Quantitative Text Analysis

Meeting 6

- Supervised
 - An outcome variable is defined
 - Focus is on prediction
- Unsupervised
 - No outcome variable has been defined
 - Focus is on patterns

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Supervised

- Objective:
 - Classification of documents into pre existing categories

Supervised

- Create a labeled data set
- Classify documents with supervised learning algorithm
- Check performance

Labeled Dataset

- How:
 - Human coders annotate parts of the corpus (what we did together)
 - Found data (e.g., self-reported profession in users' profile)

- Considerations:
 - Sampling should be representative for the corpus (e.g., Random, Stratified sample e.g., across time and source)
 - Quality of human coding matters (Assess the intercoder reliability)
 - Number of documents

Labeled Dataset

- Number of documents
 - the higher the number of categories and the lower the reliability of the coders, the higher the number of documents (Barberá et al., 2021)
- increase the sizes of manually coded validation dataset as large as possible (e.g., more than 1% of all data to be examined), assuming acceptable reliability (equal to or higher than .7) (Song et al., 2021)

Splitting the Data

- Split labeled data in training data and test data (validation data)
- Training data
 - The subset that is used to learn the model parameters

- Test data
 - Another subset used to evaluate the model's predictive quality
 - Not used for learning!

Validation data

Document Classification

- Classifier learns the mapping between features and the labels in the training set
- define a model Y=g(X)
- And apply a learning algorithm to establish which features in X (features extracted from the training documents) matter to recover Y (i.e, the labels of the training documents)
- We fit the model

Model:

$$Y = f(X)$$

Objective function (e.g.,):

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2$$

Optimisation:

$$\underset{n}{argmin}_{\hat{Y}} \frac{1}{m} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2$$

Model:

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• Optimisation:

$$argmin_{\hat{Y}} \frac{1}{n} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2$$

Model:

$$Y = f(X)$$

Machine

Objective function (e.g.,):

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2$$

• Optimisation:

$$argmin_{\hat{Y}} \frac{1}{n} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2$$

Learning

Classify documents with supervised learning

- Considerations:
 - Feature representation (Bag of words representation or embeddings)
 - Feature selection (remove irrelevant features)
 - Classifier selection
 - E.g., Naive Bayes, SVM, KNN, or ensemble methods

Checking Performance

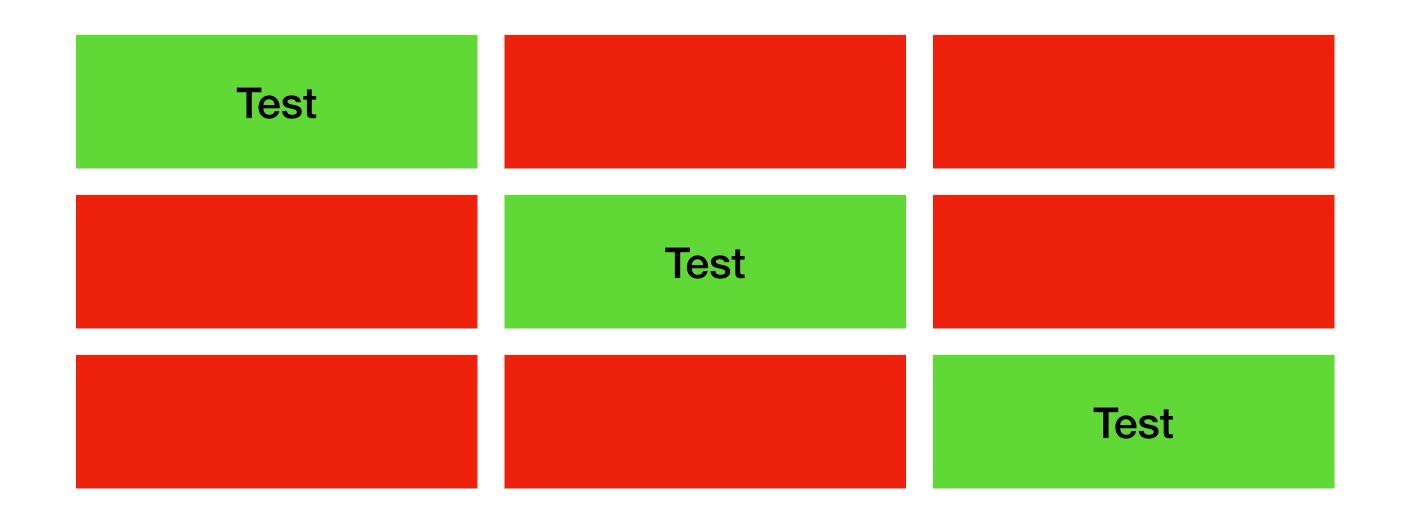
• The fitted model (the trained classifier) is applied to a held-out test set (which is a part of the labeled set but was not used for training the model).

