

THE OUTPUT RESISTANCE OF A POWER SUPPLY

AN INTRODUCTORY UNCERTAINTY ANALYSIS EXERCISE

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ABSTRACT

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1 INTRODUCTION

Sources of electricity produce a voltage potential across their terminals called an electromotive force (*emf*) or an open circuit voltage, V_{∞} . In practice, when a closed circuit is made, a current I will be drawn and the voltage at the terminals, V called *terminal voltage* will fall below V_{∞} . For most cases, many powers sources will exhibit a linear variation of R for small current values, with nonlinear behaviour at higher currents. The linear part of the curve can be described by:

$$V = V_{\infty} - RI$$

where R is the *output resistance of the powers source*. In this linear regime, according to Thevenin's theorem, the power source is completely represented by the equivalent circuit shown below.

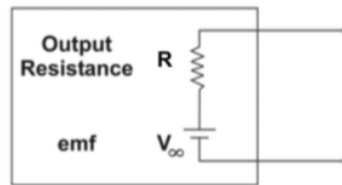


Figure 1: Equivalent circuit of an electric power source.

The output resistance (R) can be determined by attaching different external resistances of the load (R_l) to the power source, and measuring the current and voltage with a multimeter. 2 shows two possible ways of doing this. Both would be equivalent **if** the multimeter were ideal. However, in this exercise we will measure with real, not ideal, multimeters.

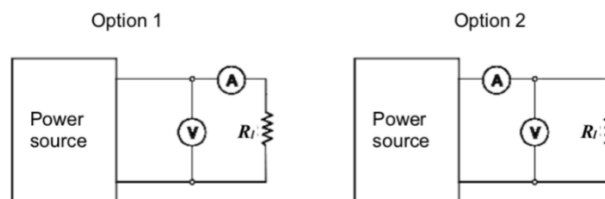


Figure 2: Possible circuits for determining the output resistance of a power source.

2 PRE-LAB EXERCISES

Without connecting circuits and making measurements, we can expect the the voltmeter and ammeter readings to differ between the two options due to current and voltage leakage. More specifically, in option 1, we can expect the current to differ as the voltmeter allows some current to pass through. The amount of leakage will depend on the load resistance. Similarly, in option 2, we can expect that the voltage will differ as the ammeter will draw some voltage. Its leakage will too depend on the load resistance.

To calculate the internal resistances of the voltmeter and the ammeter we can use basic current and voltage division. For the voltmeter, we can calculate the current that we expect to pass through the ammeter and solve for the voltmeter resistance.

$$I_{\text{ammeter}} = I \frac{R_{\text{voltmeter}}}{R_{\text{load}} + R_{\text{voltmeter}}}$$

$$I(R_{\text{load}} + R_{\text{voltmeter}}) = R_{\text{voltmeter}}$$

$$R_{\text{voltmeter}} = \frac{IR_{\text{load}}}{1 - I}$$

We can calculate the internal resistance of the ammeter similarly by using voltage division for the second circuit:

$$I_{\text{ammeter}} = \frac{V}{R_{\text{ammeter}} + R_{\text{load}}}$$

$$I(R_{\text{ammeter}} + R_{\text{load}}) = V$$

$$R_{\text{ammeter}} = \frac{V}{I_{\text{ammeter}}} - R_{\text{load}}$$

3 THE EXPERIMENT

We began by measuring the resistance values of the provided resistors. For the subsequent circuit experiments, we selected the two highest and two lowest resistance values to represent the load resistance conditions for the voltmeter and ammeter configurations, respectively. The measured values with their associated uncertainties are presented below.

Table 1: Measured Resistor Values and Uncertainties

	R_{l1}	R_{l2}	R_{l3}	R_{l4}	R_{l5}	R_{l6}
Value (Ω)	100.32	219.91	461.3	2.6960 k	26.814 k	101.57 k
Uncertainty (Ω)	± 0.25	± 0.49	± 1.4	± 5.9	± 59	± 250

INCLUDE DIAGRAM/SKETCH OF CIRCUIT OPTION 1

Table 2: Circuit 1 Readings & Results

Resistance R_{li} (Ω)	Uncertainty ΔR_{li} (Ω)	Voltage V (V)	Uncertainty ΔV (V)	Current I (mA)	Uncertainty ΔI (mA)	Ammeter Resistance R_A (Ω)	Uncertainty ΔR_A (Ω)
100.32	± 0.25	6.501	± 0.005	63.67	± 0.18		
219.91	± 0.49	6.501	± 0.005	29.315	± 0.064		
26.814 k	± 0.059 k	6.501	± 0.005	0.241	± 0.051		
101.57 k	± 0.25 k	6.501	± 0.005	0.063	± 0.005		
Average:							

INCLUDE DIAGRAM/SKETCH OF CIRCUIT OPTION 2

Table 3: Circuit 2 Readings & Results

Resistance $R_{l_i} (\Omega)$	Uncertainty $\Delta R_{l_i} (\Omega)$	Voltage $V (V)$	Uncertainty $\Delta V (V)$	Current $I (mA)$	Uncertainty $\Delta I (mA)$	Voltmeter Resistance $R_V (\Omega)$	Uncertainty $\Delta R_V (\Omega)$
100.32	± 0.25	6.386	± 0.005	63.60	± 0.18		
219.91	± 0.49	6.448	± 0.005	29.322	± 0.064		
26.814 k	± 0.059 k	6.501	± 0.005	0.243	± 0.051		
101.57 k	± 0.25 k	6.501	± 0.005	0.065	± 0.005		
					Average:		

4 DISCUSSION

5 CONCLUSION