

If a divides b or a divides c then a divides bc ,

~~it~~ does

If A does not divide BC then A does not divide
 B and A ~~and~~ does not divide C .

$$P=T \quad Q=T \quad U=F \quad V=F \quad W=T \text{ or } F$$

$$1 \quad (P \vee Q) \wedge (U \wedge W) = (T \vee T) \wedge (F \wedge T) \quad \text{w is true}$$

$$\swarrow \quad \text{or} \quad (T \vee T) \wedge (F \wedge F) \quad \text{w is false}$$

$$(T) \vee F = T$$

$$\oplus \quad \text{or} \quad \downarrow$$

$$T \vee F = T$$

The statement is a tautology.

$$2 \quad (U \wedge \neg V) \Rightarrow (P \wedge W)$$

$$(F \wedge \neg F) \Rightarrow (T \wedge T) \quad \text{if w is true}$$

$$(F \wedge T) \Rightarrow T$$

$$F \Rightarrow T$$

^T the statement is true when w is true.

$$(U \wedge \neg V) \Rightarrow (P \wedge W)$$

$$(F \wedge \neg F) \Rightarrow (T \wedge F) \quad \text{if w is false}$$

$$(F \wedge T) \Rightarrow F$$

$$F \Rightarrow F$$

^T the statement is also true when w is false.

The statement is a tautology. w is a "don't care" term.

$$3 \quad W \Rightarrow (P \vee U)$$

$$W \Rightarrow (I \wedge F)$$

$$W \Rightarrow F$$

If ~~W~~ W is false the statement is true.

If W is true true implies false is false, so we don't know if the statement #3 is true or false.

$$4 \quad P \wedge (W \Rightarrow Q)$$

$$T \wedge (W \Rightarrow T)$$

This

If W is true

$$T \wedge (T \Rightarrow T)$$

$$T \wedge T$$

$$T$$

If ~~W~~ W is false

$$T \wedge (F \Rightarrow T)$$

This is a vacuous truth.

Therefore statement #4 is a tautology.

$$(P \vee R) \wedge (\neg Q \vee R) \equiv (P \Rightarrow Q) \Rightarrow R$$

$$(R \vee P) \wedge (R \vee \neg Q) \equiv (P \Rightarrow Q) \Rightarrow R \quad \text{Commutative property of } \vee$$

$$R \vee (P \wedge \neg Q) \equiv (P \Rightarrow Q) \Rightarrow R \quad \text{Distributive property}$$

$$(P \wedge \neg Q) \vee R \equiv (P \Rightarrow Q) \Rightarrow R \quad \text{Commutative property of } \vee$$

$$\neg(\neg(P \wedge \neg Q)) \vee R \equiv (P \Rightarrow Q) \Rightarrow R \quad \text{Double Negation Property}$$

$$\neg(P \wedge \neg Q) \Rightarrow R \equiv (P \Rightarrow Q) \Rightarrow R$$

$$\neg(\neg(P \Rightarrow Q)) \Rightarrow R \equiv (P \Rightarrow Q) \Rightarrow R$$

$$(P \Rightarrow Q) \Rightarrow R \equiv (P \Rightarrow Q) \Rightarrow R$$