- Considerations:
 - Danger of overfitting (focus on features that work well with training set but do not generalize)
 - Solutions: cross-validation
 - Performance metric (i.e., recall, precision)

Checking performance

- k-fold cross-validation
 - We randomly split the data into k sets ("folds") of roughly equal size
 - Each set is hold out once as test set, while training on the remaining sets
 - The problem of a lucky split is reduced

K-Fold Cross-Validation



Confusion Matrix

	Actual label	
	Negative	Positive
Negative	True negative	False positive
Positive	False negative	True positive

Precision/Recall

```
Accuracy = \frac{True\ Negative + True\ Positive}{True\ Negative + True\ Positive + False\ Negative + True\ Positive} Precision_{positive} = \frac{True\ Positive}{True\ Positive + False\ Positive} Recall_{positive} = \frac{True\ Positive}{True\ Positive + False\ Negatives}
```

Dictionary vs. supervised machine learning

• Dictionaries can be applied directly to a new corpus (but validate!)

Supervised machine learning requires (potentially larger amounts) labeled data

If the training sample is large enough supervised learning will outperform dictionaries

Additional considerations

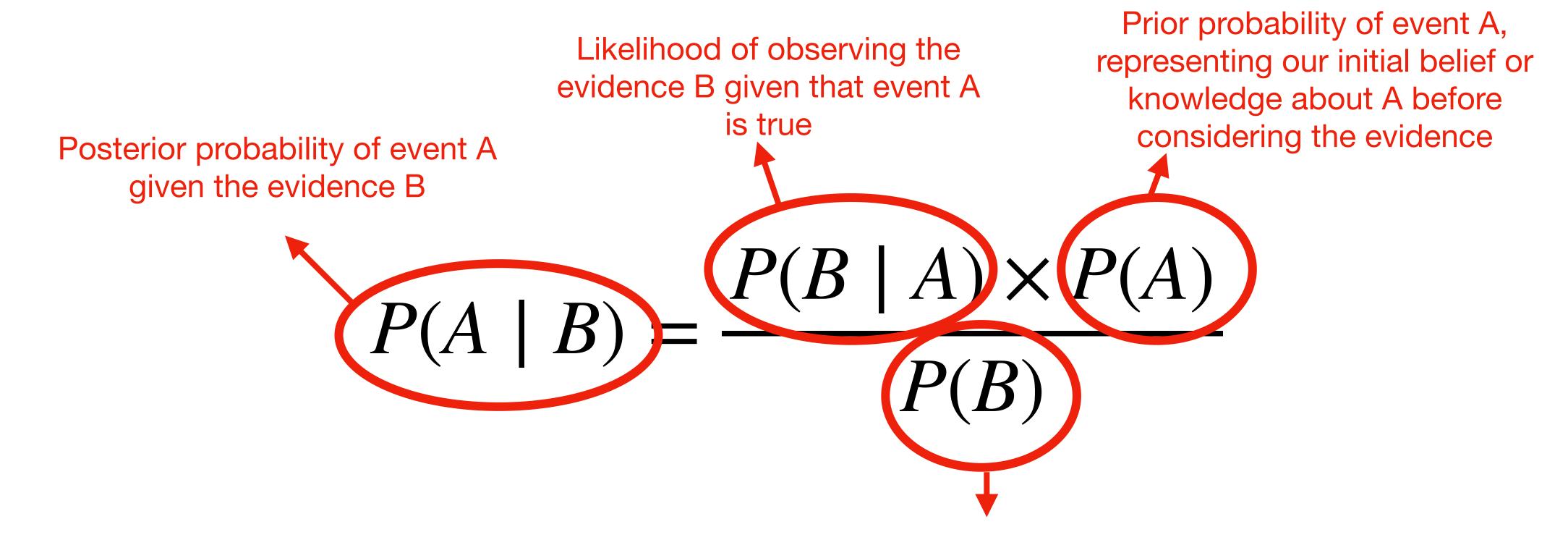
- Hyperparameter selection
 - Via systematic comparison of different hyperparameters per algorithm
- Random undersampling (Galar et al., 2011)
- Method to deal with unbalanced classes: use the max. number of positive instances per class and randomly sample the same number of instances of the negative class

