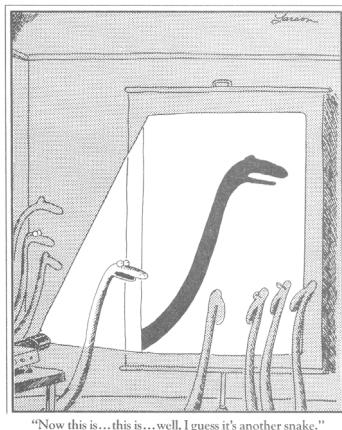
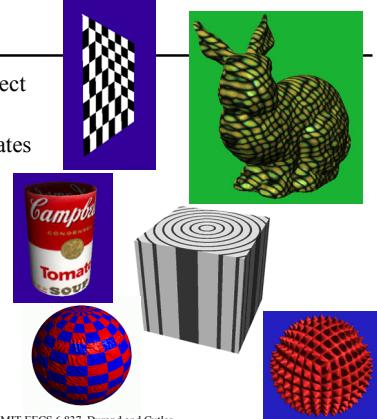


## Real-Time Shadows



## Last Time?

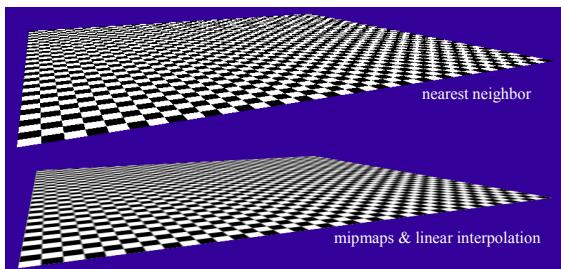
- Perspective-Correct Interpolation
- Texture Coordinates
- Procedural Solid Textures
- Other Mapping
  - Bump
  - Displacement
  - Environment
  - Lighting



MIT EECS 6.837, Durand and Cutler

## Textures can Alias

- *Aliasing* is the under-sampling of a signal, and it's especially noticeable during animation



MIT EECS 6.837, Durand and Cutler

## Schedule

- Quiz 1: Tuesday October 26<sup>th</sup>, in class (1 week from today!)
- Review Session: Monday October 25<sup>th</sup>, 7:30-9pm, 1-150
- Assignment 6: due Wednesday November 3<sup>rd</sup>

MIT EECS 6.837, Durand and Cutler

## RayTracer::traceRay Confusion

```
Vec3f RayTracer::traceRay(Ray &ray, float tmin,
                           int bounces, float weight,
                           float indexOfRefraction,
                           Hit &hit)

scene->getGroup()->intersect(ray, hit, t)
should only be called once, from within RayTracer::traceRay
```

\*\* This will help you implement and debug fast raytracing (assignment 6)

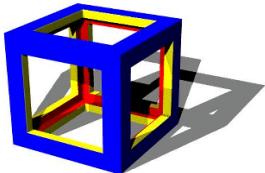
MIT EECS 6.837, Durand and Cutler

## Questions?

MIT EECS 6.837, Durand and Cutler

## Today

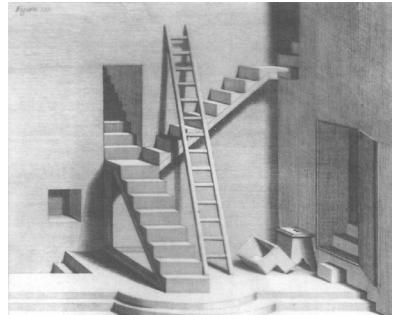
- Why are Shadows Important?
- Shadows & Soft Shadows in Ray Tracing
- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- Shadow Volumes



MIT EECS 6.837, Durand and Cutler

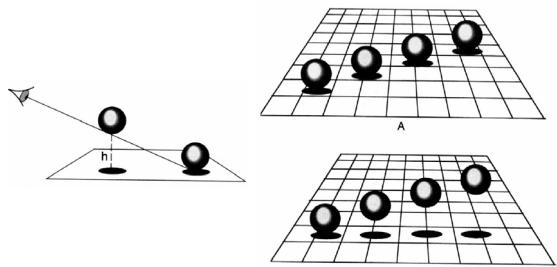
## Why are Shadows Important?

