

Portfolio

I. Proposition

A. For $A, B \subseteq U$, $(A-B) \cup (B-A) = (A \cup B) - (A \cap B)$.

1. Proof.

a. I will prove the following proposition.

$$\forall A, A \subseteq U \quad \forall B, B \subseteq U \quad A \cap B^C = \emptyset \Leftrightarrow A \subseteq B$$

1. Here \Leftrightarrow is used to denote "is logically equivalent to" or "if and only if", or "iff". The letter \emptyset is used to denote the empty set $\{\}$. The letter U is used to denote the universal set and the superscript C is used to denote the set complement.

b. Let A and B be subsets of some universal set U .

c. $(A \subseteq U) \wedge (B \subseteq U)$.

d. We will prove the propositions contrapositive.

1. The contrapositive is $A \cap B^C \neq \emptyset \Rightarrow A \not\subseteq B$.

e. Assume $A \cap B^C \neq \emptyset$. We will prove there must exist an element $p \mid (p \in A) \wedge (p \notin B)$.

$$\begin{aligned} \text{f. } (A \cap B^C \neq \emptyset \therefore (\exists p, p \in A \cap B^C) \therefore \\ (\exists p, (p \in A) \wedge (p \in B^C)) \therefore (\exists p, (p \in A) \wedge (p \notin B)) \therefore A \not\subseteq B \end{aligned}$$

B. Enter level 2 text here.

1. Enter level 3 text here.

2. Enter level 3 text here.

3. Enter level 3 text here.

C. Enter level 2 text here.

1. Enter level 3 text here.

2. Enter level 3 text here.

a. Enter level 4 text here.

b. Enter level 4 text here.

1. Enter level 5 text here.

2. Enter level 5 text here.

3. Enter level 5 text here.

c. Enter level 4 text here.

1. Enter level 5 text here.

2. Enter level 5 text here.

a. Enter level 6 text here.

b. Enter level 6 text here.