- Probabilistic classifier
- Simple
- Fast
- Good Accuracy

Bayes Theorem

$$P(A \mid B) = \frac{P(B \mid A) \times P(A)}{P(B)}$$

Bayes Theorem

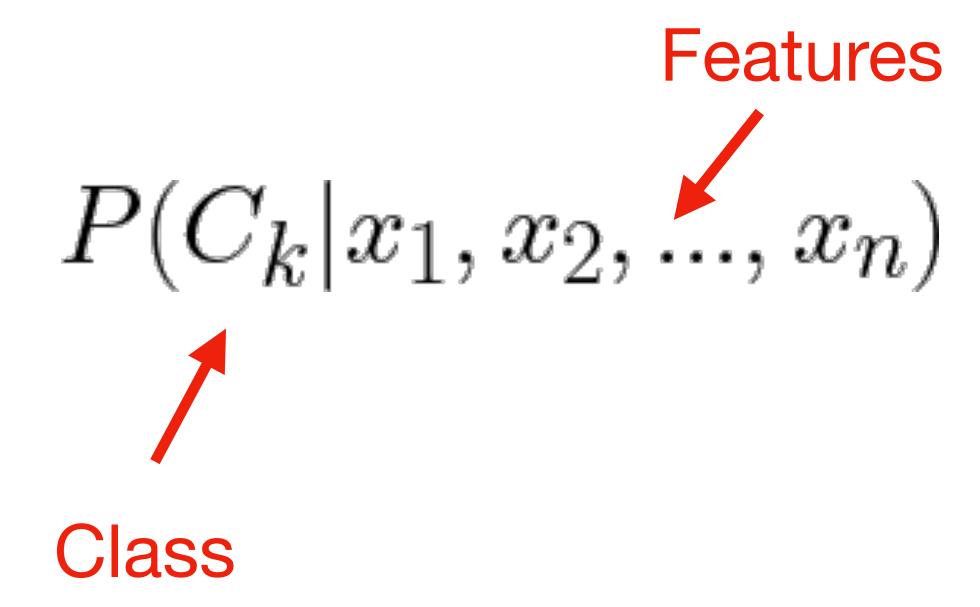


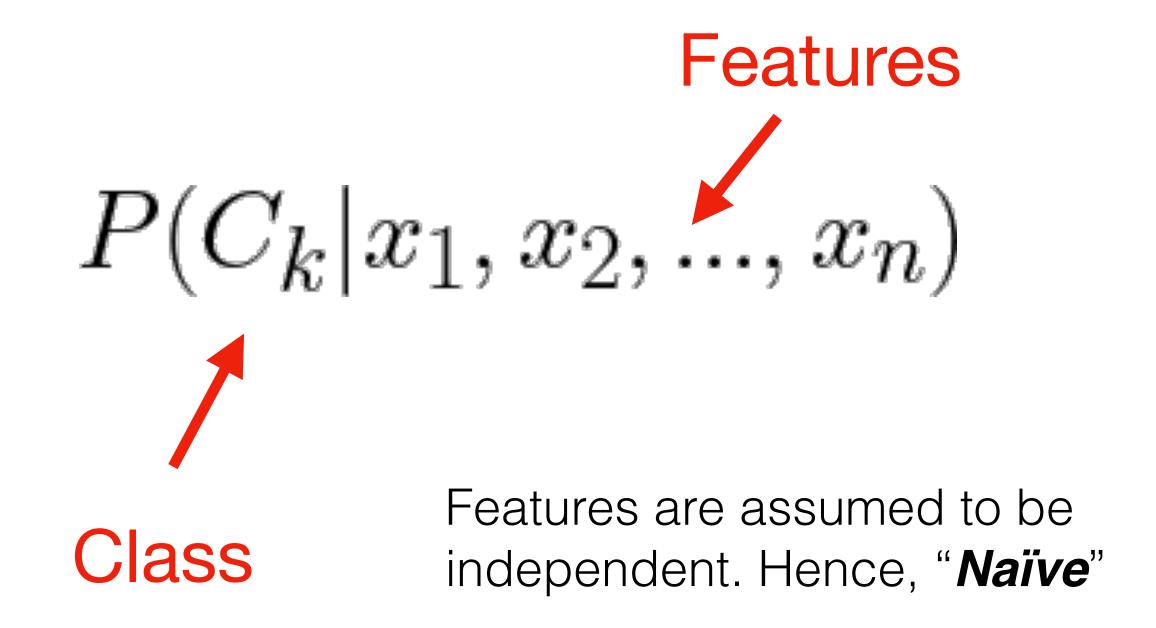
Probability of observing the evidence B

Bayes Theorem

$$P(A|B) \propto P(B|A) \times P(A)$$

$$P(C_k|x_1, x_2, ..., x_n)$$





$$P(C_k|\mathbf{x}) = \frac{P(C_k) \times P(\mathbf{x}|C_k)}{P(\mathbf{x})}$$

$$P(C_k|\mathbf{x}) \propto P(C_k) \times P(\mathbf{x}|C_k)$$

$$egin{aligned} p(C_k \mid x_1, \ldots, x_n) &\propto p(C_k, x_1, \ldots, x_n) \ &\propto p(C_k) \ p(x_1 \mid C_k) \ p(x_2 \mid C_k) \ p(x_3 \mid C_k) \ \cdots \ &\propto p(C_k) \prod_{i=1}^n p(x_i \mid C_k) \ , \end{aligned}$$

Decision Rule