- Depth cue
- Scene
- Lighting
- Realism
- Contact points



MIT EECS 6.837, Durand and Cutler

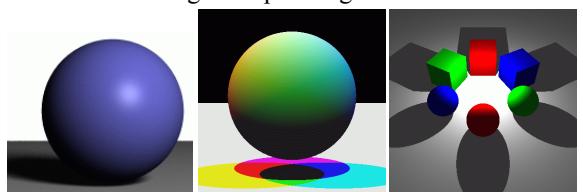
## Shadows as a Depth Cue



MIT EECS 6.837, Durand and Cutler

## For Intuition about Scene Lighting

- Position of the light (e.g. sundial)
- Hard shadows vs. soft shadows
- Colored lights
- Directional light vs. point light



MIT EECS 6.837, Durand and Cutler

## Shadows as the Origin of Painting



MIT EECS 6.837, Durand and Cutler

## Shadows and Art

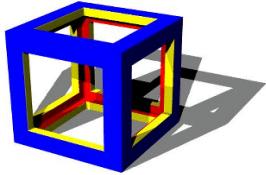
- Only in Western pictures (here Caravaggio)



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## Today

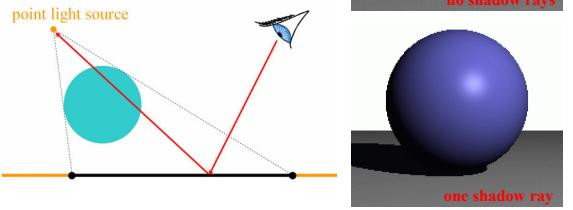
- Why are Shadows Important?
- **Shadows & Soft Shadows in Ray Tracing**
- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- Shadow Volumes



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## Shadows

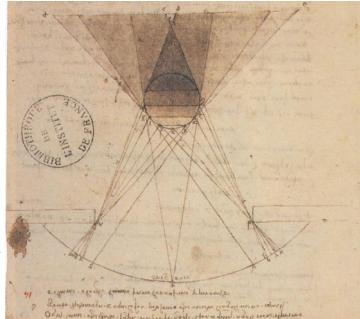
- One shadow ray per intersection per point light source



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## Soft Shadows

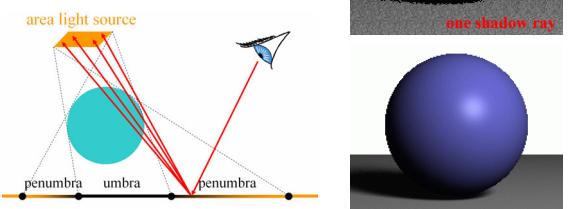
- Caused by extended light sources
- Umbra
  - source completely occluded
- Penumbra
  - Source partially occluded
- Fully lit



NVL Leonardo da Vinci (1452-1519), Lumière d'une fenêtre sur une sphère umbroise avec (en partant du haut) ombre intermédiaire, primitive, dérivée et (sur la surface, en bas) porcée. Plume et lavis sur pointe de métal sur papier, 24 x 38 cm. Paris, Bibliothèque de l'Institut de France (ms. 2185; B.N. 7058, f. 14 v).

## Soft Shadows

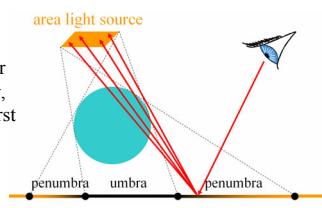
- Multiple shadow rays to sample area light source



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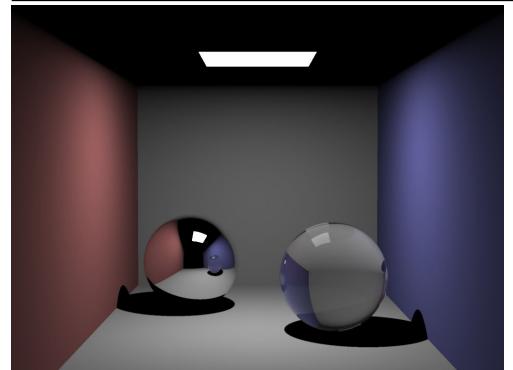
## Shadows in Ray Tracing

