

$$\begin{aligned}
\sum_{j=1}^S (1-p)^{j-1} p &= p \sum_{j=0}^{S-1} (1-p)^{j-1} \\
&= p \frac{1 - (1-p)^S}{1 - (1-p)} \\
&= 1 - (1-p)^S
\end{aligned}$$

$$U_{t-1} = \sum_{s=t}^{\infty} \frac{u_s^{1-\rho}}{1-\rho} \beta^{1+s-t}$$

$$u_t = \begin{cases} w & \text{hvis beskæftiget} \\ b e^{-\eta S} & \text{hvis ikke beskæftiget} \end{cases}$$

State variable

$$e_t = \begin{cases} 1 & \text{if employed} \\ 0 & \text{if not employed} \end{cases}$$

$$V_t(e_{t-1}) = E_t \left[\sum_{s=t}^{\infty} \frac{u(e_s, S_s)^{1-\rho}}{1-\rho} \beta^{1+s-t} \right]$$

$$u(1, S_t) = w$$

$$u(0, S_t) = b e^{-\gamma S_t}$$

$$V_t(0) = \pi^{0,1} \left(\frac{w^{1-\rho}}{1-\rho} + \beta V_{t+1}(1) \right) + \pi^{0,0} \left(\frac{(b e^{-\gamma S})^{1-\rho}}{1-\rho} + \beta V_{t+1}(0) \right)$$

$$V_t(1) = \pi^{1,1} \left(\frac{w^{1-\rho}}{1-\rho} + \beta V_{t+1}(1) \right) + \pi^{1,0} \left(\frac{(b e^{-\gamma S})^{1-\rho}}{1-\rho} + \beta V_{t+1}(0) \right)$$

$$V(0) = \pi^{0,1} \left(\frac{w^{1-\rho}}{1-\rho} + \beta V(1) \right) + (1 - \pi^{0,1}) \left(\frac{(b e^{-\gamma S})^{1-\rho}}{1-\rho} + \beta V(0) \right)$$

$$V(1) = (1 - \delta) \left(\frac{w^{1-\rho}}{1-\rho} + \beta V(1) \right) + \delta \left(\frac{(b e^{-\gamma S})^{1-\rho}}{1-\rho} + \beta V(0) \right)$$

$$\begin{aligned}
\frac{d}{dS} V(0) &= \frac{d}{dS} \pi^{0,1} \left(\frac{w^{1-\rho}}{1-\rho} + \beta V(1) \right) + \pi^{0,1} \beta \frac{d}{dS} V(1) + (1 - \pi^{0,1}) \left(-\gamma (b e^{-\gamma S})^{-\rho} b e^{-\gamma S} + \beta \frac{d}{dS} V(0) \right) \\
&\quad - \frac{d}{dS} \pi^{0,1} \left(\frac{(b e^{-\gamma S})^{1-\rho}}{1-\rho} + \beta V(0) \right)
\end{aligned}$$

$$\frac{d}{dS}V(1) = (1-\delta)\left(\frac{w^{1-\rho}}{1-\rho} + \beta \frac{d}{dS}V(1)\right) + \delta\left(-\gamma(b e^{-\gamma S})^{-\rho} b e^{-\gamma S} + \beta \frac{d}{dS}V(0)\right)$$

$$(1-\pi^{0,1})\gamma(b e^{-\gamma S})^{1-\rho} = \frac{d}{dS}\pi^{0,1}\left(\frac{w^{1-\rho}}{1-\rho} - \frac{(b e^{-\gamma S})^{1-\rho}}{1-\rho} + \beta(V(1)-V(0))\right)$$

$$\delta\gamma(b e^{-\gamma S})^{1-\rho} = (1-\delta)\left(\frac{w^{1-\rho}}{1-\rho}\right)$$

$$\begin{aligned}\pi^{0,1} &= 1 - (1-p)^S \\ &= 1 - e^{S \log(1-p)}\end{aligned}$$

such that

$$\frac{d}{dS}\pi^{0,1} = -\log(1-p)(1-\pi^{0,1})$$

$$S = -\frac{1}{\gamma}\left(\frac{1}{1-\rho}\log\left(\frac{1-\delta}{\delta\gamma(1-\rho)}\right) + \log\left(\frac{w}{b}\right)\right)$$