$$\hat{y} = argmax \ p(C_k) \prod_{i=1}^{n} p(x_i | C_k)$$

Implemented in many stats/ML packages

Support Vector Machine

- Comes from computer science
- Very good
- Rather difficult math

Considered one of the best of-the-shelf classification algorithms

Hyperplane

n-1 dimensional plane that separates the n-dimensional space

Hyperplane

- n-1 dimensional plane that separates the n-dimensional space
- 2-dimensional hyperplane:

$$\beta_0 + \beta_1 X_1 = 0$$

Hyperplane

- n-1 dimensional plane that separates the n-dimensional space
- 2-dimensional hyperplane:
- line equation

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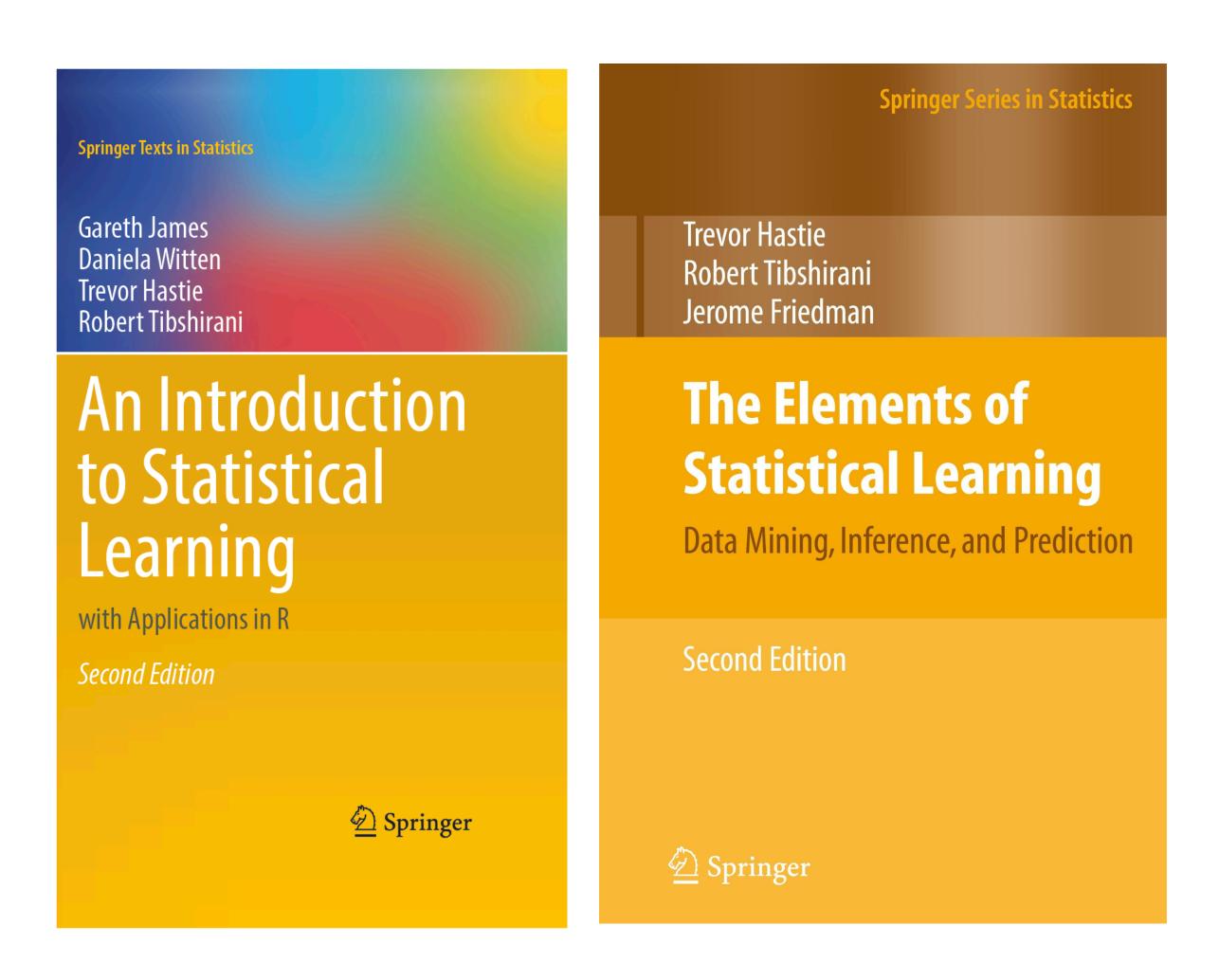
$$\beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_p X_p = 0$$

