

## Abstract

Ultra high energy cosmic rays and astrophysical neutrinos are two of the most energetic observables we have into the universe, yet their origins remain a mystery. Each class of particles has different advantages and disadvantages when it comes to determining their sources. I will present techniques well suited for each class. For cosmic rays, ground based experiments can't see the whole sky and I will discuss the penalty they pay for this. For neutrinos, I will present a general technique for determining their origin.

# Finding Anisotropies in Cosmic Rays and Neutrinos

Peter B. Denton

NBIA Astroparticle Seminar

April 24, 2017

[1409.0883](#), [1505.03922](#), [1703.09721](#)  
with Tom Weiler and Danny Marfatia

[github.com/PeterDenton/ANA](https://github.com/PeterDenton/ANA)

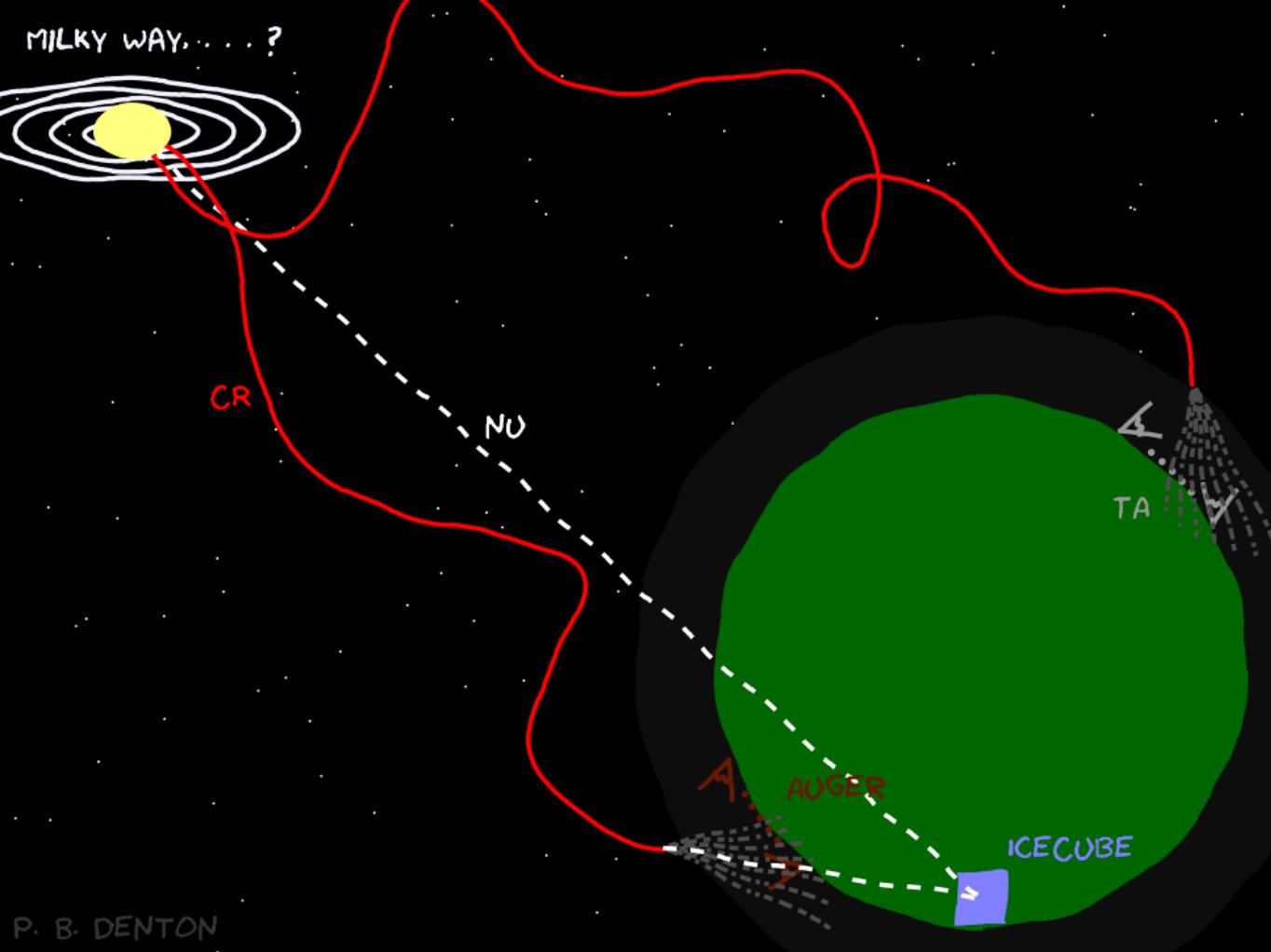


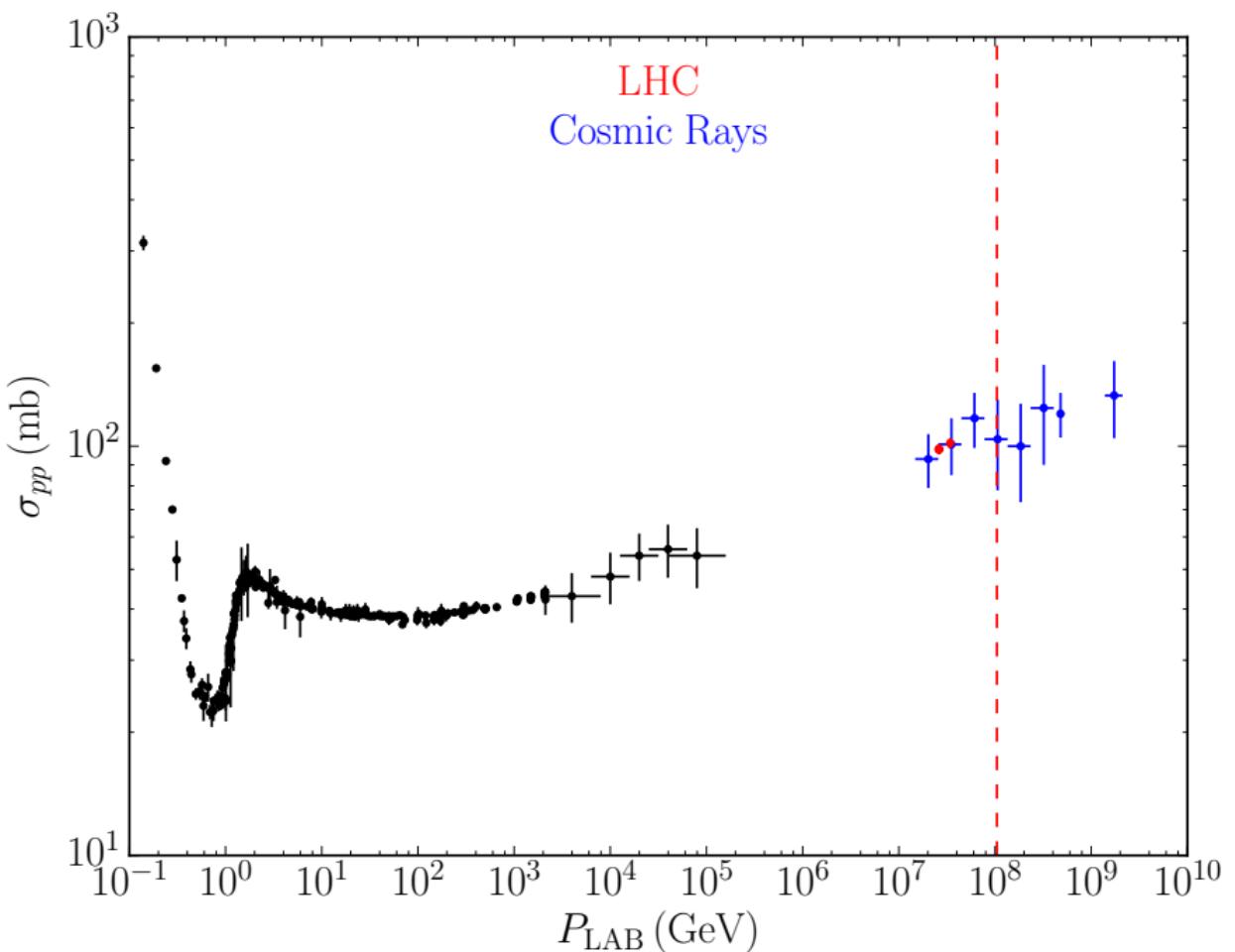
The Niels Bohr  
International Academy

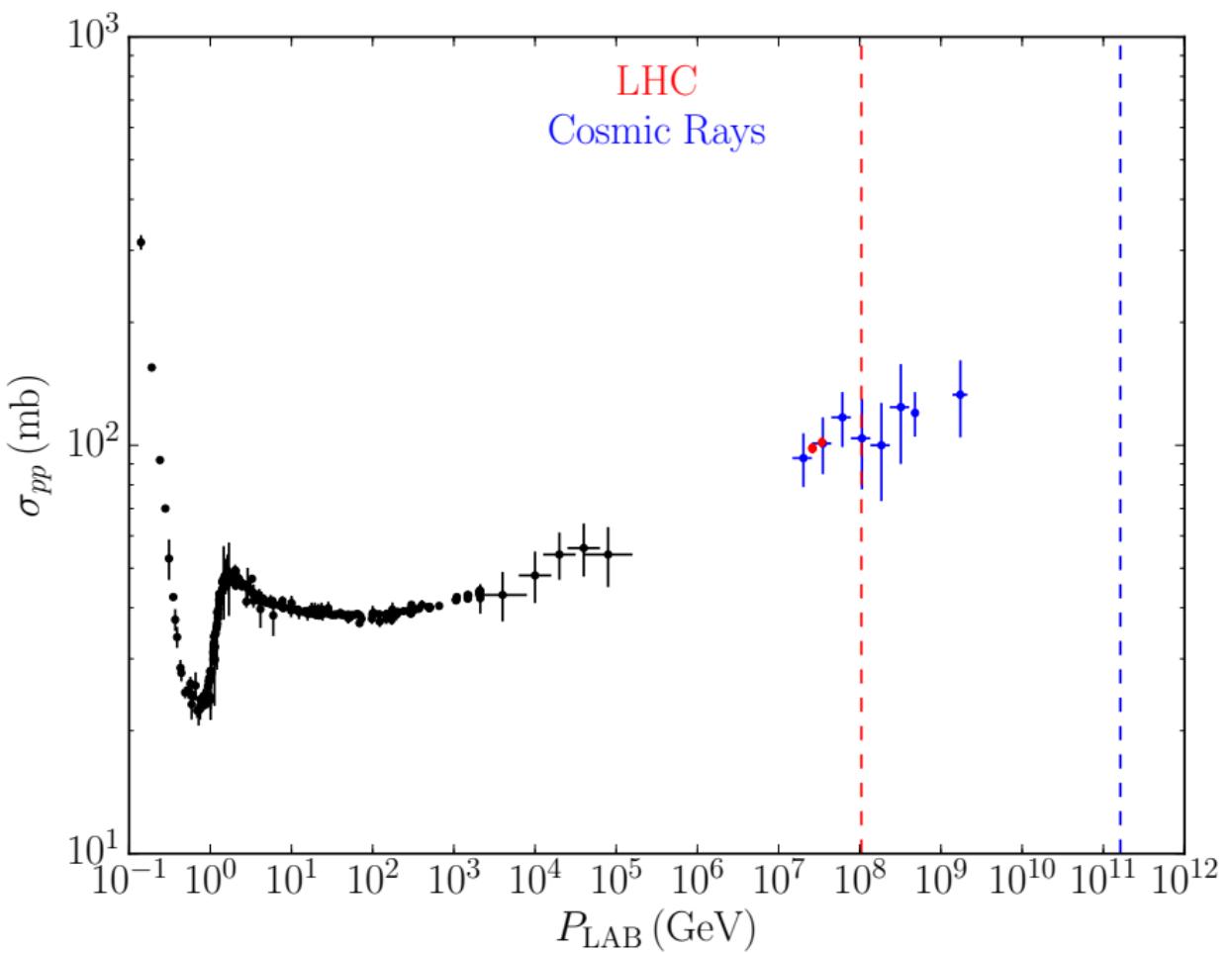
VILLUM FONDEN



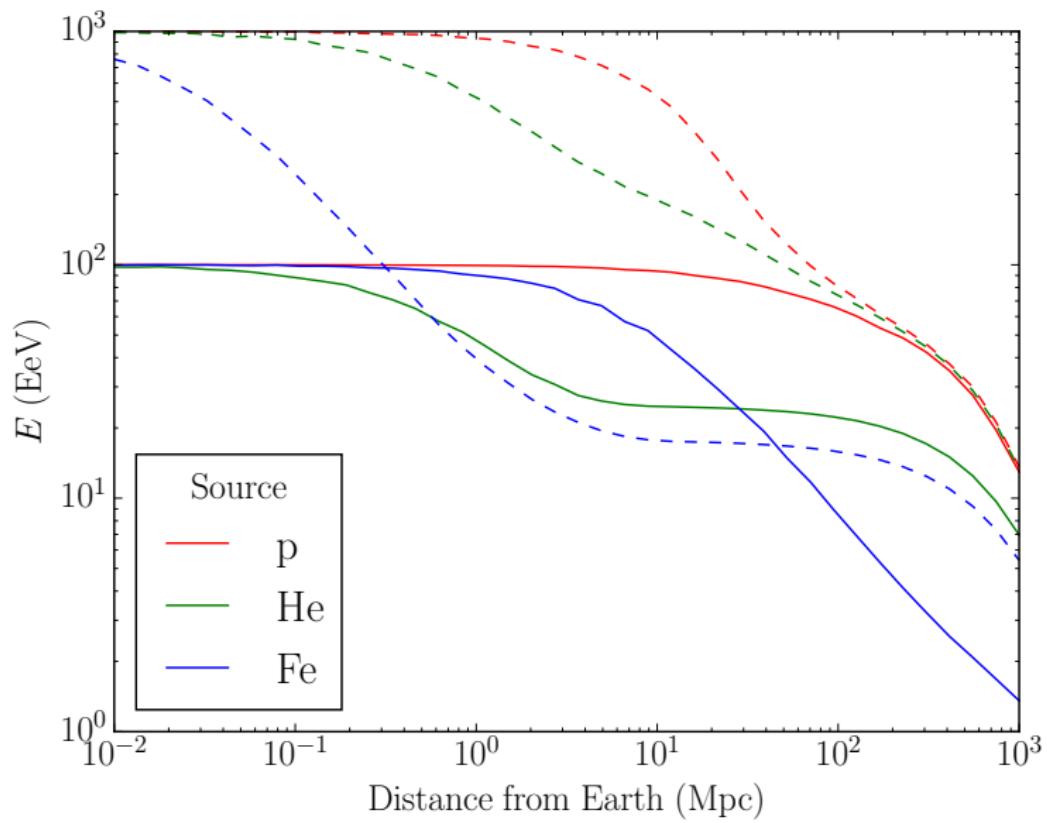
MILKY WAY... . . . ?