- Shoot ray from visible point to light source
- If blocked, discard light contribution
- Optimizations?
  - Stop after first intersection (don't worry about  $t_{min}$ )
  - Coherence: remember the previous occluder, and test that object first

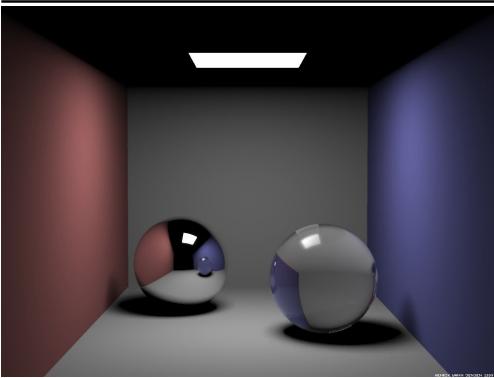


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## Traditional Ray Tracing

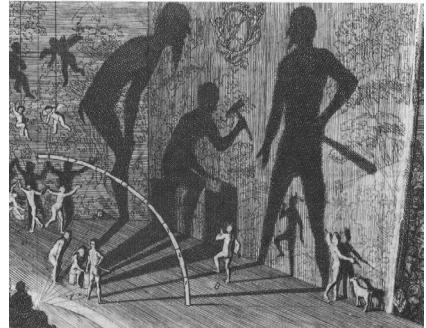


## Ray Tracing + Soft Shadows



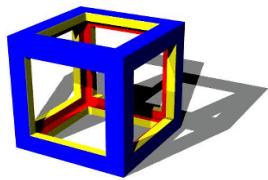
## Questions?

Plate 50 Samuel van Hoogstraten, *Shadow Theatre*. From *Inleyding tot de hooge schooler schilderkonst* 1678.



## Today

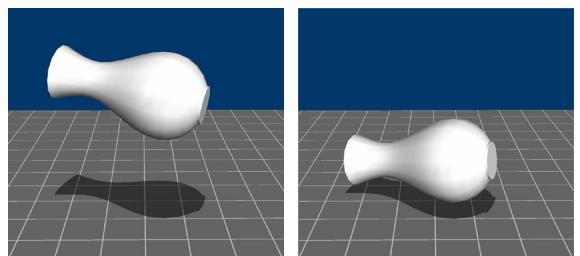
- Why are Shadows Important?
- Shadows & Soft Shadows in Ray Tracing
- Planar Shadows
- Projective Texture Shadows
  - Shadow View Duality
  - Texture Mapping
- Shadow Maps
- Shadow Volumes



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## Cast Shadows on Planar Surfaces

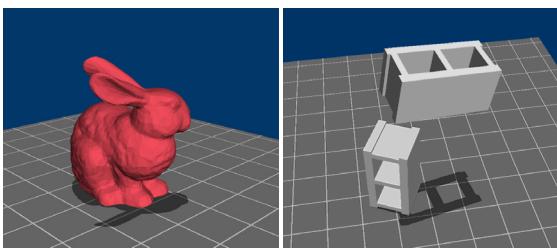
- Draw the object primitives a second time, projected to the ground plane



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## Limitations of Planar Shadows

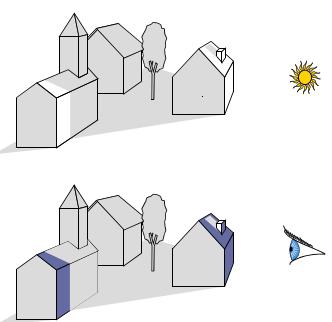
- Does not produce self-shadows, shadows cast on other objects, shadows on curved surfaces, etc.



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## Shadow/View Duality

- A point is lit if it is visible from the light source
- Shadow computation similar to view computation



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## Texture Mapping

- Don't have to represent everything with geometry



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## Projective Texture Shadow Limitations

- Must specify occluder & receiver
- No self-shadows
- Resolution

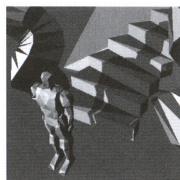
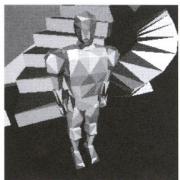


Figure from Moller & Haines "Real Time Rendering"