Classification

$$\beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_p X_p > 0.$$

$$\beta_0 + \beta_1 X_1 + \beta_2 X_2 + \ldots + \beta_p X_p < 0$$

Following images from:



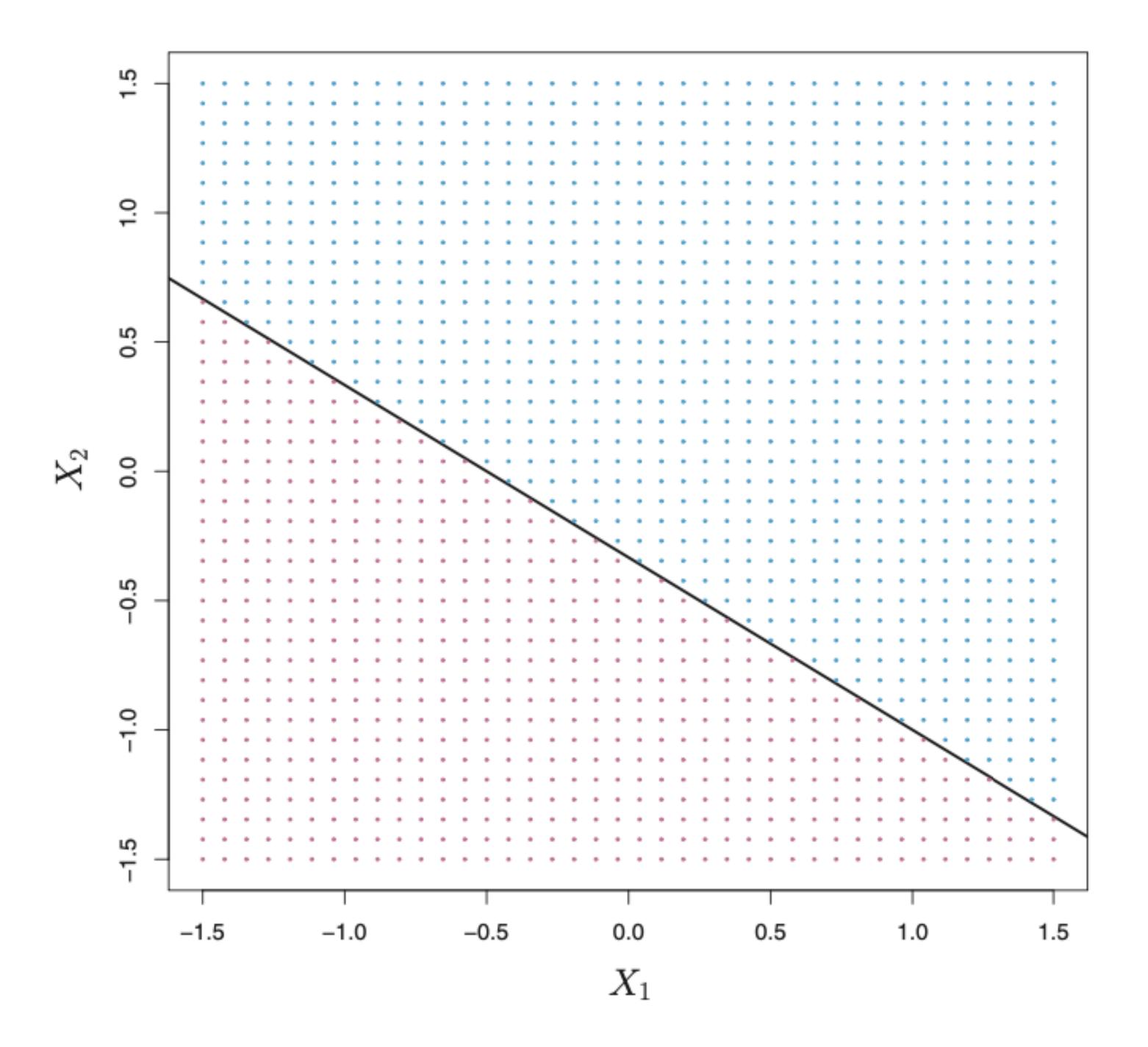
Springer Texts in Statistics

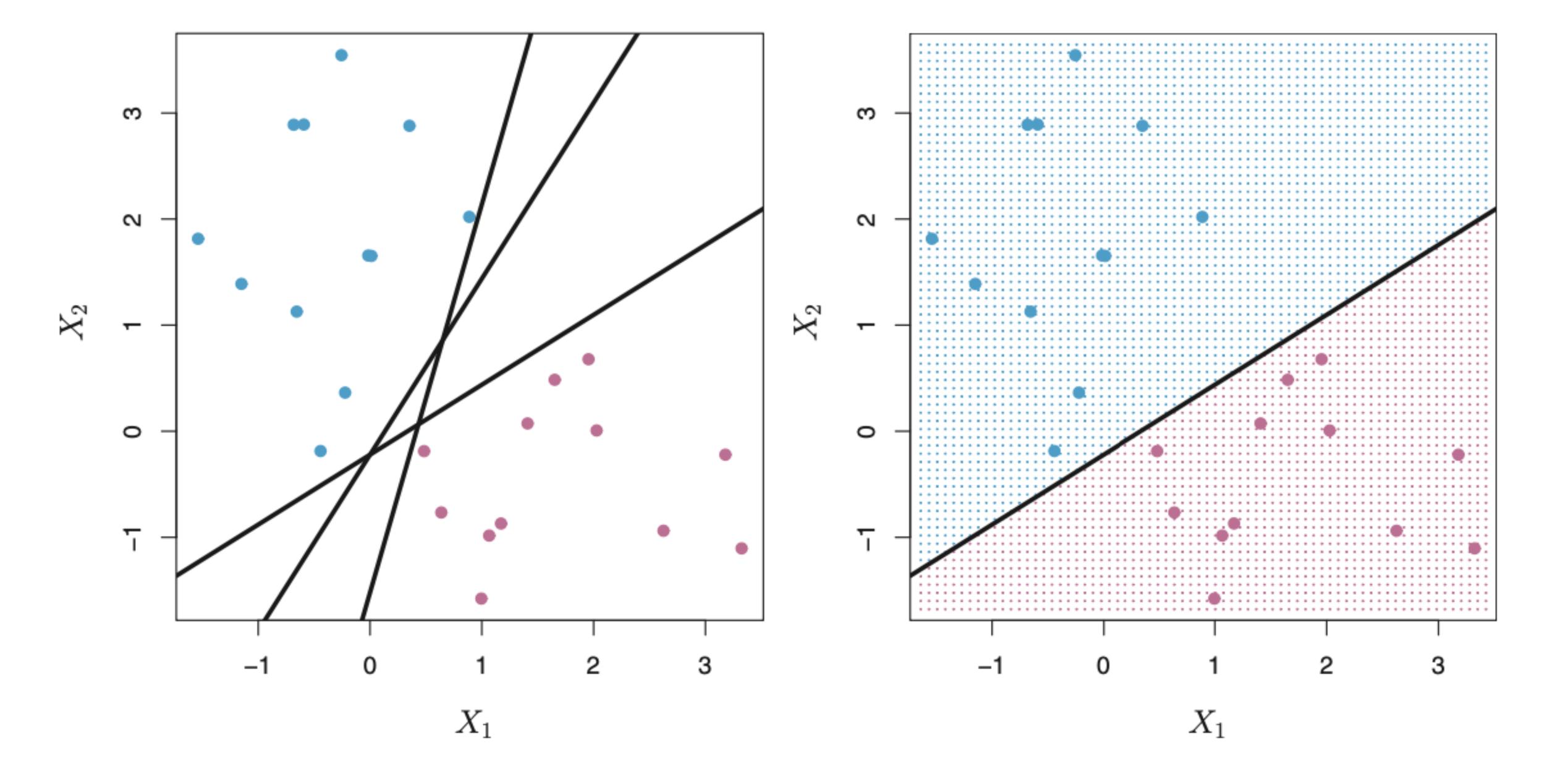
Gareth James · Daniela Witten · Trevor Hastie · Robert Tibshirani · Jonathan Taylor

