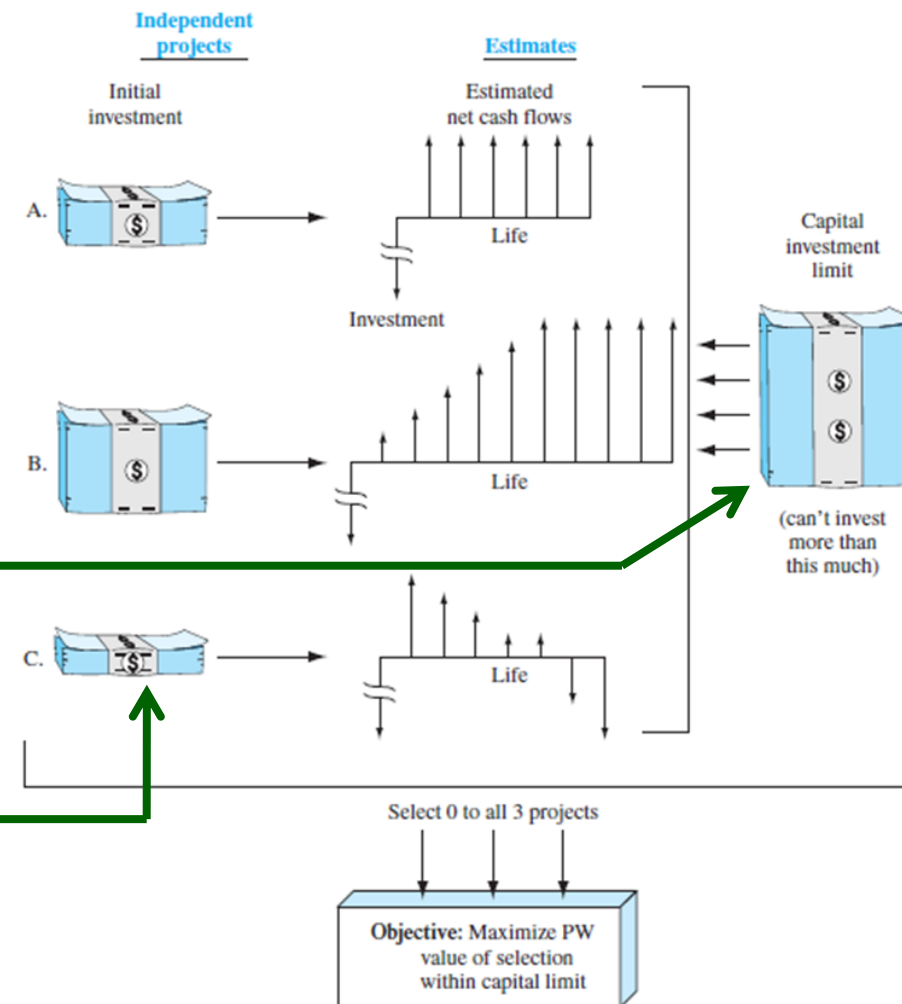
# Overview of Capital Rationing

Capital is a **scarce resource**;  
never enough to fund all  
projects

Each project is **independent of others**; select one, two, or more  
projects; don't exceed budget  
limit **b**

'**Bundle**' is a collection of  
independent projects that are  
**mutually exclusive (ME)**

For 3 projects, there are  
 $2^3 = 8$  ME bundles, e.g., A, B, C,  
AB, AC, BC, ABC, Do nothing  
(DN)



# Capital Budgeting Problem

Each project **selected entirely** or **not selected at all**

**Budget limit** restricts total investment allowed

Projects usually quite **different from each other** and have **different lives**

## *Objective of Capital Budgeting*

Maximize return on project investments using a specific measure of worth, usually PW

# Capital Budgeting for Equal-Life Projects

## Procedure

Develop  $\leq 2^m$  ME bundles that do not exceed budget  $b$

Determine NCF for projects in each viable bundle

Calculate PW of each bundle  $j$  at MARR (i)