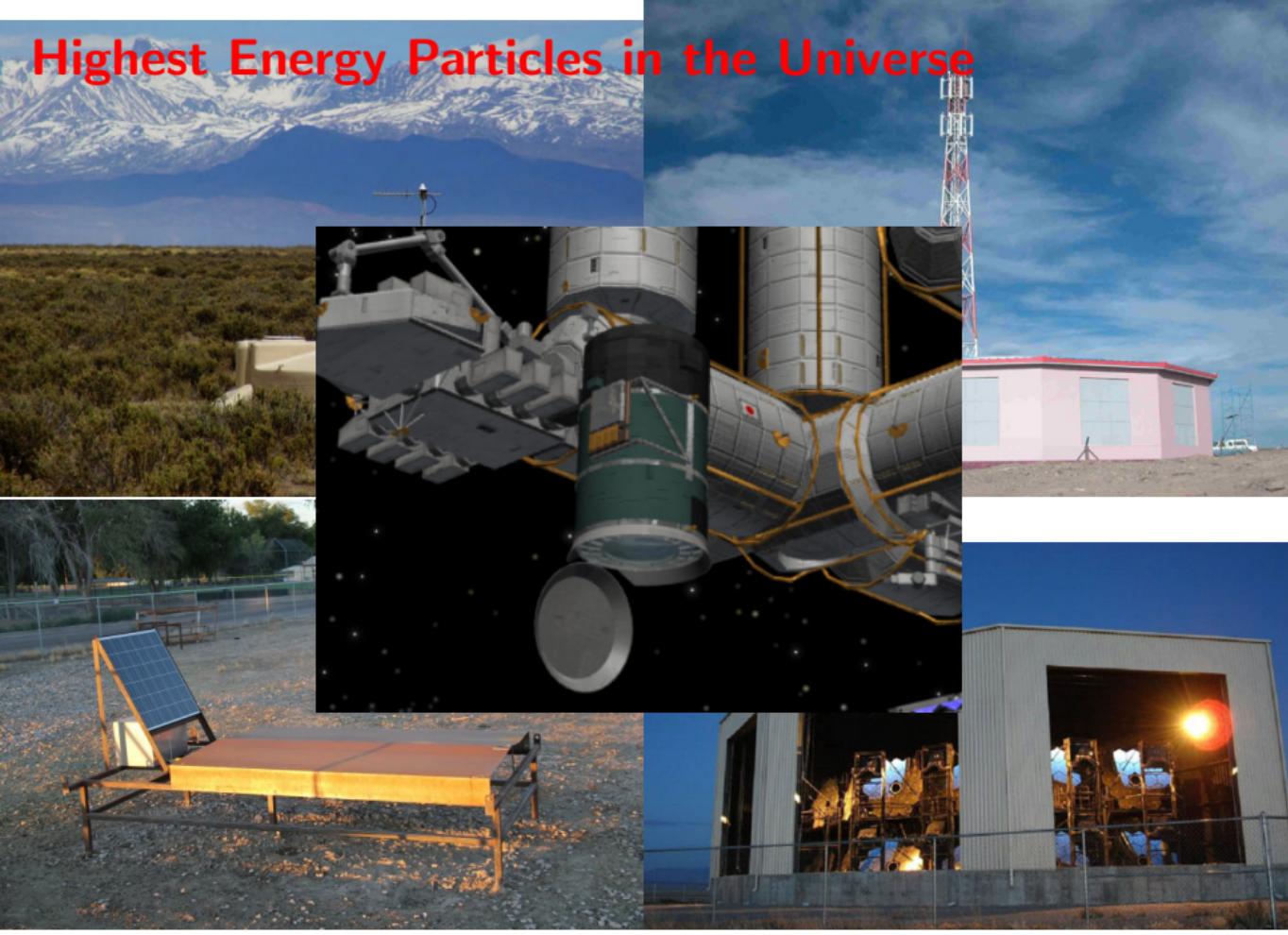
# Energy Loss Rates



# Highest Energy Particles in the Universe



# Highest Energy Particles in the Universe



# UHECR Anisotropy Unknowns

- ▶ How strong are the magnetic fields inside and between galaxies?  
Pshirkov et. al.: [1103.0814](#)  
Jansson, Farrar: [1204.3662](#)
- ▶ What is the composition of UHECRs? Protons? Iron nuclei?
- ▶ What are the sources of UHECRs?
- ▶ How are UHECRs accelerated to such extreme energies?

Gunn, Ostriker: PRL 22 (1969)

Pruet, Guiles, Fuller: [astro-ph/0205056](#)

Groves, Heckman, Kauffmann: [astro-ph/0607311](#)

Fang, Kotera, Olinto: [1201.5197](#)

- ▶ What is the cause of the suppression at the end of the spectrum?
- ▶ New physics...?

## UHECR Anisotropy Knowns

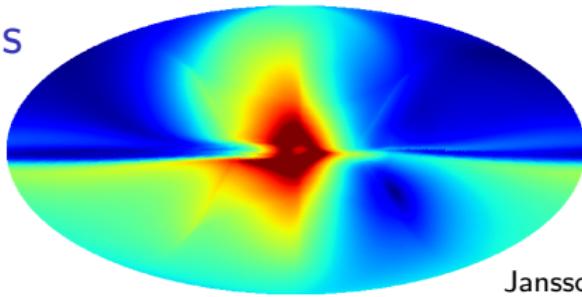
- ▶ UHECRs can't be contained by the Milky Way's magnetic field  $\Rightarrow$  extragalactic.
- ▶ UHECRs with energies above  $\sim 50$  EeV lose energy via interactions with the CMB.

Greisen: [PRL 16 \(1966\)](#)

Zatsepin, Kuzmin: [JETP Lett. 4 \(1966\)](#)

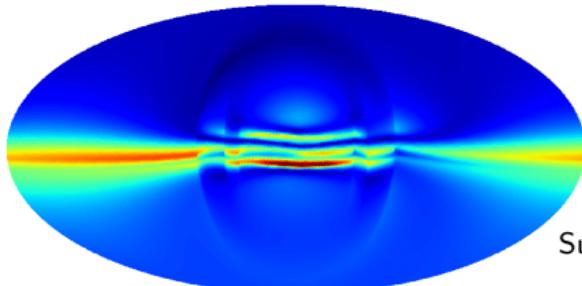
- ▶ UHECR sources must be close  $\Rightarrow$  anisotropies.
- ▶ UHECRs bend in Galactic and extragalactic magnetic fields.
- ▶ No conclusive anisotropies found yet.

# Galactic $B$ Fields

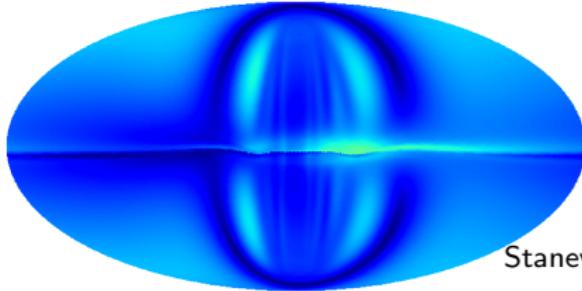


60 EeV proton

Jansson, Farrar: 1204.3662



Sun, et. al.: 0711.1572

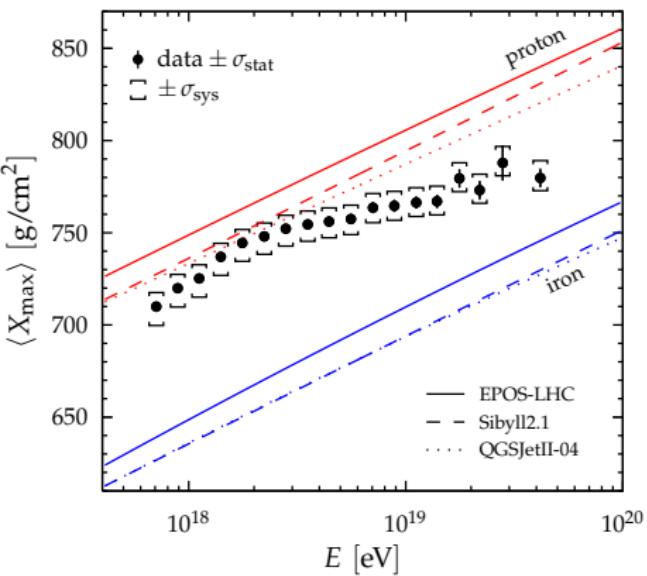


Stanev: astro-ph/9607086

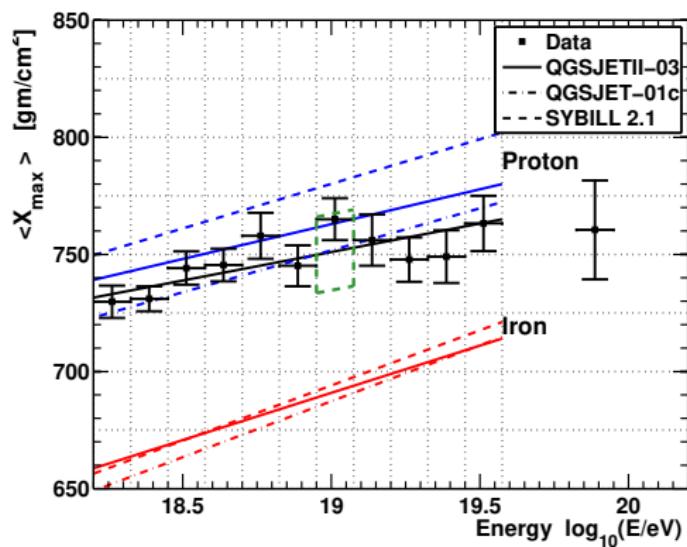


# Composition

Auger: heavy composition



TA: light composition

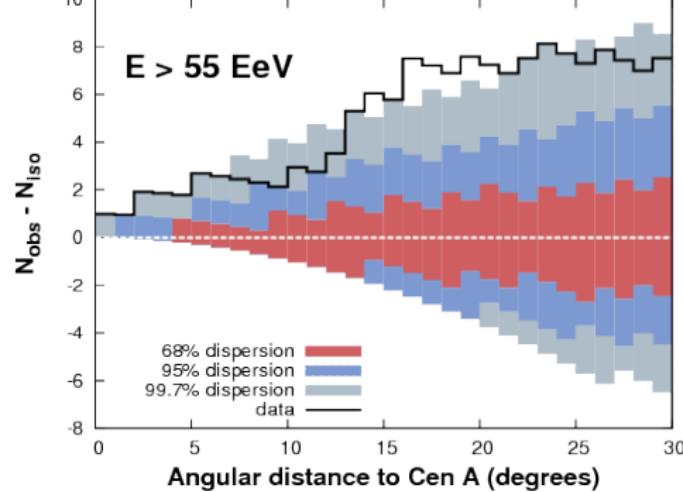


Disagreement.

Auger and TA: [1503.07540](#)

# UHECR Anisotropy Searches

Targeted searches  
have weak evidence.

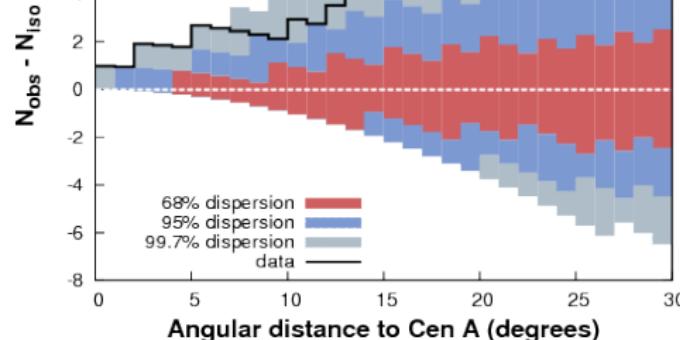


Auger: [1207.4823](#)

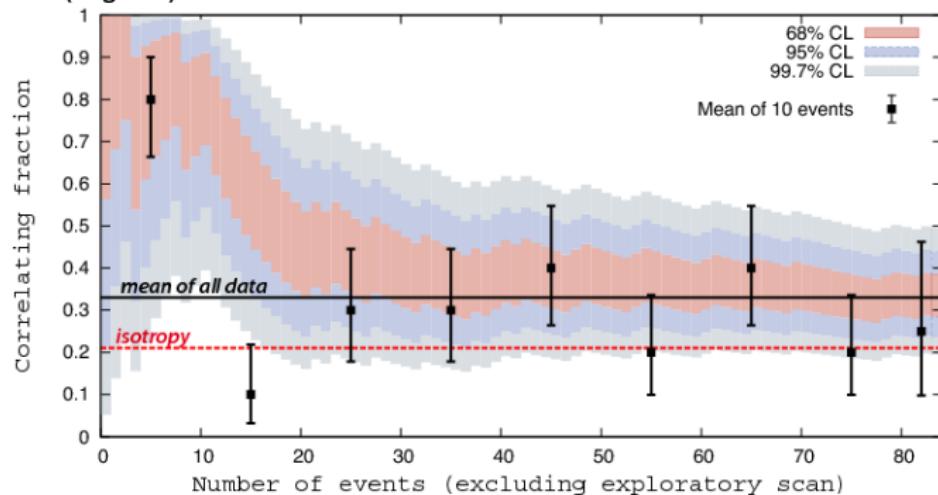
$E > 55 \text{ EeV}$

# UHECR Anisotropy Searches

Targeted searches  
have weak evidence.

