

Clocks Broadcast

Source:

- IB Distributed System
- [y2014p5q7](#)
- [y2020p5q8](#)

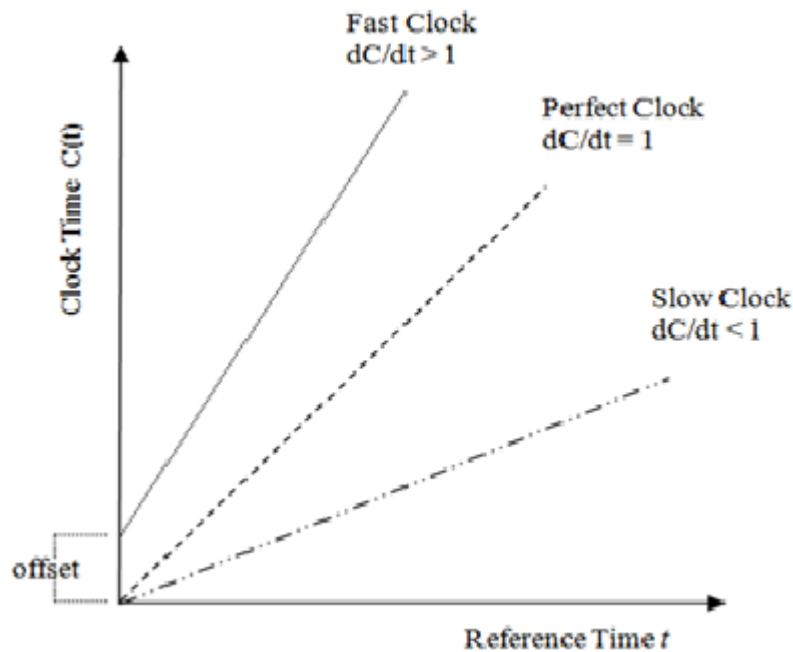
Clock	Physical	Logical
measure	seconds	events with causality
example	analogue/mechanic digital: Quartz (drift) Atomic, GPS	Lamport Vector

Physical Clock

Time-of-day and Monotonic

Physical Clock	Real Time	Monotonic
since	a fixed date time	arbitrary point (start-up)
correction	<i>slew</i> \implies <i>step</i>	always <i>slewforward</i>
behaviour	human readable; compare ts among nodes if sync	measure elapsed time on a single node
usage	certificate time	measure intervals / timeouts

Synchronization



The time of a clock in a machine p is $C_p(t)$, frequency/rate of a clock is $C'_p(t)$

- perfect clock $\Leftrightarrow C_p(t) = t$

Clock skew / offset

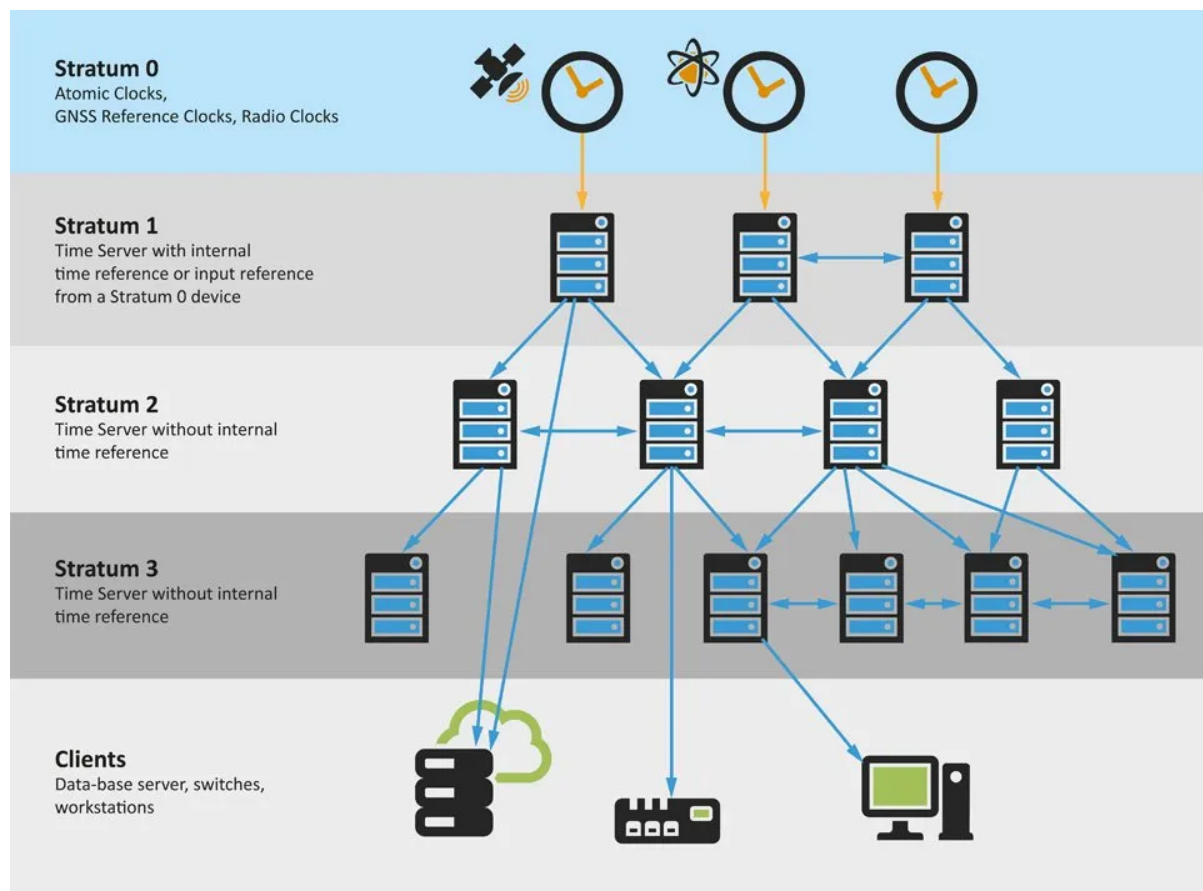
- the difference between the time on two clocks
- skew $\Delta_s = C_a(t) - C_b(t)$ (ms)
- measure: RTT δ , Cristian's Algorithm [wiki](#)
 - assumption:
 - symmetric latency
 - not consider the derivative of the clock (i.e. drift) or higher derivatives
- correction
 - as Δ_s increases, *slew* \Rightarrow *step* \Rightarrow *panic*

