# Using Integral Dispersion Relations to Extend the LHC Reach for New Physics

Peter Denton

TASI

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#### Overview

- 1. Brief derivation of IDRs
- 2. TOTEM experiment
- 3. Three ways of modeling new physics
- 4. Results: measurable effects

## Some necessary formulas

1. Cauchy's integral formula

$$f(z') = \frac{1}{2\pi i} \oint_{\partial A} \frac{f(z)}{z - z'} dz$$

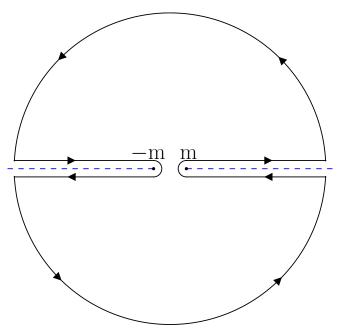
2. The optical theorem

$$\sigma_{tot} = \frac{4\pi}{p} \Im f(\theta = 0)$$

3. Definitions

$$\rho(E) \equiv \frac{\Re f(E, t = 0)}{\Im f(E, t = 0)} \qquad E \equiv \frac{s - u}{4m}$$

## Integration contour



#### Integral Dispersion Relations

$$\rho_{pp}(E)\sigma_{pp}(E) = \frac{4\pi}{p}\Re f(0) + \frac{E}{p\pi}\mathcal{P}\int_{m}^{\infty}dE'\frac{p'}{E'}\left[\frac{\sigma_{pp}(E')}{E'-E} - \frac{\sigma_{p\bar{p}}(E')}{E'+E}\right]$$

IDR  $\Rightarrow$  model dependent calculation of  $\rho$ .

### Comparing $\rho$

$$16\pi \left. \frac{d\sigma}{dt} \right|_{t=0} = (\rho^2 + 1)\sigma_{tot}^2$$

 $\Rightarrow$  model independent calculation of  $\rho.$ 

#### SM parametrization

- 1. Froissart bound says  $\sigma \leq C \log^2(E/E_0)$  asymptotically for some constants
- 2. Pomeranchuk theorem ( $c_4$ ) says that  $\sigma_{pp}-\sigma_{p\bar{p}} \to 0$  as  $E \to \infty$
- 3. Standard parametrization:

$$\sigma_{pp,p\bar{p}}(E) = c_0 + c_1 \log(E/m) + c_2 \log^2(E/m) + c_3(E/m)^{-\frac{1}{2}} \pm c_4(E/m)^{\alpha-1}$$

#### Experiment

- 1. TOTEM:  $\rho = 0.145$  at  $\sqrt{s} = 7$  TeV (large errors)
- 2. SM Prediction:  $\rho = 0.1345$  at  $\sqrt{s} = 7$  TeV
- 3. "Signal":  $(\rho-\rho_{\rm SM})/\rho_{\rm SM}=$  0.0781 (a 0.1 $\sigma$  "signal")

#### SM pp cross section and three simple modifications

We want to retain the  $\log^2 s$  growth asymptotically

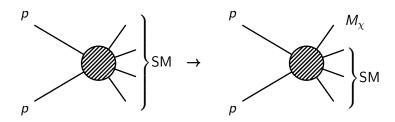
$$\sigma(s) = \sigma_{SM}(s)[1 + h_i(s)].$$

The first modification is a simple step function:

$$h_1(s) = d\Theta(s - s_{thr})$$
.

#### More physical modifications to the pp cross section

SUSY contributions are too small  $\mathcal{O}(10^{-9})$ . RPV SUSY could provide a much larger effect.



#### More physical modifications to the pp cross section

We reduce the cross section by a phase space ratio given by

$$\sqrt{\frac{\lambda(\hat{\mathfrak{s}},M_\chi^2,0)}{\lambda(\hat{\mathfrak{s}},0,0)}}=1-\frac{M_\chi^2}{\hat{\mathfrak{s}}}$$

We integrate this in terms of the parton distribution functions giving a modification of

$$h_2(s, M_{\chi}) = z \sum_{i,j} \int_{x_1 x_2 > M_{\chi}^2/s} dx_1 dx_2$$

$$\times f_i(x_1, M_{\chi}) f_j(x_2, M_{\chi}) x_1 x_2 \left( 1 - \frac{M_{\chi}^2}{\hat{s}} \right)$$

Where  $z = \sigma_{inel}/\sigma_{tot} \sim 0.7$ .

#### Yet another pp cross section modification

We cut final states into two blocks by pseudorapidity and we let  $M_X$  be the mass of the more massive one. Let  $\xi \equiv M_X^2/s$ .

$$\frac{d\sigma}{d\xi} = \frac{1+\xi}{\xi^{1+\epsilon}} \qquad \qquad \epsilon \sim 0.08$$

To modify the pp cross section the integration bounds change.

$$h_3(s) = z \frac{1 - 2\epsilon + (\epsilon - 1)\xi_{\chi}^{-\epsilon} + \epsilon \xi_{\chi}^{1 - \epsilon}}{1 - 2\epsilon + (\epsilon - 1)\xi_{\rho}^{-\epsilon} + \epsilon \xi_{\rho}^{1 - \epsilon}} \Theta(1 - \xi_{\chi})$$

