4850_assignment1

Yufei xia

2020/2/24

```
theta1 = numeric(0)
theta2 = numeric(0)
simulate = function(sigma_sq) {
beta0 = 1
beta1 = 1
x = rnorm(1000, 4, 1)
y = beta0 + beta1*x + rnorm(1000,0,sqrt(sigma_sq))
xstar = x + rnorm(1000, 0, sigma_sq)
model2 = lm(y\sim xstar)
model1 = lm(y~x)
\textbf{return} (\texttt{c} (\texttt{summary} (\texttt{model1}) \$ \texttt{coefficients} [2,1] - 1, \texttt{summary} (\texttt{model2}) \$ \texttt{coefficients} [2,1] - 1)))
sigma = c(0.15, 0.55, 0.75)
sigmal= replicate(n = 1000, simulate(0.15))
print("the bias for beta1 and beta2 when varience = 0.15")
\#\# [1] "the bias for beta1 and beta2 when varience = 0.15"
apply(sigma1,1,mean)
## [1] -0.0001667277 -0.0221529250
print("the varience for beta1 and beta2 when varience = 0.15")
## [1] "the varience for betal and beta2 when varience = 0.15"
apply(sigma1,1,var)
## [1] 0.0001475472 0.0001630140
sigmal= replicate(n = 1000, simulate(0.55))
print("the bias for betal and beta2 when varience = 0.55")
\#\# [1] "the bias for beta1 and beta2 when varience = 0.55"
apply(sigma1,1,mean)
## [1] 3.205932e-06 -2.332582e-01
print("the varience for beta1 and beta2 when varience = 0.55")
## [1] "the varience for betal and beta2 when varience = 0.55"
apply(sigma1,1,var)
## [1] 0.0004975920 0.0005924441
sigmal = replicate(n = 1000, simulate(0.75))
print("the bias for beta1 and beta2 when varience = 0.75")
\#\# [1] "the bias for beta1 and beta2 when varience = 0.75"
```

```
apply(sigma1,1,mean)

## [1] 0.000146004 -0.358906868

print("the varience for beta1 and beta2 when varience = 0.75")

## [1] "the varience for beta1 and beta2 when varience = 0.75"

apply(sigma1,1,var)

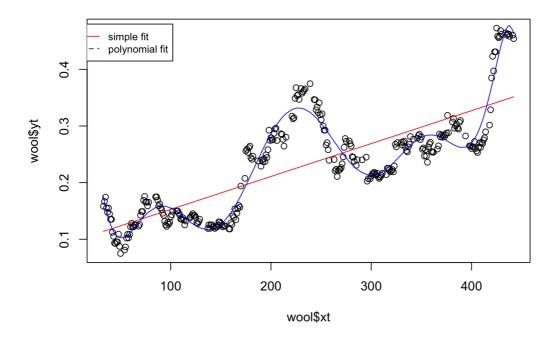
## [1] 0.0007707348 0.0007235687

#result = apply(m,1,mean)
#print(result)
```

from the result we can see the bias for beta1 doesn't grow as the sigma increase, however, the bias for second beta become bigger as the sigma go up, which prove our part b, w2 is not equal to 1 and decrease as sigma increase. in term of the varience of beta1 and beta2, we know that they are increase as sigma go up. which satisfy with the formula we calculated in the partc.also the varience is equal according to question 3.