MIT EECS 6.837, Durand and Cutler

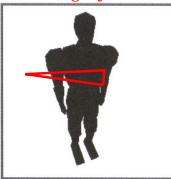
## Fake Shadows using Projective Textures

- Separate obstacle and receiver
- Compute b/w image of obstacle from light
- Use image as projective texture for each receiver

*Image from light source*



*BW image of obstacle*



*Final image*

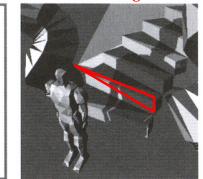


Figure from Möller & Haines "Real Time Rendering"

MIT EECS 6.837, Durand and Cutler

## Questions?

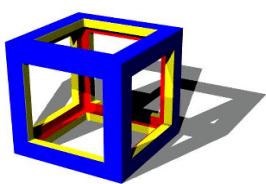


Plate 52 Grandville, *The Shadows (The French Cabinet)* from *La Caricature*, 1830.

MIT EECS 6.837, Durand and Cutler

## Today

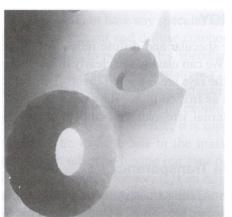
- Why are Shadows Important?
- Shadows & Soft Shadows in Ray Tracing
- Planar Shadows
- Projective Texture Shadows
- **Shadow Maps**
- Shadow Volumes



MIT EECS 6.837, Durand and Cutler

## Shadow Maps

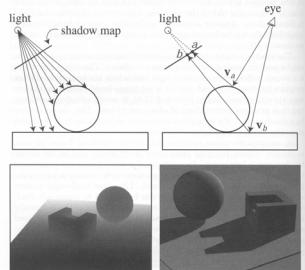
- In Renderman
  - (High-end production software)



MIT EECS 6.837, Durand and Cutler

## Shadow Mapping

- Texture mapping with depth information
- Requires 2 passes through the pipeline:
  - Compute shadow map (depth from light source)
  - Render final image, check shadow map to see if points are in shadow

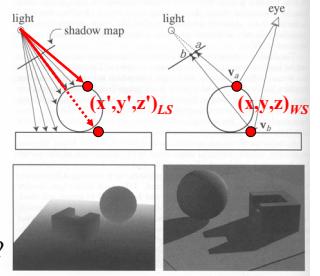


Foley et al. "Computer Graphics Principles and Practice"

MIT EECS 6.837, Durand and Cutler

## Shadow Map Look Up

- We have a 3D point  $(x, y, z)_{WS}$
- How do we look up the depth from the shadow map?

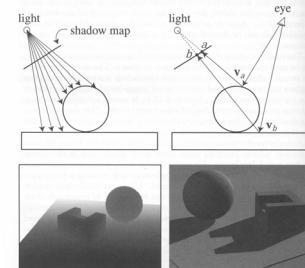


Foley et al. "Computer Graphics Principles and Practice"

MIT EECS 6.837, Durand and Cutler

## Limitations of Shadow Maps

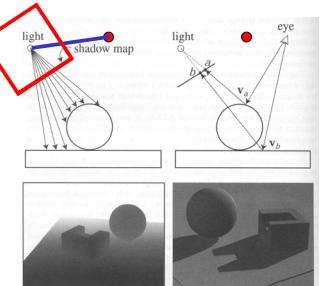
1. Field of View
2. Bias (Epsilon)
3. Aliasing



MIT EECS 6.837, Durand and Cutler

## 1. Field of View Problem

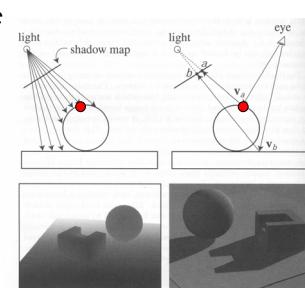
- What if point to shadow is outside field of view of shadow map?
  - Use cubical shadow map
  - Use only spot lights!



