# **MOOC** Econometrics

Lecture 3.3 on Model Specification: Transformation

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## Taking logarithms

Use for:

• Exponential growth.

#### Data transformation

Setting:

$$y_i = x_i'\beta + \varepsilon_i, \qquad i = 1, \ldots, n,$$

or

$$y = X\beta + \varepsilon$$

in matrix form.

What is the most appropriate form of the data (y and X)?

- All variables should be incorporated in a compatible manner.
- If this is not the case, data can be transformed.

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### Taking differences

Use for:

- Trending patterns
  - $\rightarrow$  Statistical assumptions may not hold.

First difference:

$$\Delta y_i = y_i - y_{i-1}.$$

#### Test

What is the result if you take the difference of  $y_i = i$ ?

Answer: For  $y_i = i$  the difference is:

$$\Delta y_i = y_i - y_{i-1} = i - (i-1) = 1.$$



#### Non-linear effects

$$y_i = x_i'\beta + \varepsilon_i = \beta_1 + \sum_{i=2}^k \beta_i x_{ji} + \varepsilon_i, \qquad i = 1, \ldots, n,$$

has linear set-up with fixed marginal effects  $(dy_i/dx_{ji} = \beta_j)$ .

Extension with interaction and quadratic terms:

$$y_i = \beta_1 + \sum_{j=2}^k \beta_j x_{ji} + \sum_{j=2}^k \gamma_{jj} x_{ji}^2 + \sum_{j=2}^k \sum_{h=j+1}^k \gamma_{jh} x_{ji} x_{hi} + \varepsilon_i.$$

Advantages:

- Get non-linear functional form.
- May provide economically meaningful specification.



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#### Dummy variables

Quarterly data

$$y_i = \alpha_i + \sum_{j=2}^k \beta_j x_{ji} + \varepsilon_i, \qquad i = 1, \dots, n,$$

where  $\alpha_i$  is the quarter-specific mean level.

Use dummy variables:

- $D_{hi}$  for h = 1, 2, 3, 4, with  $D_{hi} = 1$  if observation i is in quarter h (and  $D_{hi} = 0$  otherwise).
- Then

$$y_i = \alpha_1 D_{1i} + \alpha_2 D_{2i} + \alpha_3 D_{3i} + \alpha_4 D_{4i} + \sum_{j=2}^k \beta_j x_{ji} + \varepsilon_i$$

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## Example (from lecture 2.2)

•  $log(Wage)_i =$   $\beta_1 + \beta_2 Female_i + \beta_3 Age_i + \beta_4 Educ_i + \beta_5 Parttime_i + \varepsilon_i.$ 

•  $\log(\mathsf{Wage})_i =$   $\beta_1 + \beta_2 \mathsf{Female}_i + \beta_3 \mathsf{Age}_i + \beta_4 \mathsf{Educ}_i + \beta_5 \mathsf{Parttime}_i +$   $\gamma_1 \mathsf{Female}_i \mathsf{Educ}_i + \gamma_2 \mathsf{Age}_i^2 + \varepsilon_i.$ 

Now:

- Wage differential may depend on **gender**  $(\beta_2 + \gamma_1 \mathsf{Educ}_i)$ .
- Age has non-linear effect for wage  $(\beta_3 + 2\gamma_2 Age_i)$ .

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### **Dummy variables**

$$y_i = \alpha_1 D_{1i} + \alpha_2 D_{2i} + \alpha_3 D_{3i} + \alpha_4 D_{4i} + \sum_{j=2}^k \beta_j x_{ji} + \varepsilon_i.$$

#### Test

Can we add a constant term to the above specification that has a dummy for each quarter?

Answer: Only if one of the dummy parameters is set to 0.

If we omit  $D_{1i}$ , so  $\alpha_1 = 0$ , we get

$$y_i = \alpha_1 + \gamma_2 D_{2i} + \gamma_3 D_{3i} + \gamma_4 D_{4i} + \sum_{i=2}^k \beta_i x_{ji} + \varepsilon_i,$$

where  $\gamma_h = \alpha_h - \alpha_1$  for h = 2, 3, 4.

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## TRAINING EXERCISE 3.3

- Train yourself by making the training exercise (see the website).
- After making this exercise, check your answers by studying the webcast solution (also available on the website).

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