question4 part1

```
wool = read.csv("wool.txt", sep = "")
model_fit = lm("yt~xt", data = wool)
model_fit2 = lm("yt~poly(xt,10)", data = wool)
plot(wool$xt,wool$yt)
lines(wool$xt,predict(model_fit),col = "red")
lines(wool$xt,predict(model_fit2),col = "blue")
legend(1,0.48,legend=c("simple fit", "polynomial fit"),col=c("red", "blue"),lty=1:2, cex=0.8)
```



```
llg_normal = function(data,x,h) {
 train_x = as.numeric(data[,1])
 train_y = as.numeric(data[,2])
 vx = train_x-x
 w = as.numeric(dnorm(vx, 0, h))
 weight = w/sum(w)
 oldw =getOption("warn")
 options (warn = -1)
 fit = lm(train_y ~ vx, weights = weight)
 options(warn = oldw)
 response = fit$coef[1]
 as.numeric(response)
leave_out_normal = function(i,data,h){
 xi = data[i,1]
 newdata = data[-i,]
 yi = data[i,2]
 response = llg_normal(newdata,xi,h)
 c(yi,response)
cv.glm_normal =function(data,h){
 index = as.matrix(1:nrow(data))
 output = apply(index,1,leave_out_normal,data =data,h=h)
 output<-t(output)
 error = sum((output[,1]-output[,2])^2)
 error
cvglm linear normal = function(data,interval) {
 optimize(cv.glm normal,interval = interval,data = data)$minimum
optmized_bindwith_linear = cvglm_linear_normal(wool,c(0,length(wool[,1])))
print("the optimized bindwith is for linear fit is")
```

```
## [1] "the optimized bindwith is for linear fit is"
```

```
optmized_bindwith_linear
```

```
## [1] 1.74673
```

```
response_linear= NULL

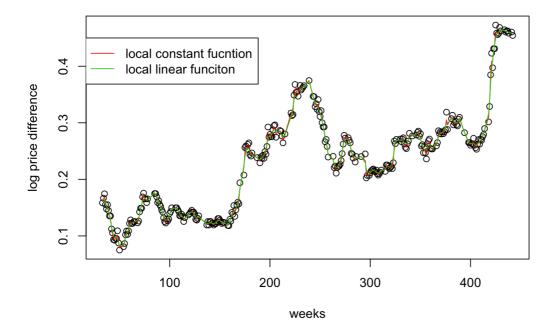
for (i in 1:length(wool[,1]) ) {
   response_linear[i] = llg_normal(wool,wool[i,1],optmized_bindwith_linear)
}

linear_data = cbind(wool[,1],response_linear)
linear_data = linear_data[order(linear_data[,1]),]
```

```
llg_normal_const = function(data,x,h) {
 train x = as.numeric(data[,1])
 train_y = as.numeric(data[,2])
 vx = train_x-x
 w = as.numeric(dnorm(vx, 0, h))
 weight = w/sum(w)
 oldw =getOption("warn")
 options (warn = -1)
 fit = lm(train_y ~ 1, weights = weight)
 options(warn = oldw)
 response = fit$coef[1]
 as.numeric(response)
leave_out_normal_const = function(i,data,h){
 xi = data[i,1]
 newdata = data[-i,]
 yi = data[i,2]
 response = llg_normal_const(newdata,xi,h)
 c(yi,response)
cv.glm_normal_const =function(data,h){
 index = as.matrix(1:nrow(data))
 output = apply(index,1,leave_out_normal_const,data =data,h=h)
 output<-t(output)
 error = sum((output[,1]-output[,2])^2)
cvglm_linear_normal_const = function(data,interval) {
 optimize(cv.glm_normal_const,interval = interval,data = data)$minimum
optmized_bindwith_const = cvglm_linear_normal_const(wool,c(0,length(wool[,1])))
print("the optimized bindwith is for constant fit is ")
\#\# [1] "the optimized bindwith is for constant fit is "
optmized_bindwith_const
## [1] 0.7162969
response const= NULL
for (i in 1:length(wool[,1]) ){
 response const[i] = llg_normal_const(wool,wool[i,1],optmized_bindwith_const)
```

```
const_data = cbind(wool[,1],response_const)
const data = const_data[order(const_data[,1]),]
```

```
plot(x = wool[,1],y=wool[,2],xlab="weeks",ylab ="log price difference")
lines(const_data[,1],const_data[,2],col="2")
lines(linear_data[,1],linear_data[,2],col="3")
legend(10,0.45,c("local constant fucntion","local linear funciton"),col=c(2,3),lty=c(1,1))
```

