

▼ CSCI-SHU 210 Data Structures

Recitation 5 Stacks and Queues

▼ Bad Queue Example

```
class ArrayQueue():

    DEFAULT_CAPACITY = 10

    def __init__(self):
        self._data = []

    def __len__(self):
        return len(self._data)

    def is_empty(self):
        return len(self._data) == 0

    def first(self):
        return self._data[0]

    def dequeue(self):
        return self._data.pop(0)

    def enqueue(self, e):
        self._data.append(e)

    def __str__(self):
        ''' You can simply print self._data '''
        return str(self._data)

def main():
    # Empty Queue, size 10.
    queue = ArrayQueue()

    # Enqueue 0, 1, 2, 3, 4, 5, 6, 7
    for i in range(8):
        queue.enqueue(i)
    print(queue)      # [0, 1, 2, 3, 4, 5, 6, 7, None, None]

    # Dequeue 5 times.
    for j in range(5):
        queue.dequeue()
    print(queue)      # [None, None, None, None, None, 5, 6, 7, None, None]

    # Enqueue 8, 9, 10, 11, 12
    for k in range(5):
```

```

        queue.enqueue(k + 8)
    print(queue)    #  [10, 11, 12, None, None, 5, 6, 7, 8, 9]

if __name__ == '__main__':
    main()

```

```

[0, 1, 2, 3, 4, 5, 6, 7]
[5, 6, 7]
[5, 6, 7, 8, 9, 10, 11, 12]

```

▼ 1. Array Queue

```

class ArrayQueue():

    DEFAULT_CAPACITY = 10

    def __init__(self):
        self._data = [None] * ArrayQueue.DEFAULT_CAPACITY
        self._size = 0
        self._front = 0

    def __len__(self):
        return self._size

    def is_empty(self):
        return self._size == 0

    def first(self):
        if self.is_empty():
            raise Exception("Queue is Empty")
        return self._data[self._front]

    def dequeue(self):
        if self.is_empty():
            raise Exception("Queue is Empty")
        ans = self._data[self._front]
        self._data[self._front] = None
        self._front = (self._front + 1) % len(self._data)
        self._size -= 1
        return ans

    def enqueue(self, e):
        if self._size == len(self._data):
            raise Exception("Queue is Full")
        loc = (self._front + self._size) % len(self._data)
        self._data[loc] = e
        self._size += 1

    def __str__(self):
        return str(self._data)

```

```

def main():
    # Empty Queue, size 10.
    queue = ArrayQueue()

    # Enqueue 0, 1, 2, 3, 4, 5, 6, 7
    for i in range(8):
        queue.enqueue(i)
    print(queue)      # [0, 1, 2, 3, 4, 5, 6, 7, None, None]

    # Dequeue 5 times.
    for j in range(5):
        (queue.dequeue())
    print(queue)      # [None, None, None, None, None, 5, 6, 7, None, None]

    # Enqueue 8, 9, 10, 11, 12
    for k in range(5):
        queue.enqueue(k + 8)
    print(queue)      # [10, 11, 12, None, None, 5, 6, 7, 8, 9]

if __name__ == '__main__':
    main()

```

```

[0, 1, 2, 3, 4, 5, 6, 7, None, None]
[None, None, None, None, None, 5, 6, 7, None, None]
[10, 11, 12, None, None, 5, 6, 7, 8, 9]

```

▼ 2. Computing Spans

```

class ArrayStack:
    ''' Stack implemented with python list append/pop'''
    def __init__(self):
        self.array = []

    def __len__(self):
        return len(self.array)

    def is_empty(self):
        return len(self.array) == 0

    def push(self, e):
        self.array.append(e)

    def top(self):
        if self.is_empty():
            raise Exception()
        return self.array[-1]

    def pop(self):
        if self.is_empty():