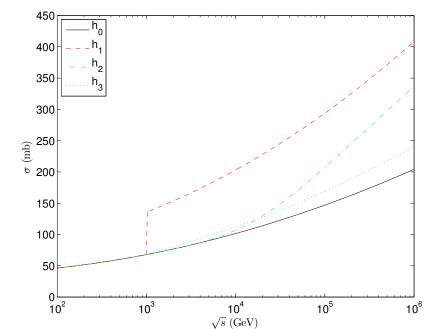
#### Exotic models

Other exotic models may give rise to significant  $\sigma_{pp}$  increases:

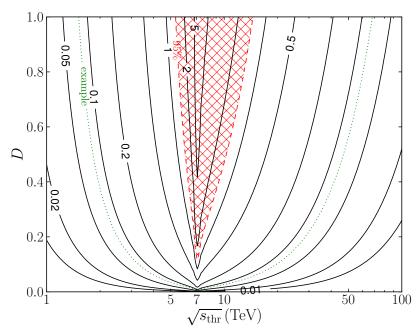
- 1. Kaluza-Klein modes
- 2. Weak scale gravity

These can be generally described as a step function,  $h_1$ , at the relevant energy with the magnitude of the step large - up to a factor of ten.

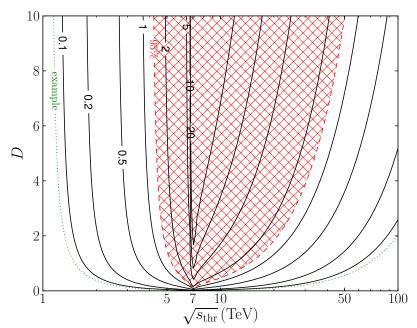
#### pp cross section modifications



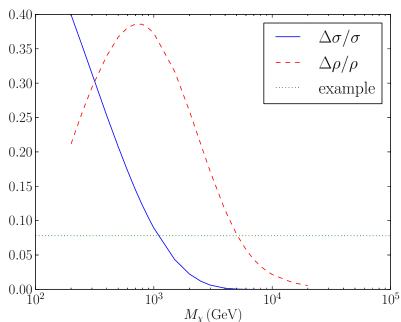
### Results: $h_1$ step function



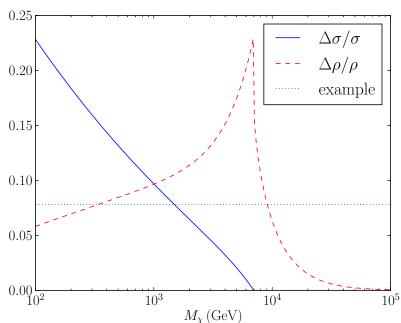
## Results: $h_1$ step function to large d



## Results: $h_2$ perturbative approach



### Results: $h_3$ non-perturbative approach



#### Discussion and confusions

- 1. IDRs can be used to detect large changes in  $\sigma_{pp}$ .
- 2. Perturbative models do not allow for large enough modifications.
- 3. A non-perturbative approach is more successful in a narrow region.

UHECR  $\Rightarrow E_{CR} \gtrsim 50 \text{ EeV} = 5 \times 10^{19} \text{ eV}.$ 

Things we don't know:

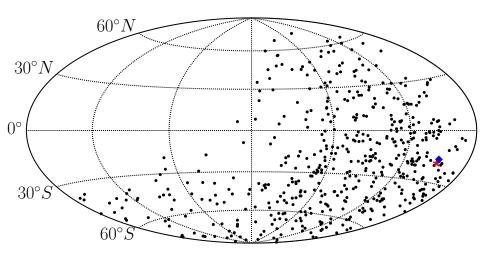
- 1. Composition: If UHECR are p, Fe, something inbetween.
- 2. Acceleration: How the flux we see is accelerated in astrophysical phenomena.
- 3. Sources: Where exactly do they come from.
- 4. Magnetic fields: How much UHECRs are bent inbetween galaxies and in our own galaxy.
- 5. Extensive air showers: How the showers propagate in the atmosphere.

# Backup: Non-perturbative cross section reproduces Froissart bound when properly expanded

We noted that the cross section function that goes into the modification  $h_3$  rises like  $\log^2 s$  in the appropriate limit:

$$\begin{split} \sigma &\propto 1 - \xi_p - \log \xi_p \\ &+ \left(1 - \xi_p + \xi_p \log \xi_p + \frac{1}{2} \log^2 \xi_p\right) \epsilon + \mathcal{O}(\epsilon^2) \end{split}$$

with higher order  $\epsilon$  terms resulting in higher orders of log s following the above pattern.



- 1. Several partial-sky experiments look at the sky: HiRes (Utah) and Pierre Auger Observatory (Argentina).
- 2. There is no (significant) evidence of anisotropy from these experiments.
- 3. Reconstructing anisotropies with partial-sky coverage is non-trivial.
- 4. One (of several) proposed new experiments is EUSO on the ISS to provide near uniform full-sky coverage.

Parameterize anisotropies in spherical harmonics and the power spectrum,

$$I(\Omega) = \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} a_{\ell}^m Y_{\ell}^m(\Omega)$$

$$C_{\ell} = \frac{1}{2\ell+1} \sum_{m=-\ell}^{\ell} |a_{\ell}^m|^2$$

See 1401.5757 (conference proceedings) for an introduction to our approaches.