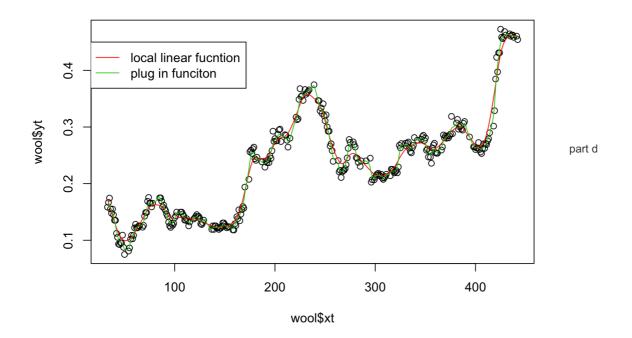


part c

```
library (KernSmooth)
```

```
## KernSmooth 2.23 loaded
## Copyright M. P. Wand 1997-2009
```

```
plot(wool$xt, wool$yt)
h <- dpill(wool$xt, wool$yt)
plugin_fit <- locpoly(wool$xt, wool$yt, bandwidth = h,degree = 1)
lines(plugin_fit,col="2")
linear_fit<- locpoly(wool$xt, wool$yt, bandwidth = optmized_bindwith_linear,degree = 1)
lines(linear_fit,col="3")
legend(10,0.45,c("local linear fucntion","plug in funciton"),col=c(2,3),lty =c(1,1))</pre>
```



```
predy =list(predict(model_fit),predict(model_fit2),response_const,response_linear,plugin_fit$y)
sapply(predy,function(x) {sum((x-wool[,2])^2)})
```

```
## Warning in x - wool[, 2]: longer object length is not a multiple of shorter
## object length
```

```
## [1] 0.962803050 0.160136905 0.004264583 0.012269386 5.622580024
```

we can see that from the result we get, the local constant estimator sum of square error is 0.0042645, which is lowest. and also the plug in method has largest SSE. also as we predicted, the more degree you have, the less SSE for training data, we polynomial fit has less SSE. also we can see that the local constant estimator has less SSE than local linear estimator.

qustion 5 part a

```
ky = read.csv("kyphosis.txt",sep ="")
newda = cbind(ky["age"],ifelse(ky["kyphosis"]=="absent",0,1))
library("KernSmooth")
library("locpol")
llg = function(data,x,h) {
 train x = as.numeric(data[,1])
 train y = as.numeric(data[,2])
 vx = train_x-x
 w = as.numeric(dnorm(vx, 0, h))
 weight = w/sum(w)
 oldw =getOption("warn")
 options (warn = -1)
 fit = glm(train_y ~ vx, family = binomial(link=logit), weights = weight)
 options(warn = oldw)
 beta0 = fit$coef[1]
 p = \exp(beta0) / (1+exp(beta0))
 as.numeric(p)
leave out = function(i,data,h) {
 xi = data[i,1]
 newdata = data[-i,]
 yi = data[i,2]
 fit = llg(newdata,xi,h)
 c(yi,fit)
cv.glm =function(data,h) {
 index = as.matrix(1:nrow(data))
 output = apply(index,1,leave_out,data =data,h=h)
 output<-t(output)
 error = -sum(output[,1]*log(output[,2])+(1-output[,1])*log(1-output[,2]))
cvglm_linear = function(data,interval) {
 optimize(cv.glm,interval = interval,data = data)$minimum
bindwith_linear = cvglm_linear(newda,c(0,81))
print("the bindwith using local linear function is")
```

```
## [1] "the bindwith using local linear function is"
```

```
bindwith_linear
```

```
## [1] 43.26988
```

```
prob_est_linear = NULL
for (i in 1:length(newda[,1]) ) {
  prob_est_linear[i] = llg(newda,newda[i,1],bindwith_linear)
print("the estimated pi is equal to")
## [1] "the estimated pi is equal to"
prob_est_linear
## [1] 0.24310999 0.17672473 0.27561089 0.04573366 0.04382350 0.04382350
    [7] 0.21587319 0.14043253 0.29335165 0.20999094 0.26769889 0.21748010
## [13] 0.08318262 0.04382350 0.13317788 0.04382350 0.25950847 0.10384148
## [19] 0.26371814 0.10910286 0.09435296 0.29406893 0.28838169 0.26935129
## [25] 0.07523235 0.06056700 0.05829360 0.29171142 0.04971190 0.20582989
## [31] 0.12140588 0.28095547 0.27153938 0.29375801 0.24518500 0.28508882
## [37] 0.04382350 0.18855913 0.08869083 0.28253149 0.24804525 0.13403371
## [43] 0.23542569 0.21587319 0.28933000 0.24825660 0.25690337 0.26935129
## [49] 0.28666544 0.09592561 0.23536369 0.06056700 0.24825660 0.04573366
## [55] 0.24518500 0.24560137 0.04573366 0.28784266 0.18541169 0.29290165
## [61] 0.27153938 0.29285186 0.26573772 0.28990076 0.28990076 0.08048966
## [67] 0.03952567 0.17241275 0.08318262 0.07523235 0.17672473 0.27749407
## [73] 0.27658826 0.01966326 0.06526337 0.09206763 0.18100784 0.10609131
## [79] 0.28784266 0.15655665 0.13722761
cvglm const = function(data,interval) {
optimize(cv.glm const,interval = interval,data = data)$minimum
 lc = function(data, x, h) {
  train_x = as.numeric(data[,1])
  train y = as.numeric(data[,2])
  vx = train_x-x
  w = as.numeric(dnorm(vx, 0, h))
  weight = w/sum(w)
  oldw =getOption("warn")
  options (warn = -1)
  fit = glm(train_y ~ 1, family = binomial(link=logit), weights = weight)
  options(warn = oldw)
  beta0 = fit$coef[1]
  p = \exp(beta0) / (1+exp(beta0))
  as.numeric(p)
leave out const = function(i,data,h){
 xi = data[i,1]
 newdata = data[-i,]
 yi = data[i,2]
 fit = lc(newdata, xi, h)
  c(yi,fit)
cv.glm_const =function(data,h) {
  index = as.matrix(1:nrow(data))
  output = apply(index,1,leave_out_const,data =data,h=h)
  output<-t (output)
  \texttt{error} = -\texttt{sum}(\texttt{output}[,1] * \texttt{log}(\texttt{output}[,2]) + (1-\texttt{output}[,1]) * \texttt{log}(1-\texttt{output}[,2]))
  error
  }
bindwith_const = cvglm_const(newda, c(0, 81))
print("the optimized bindwith for local regression is")
```