An Introduction to Statistical Learning

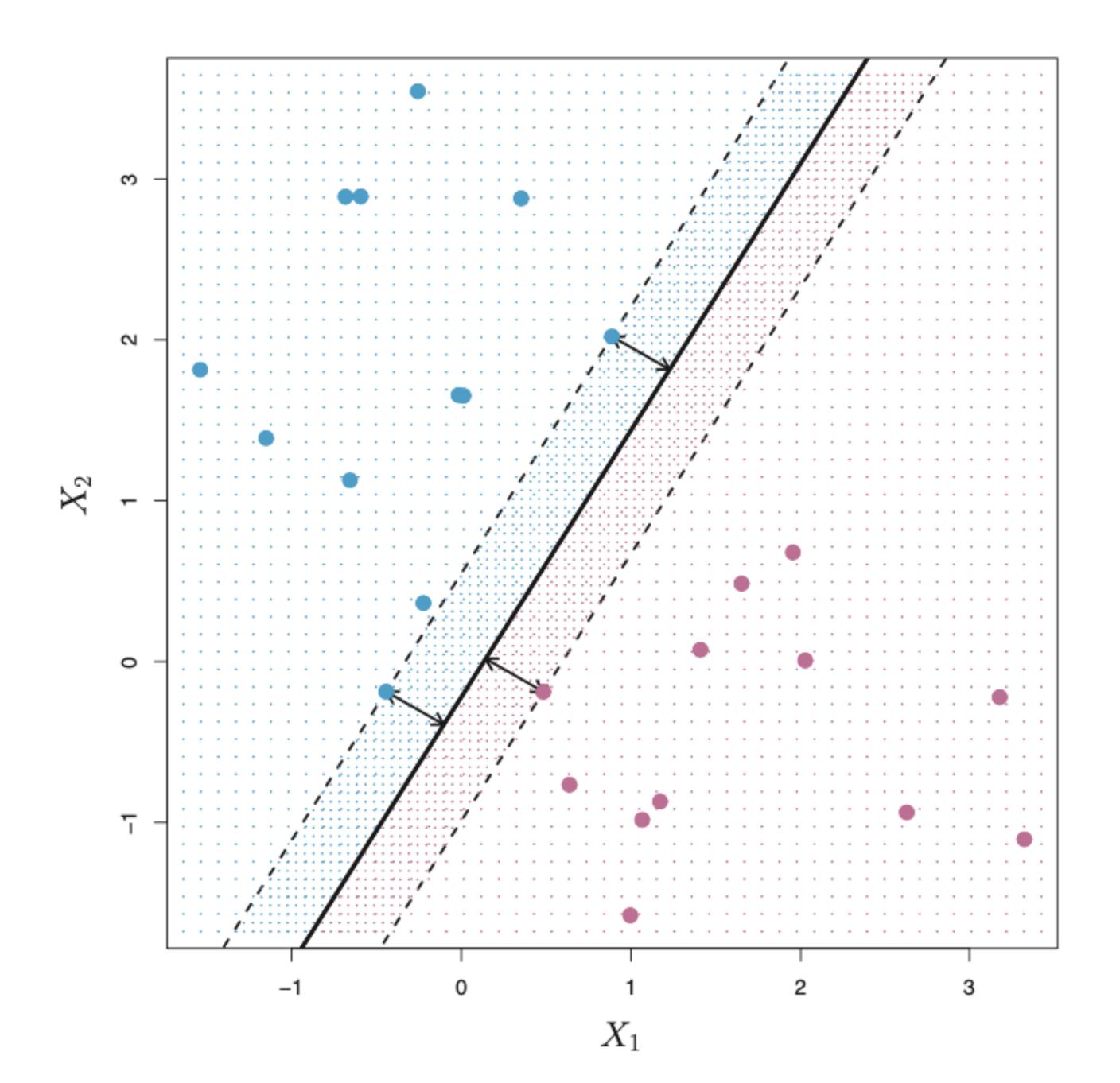
with Applications in Python







SV Classifier



Support Vector Machine

- Non-linear version of the Support Vector Classifier
- Extension using Kernels

Support Vector Machines

$$f(x) = \beta_0 + \sum_{i \in \mathcal{S}} \alpha_i \langle x, x_i \rangle$$

$$f(x) = \beta_0 + \sum_{i \in \mathcal{S}} \alpha_i K(x, x_i)$$

Support Vector Machines