MIT EECS 6.837, Durand and Cutler

## 2. The Bias (Epsilon) Nightmare

- For a point visible from the light source  
 $\text{ShadowMap}(x', y') \approx z'$
- How can we avoid erroneous self-shadowing?
  - Add bias (epsilon)

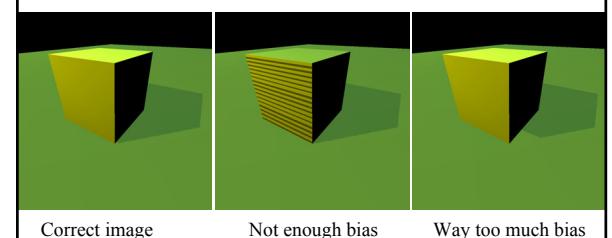


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## 2. Bias (Epsilon) for Shadow Maps

$\text{ShadowMap}(x', y') + \text{bias} < z'$

Choosing a good bias value can be very tricky



Correct image

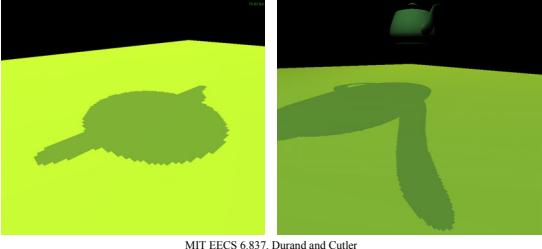
Not enough bias

Way too much bias

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### 3. Shadow Map Aliasing

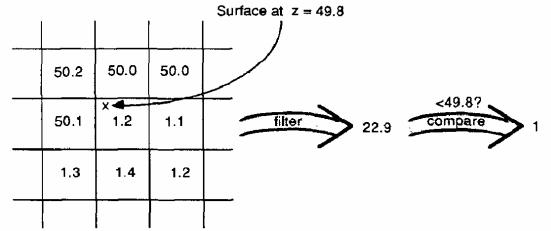
- Under-sampling of the shadow map
- Reprojection aliasing – especially bad when the camera & light are opposite each other



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### 3. Shadow Map Filtering

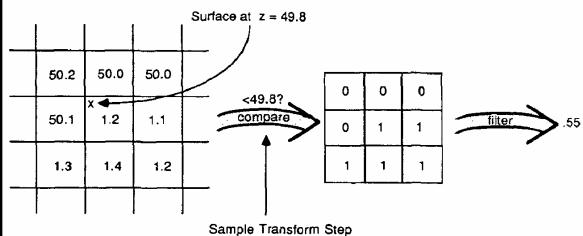
- Should we filter the depth? (weighted average of neighboring depth values)
- No... filtering depth is not meaningful



a) Ordinary texture map filtering. Does not work for depth maps.

### 3. Percentage Closer Filtering

- Instead filter the result of the test (weighted average of comparison results)
- But makes the bias issue more tricky



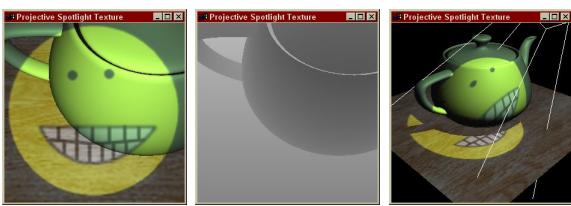
### 3. Percentage Closer Filtering

- 5x5 samples
- Nice antialiased shadow
- Using a bigger filter produces fake soft shadows
- Setting bias is tricky



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### Projective Texturing + Shadow Map



Light's View

Depth/Shadow Map

Eye's View

Images from Cass Everitt et al.,  
“Hardware Shadow Mapping”  
NVIDIA SDK White Paper

MIT EECS 6.837, Durand and Cutler

### Shadows in Production

- Often use shadow maps
- Ray casting as fallback in case of robustness issues



Figure 12. Frame from *Laco Jr.*

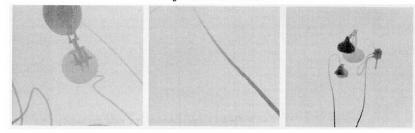
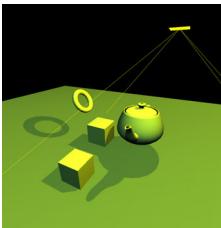


Figure 13. Shadow maps from *Laco Jr.*

## Hardware Shadow Maps

- Can be done with hardware texture mapping
  - Texture coordinates u,v,w generated using 4x4 matrix
  - Modern hardware permits tests on texture values



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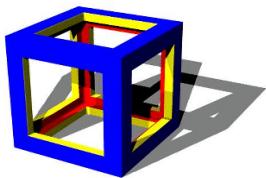
## Questions?