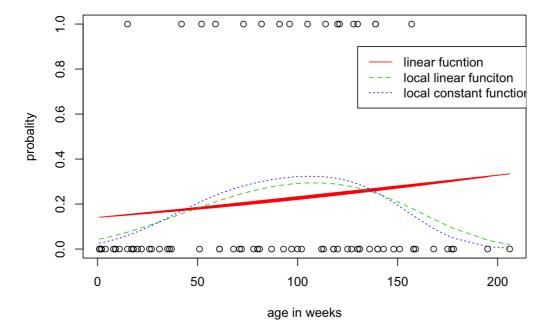
```
## [1] "the optimized bindwith for local regression is"
```

```
bindwith_const
## [1] 29.02671
prob_est_const = NULL
print("the estimated pi equal to")
## [1] "the estimated pi equal to"
for (i in 1:length(newda[,1]) ){
 prob est const[i] = llg(newda, newda[i,1], bindwith const)
prob_est_const
## [1] 0.275743625 0.147288812 0.295750239 0.028287096 0.026480290
## [6] 0.026480290 0.245624804 0.147329752 0.321507174 0.238681282
## [11] 0.300108093 0.206897204 0.070126783 0.026480290 0.091267560
## [16] 0.026480290 0.292270121 0.059567199 0.296330818 0.104068077
## [21] 0.084409586 0.323550673 0.318900913 0.286403458 0.060377246
## [26] 0.043519368 0.041056009 0.321760437 0.032169313 0.189350188
## [31] 0.120924001 0.303609668 0.289686231 0.322138885 0.249453386
## [36] 0.315997267 0.026480290 0.212155652 0.077092531 0.313716307
## [41] 0.280840718 0.138437001 0.234394730 0.245624804 0.319726957
## [46] 0.254190822 0.267486291 0.286403458 0.311866917 0.051965782
## [51] 0.267521670 0.043519368 0.254190822 0.028287096 0.249453386
## [56] 0.278330299 0.028287096 0.313552973 0.208110025 0.322727533
## [61] 0.289686231 0.320756948 0.298254536 0.316494366 0.316494366
## [66] 0.066781827 0.011132192 0.141330884 0.070126783 0.060377246
## [71] 0.147288812 0.298533375 0.308344056 0.003206261 0.048742208
## [76] 0.048416120 0.153284160 0.099995704 0.313552973 0.169599816
## [81] 0.142876721
```