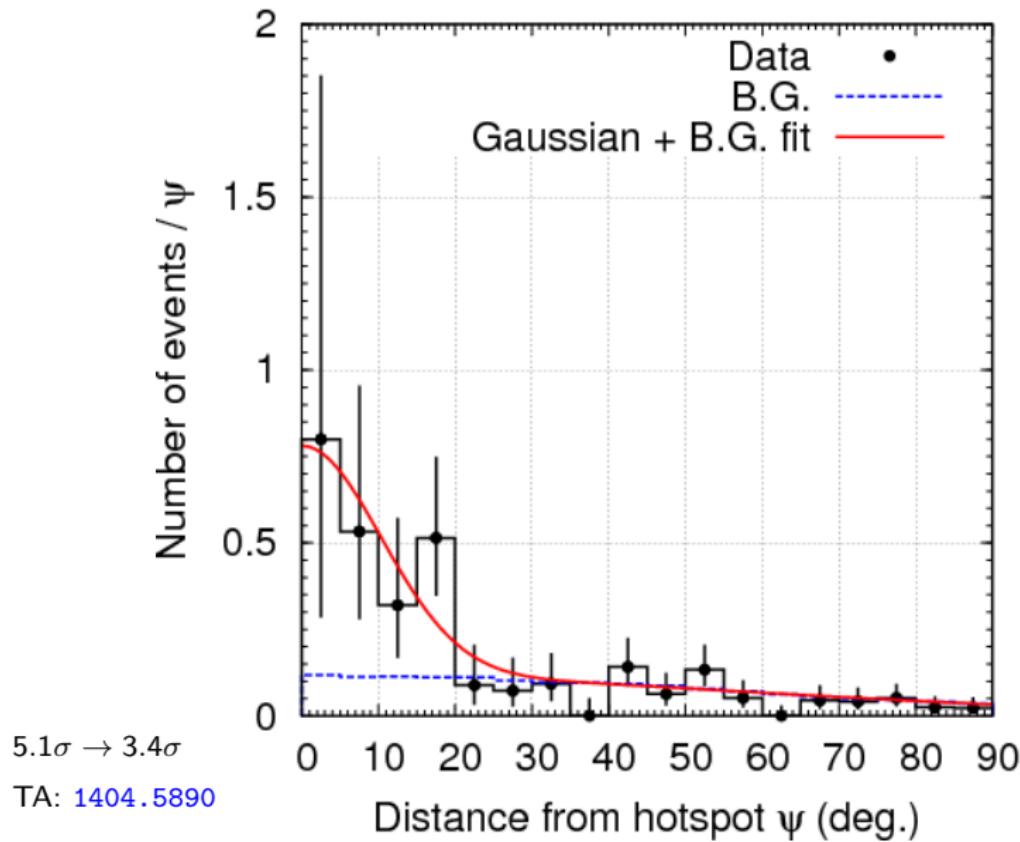


Angular distance to Cen A (degrees)



Auger: 1207.4823

# UHECR Anisotropy Searches



# Spherical Harmonics: Distributions on the Sky

- ▶  $Y_\ell^m$ 's provide an orthogonal expansion of any distribution on the sky.
- ▶ Useful in low statistics, high uncertainty experiments:
  - ▶ unknown magnetic fields,
  - ▶ unknown UHECR composition.
- ▶ The true distribution as seen at earth:

$$I(\Omega) = \sum_{\ell,m} a_\ell^m Y_\ell^m(\Omega).$$

- ▶ The power spectrum is rotational invariant.

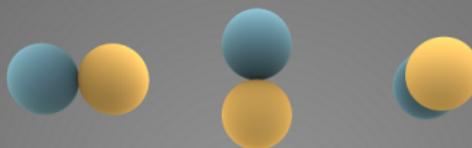
$$C_\ell = \frac{1}{2\ell+1} \sum_m |a_\ell^m|^2.$$

# Spherical Harmonics Visualizations

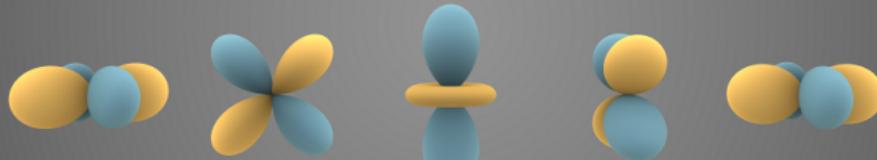
$\ell = 0$



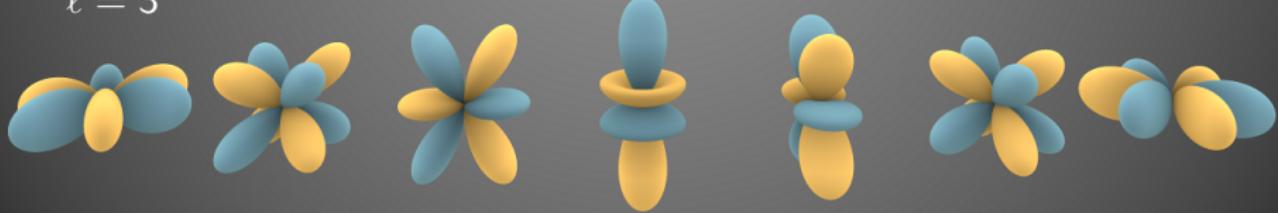
$\ell = 1$



$\ell = 2$



$\ell = 3$



[en.wikipedia.org/wiki/Spherical\\_harmonics](https://en.wikipedia.org/wiki/Spherical_harmonics)

# Spherical Harmonics: Possible Sources

Identifiable sources: Cen A, TA hotspot, supergalactic plane, etc.  
use specific  $Y_\ell^m$ 's.

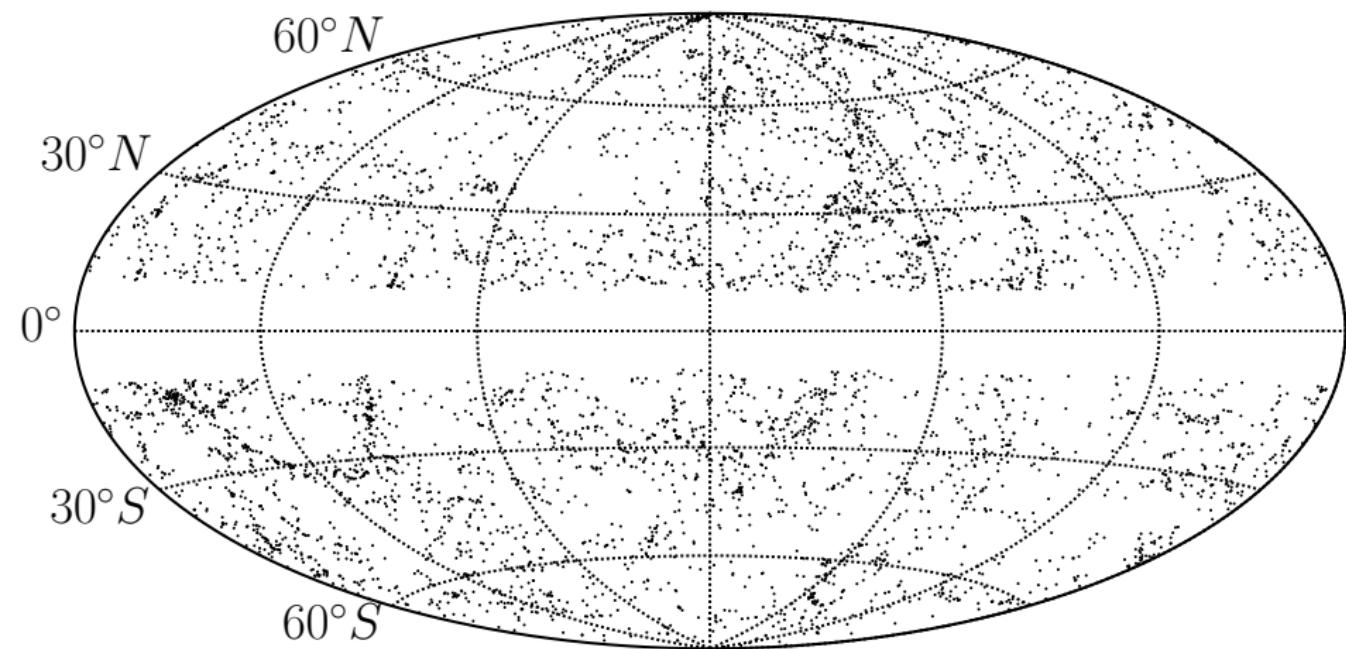
$$\begin{aligned} \text{Point source} &\Rightarrow \text{dipole: } I_D \propto a_0^0 Y_0^0 + a_1^0 Y_1^0. \\ \text{Planar source} &\Rightarrow \text{quadrupole: } I_Q \propto a_0^0 Y_0^0 + a_2^0 Y_2^0. \end{aligned}$$

Each  $Y_\ell^m$  partitions the sky into nodal zones,

$$\langle N_Z(\ell) \rangle = \frac{\ell+1}{3(2\ell+1)} (2\ell^2 + 4\ell + 3) \xrightarrow[\ell \rightarrow \infty]{} \frac{\ell^2}{3},$$

so  $\ell_{\max} < \sqrt{3N}$ .

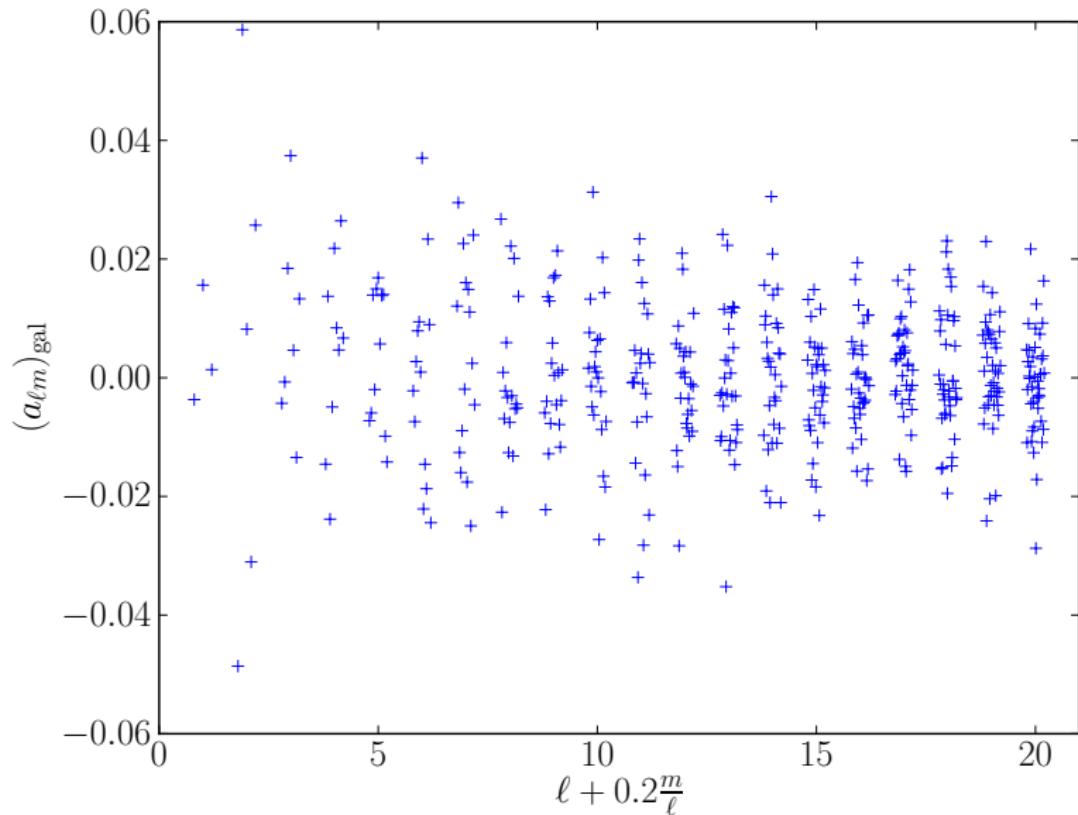
# 2MRS Sky Map



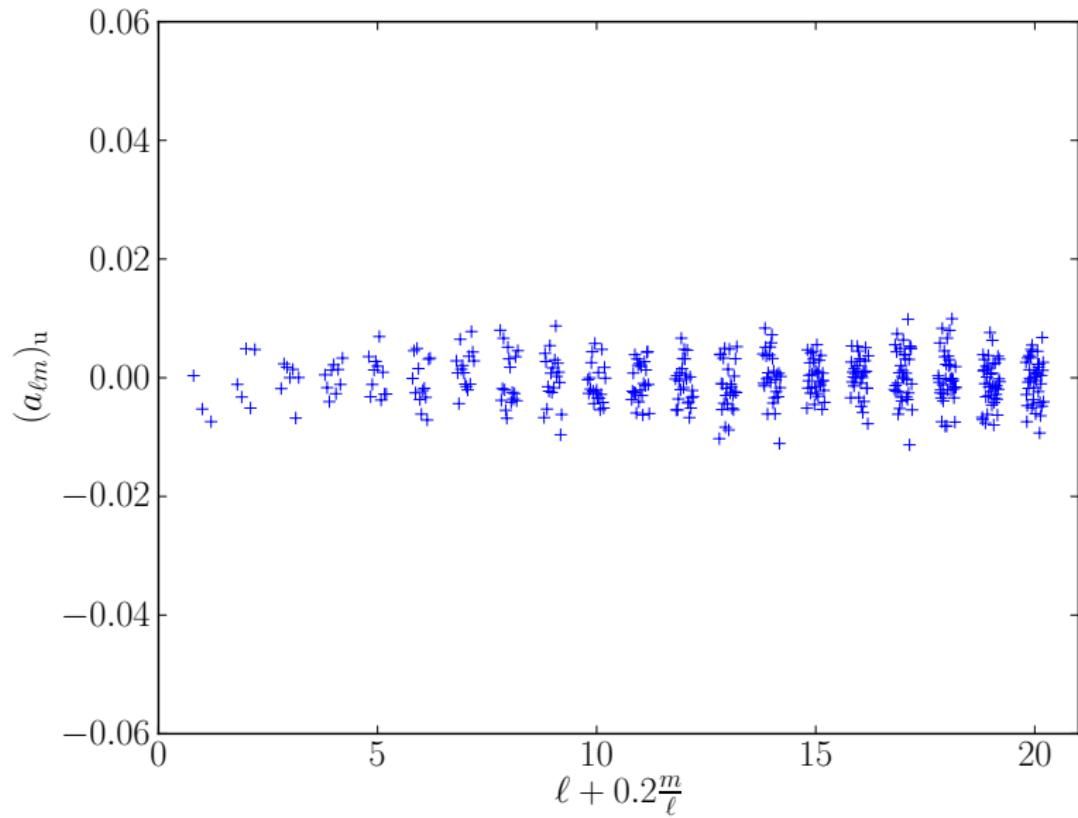
Structure in the local universe  $\Rightarrow$  anisotropies in UHECRs.