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## Today

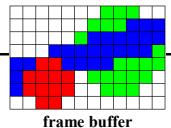
- Why are Shadows Important?
- Shadows & Soft Shadows in Ray Tracing
- Planar Shadows
- Projective Texture Shadows
- Shadow Maps
- **Shadow Volumes**
  - The Stencil Buffer



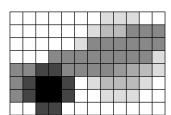
MIT EECS 6.837, Durand and Cutler

## Stencil Buffer

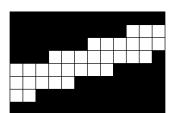
- Tag pixels in one rendering pass to control their update in subsequent rendering passes
  - "For all pixels in the frame buffer" → "For all *tagged* pixels in the frame buffer"
- Can specify different rendering operations for each case:
  - stencil test fails
  - stencil test passes & depth test fails
  - stencil test passes & depth test passes



frame buffer



depth buffer

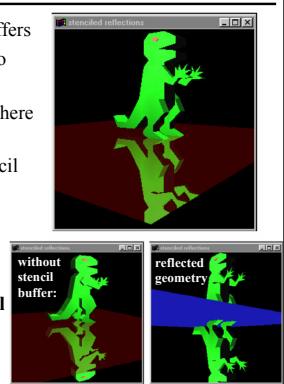


stencil buffer

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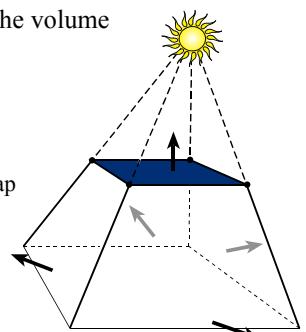
## Stencil Buffer – Real-time Mirror

- Clear frame, depth & stencil buffers
- Draw all non-mirror geometry to frame & depth buffers
- Draw mirror to stencil buffer, where depth buffer passes
- Set depth to infinity, where stencil buffer passes
- Draw reflected geometry to frame & depth buffer, where stencil buffer passes



## Shadow Volumes

- Explicitly represent the volume of space in shadow
- For each polygon
  - Pyramid with point light as apex
  - Include polygon to cap
- Shadow test similar to clipping



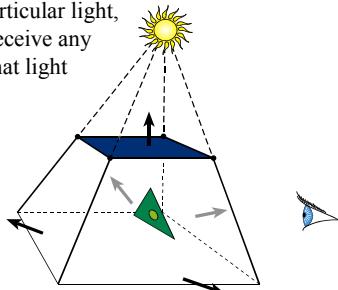
MIT EECS 6.837, Durand and Cutler

See NVIDIA's stencil buffer tutorial  
<http://developer.nvidia.com>

also discusses blending, multiple mirrors, objects behind mirror, etc...

## Shadow Volumes

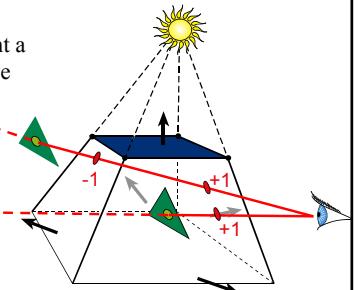
- If a point is inside a shadow volume cast by a particular light, the point does not receive any illumination from that light
- Cost of naive implementation:  
#polygons \* #lights



MIT EECS 6.837, Durand and Cutler

## Shadow Volumes

- Shoot a ray from the eye to the visible point
- Increment/decrement a counter each time we intersect a shadow volume polygon (*check z buffer*)
- If the counter  $\neq 0$ , the point is in shadow



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## Shadow Volumes w/ the Stencil Buffer

Initialize stencil buffer to 0

Draw scene with ambient light only

Turn off frame buffer & z-buffer updates

Draw front-facing shadow polygons

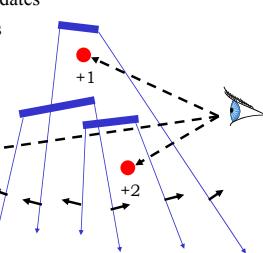
If z-pass → increment counter

Draw back-facing shadow polygons

If z-pass → decrement counter

Turn on frame buffer updates

Turn on lighting and  
redraw pixels with  
counter = 0



MIT EECS 6.837, Durand and Cutler

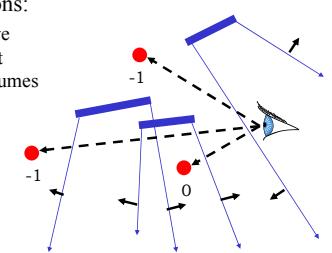
## If the Eye is in Shadow...