part2

```
#assume it is linear function bew
#so we have
fit = glm(newda[,2]~newda[,1],family = binomial)
plot(newda[,1],newda[,2],xlab ="age in weeks", ylab ="probality")
prob = function(t) {
   exp(fit$coef[1]+fit$coef[2]*t)/(1+exp(fit$coef[1]+fit$coef[2]*t))
}

model_linear = cbind(newda[,1],prob_est_linear)
model_linear = model_linear[order(model_linear[,1]),]
model_const = cbind(newda[,1],prob_est_const)
model_const = model_const[order(model_const[,1]),]
lines(newda[,1],prob(newda[,1]),col ="2",lty =1)
lines(model_linear[,1],model_linear[,2],col ="3",lty =2 )
lines(model_const[,1],model_const[,2],col="4",lty =3)
legend(130,0.9,c("linear fucntion", "local linear funciton", "local constant function"),col=c(2,3,4),lty =c(1,2,3))
```



```
#we can get that the plot is not likely to be linear
```

from the plot we get, apprantly the linear assumption for f(x) is not reasonable beacause the plot doesn't follow the same pattern for linear function and local function.

question 6 part b

```
crab = read.csv("crab.txt", sep ="")
llg_pos = function(data,x,h) {
  train_x = as.numeric(data[,1])
  train_y = as.numeric(data[,2])
  vx = train_x-x
  w = as.numeric(dnorm(vx, 0, h))
  weight = w/sum(w)
  oldw =getOption("warn")
 options (warn = -1)
  fit = glm(train_y ~ vx,family = poisson(link = "log"), weights = weight)
  options(warn = oldw)
  sigma = exp(fit$coef[1])
  as.numeric(sigma)
leave_out_pos = function(i,data,h) {
 xi = data[i,1]
 newdata = data[-i,]
 yi = data[i,2]
 sigma = llg_pos(newdata,xi,h)
  c(yi, sigma)
cv.glm_pos =function(data,h) {
 index = as.matrix(1:nrow(data))
 output = apply(index,1,leave_out_pos,data =data,h=h)
 output<-t(output)
  error = -sum(output[,1]*log(output[,2])-output[,2])
  error
cvglm_linear_pos = function(data,interval){
  optimize(cv.glm pos,interval = interval,data = data)$minimum
pos_bindwith = cvglm_linear_pos(crab,interval = c(0,length(crab[,1])))
print("the optimized bw is")
```

```
## [1] "the optimized bw is"
pos bindwith
## [1] 3.434197
POS LINEAR =NULL
for(i in 1:length(crab[,1])){
POS_LINEAR[i] = llg_pos(crab,crab[i,1],pos_bindwith)
print("the predicted mu is")
## [1] "the predicted mu is"
POS LINEAR
     [1] 3.8842716 2.6439340 2.4461765 0.7720491 4.2726315 2.1637376 2.7454330
    [8] 2.1184143 2.4949353 3.4395078 2.6944741 4.2175941 4.9568645 1.3243807
##
   [15] 2.7454330 1.9423195 4.8056674 2.7454330 2.3500736 2.3500736 3.4395078
##
   [22] 3.1665786 1.7341816 4.1069586 2.9006976 1.9423195 3.3296433 2.9006976
   [29] 2.1637376 1.0385643 4.9070163 2.3500736 2.1184143 2.5441542 3.2750370
##
   [36] 5.0547977 2.1637376 4.8056674 1.3243807 1.6941797 2.6439340 2.5441542
##
##
    [43] 4.2726315 2.9006976 1.1918846 1.6547244 1.8574480 2.6439340 2.0293183
    [50] 1.1918846 4.1069586 4.4362640 3.0060608 1.5023936 3.5500949 3.8284733
    [57] 2.0293183 2.4949353 3.6056017 3.1665786 4.2726315 2.4461765 1.8158178
##
##
    [64] 2.4949353 1.3939310 3.9957733 4.6498802 1.3939310 1.9423195 3.4395078
   [71] 2.7967985 3.6056017 5.6655425 2.1637376 2.7454330 3.9400476 1.9423195
##
   [78] 3.6612185 2.1637376 4.2726315 5.5866757 3.4947224 1.9423195 1.6547244
##
## [85] 3.8284733 1.7747283 3.7169199 2.6439340 2.0293183 2.5441542 3.2206755
## [92] 3.3844741 3.0060608 3.0592535 2.5441542 1.6158170 3.6612185 4.8056674
## [99] 2.1637376 3.5500949 3.8842716 2.3978865 2.6439340 2.7454330 1.3588802
## [106] 1.3243807 2.2095711 2.5938237 2.3978865 3.0592535 4.2726315 3.9957733
## [113] 2.0293183 4.2726315 3.1665786 1.6158170 3.1665786 1.8158178 1.1918846
## [120] 2.2095711 2.1184143 3.4395078 1.8574480 4.5438212 2.7454330 2.0293183
## [127] 4.7022767 2.4949353 2.7454330 3.1665786 2.0736063 1.6158170 3.8284733
## [134] 2.2559091 1.4295335 2.5441542 3.4395078 2.4949353 3.0592535 3.4395078
## [141] 3.9957733 3.9957733 3.3844741 3.2750370 3.2206755 3.7169199 2.9006976
## [148] 1.3588802 2.6439340 1.9423195 2.5441542 1.5396508 3.0060608 2.3978865
```

```
pos_linear_data = cbind(crab$x,POS_LINEAR)
pos_linear_data = pos_linear_data[order(pos_linear_data[,1]),]
```