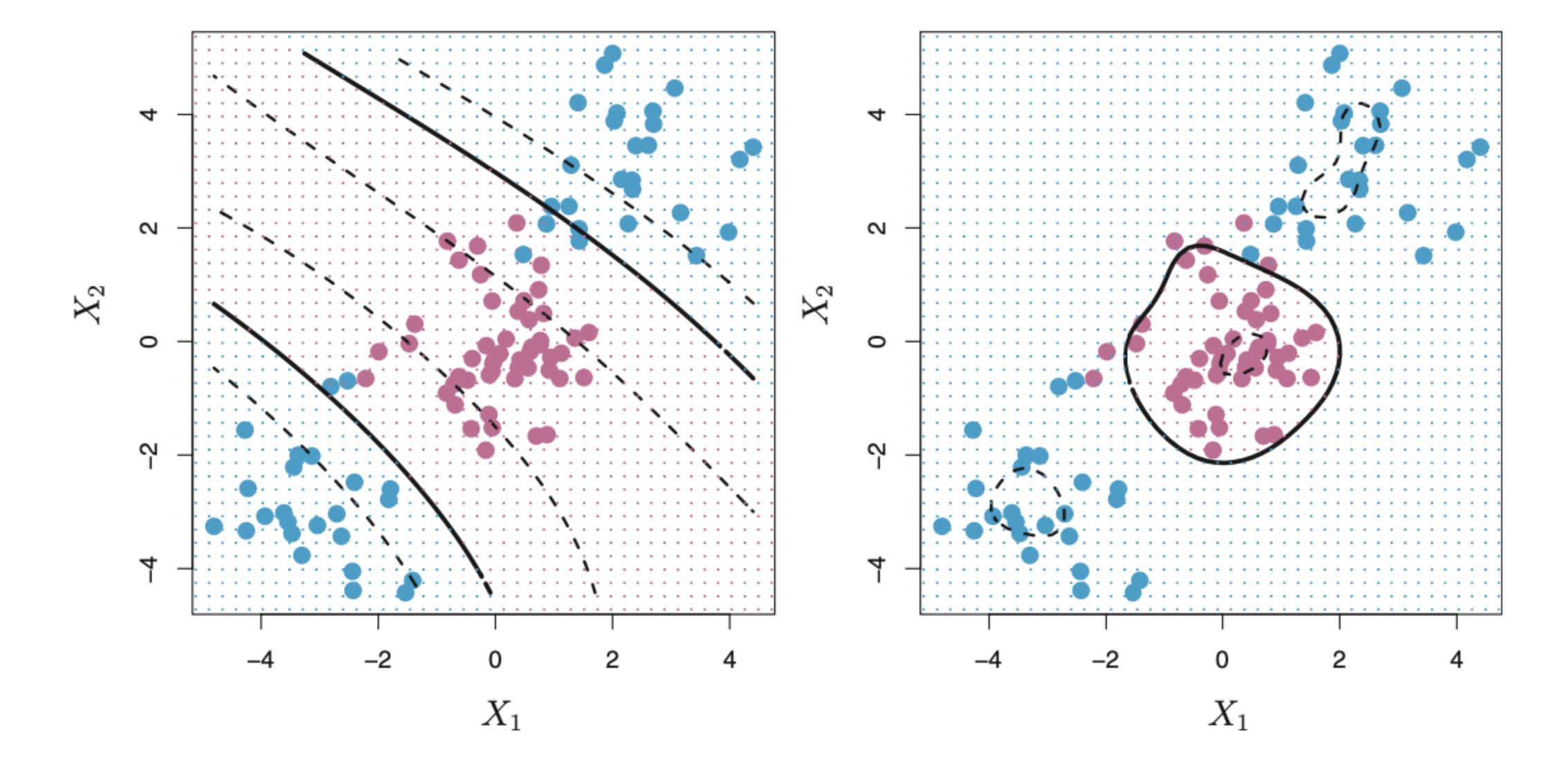
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$$f(x) = \beta_0 + \sum_{i \in \mathcal{S}} \alpha_i K(x, x_i)$$

Kernel function

Support Vector Machines

$$K(x_i, x_{i'}) = (1 + \sum_{j=1}^{p} x_{ij} x_{i'j})^d$$

Polynomial Kernel



Kernel Trick

Kernel Trick

- Actual name
- Attempt to place n-dimensional data into n+1 dimensional space

-5.0 -2.5 0.0 2.5 5.0 x1

-5.0

-2.5

0.0 **x**1 2.5

5.0

