

SOLUTIONS TO ASSIGNMENT

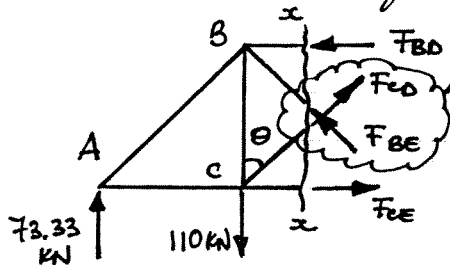
1. Calculate the reaction forces on the FBD of the whole truss:

$$\sum M_A = 0 \quad F_y(12) - 110(4) = 0 \quad \therefore F_y = 36.67 \text{ kN} \uparrow$$

$$\sum F_x = 0 \quad \therefore A_x = 0$$

$$\sum F_y = 0 \quad A_y + 36.67 - 110 = 0 \quad \therefore A_y = 73.33 \text{ kN} \uparrow$$

- Cut the truss through members BD, BE, CD and CE and use the LHS of the resulting FBD.



One of these members must be in tension while the other must "go into compression" and hence go slack with zero force. For vertical equilibrium, the one in tension must have an upward vertical component of $110 - 73.33 = 36.67 \text{ kN}$, and that member can only be member CD. Therefore, $F_{BE} = 0 \text{ kN}$. Then,

$$\sum M_C = 0 \quad (-73.33)(4) + F_{BD}(3) = 0 \quad \therefore F_{BD} = 97.8 \text{ kN (C)}$$

$$\sum M_D = 0 \quad (-73.33)(8) + (110)(4) + F_{CE}(3) = 0 \quad \therefore F_{CE} = 48.9 \text{ kN (T)}$$

$$\sum F_y = 0 \quad 73.33 + F_{CD} \cos \theta - 110 = 0 \quad \therefore F_{CD} = 81.1 \text{ kN (T)}$$

- Design of member CE (Tension): Factored load: $F_f = (1.8)(48.9) = 88.02 \text{ kN}$

$$A_{req'd} = \frac{F_f}{\phi_y} = \frac{88.02 \times 10^3}{300} = 293.4 \text{ mm}^2; \quad \text{Select } \underline{L 55 \times 55 \times 3} \text{ with } A = 321 \text{ mm}^2$$

- Design of member BD (Compression): Factored load: $F_f = (2.0)(97.8) = 195.6 \text{ kN}$

- Yielding: $A_{req'd} = \frac{F_f}{\phi_y} = \frac{195.6 \times 10^3}{300} = 652 \text{ mm}^2$

- Buckling: $I_{req'd} = \frac{F_f L^2}{\pi^2 E} = \frac{(195.6 \times 10^3)(4000)^2}{\pi^2 (200,000)} = 1.585 \times 10^6 \text{ mm}^4$

Select a section with both $A \geq A_{req'd}$ and $I \geq I_{req'd}$

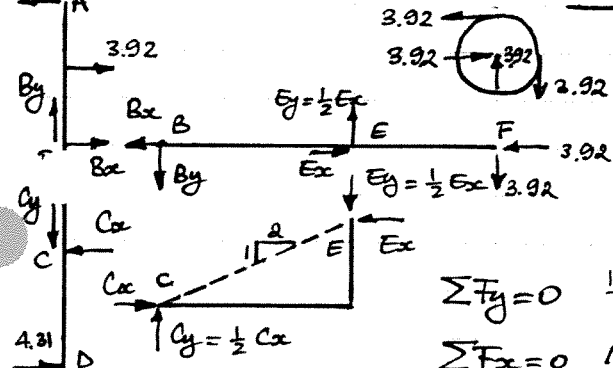
Sections which can be selected: $\left\{ \begin{array}{l} L 90 \times 90 \times 13, A = 2,170 \text{ mm}^2, I = 1.60 \times 10^6 \text{ mm}^4 \\ L 100 \times 100 \times 10, A = 1,900 \text{ mm}^2, I = 1.80 \times 10^6 \text{ mm}^4 \end{array} \right.$

Of these, select L 100 x 100 x 10 since it has a lower mass (14.9 kg/m) and, hence, is cheaper.