2MRS: 1108.0669

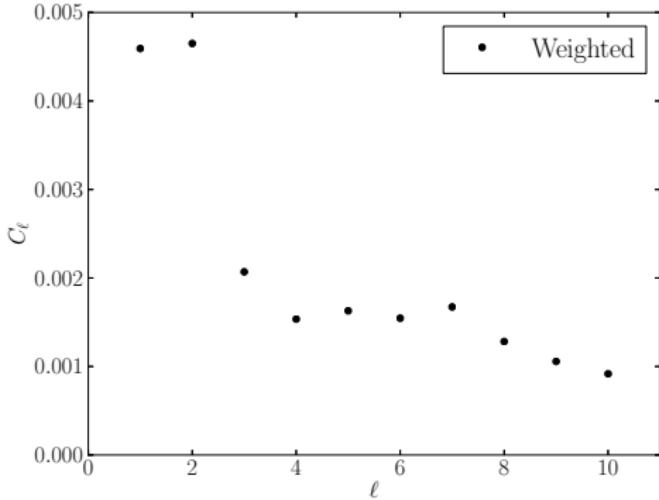
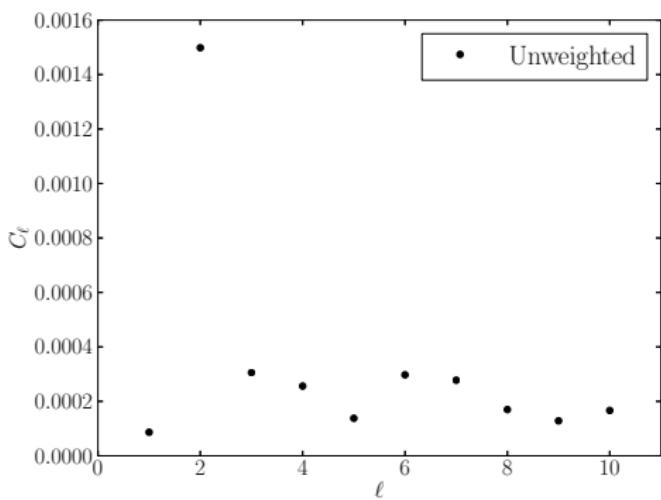
# Spherical Harmonic Coefficients: Galaxies



# Spherical Harmonic Coefficients: Uniform

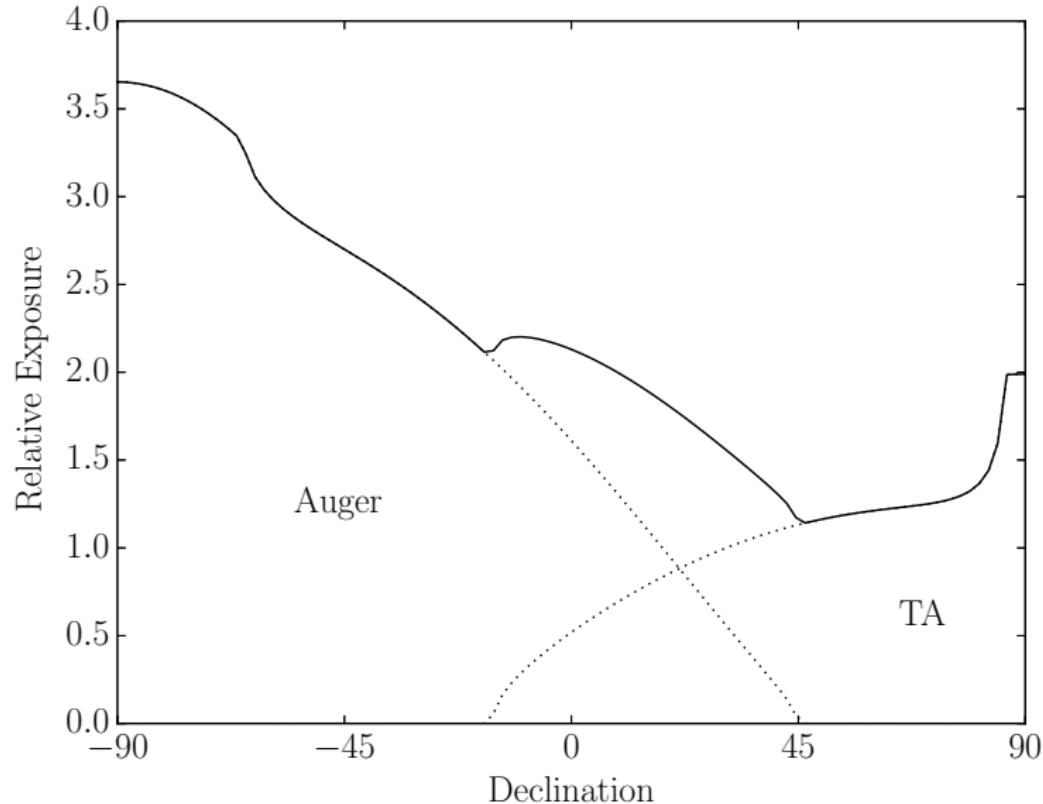


# Spherical Harmonics: Possible Sources



Dipole and quadrupole: well motivated.

# Auger and TA's Nonuniform Partial Sky Coverage



# Auger and TA Exposure Combination

Combined exposure:

$$\omega(\Omega, b) = \omega_{\text{TA}}(\Omega) + b\omega_{\text{Auger}}(\Omega)$$

“Fudge factor”:

$$\bar{b}^{(0)} = \frac{\Delta N_{\text{Auger}}}{\Delta N_{\text{TA}}} \frac{\int_{\Delta\Omega} d\Omega \omega_{\text{TA}}(\Omega)}{\int_{\Delta\Omega} d\Omega \omega_{\text{Auger}}(\Omega)}$$

P. Billoir for Auger [1403.6314](#)

Problems:

1. Statistics are low in the intersection region.
2.  $\bar{b}^{(0)}$  is a zeroth order approximation to  $b$  under the assumption of isotropy.
3. Corrections to  $\bar{b}^{(0)}$  need to be fit iteratively along with anisotropy parameters.
4. Large systematic energy uncertainty between the experiments.

# Anisotropy Measures

A general anisotropy measure:

$$\alpha \equiv \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} \in [0, 1].$$

Define

$$\alpha_D \equiv \sqrt{3} \frac{|a_1^0|}{a_0^0} \quad \alpha_Q \equiv \frac{-3 \sqrt{\frac{5}{4} \frac{a_2^0}{a_0^0}}}{2 + \sqrt{\frac{5}{4} \frac{a_2^0}{a_0^0}}} \quad (\text{'New' later}),$$

Then  $\alpha_D = \alpha$  for a purely dipolar distribution and  $\alpha_Q = \alpha$  for a purely quadrupolar distribution.

# Reconstructing $a_\ell^m$ 's for Nonuniform Partial Sky Coverage

Nonuniform exposure is a manageable problem:

$$\bar{a}_\ell^m = \frac{1}{N} \sum_i^N Y_\ell^{m*}(\Omega_i) \rightarrow \frac{1}{N} \sum_i^N \frac{Y_\ell^{m*}(\Omega_i)}{\omega(\Omega_i)},$$

where  $\mathcal{N} = \sum_i^N \frac{1}{\omega(\Omega_i)}$ ,  
 $\omega$  is the exposure function.

Sommers: [astro-ph/0004016](#)

# Reconstructing $a_\ell^m$ 's for Nonuniform Partial Sky Coverage

Nonuniform exposure is a manageable problem:

$$\bar{a}_\ell^m = \frac{1}{N} \sum_i^N Y_\ell^{m*}(\Omega_i) \rightarrow \frac{1}{N} \sum_i^N \frac{Y_\ell^{m*}(\Omega_i)}{\omega(\Omega_i)},$$

where  $\mathcal{N} = \sum_i^N \frac{1}{\omega(\Omega_i)}$ ,  
 $\omega$  is the exposure function.

Sommers: [astro-ph/0004016](#)

Partial sky is more challenging: no information from part of the sky.

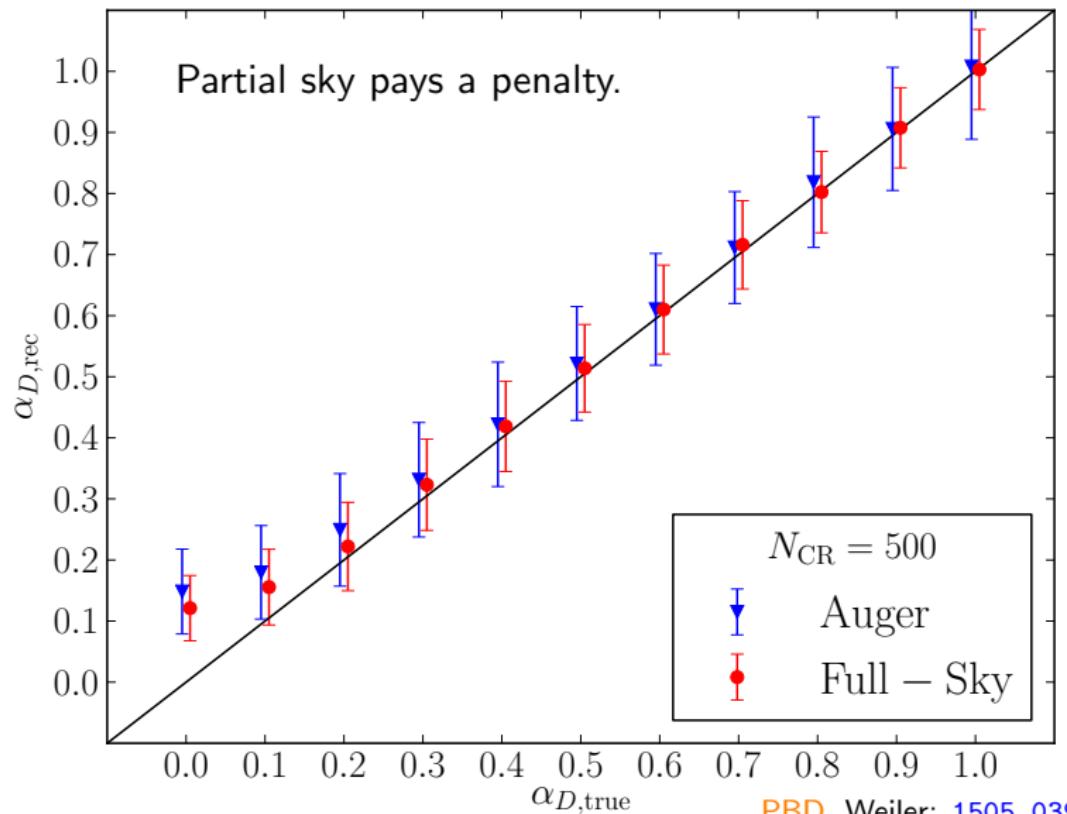
$$[K]_{\ell m}^{\ell' m'} \equiv \int d\Omega \omega(\Omega) Y_\ell^m(\Omega) Y_{\ell'}^{m'}(\Omega)$$

$$b_\ell^m = \sum_{\ell' m'} [K]_{\ell m}^{\ell' m'} a_{\ell'}^{m'} \quad \Rightarrow \quad a_\ell^m = \sum_{\ell' m'}^{\ell_{\max}} [K^{-1}]_{\ell m}^{\ell' m'} b_{\ell'}^{m'}$$

$b_\ell^m \rightarrow$  uncorrected (observed on earth),  
 $a_\ell^m \rightarrow$  nature's true anisotropy.