Clock drift

- the difference of clock rate of oscillations / ticks
- drift $\Delta_d = C'_a(t) - C'_b(t) = \Delta_s(t_1) - \Delta_s(t_2)$ (ms/day, parts per million)
 - affected by temperature, etc.
- measure: Cristian's Algorithm twice
 - assumption
 - symmetric latency
 - not considering the second or higher derivatives of the clock

NTP / PTP (Stratum 0-2)

- Less accurate synchronization
 - Time source (higher stratum)
 - Assumption of Cristian's Algorithm



Logical Clock

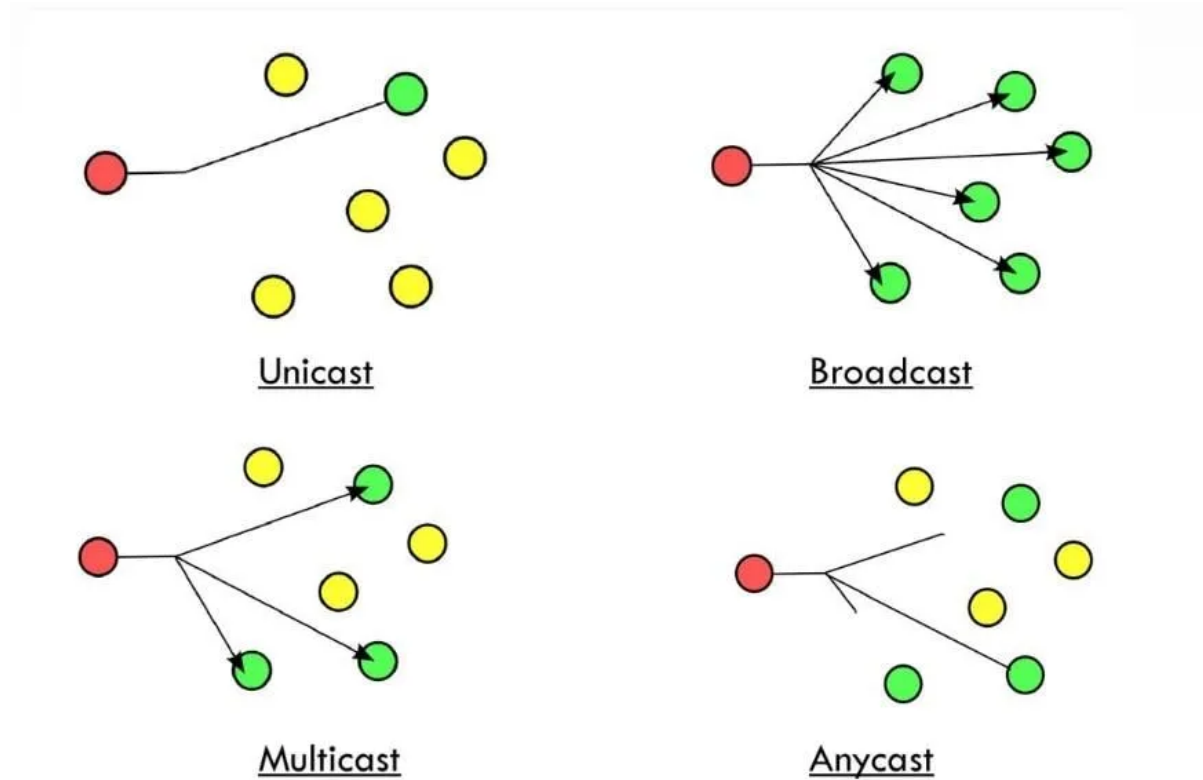
- causal / happen-before dependency $e_1 \rightarrow e_2$
 - e_1 and e_2 occurred at the same node, different by execution time
 - e_1 is sending message to e_2
 - transitivity, $\exists e_3. (e_1 \rightarrow e_3) \wedge (e_3 \rightarrow e_2) \implies e_1 \rightarrow e_2$.
 - (strict) partial order, asymmetric, undefined when race condition has occurred $e_1 \parallel e_2$
- logical clock timestamp is consistency with causal dependency
 - But lamport may not get causal dependency of events back from logical timestamps.