2. The frame is RIGID if removed from its supports, so calculate the reactions at A and D first

$$W = (400)(9.81) = 3.92 \text{ kN}. \quad \sum M_A = 0 \quad (-3.92)(5.5) + D_x(5) = 0 \quad \therefore D_x = 4.31 \text{ kN} \rightarrow$$

$$\sum F_x = 0 \quad 4.31 - A_x = 0 \quad \therefore A_x = 4.31 \text{ kN} \leftarrow; \quad \sum F_y = 0 \quad A_y - 3.92 = 0 \quad \therefore A_y = 3.92 \text{ kN} \uparrow$$



Then, separate the component parts and draw FBDs as shown. Note that member CE is a two force member being acted upon by two forces along line CE, or by the equivalent forces shown.

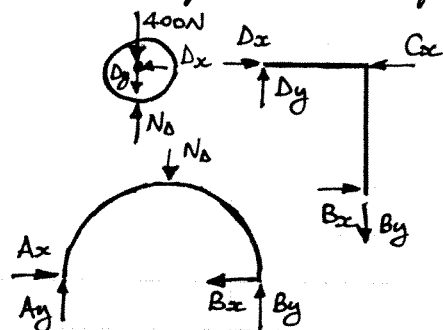
• On FBD of member BF: $\sum M_B = 0 \quad (-3.92)(5) + \frac{1}{2} E_x(3) = 0$
 $\therefore E_x = 13.07 \text{ kN} \rightarrow$ and $E_y = \frac{1}{2} E_x = 6.54 \text{ kN} \uparrow$ (on BF)

$\sum F_y = 0 \quad \frac{13.07}{2} - B_y - 3.92 = 0 \quad \therefore B_y = 2.62 \text{ kN} \downarrow$
 $\sum F_x = 0 \quad 13.07 - B_x - 3.92 = 0 \quad \therefore B_x = 9.15 \text{ kN} \leftarrow$ } on BF

- On FBD of member CE: $\sum F_x = 0 \quad C_x = E_x = 13.07 \text{ kN} \rightarrow$
 $\sum F_y = 0 \quad C_y = E_y = 6.54 \uparrow$ } on CE.

3. Since the frame is RIGID, start by calculating the external reactions on a FBD of the entire frame
- $$\sum M_A = 0 \quad (-400)(3) + C_x(3.5) = 0 \quad \therefore C_x = 342.9 \text{ N} \leftarrow$$
- $$\sum F_x = 0 \quad A_x - 342.9 = 0 \quad \therefore A_x = 342.9 \text{ N} \rightarrow$$
- $$\sum F_y = 0 \quad A_y - 400 = 0 \quad \therefore A_y = 400 \text{ N} \uparrow$$

Then, separate the component parts and draw FBDs as shown:



- On FBD of member AB: $\sum F_x = 0 \quad 342.9 - B_x = 0 \quad \therefore B_x = 342.9 \text{ N} \leftarrow$ (on AB)
 $\sum M_B = 0 \quad (-400)(6) + N_D(3) = 0 \quad \therefore N_D = 800 \text{ N} \downarrow$
 $\sum F_y = 0 \quad 400 - 800 + B_y = 0 \quad \therefore B_y = 400 \text{ N} \uparrow$
- On FBD of the Disc: $\sum F_x = 0 \quad \therefore D_x = 0$ (on Disc)
 $\sum F_y = 0 \quad 800 - 400 - D_y = 0 \quad \therefore D_y = 400 \text{ N} \downarrow$

