2.
$$y_i \sim N(0,1)$$
 $Z = \sum_{i=1}^{n} y_i^{2}$
 $Yar(2) = f[(\sum_{i=1}^{n} y_i^{2} - n)^{2}] = f[\sum_{i=1}^{n} \sum_{j=1}^{n} y_i^{2} y_j^{2}] = 2n f[\sum_{i=1}^{n} y_i^{2}] + n^{2}$
 $= f[\sum_{i=1}^{n} y_i^{2}] + 2f[\sum_{i=1}^{n} \sum_{j=1}^{n} y_i^{2} y_j^{2}] - n^{2}$
 $= \sum_{i=1}^{n} f[y_i^{4}] + 2\sum_{i=1}^{n} \sum_{j=1}^{n} f[y_i^{2}] f[y_j^{2}] - n^{2}$
 $= 3n + 2 \cdot \frac{1}{2} n(n-1) - n^{2}$
 $= 3n + n^{2} - n - n^{2}$
 $= 2n$

E[yi4] = 3 y: and y, independent

3.
$$Z_i = \sum_{l=1}^{ki} y_1^2$$
 $Z_1 + Z_2 = \sum_{l=1}^{2} \sum_{j=1}^{ki} y_j^2$ $Z_1 + Z_2 = \sum_{l=1}^{2} \sum_{j=1}^{ki} y_j^2$

4. a)
$$E[y] = E[(-1(x-M))] = L^{-1}(E[x]-M) = L^{-1}(M-M) = 0$$

 $Var[y] = Var[L^{-1}(x-M)] = L^{-1}Var[x](L^{-1})^{2}$
 $= L^{-1}Z(L^{-1})^{2} = L^{-1}LL^{2}(L^{-1})^{2}$
 $= IL^{2}(L^{2})^{-1} = II$
 $= I$
 $y \sim N(0, I)$
b) $2 = (x-M)^{2}Z^{-1}(x-M) = (x-M)^{2}(LL^{2})^{-1}(x-M)$
 $= (x-M)^{2}(L^{2})^{-1}L^{-1}(x-M) = (x-M)^{2}(L^{-1})^{2}L^{-1}(x-M)$
 $= (L^{-1}(x-M))^{2}L^{-1}(x-M)$
(note the red prime '; the inverse in the video is a typo)
 $2 \sim \chi^{2}(n)$
 $x \sim x^{2}(n)$
 $= \frac{x^{2}}{n} \sim x^{2}(n)$
 $= \frac{x^{2}}{n} \sim x^{2}(n)$