$$e_1 \rightarrow e_2 \implies T(e_1) < T(e_2)$$

	Lamport	Vector
format	$(N(e), L(e))$ (i, Seq)	$\langle N_1, \dots, N_n \rangle$ $V(e) = \langle t_1, \dots, t_n \rangle$
order	<i>total</i> \prec	<i>partial</i> $< $
timestamp	scalar	vector
	\implies	\iff
initial	$(i, 0)$	$\langle 0, \dots, 0, \dots, 0 \rangle$
event occur	$(i, t) \rightarrow (i, t + 1)$	$T_V[i] := T_V[i] + 1$

	Lamport	Vector
$receive(t'/T', m)$	$t := \max(t, t') + 1$	$T_V := \max_j(T_V, T')$ $T_V[i] := T_V[i] + 1$
$e = broadcast(m)$	FIFO of each sender	Causal

Broadcast



$$sendSeq := 0, delivered = \langle 0, \dots, 0 \rangle, buffer := \{\}$$

FIFO

- any messages sent by the same sender are delivered in the order in which they were sent.
 - $\forall m_1. (broadcast(m_1) \rightarrow broadcast(m_2))$ from the same sender, then every message (m_1) causally preceding $(\rightarrow) m_2$, from the same sender, must be sent before m_2 .
- send**
 - $(i, sendSeq, m)$ via reliable broadcast
- receive**
 - if $delivered[senderID] = sendSeq$, deliver the msg & update the accumulator *delivered*
 - otherwise, hold back (delay/buffer) message
 - $buffer := buffer \cup \{msg\}, buffer := buffer - \{msg\}$

Causal

- any messages are delivered in the order of causality of broadcast events.
 - $\forall m_1. (broadcast(m_1) \rightarrow broadcast(m_2))$, then every message m_1 causally preceding (\rightarrow) m_2 must be sent before m_2 .
 - **causality** between broadcast events is preserved by the corresponding delivery events.
 - concurrent broadcast events give *multiple* delivery choices, thus require commutative
- **send**
 - $(i, delivered', m)$ via reliable broadcast
- **receive**
 - if $delivered' \leq delivered$, deliver the msg & update the *accumulator delivered*
 - otherwise, hold back (delay/buffer) message

Total order

- the order of delivery is the same across all nodes.
 - If m_1 is delivered before m_2 on one node, then the same on all other nodes.
 - even need to hold back/delay/buffer message for itself.
- Implementation
 - Single Leader
 - Problem: Single Point of Failure
 - FIFO Total order

node crashes	links / broadcast	fault tolerance	Timing
crash-recovery			synchronous
fail-arbitrary	Total order		partially syn
crash-stop			asynchronous
	Causal order <i>concurrent commute</i>	$V(e) = \langle t_1, \dots, t_n \rangle$	
	FIFO order	(i, Seq)	
	Reliable <i>commute</i>		
	Fair-loss (<i>idempotent</i>)	retry+dedup	
	Best-effort (<i>node crashes</i>)	n:eager / 3:gossip	
	Arbitrary	TLS	