[155] 3.8284733 2.2559091 2.3027454 2.4949353 4.4362640 1.6547244 3.3844741 ## [162] 2.7454330 3.7169199 3.9400476 6.2138788 2.5441542 1.7341816 1.3939310

[169] 3.8842716 2.9006976 2.9006976 2.6944741 1.9423195

```
llg_pos_const = function(data,x,h) {
 train_x = as.numeric(data[,1])
 train_y = as.numeric(data[,2])
 vx = train_x-x
 w = as.numeric(dnorm(vx, 0, h))
 weight = w/sum(w)
 oldw =getOption("warn")
 options (warn = -1)
 fit = glm(train_y ~ 1,family = poisson(link = "log"), weights = weight)
 options(warn = oldw)
 sigma = exp(fit$coef[1])
 as.numeric(sigma)
leave_out_pos_const = function(i,data,h){
 xi = data[i,1]
 newdata = data[-i,]
 yi = data[i,2]
 sigma = llg_pos_const(newdata,xi,h)
 c(yi,sigma)
cv.glm_pos_const =function(data,h) {
 index = as.matrix(1:nrow(data))
 output = apply(index,1,leave_out_pos_const,data =data,h=h)
 output<-t(output)
 error = -sum(output[,1]*log(output[,2])-output[,2])
 error
cvglm_linear_pos_const = function(data,interval){
 optimize(cv.glm_pos_const,interval = interval,data = data)$minimum
print("the optimized bw is")
## [1] "the optimized bw is"
\verb|pos_bindwith_const| = \verb|cvglm_linear_pos_const(crab, interval| = \verb|c(0, length(crab[,1]))|)|
pos_bindwith_const
## [1] 1.206288
print("the predicted mu is")
## [1] "the predicted mu is"
POS CONST =NULL
for(i in 1:length(crab[,1])){
POS_CONST[i] = llg_pos_const(crab,crab[i,1],pos_bindwith_const)
POS_CONST
```

```
[1] 3.8423633 2.7768852 2.6397275 0.9223349 4.1405158 2.4307243 2.8491399
     [8] 2.3935108 2.6735550 3.4370666 2.8125607 4.1026216 4.4463634 1.5241577
##
##
    [15] 2.8491399 2.2347067 4.4128154 2.8491399 2.5718768 2.5718768 3.4370666
   [22] 3.1869458 2.0151431 4.0218900 2.9656929 2.2347067 3.3346342 2.9656929
##
   [29] 2.4307243 1.2099792 4.4382596 2.5718768 2.3935108 2.7075649 3.2844260
##
## [36] 4.4525451 2.4307243 4.4128154 1.5241577 1.9693165 2.7768852 2.7075649
## [43] 4.1405158 2.9656929 1.3726110 1.9231995 2.1492984 2.7768852 2.3161592
## [50] 1.3726110 4.0218900 4.2436836 3.0500261 1.7394339 3.5407708 3.7942123
   [57] 2.3161592 2.6735550 3.5925447 3.1869458 4.1405158 2.6397275 2.1052758
##
   [64] 2.6735550 1.6073041 3.9349418 4.3540950 1.6073041 2.2347067 3.4370666
##
   [71] 2.8867731 3.5925447 4.2005023 2.4307243 2.8491399 3.8893109 2.2347067
##
   [78] 3.6439747 2.4307243 4.1405158 4.2385239 3.4888704 2.2347067 1.9231995
##
   [85] 3.7942123 2.0605133 3.6948541 2.7768852 2.3161592 2.7075649 3.2351429
##
    [92] 3.3855824 3.0500261 3.0943053 2.7075649 1.8769693 3.6439747 4.4128154
    [99] 2.4307243 3.5407708 3.8423633 2.6058953 2.7768852 2.8491399 1.5651625
## [106] 1.5241577 2.4670564 2.7419463 2.6058953 3.0943053 4.1405158 3.9349418
## [113] 2.3161592 4.1405158 3.1869458 1.8769693 3.1869458 2.1052758 1.3726110
## [120] 2.4670564 2.3935108 3.4370666 2.1492984 4.3030596 2.8491399 2.3161592
## [127] 4.3761904 2.6735550 2.8491399 3.1869458 2.3553393 1.8769693 3.7942123
## [134] 2.5026075 1.6504822 2.7075649 3.4370666 2.6735550 3.0943053 3.4370666
## [141] 3.9349418 3.9349418 3.3855824 3.2844260 3.2351429 3.6948541 2.9656929
## [148] 1.5651625 2.7768852 2.2347067 2.7075649 1.7849035 3.0500261 2.6058953
## [155] 3.7942123 2.5026075 2.5375003 2.6735550 4.2436836 1.9231995 3.3855824
## [162] 2.8491399 3.6948541 3.8893109 5.1545360 2.7075649 2.0151431 1.6073041
## [169] 3.8423633 2.9656929 2.9656929 2.8125607 2.2347067
```

