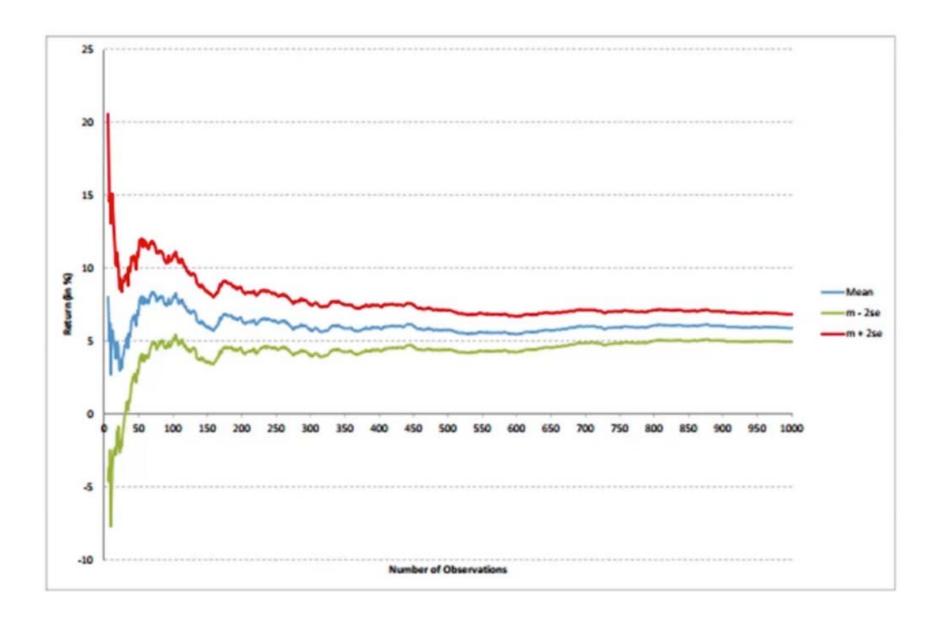
1 a) SE_i = $\sqrt{var(m_i)} = \sqrt{s^2/i} = s/\sqrt{i}$, where $s^2 = \frac{1}{i-1}\sum_{h=1}^{i}(y_h - m_i)^2$



b)
$$SC = \sigma/\sqrt{n}$$
 $4\sigma/\sqrt{n} = 1$ $n = 16\sigma^{2}$
 $\sigma = 15\%$ $16 \cdot 15^{2} = 3600$ years

2a) $E[y] = H R = \begin{pmatrix} u_{11} & o_{11} \\ o_{12} & u_{12} \end{pmatrix} \begin{pmatrix} u_{11} \\ v_{22} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} \begin{pmatrix} u_{11} & o_{11} \\ o_{12} & u_{22} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{12} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{12} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{11} + o_{11} \\ o_{11} & u_{11} + o_{11} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{11} + o_{11} \\ o_{11} & u_{11} + o_{11} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & o_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{12} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{11} \\ o_{11} & u_{11} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{11} \\ o_{11} & u_{11}$

$$\begin{array}{l} \text{e)} \ \ M = \ \prod_{n} - H \prod_{n} \prod_{n} \\ = \left(\begin{array}{c} I_{n_{1}} & O_{n_{1},n_{2}} \\ O_{n_{2}}n_{1} & I_{n_{2}} \end{array} \right) - \left(\begin{array}{c} I_{n_{1}} & O_{n_{1}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & O_{n_{1}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) - \left(\begin{array}{c} I_{n_{1}} & O_{n_{1}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & O_{n_{1}} \\ O_{n_{1}} & I_{n_{2}} \end{array} \right) - \left(\begin{array}{c} I_{n_{1}} & I_{n_{1}} \\ O_{n_{1}} & I_{1} & I_{1} \end{array} \right) - \left(\begin{array}{c} I_{n_{1}} & I_{n_{1}} \\ O_{n_{1}} & I_{1} & I_{1} \end{array} \right) - \left(\begin{array}{c} I_{n_{1}} & I_{n_{1}} \\ O_{n_{1}} & I_{1} & I_{1} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & O_{n_{1}} \\ O_{n_{1}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & O_{n_{1}} \\ O_{n_{1}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} & I_{n_{2}} \end{array} \right) \left(\begin{array}{c} I_{n_{1}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} & I_{n_{2}} \\ O_{n_{2}} &$$

$$=\begin{pmatrix} H_1 & O_{N_1}N_2 \\ O_{2N_1} & M_2 \end{pmatrix} = M$$

$$f$$
) $Var(2) = M var(y)M' = M\sigma^2IM = O^2M$
 $f(z'Z) = f(tr(z'Z)) = f(tr(zz')) = tr(f(zz')) = tr(Z_z)$
 $= \sigma^2 tr(M) = (n-2)\sigma^2$

9)
$$f(z'z) = (n-2)\sigma^2$$

 $\frac{1}{n-2}z'z = \frac{1}{n-2}y' My = \frac{1}{n-2}(y-Hm)' (y-Hm)$

3.
$$\tilde{S}^{2} = \frac{n-1}{n} S^{2}$$

$$Var[\tilde{S}^{2}] = \frac{(n-1)^{2}}{n} Var[S^{2}] = \frac{(n-1)^{2}}{n^{2}} \frac{2\sigma^{4}}{n-1} = \frac{2(n-1)}{n^{2}} \sigma^{4}$$

$$E[\tilde{S}^{2}] = \frac{n-1}{n} \sigma^{2} \longrightarrow \sigma^{2} \quad \text{for } n \longrightarrow \infty$$

$$Var[\tilde{S}^{2}] = \frac{2(n-1)}{n^{2}} \sigma^{4} \longrightarrow \sigma \quad \text{for } n \longrightarrow \infty$$