Billoir, Deligny: [0710.2290](#)

# Dipole Reconstruction Effectiveness

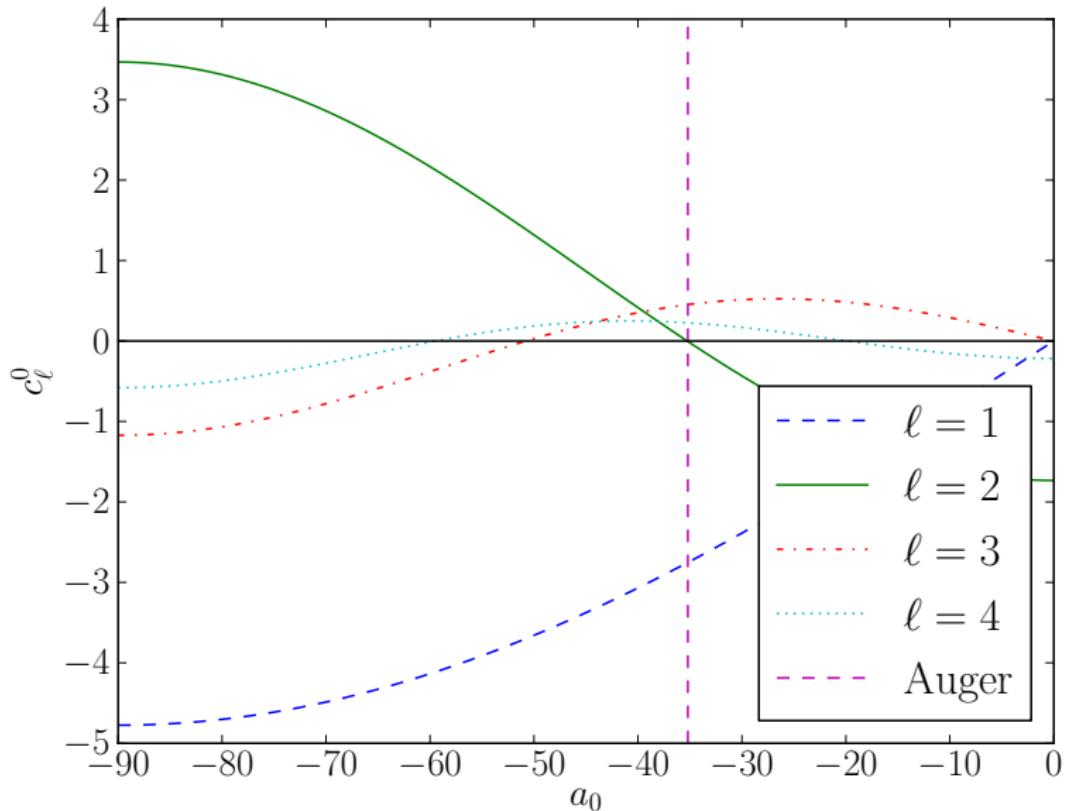


# Reconstructing $a_\ell^m$ 's for Nonuniform Partial Sky Coverage

- ▶ An alternative formalism to the  $K$ -matrix approach.
- ▶ Expand the exposure  $\omega(\Omega) = \sum_{\ell,m} c_\ell^m Y_\ell^m(\Omega)$ .
- ▶  $\omega$  does not depend on RA  $\Rightarrow$  only  $m = 0$  coefficients are nonzero.
- ▶ Fortunately,  $c_2^0 = 0$  for Auger's exposure  
(nearly equal to zero for Telescope Array).

PBD, Weiler: [1409.0883](#)

# Quadrupole Component of Exposure



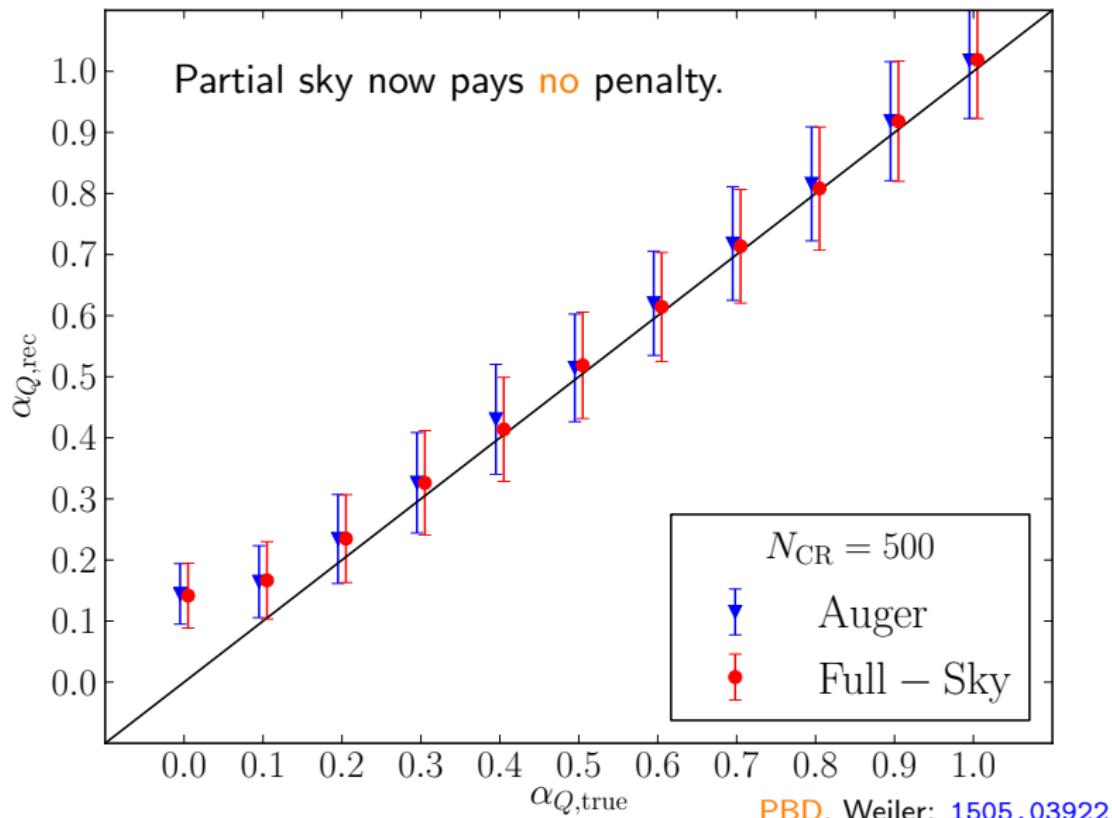
## Reconstructing $a_\ell^m$ 's for Nonuniform Partial Sky Coverage

When reconstructing a pure quadrupole, Auger and TA's exposures may be ignored,

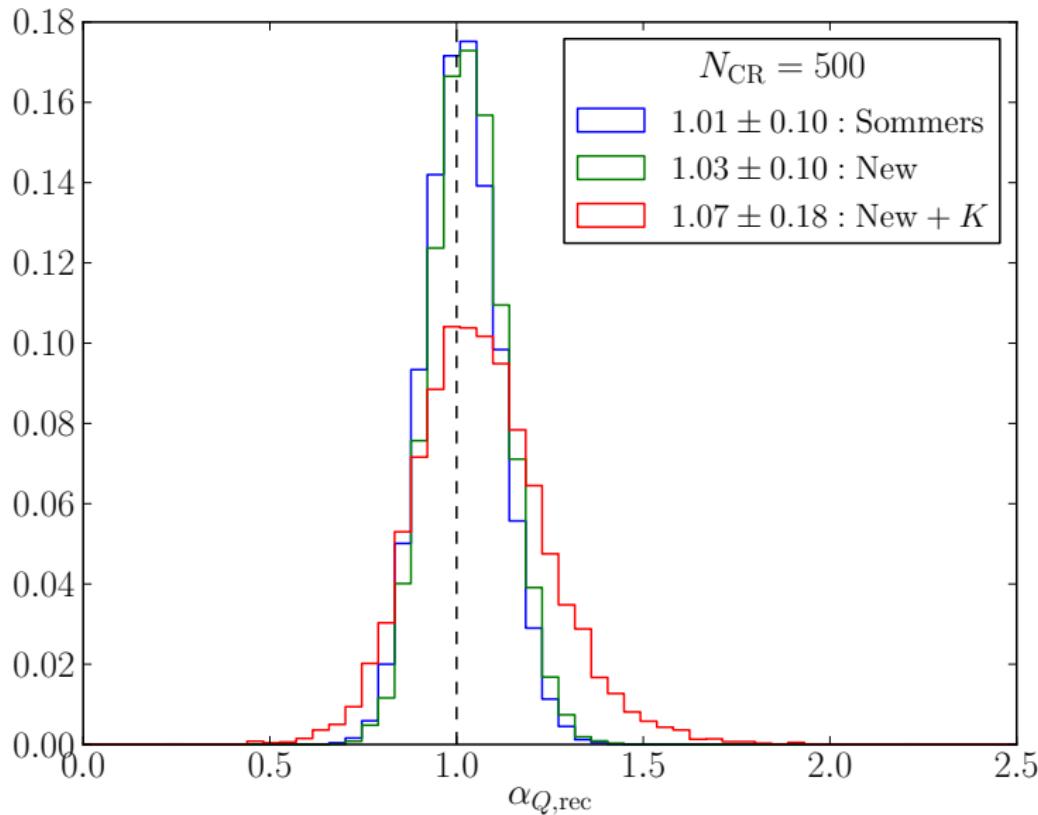
$$b_2^m = a_2^m \left[ 1 + \frac{(-1)^m c_4^0 f(m)}{7\sqrt{4\pi}} \right]$$

A correction of 0.05, -0.04, 0.009 for  $|m| = 0, 1, 2$ .

# Quadrupole Reconstruction Effectiveness



# Quadrupole Reconstruction Technique Effectiveness

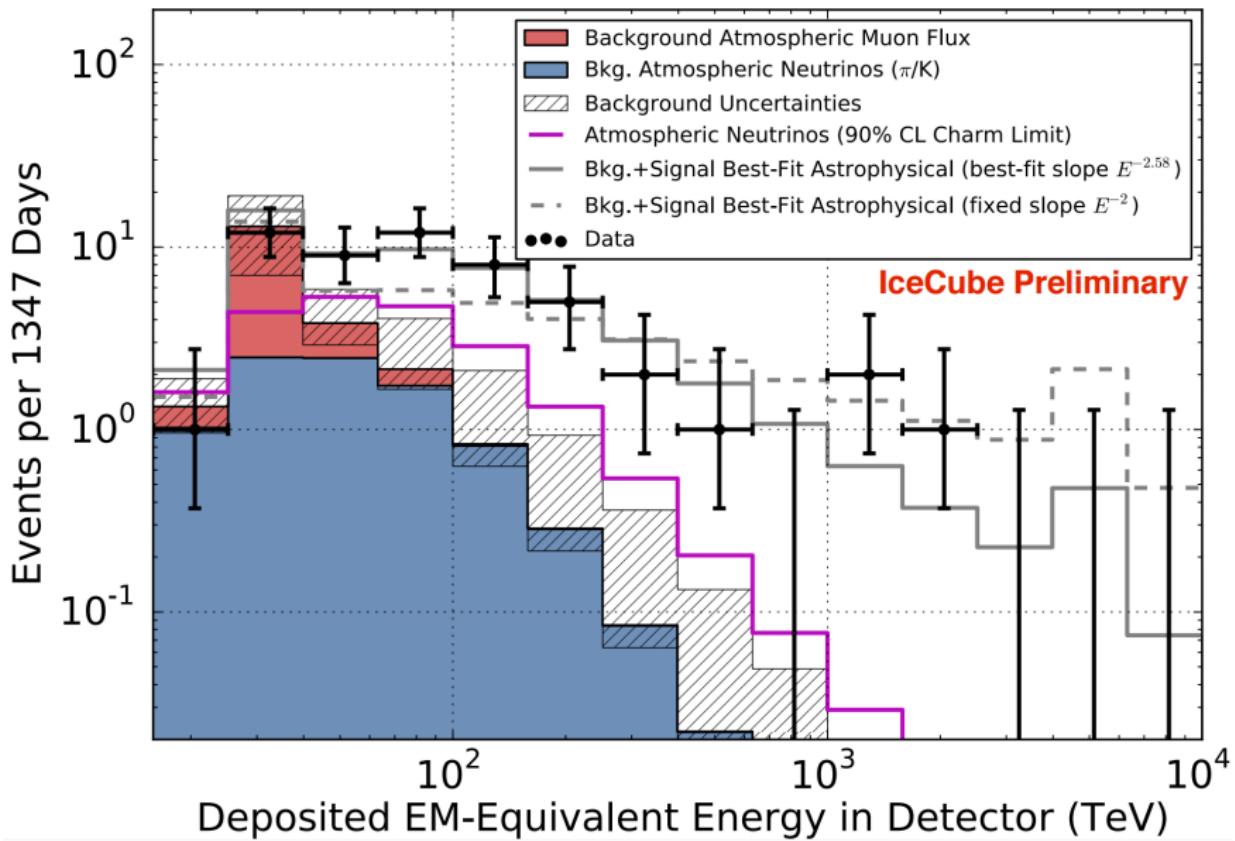


## UHECR Conclusions

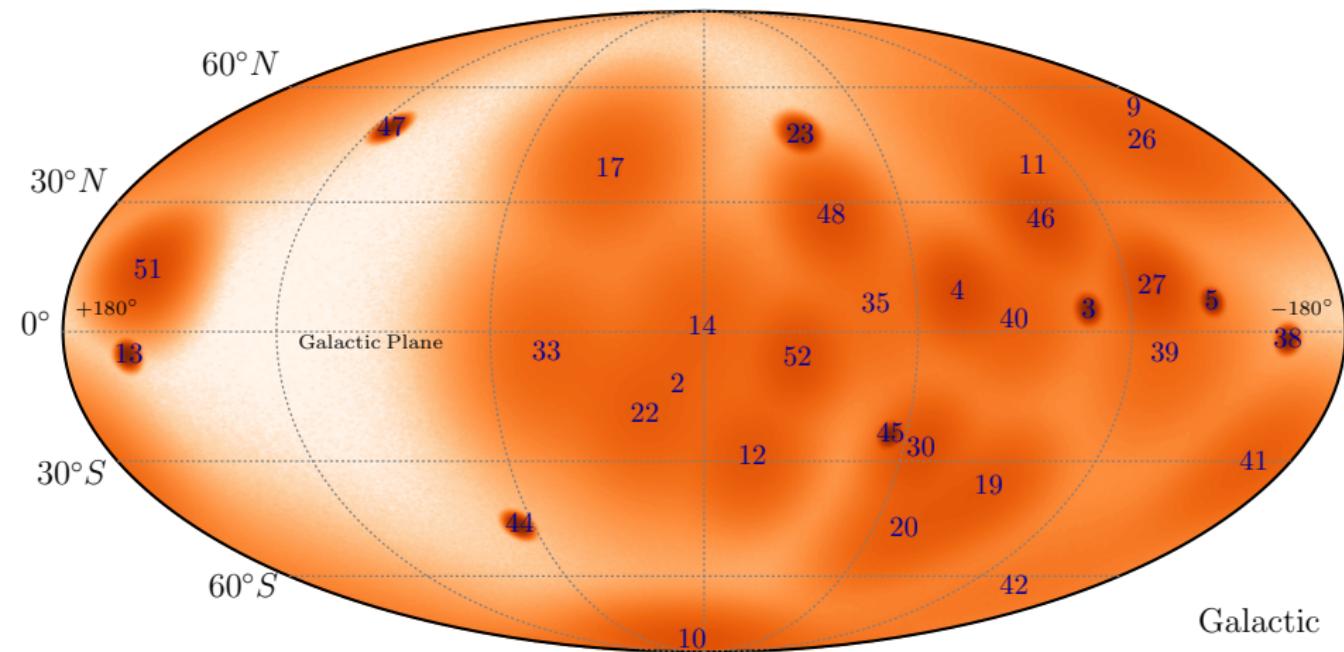
- ▶ Theoretical uncertainties in composition and magnetic fields makes point source searches difficult.
- ▶ Spherical harmonics provide a good multi-purpose tool to overcome these.
- ▶ An analytic treatment can improve sensitivity of certain analyses.