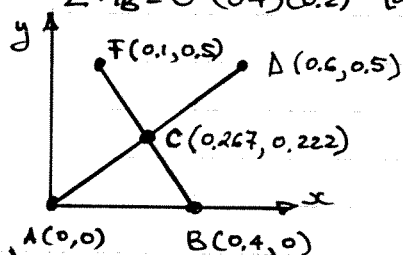
4. Again, this frame is RIGID, hence calculate the external reactions first:

$$\sum F_x = 0 \quad 24 - 28 \cos \theta = 0, \text{ where } \theta = \tan^{-1}(3/5) = 30.96^\circ. \text{ OK! (satisfied identically)}$$

$$\sum F_y = 0 \quad A_y + B_y - 84 - 28 \sin \theta = 0$$

$$\sum M_B = 0 \quad (84)(0.2) - (24)(0.5) - 0.4(A_y) + (28)\left(0.3 + \frac{0.5}{\cos 30.96^\circ}\right) = 0 \quad \therefore A_y = 73.82 \text{ N} \uparrow$$

$$B_y = 24.58 \text{ N} \uparrow$$



- To calculate the point of intersection of AD and BF (point C) write the equations of AD and BF and solve for x and y:

$$AD: y = \frac{0.5}{0.6}x = 0.833x; \quad BF: y = -\frac{0.5}{0.3}x + 0.667 = -1.667x + 0.667$$

$$\text{Hence, } x = 0.267 \text{ and } y = 0.222 \text{ and } C(0.267, 0.222)$$

Then, separate the component parts as shown:

- On FBD of DF:

$$\sum M_D = 0 \quad (84)(0.4) - (0.5)F_y = 0 \quad \therefore F_y = 67.2 \text{ N} \uparrow$$

$$\sum F_y = 0 \quad F_y + D_y - 84 = 0 \quad \therefore D_y = 16.8 \text{ N} \uparrow$$

$$\sum F_x = 0 \quad D_x - F_x + 24 = 0 \quad D_x = F_x - 24$$

- On FBD of BH:

$$\sum F_x = 0 \quad F_x + (x - (28) \cos 30.96^\circ) = 0 \quad \therefore C_y = 57.0 \text{ N} \uparrow$$

$$\sum F_y = 0 \quad 24.58 + C_y - 67.2 - 28 \sin 30.96^\circ = 0 \quad \therefore C_x = 91.0 \text{ N} \leftarrow$$

$$\sum M_C = 0 \quad (28)\left(0.3 + (0.167)/\sin 30.96^\circ\right) + (24.58)(0.133) + (67.2)(0.167) - F_x(0.278) = 0 \quad \therefore F_x = 115.1 \text{ N} \rightarrow$$

$$F_y = 67.2 \text{ N} \downarrow$$

5. The frame is NON-RIGID, so analyse the component parts first:

- On FBD of CD:

$$\sum F_x = 0 \quad D_x = 0$$

$$\sum M_D = 0 \quad C_y(3) - (6)(4) = 0 \quad \therefore C_y = 8 \text{ kN} \uparrow$$

$$\sum F_y = 0 \quad 8 - 6 - D_y = 0 \quad \therefore D_y = 2 \text{ kN} \downarrow$$

- On FBD of AC:

$$\sum M_A = 0 \quad (-8)(4) + B_y(2) = 0 \quad \therefore B_y = 16 \text{ kN} \uparrow \text{ on AC}$$

- On FBD of BE:

$$\sum M_E = 0 \quad (2)(1) - (0)(1) - 16(2) - B_x(2) = 0 \quad \therefore B_x = 15 \text{ kN} \leftarrow \text{on B}$$

- On FBD of AC:

$$\sum F_y = 0 \quad -8 + 16 - A_y = 0 \quad \therefore A_y = 8 \text{ kN} \downarrow$$

$$\sum F_x = 0 \quad 15 - A_x = 0 \quad \therefore A_x = 15 \text{ kN} \leftarrow$$