- ... then a counter of 0 does not necessarily mean lit



- 3 Possible Solutions:

- Explicitly test eye point with respect to all shadow volumes
- Clip the shadow volumes to the view frustum
- "Z-Fail" shadow volumes



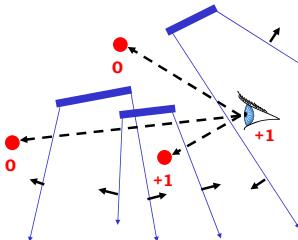
MIT EECS 6.837, Durand and Cutler

## 1. Test Eye with Respect to Volumes

- Adjust initial counter value



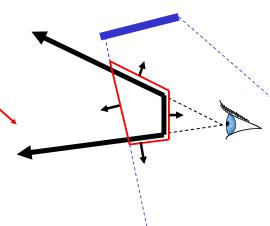
*Expensive*



MIT EECS 6.837, Durand and Cutler

## 2. Clip the Shadow Volumes

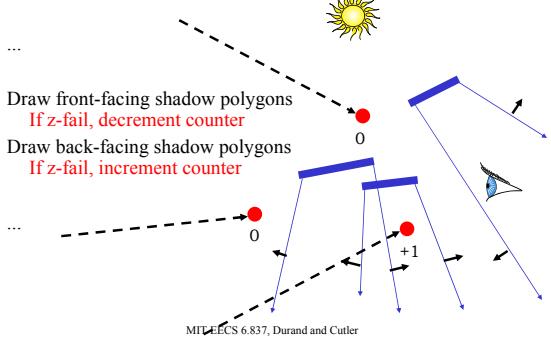
- Clip the shadow volumes to the view frustum and include these new polygons
- Messy CSG*



MIT EECS 6.837, Durand and Cutler

### 3. "Z-Fail" Shadow Volumes

Start at infinity



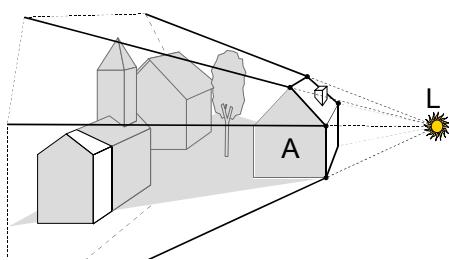
### 3. "Z-Fail" Shadow Volumes

- Introduces problems with far clipping plane
- Solved by clamping the depth during clipping

MIT EECS 6.837, Durand and Cutler

### Optimizing Shadow Volumes

- Use silhouette edges only (edge where a back-facing & front-facing polygon meet)



### Limitations of Shadow Volumes

- Introduces a lot of new geometry
- Expensive to rasterize long skinny triangles
- Limited precision of stencil buffer (counters)
  - for a really complex scene/object, the counter can overflow
- Objects must be watertight to use silhouette trick
- Rasterization of polygons sharing an edge must not overlap & must not have gap

MIT EECS 6.837, Durand and Cutler

### Questions?

- From last year's quiz: Check the boxes to indicate the features & limitations of each technique

Features / Limitations	Planar Fake Shadows	Projective Texture Shadows	Shadow Maps	Shadow Volumes	Ray Casting Shadows
Allows objects to cast shadows on themselves (self shadowing)					
Permits shadows on arbitrary surfaces (i.e. curved)					
Renders geometry from the viewpoint of the light					
Generates extra geometric primitives					
Limited resolution of intermediate representation can result in jaggie shadow artifacts					

MIT EECS 6.837, Durand and Cutler

### Next Time:

## Global Illumination: Radiosity & The Rendering Equation

MIT EECS 6.837, Durand and Cutler