# IceCube Detects Astrophysical Neutrinos

IC: 1510.05223



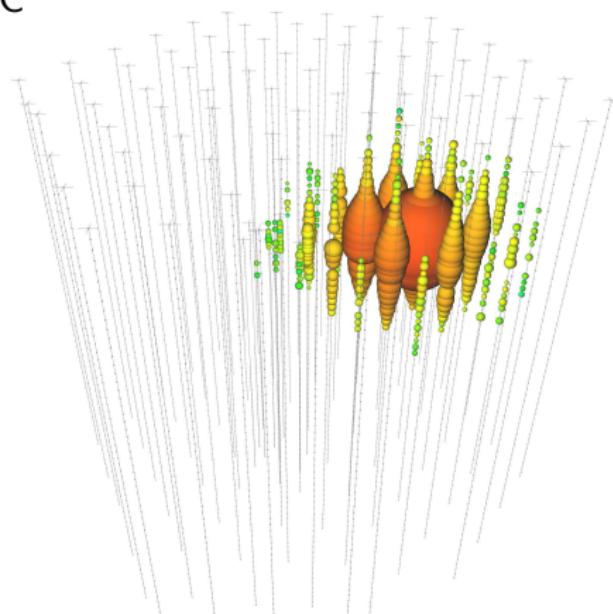
# IceCube Detects Astrophysical Neutrinos



32 events with  $E_{\text{dep}} > 60 \text{ TeV}$  from IC 4 year HESE

# IceCube Detects Astrophysical Neutrinos

Event 14  
 $E = 1 \text{ PeV}$   
1.2° from the GC  
 $\alpha_{50\%} = 13.2^\circ$

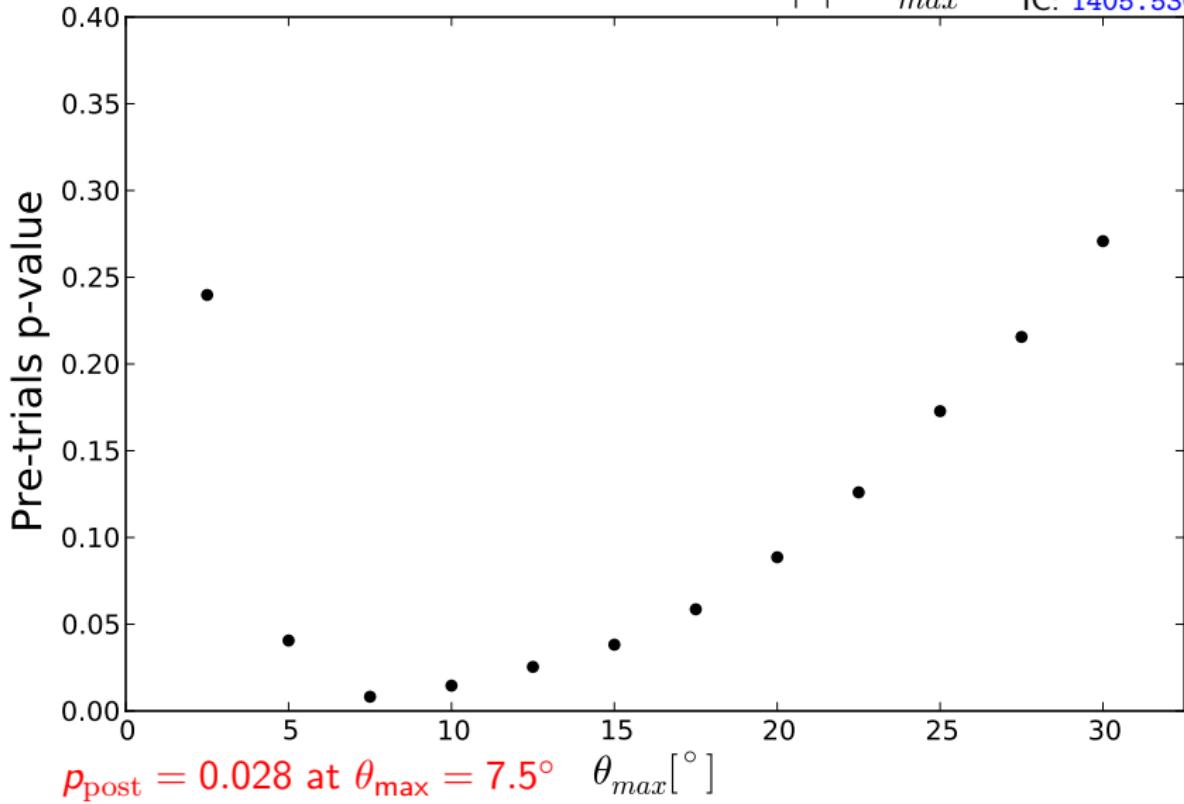


IC: 1311.5238

# Significance of the Galaxy as the Source

Galactic Plane with  $|b| < \theta_{max}$

IC: 1405.5303



# Galactic or Extragalactic?

Various methods to search for anisotropies:

- ▶ Windowed search around the Galactic center/plane.

IC: [1311.5238](#), [1405.5303](#)

Ahlers, Murase: [1309.4077](#)

Anchordoqui, et. al.: [1410.0348](#)

Palladino, Vissani: [1601.06678](#)

- ▶ Known Galactic sources:

CRs,  $\gamma$ -ray correlations, GC, misc. Galactic catalogs, ...

IC: [1406.6757](#)

Ahlers, et. al.: [1505.03156](#)

Troitsky: [1511.01708](#)

Celli, Palladino, Vissani: [1604.08791](#)

- ▶ Known extragalactic sources: AGNs, blazars, SFGs, GRBs, ...

Bechtol, et. al.: [1511.00688](#)

Murase: [1511.01590](#)

IC: [1601.06484](#)

Padovani, et. al.: [1601.06550](#)

## A More General Approach

- ▶ Treat the extragalactic flux as isotropic,  $\Phi_{\text{exgal}}(\Omega) = \frac{1}{4\pi}$ .
- ▶ Scale the galactic flux with the matter distribution  $\rho_{\text{gal}}$ ,

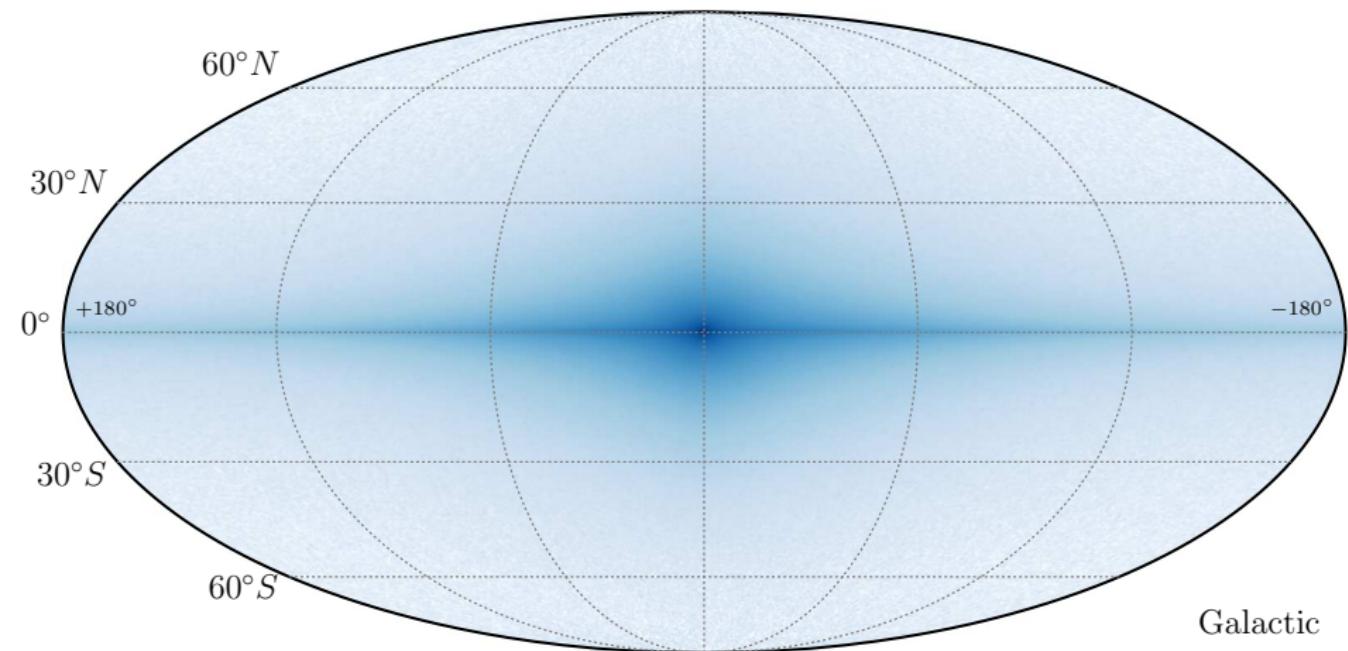
McMillan: [1102.4340](#)

$$\Phi_{\text{gal}}(\Omega) = \frac{\int ds \rho_{\text{gal}}(s, \Omega)}{\int ds d\Omega' \rho_{\text{gal}}(s, \Omega')} .$$

- ▶  $f_{\text{gal}}$  is the fraction of the astrophysical flux from the Galaxy,

$$\Phi_{\text{astro}}(\Omega, f_{\text{gal}}) = f_{\text{gal}} \Phi_{\text{gal}}(\Omega) + (1 - f_{\text{gal}}) \Phi_{\text{exgal}}(\Omega) .$$

# Expected Distribution From the Galaxy



# Energy and Topology Information for Backgrounds

- ▶ For  $E_{\text{dep}} > 60 \text{ TeV}$ , we expect  $< 4$  events from backgrounds.
- ▶  $\Gamma_{\text{bkg}} \sim 3.7$  while the best fit  $\Gamma_{\text{astro}} \sim 2.58$ .  
Results are largely independent to uncertainties in the spectra.
- ▶ The background and astrophysical likelihoods for event  $i$  are,

$$\mathcal{L}_{\text{bkg},i} = f_{\text{bkg},i} \frac{dN_{\text{bkg}}}{dE}(E_i),$$

$$\mathcal{L}_{\text{astro},i} = f_{\text{astro},i} \frac{dN_{\text{astro}}}{dE}(E_i),$$

where  $f_{\text{bkg}(\text{astro}),i}$  is the expected fraction of events with topology and declination that are background (astrophysical).