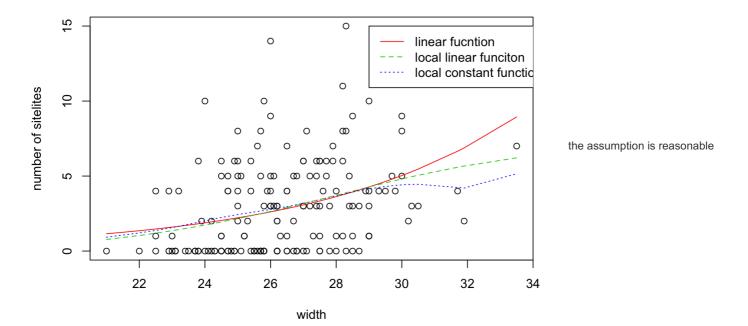
```
pos bindwith const
```

```
## [1] 1.206288
```

```
pos_const_data = cbind(crab$x,POS_CONST)
pos_const_data = pos_const_data[order(pos_const_data[,1]),]
```

partc

```
fit = glm(crab[,2]~crab[,1],family =poisson(link = "log"))
plot(crab[,1],crab[,2],xlab ="width",ylab ="number of sitelites")
prob2 = function(t) {
    exp(fit$coef[1]+fit$coef[2]*t)
}
normal_possion_regression = cbind(crab[,1],prob2(crab[,1]))
normal_possion_regression = normal_possion_regression[order(normal_possion_regression[,1]),]
lines(normal_possion_regression[,1],normal_possion_regression[,2],col ="2",lty =1)
lines(pos_const_data[,1],pos_const_data[,2],col ="4",lty = 3)
lines(pos_linear_data[,1],pos_linear_data[,2],col ="3",lty = 2)
legend(29,15,c("linear fucntion","local linear funciton","local constant function"),col=c(2,3,4),lty=c(1,2,3))
```



because overall, those three lines show same pattern except some distortion on the right side.