$PW_j = \text{PW of bundle net cash flows} - \text{initial investment}$

$$= \sum_{t=1}^{t=n_j} NCF_{jt}(P/F, i, t) - NCF_{j0}$$

**Note:** Discard any bundle with  $PW < 0$ ; it does not return at least MARR

Select bundle with maximum PW (numerically largest)

Select projects to maximize PW at  $i = 15\%$  and  $b = \$70,000$

Project	Initial investment, \$	Annual NCF, \$	Life, years	Salvage value, \$
A	−25,000	+6,000	4	+4,000
B	−20,000	+9,000	4	0
C	−50,000	+15,000	4	+20,000

**Solution:** Five bundles meet budget restriction. Calculate NCF and PW values

**Conclusion:**  
Select projects  
**B and C**  
with max PW  
value

Bundle, j	Projects	NCF <sub>j0</sub> , \$	NCF <sub>jt</sub> , \$	SV, \$	PW <sub>j</sub> , \$
1	A	−25,000	+6,000	+4,000	−5,583
2	B	−20,000	+9,000	0	+5,695
3	C	−50,000	+15,000	+20,000	+4,261
4	A, B	−45,000	+15,000	+4,000	+112
<b>5</b>	<b>B, C</b>	<b>−70,000</b>	<b>+24,000</b>	<b>+20,000</b>	<b>+9,956</b>
6	DN	0	0	0	0



**LCM is not necessary** in capital budgeting; use PW over respective lives to select independent projects

**Same procedure** as that for equal lives

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**Example:** If MARR is 15% and  **$b = \$20,000$**  select projects

Project	Initial Investment, \$	Annual Net Cash Flow, \$	Project Life, Years
A	−8,000	3870	6
B	−15,000	2930	9
C	−8,000	2680	5
D	−8,000	2540	4





# Capital Budgeting Using LP Formulation

Why use linear programming (LP) approach? --

Manual approach not good for large number of projects as  $2^m$  ME bundles grows too rapidly

Apply 0-1 integer LP (ILP) model to:

- **Objective:** Maximize Sum of PW of NCF at MARR for projects
- **Constraints:** Sum of investments  $\leq$  investment capital limit  
Each project selected ( $x_k = 1$ ) or not selected ( $x_k = 0$ )

LP formulation strives to maximize  $Z$

$$\text{Maximize: } \sum_{k=1}^{k=m} PW_k X_k = Z$$

$$\text{Constraints: } \sum_{k=1}^{k=m} NCF_{k0} X_k \leq b$$

$$x_k = 0 \text{ or } 1 \quad \text{for } k = 1, 2, \dots, m$$

## Example: LP Solution of Capital Budgeting Problem

**MARR is 15%; limit is \$20,000; select projects using LP**

Project	Initial Investment, \$	Annual Net Cash Flow, \$	Project Life, Years	PW @ 15%, \$
A	−8,000	3870	6	6646
B	−15,000	2930	9	−1019
C	−8,000	2680	5	984
D	−8,000	2540	4	−748

**LP formulation for projects A, B, C, D labeled  $k = 1, 2, 3, 4$  and  $b = \$20,000$  is:**

**Maximize:**  $6646x_1 - 1019x_2 + 984x_3 - 748x_4$

**Constraints:**  $8000x_1 + 15,000x_2 + 8000x_3 + 8000x_4 \leq 20,000$   
 $x_1, x_2, x_3, \text{ and } x_4 = 0 \text{ or } 1$

## Let's Practice

The independent project estimates below have been developed by the engineering and finance managers. The corporate MARR is 8% per year, and the capital investment limit is \$4 million. Use linear programming and spreadsheet to solve it.

Project	Project Cost, \$ M	Life, Years	NCF, \$ per Year
1	-1.5	8	360,000
2	-3	10	600,000
3	-1.8	5	520,000
4	-2	4	820,000

QUESTIONS?