# Galactic or Extragalactic?

Given that an event is astrophysical, the conditional likelihoods are,

$$\mathcal{L}_{\text{gal|astro},i}(f_{\text{gal}}) = f_{\text{gal}} \Phi_{\text{gal}}(\Omega_i),$$

$$\mathcal{L}_{\text{exgal|astro},i}(f_{\text{gal}}) = (1 - f_{\text{gal}}) \Phi_{\text{exgal}}(\Omega_i).$$

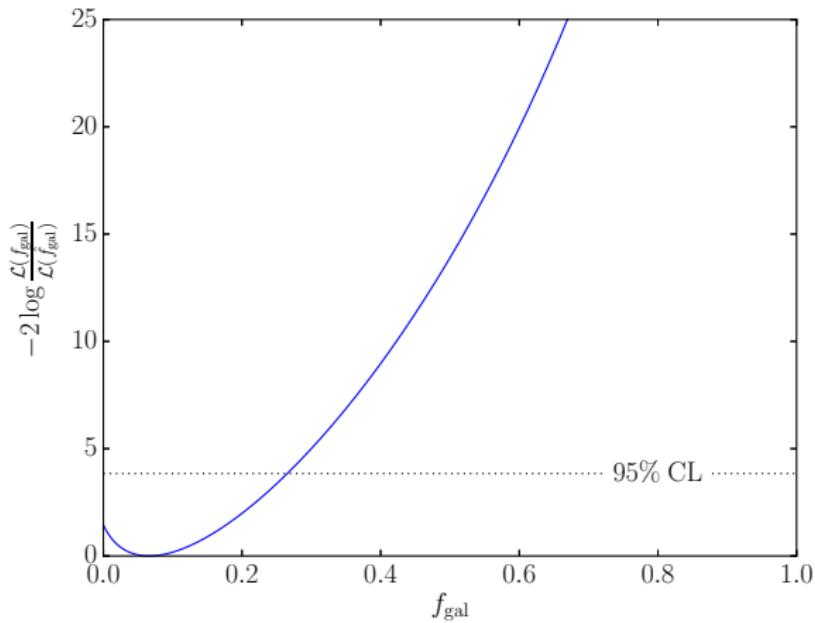
The likelihood that event  $i$  is described by this model is,

$$\mathcal{L}_i(f_{\text{gal}}) = \mathcal{L}_{\text{bkg},i} + \mathcal{L}_{\text{astro},i} [\mathcal{L}_{\text{gal|astro},i}(f_{\text{gal}}) + \mathcal{L}_{\text{exgal|astro},i}(f_{\text{gal}})],$$

and the total likelihood is the product,

$$\mathcal{L}(f_{\text{gal}}) = \prod_i \mathcal{L}_i(f_{\text{gal}}).$$

# Results



$$\hat{f}_{\text{gal}} = 0.066^{+0.090}_{-0.058}$$

$f_{\text{gal}} = 0$  allowed at  $1.2\sigma$

CL	$f_{\text{gal}}$
$1\sigma$	[0.008, 0.16]
90%	< 0.23
$2\sigma$	< 0.27
$3\sigma$	< 0.4

# Likelihoods to Probabilities

$$p_{\text{bkg},i} = \frac{\mathcal{L}_{\text{bkg},i}}{\mathcal{L}_{\text{astro},i} + \mathcal{L}_{\text{bkg},i}}$$

$$p_{\text{gal},i} = p_{\text{astro},i} \frac{\mathcal{L}_{\text{gal|astro},i}(\hat{f}_{\text{gal}})}{\mathcal{L}_{\text{gal},i}(\hat{f}_{\text{gal}}) + \mathcal{L}_{\text{exgal},i}(\hat{f}_{\text{gal}})}$$

$$p_{\text{exgal},i} = p_{\text{astro},i} \frac{\mathcal{L}_{\text{exgal|astro},i}(\hat{f}_{\text{gal}})}{\mathcal{L}_{\text{gal},i}(\hat{f}_{\text{gal}}) + \mathcal{L}_{\text{exgal},i}(\hat{f}_{\text{gal}})}$$

$$\sum_i p_{\text{gal},i} = 1.7, \quad \sum_i p_{\text{exgal},i} = 29.3, \quad \sum_i p_{\text{bkg},i} = 1.0$$

# Event-By-Event Probabilities

At  $\hat{f}_{\text{gal}} = 0.066$ :

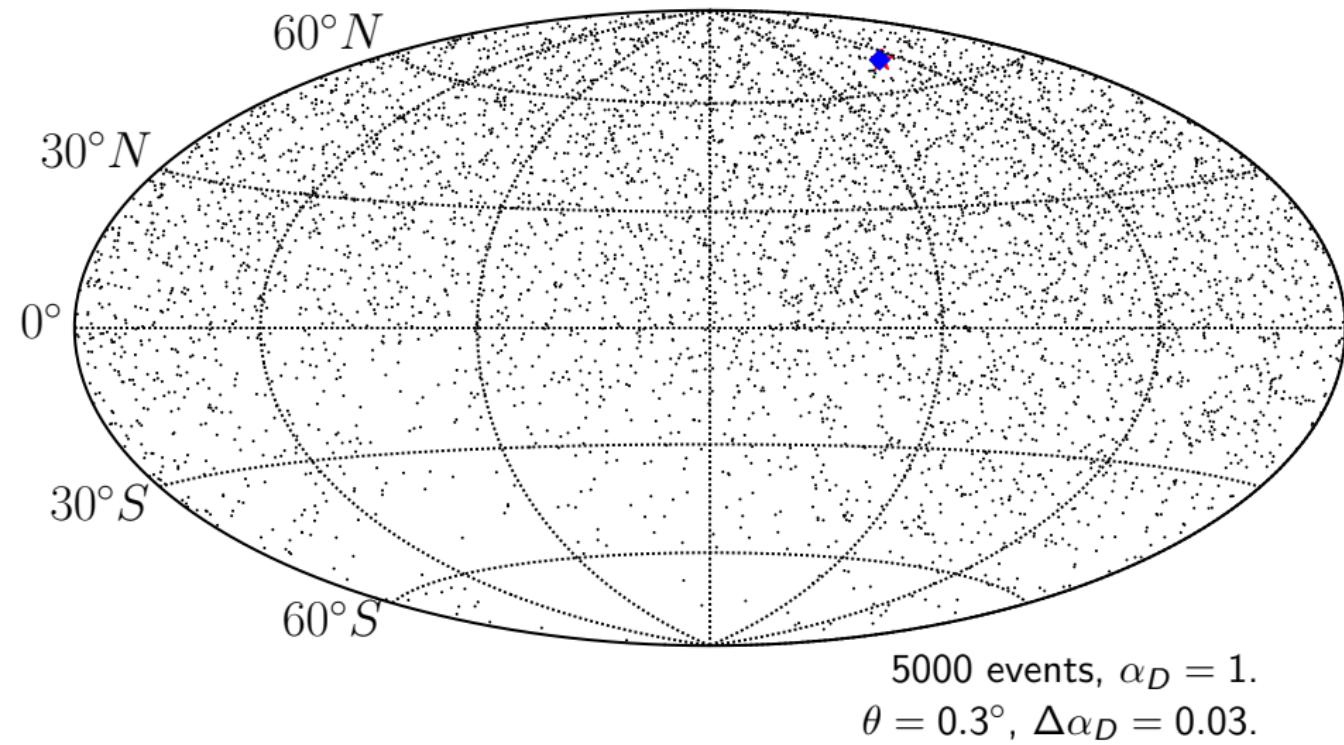
$E$	id	$p_{\text{gal}}$	$p_{\text{exgal}}$	$p_{\text{bkg}}$	$E$	id	$p_{\text{gal}}$	$p_{\text{exgal}}$	$p_{\text{bkg}}$
2003	35	0.048	0.95	0	152	3	0.0024	0.96	0.041
1140	20	1.8e-4	1	0	143	47	3.9e-4	0.95	0.051
1040	14	0.75	0.25	5.7e-4	137	5	3.7e-4	0.82	0.18
885	45	4.1e-4	1	0	128	30	5.9e-4	1	0
512	13	0.0016	0.98	0.02	117	2	0.42	0.57	0.0066
404	38	0.0035	0.95	0.045	104	48	0.0015	0.99	0.0074
384	33	0.058	0.93	0.016	104	12	0.01	0.99	0.0014
219	22	0.2	0.79	0.0084	101	39	0.001	0.98	0.02
210	26	4.2e-5	0.98	0.018	97	10	1.5e-5	0.99	0.008
199	17	0.0012	0.98	0.019	88	11	1.7e-4	0.93	0.065
165	4	0.0093	0.99	8.2e-4	87	41	9e-5	0.92	0.081
164	44	1.9e-4	0.82	0.18	76	42	3.9e-5	0.99	0.011
159	23	7.4e-6	0.93	0.067	71	19	7.4e-5	1	0
158	52	0.19	0.81	0	66	51	3.2e-4	0.98	0.024
158	46	2e-4	0.99	0.012	63	9	5.5e-5	0.95	0.046
157	40	0.007	0.99	8.7e-4	60	27	0.0013	0.96	0.035

# Conclusions

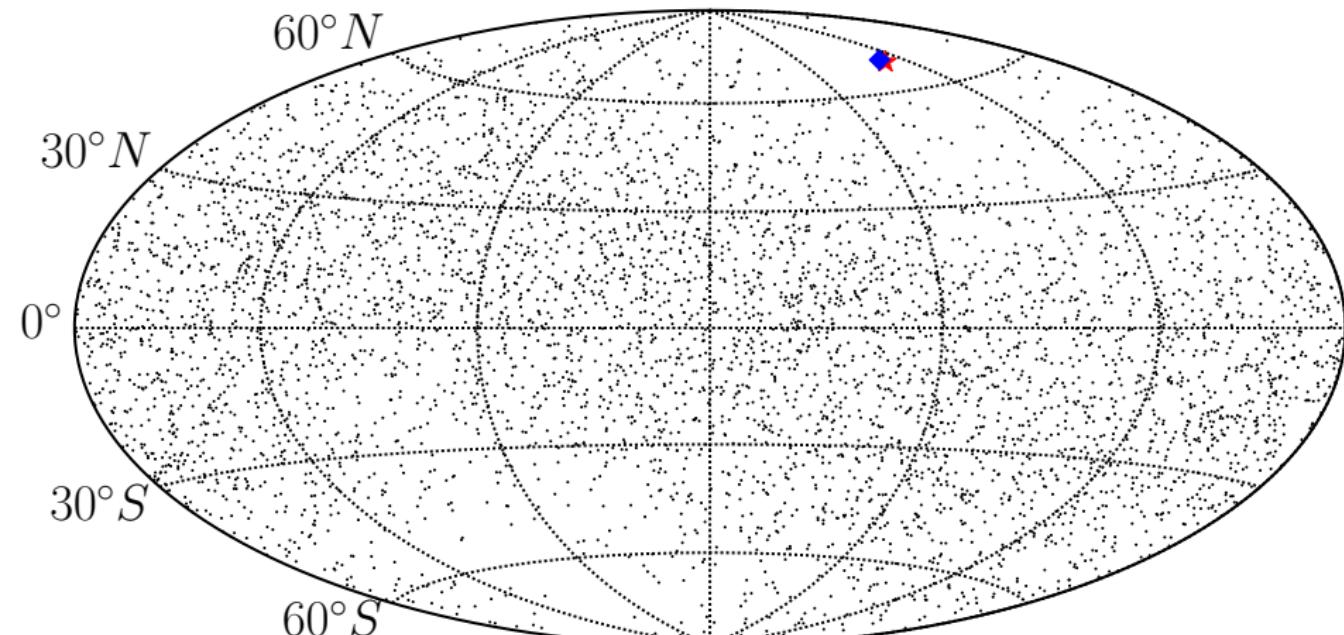
- ▶ The sources of UHECRs and astrophysical  $\nu$ 's is still an open question.
- ▶ UHECRs are still a background-free observable, but with large uncertainties.
- ▶ Handling partial sky exposure analytically can be useful.
- ▶ High energy neutrinos point at their sources, but carry backgrounds.
- ▶ The astrophysical neutrino flux is largely extragalactic.
  - ▶ A small galactic component  $\sim 7\%$  is allowed.

# Backups

## Sample Dipole

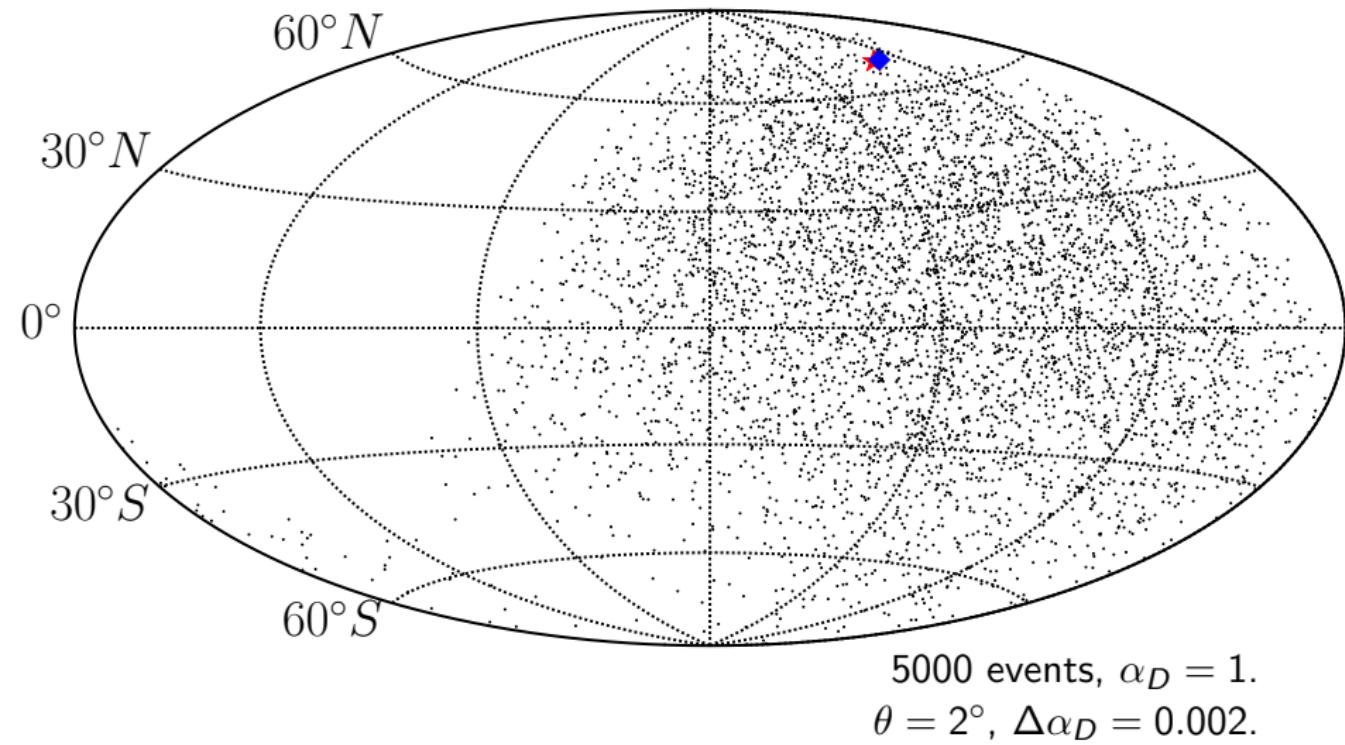


## Sample Quadrupole

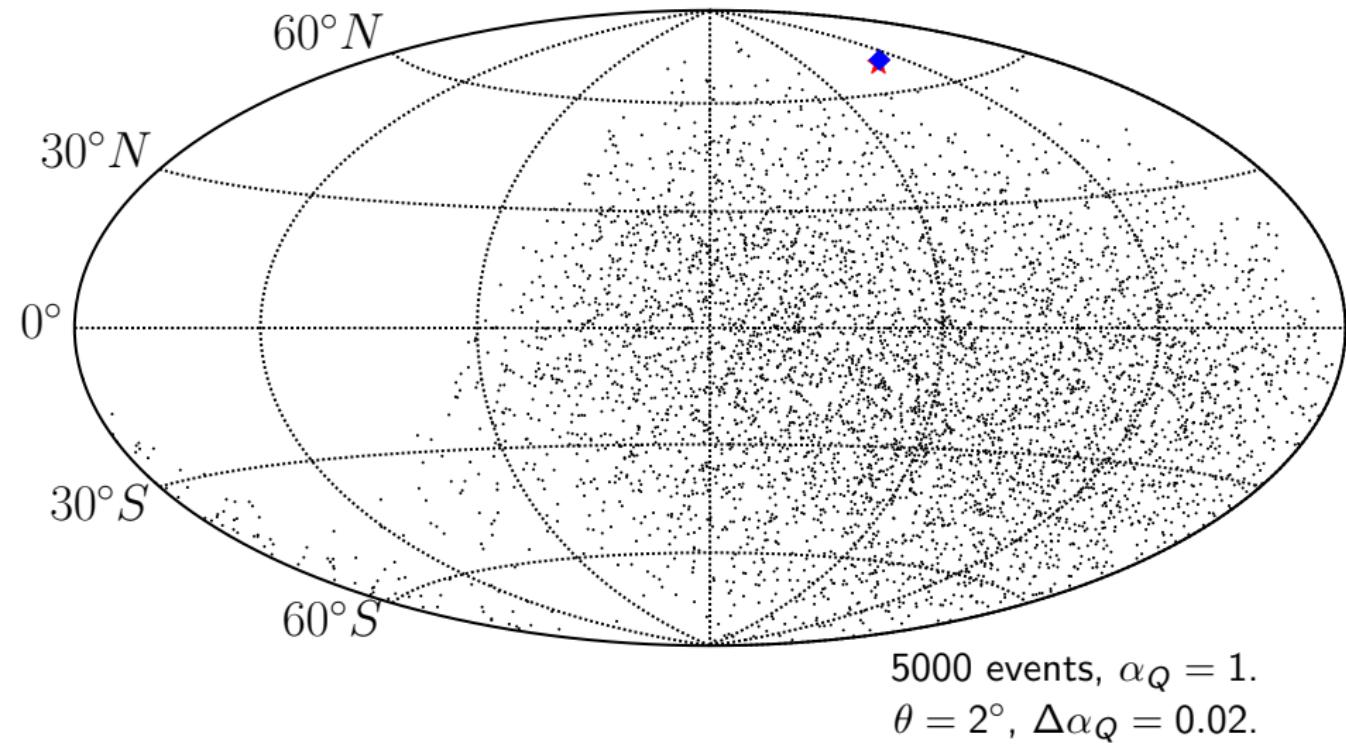


5000 events,  $\alpha_Q = 1$ .  
 $\theta = 0.8^\circ$ ,  $\Delta\alpha_Q = 0.02$ .

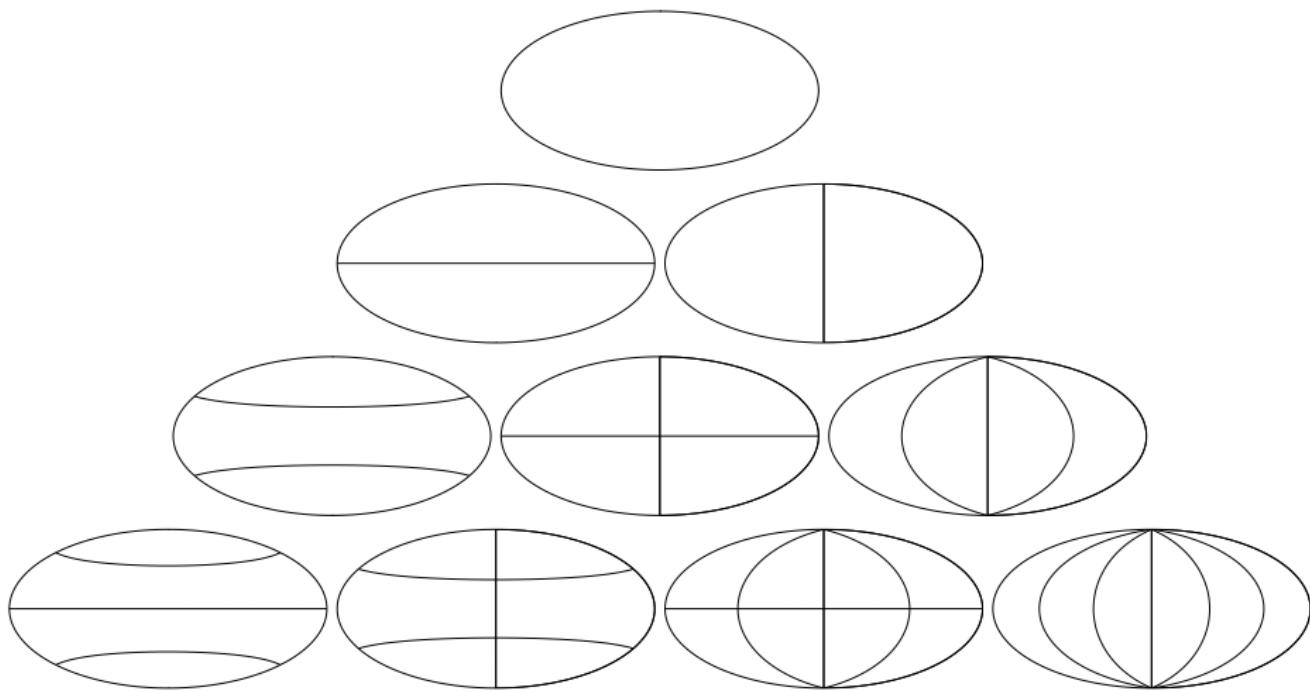
# Sample Dipole with Auger's Exposure



# Sample Quadrupole with Auger's Exposure



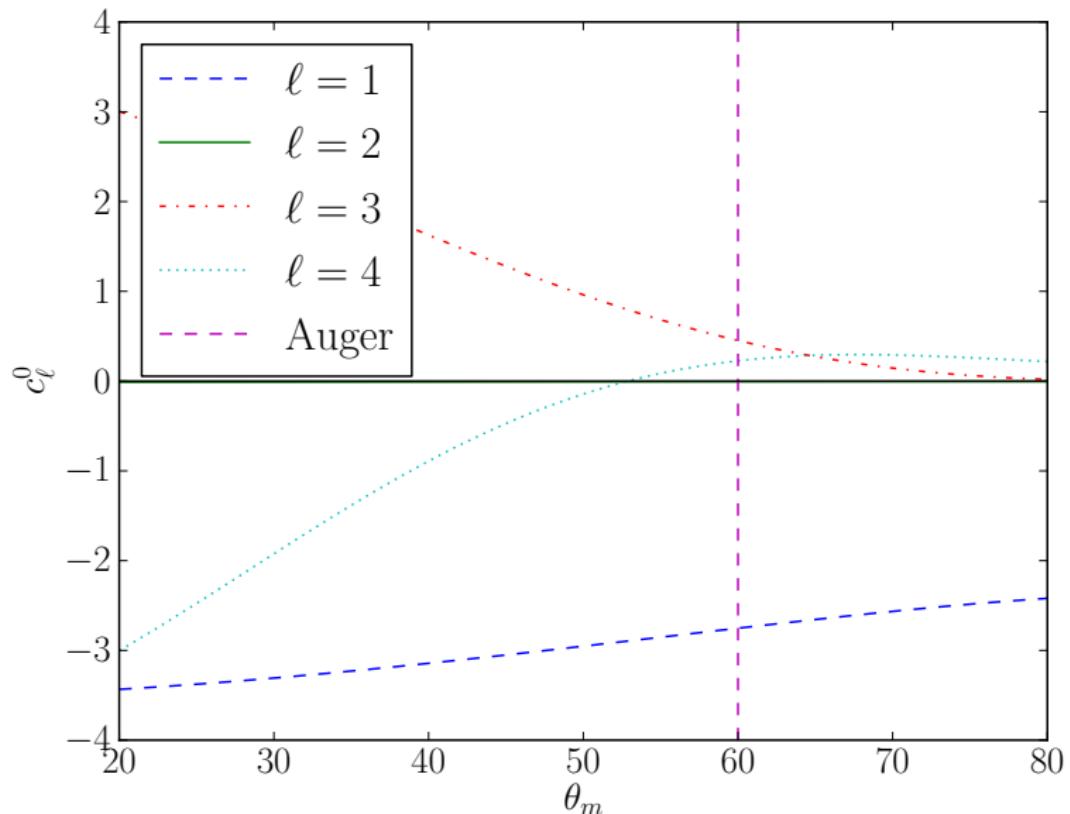
# Spherical Harmonics Visualizations



## Catalogs

- ▶ We consider galactic catalogs.
- ▶ The catalog used is the 2MRS.
- ▶ Contains 5310 galaxies out to redshift 0.03: 120 Mpc.
- ▶ Nearby galaxies need their distances adjusted for peculiar velocities.

# Quadrupole Component of Exposure



# Rotational Invariance of the Power Spectrum

$$I(\Omega) = \frac{1}{N} \sum_{i=1}^N \delta(\mathbf{u}_i, \Omega),$$

$$\bar{a}_\ell^m = \frac{1}{N} \sum_{i=1}^N Y_\ell^{m*}(\mathbf{u}_i),$$

$$\bar{C}_\ell = \frac{1}{N^2(2\ell+1)} \sum_{|m| \leq \ell} \left| \sum_{i=1}^N Y_\ell^{m*}(\mathbf{u}_i) \right|^2.$$

The addition formula for spherical harmonics:

$$P_\ell(\mathbf{x} \cdot \mathbf{y}) = \frac{4\pi}{2\ell+1} \sum_{|m| \leq \ell} Y_\ell^{m*}(\mathbf{x}) Y_\ell^m(\mathbf{y}).$$

e.g. Arfken, Weber: *Mathematical Methods for Physicists*

$$\bar{C}_\ell = \frac{1}{4\pi N} + \frac{1}{2\pi N^2} \sum_{i < j} P_\ell(\mathbf{u}_i \cdot \mathbf{u}_j).$$

## b10-cut: Analytical Derivation

We conservatively fill in the unknown region of the Galactic distribution with a uniform distribution,

$$I_g(\Omega) = I_{g,>10}(\Omega) + I_{u,<10}(\Omega).$$

$$(a_\ell^m)_g = (a_\ell^m)_{g,>10} + (a_\ell^m)_{u,<10},$$

Note the following properties of the  $(a_\ell^m)_{u,<10}$ :

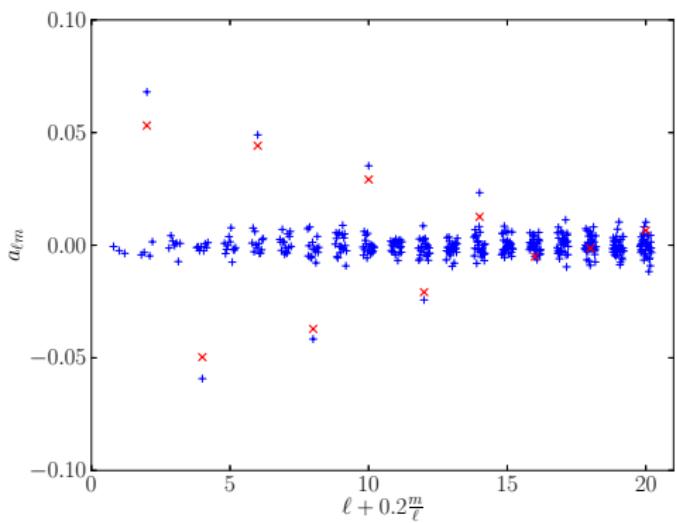
- ▶  $I_{u,<10}$  isn't a function of  $\phi$ .

$$a_\ell^m = 2\pi \sqrt{\frac{2\ell+1}{4\pi}} \int P_\ell(x) I(x) dx \delta_{m0}.$$

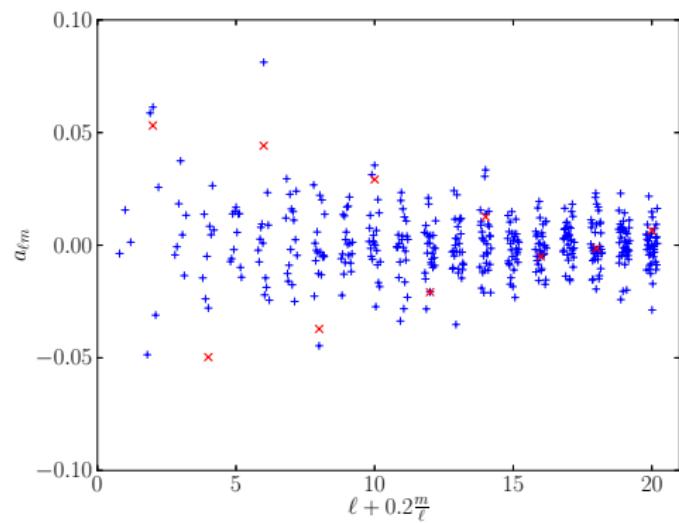
- ▶  $I_{u,<10}$  has even parity (the  $P_\ell$  have definite parity).

$$(a_\ell^0)_{u,<10} = \sqrt{\frac{2\ell+1}{4\pi}} \int_0^{\cos(80^\circ)} P_\ell(x) dx.$$

# b10-cut: Numerical Verification



Uniform



2MRS