```

```

        raise Exception()
    return self.array.pop(-1)

    def __repr__(self):
        return str(self.array)

def spans1(X):    # O(N^2)
    ans = []
    for i in range(len(X)):
        span = 1
        while i - span >= 0 and X[i - span] <= X[i]:
            span += 1
        ans.append(span)
    return ans

def spans2(X):    # O(N): Think about how many times a stack is pushed and popped. Th
    ans = []
    stack = ArrayStack()
    for i in range(len(X)):
        while len(stack) > 0 and X[stack.top()] <= X[i]:
            stack.pop()

        if len(stack) == 0:
            ans.append(i + 1)
        else:
            ans.append(i - stack.top())

        stack.push(i)

    return ans

def main():
    print(spans1([6,3,4,5,2])) # [1, 1, 2, 3, 1]
    print(spans1([6,7,1,3,4,5,2])) # [1, 2, 1, 2, 3, 4, 1]
    print(spans2([6,3,4,5,2])) # [1, 1, 2, 3, 1]
    print(spans2([6,7,1,3,4,5,2])) # [1, 2, 1, 2, 3, 4, 1]

if __name__ == '__main__':
    main()

```

```

[1, 1, 2, 3, 1]
[1, 2, 1, 2, 3, 4, 1]
[1, 1, 2, 3, 1]
[1, 2, 1, 2, 3, 4, 1]

```

▼ 3. Double ended queue

```

class ArrayDeque:
    DEFAULT_CAPACITY = 10

```

```

def __init__(self):
    self._data = [None] * ArrayDeque.DEFAULT_CAPACITY
    self._size = 0
    self._front = 0

def __len__(self):
    return self._size

def is_empty(self):
    return self._size == 0

def is_full(self):
    return self._size == len(self._data)

def first(self):
    if self.is_empty():
        raise Exception("Queue is empty")
    return self._data[self._front]

def last(self):
    if self.is_empty():
        raise Exception("Queue is empty")
    loc = (self._front + self._size - 1) % len(self._data)
    return self._data[loc]

def delete_first(self):
    if self.is_empty():
        raise Exception("Queue is empty")
    ans = self._data[self._front]
    self._data[self._front] = None
    self._front = (self._front + 1) % len(self._data)
    self._size -= 1
    return ans

def add_first(self, e):
    if self.is_full():
        raise Exception("Queue is full")
    loc = (self._front - 1) % len(self._data)
    self._data[loc] = e
    self._front = (self._front - 1) % len(self._data)
    self._size += 1

def delete_last(self):
    if self.is_empty():
        raise Exception("Queue is empty")
    loc = (self._front + self._size - 1) % len(self._data)
    ans = self._data[loc]
    self._data[loc] = None
    self._size -= 1
    return ans

def add_last(self, e):
    if self.is_full():
        raise Exception("Queue is full")
    loc = (self._front + self._size) % len(self._data)

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        self._data[loc] = e
        self._size += 1

    def __str__(self):
        return str(self._data)

def main():
    # Empty Queue, size 10.
    deque = ArrayDeque()

    # Add 0, 1, 2, 3 following FIFO.
    for i in range(4):
        deque.add_first(i)
    print(deque)    # [None, None, None, None, None, None, 3, 2, 1, 0]

    # Add 4, 5, 6, 7 following LIFO.
    for j in range(4):
        deque.add_last(j + 4)
    print(deque)    # [4, 5, 6, 7, None, None, 3, 2, 1, 0]

    # Remove first one
    print(deque.delete_first()) # 3

    # Remove last one
    print(deque.delete_last()) # 7

if __name__ == '__main__':
    main()

```

```

[None, None, None, None, None, None, 3, 2, 1, 0]
[4, 5, 6, 7, None, None, 3, 2, 1, 0]
3
7

```

▼ 4. Evaluation of arithmetic expressions

```

class ArrayStack:
    ''' Stack implemented with python list append/pop'''
    def __init__(self):
        self.array = []

    def __len__(self):
        return len(self.array)

    def is_empty(self):
        return len(self.array) == 0

    def push(self, e):
        self.array.append(e)

    def top(self):

```

```

        if self.is_empty():
            raise Exception()
        return self.array[-1]

def pop(self):
    if self.is_empty():
        raise Exception()
    return self.array.pop(-1)

def __repr__(self):
    return str(self.array)

def compute(left, right, operator):
    if (operator == "+"):
        return left + right
    elif (operator == "-"):
        return left - right
    elif (operator == "/"):
        return left / right
    elif (operator == "*"):
        return left * right

def evaluate(string):
    operator_stack = ArrayStack()
    operand_stack = ArrayStack()
    table = {"+":2, "-":2, "*":3, "/":3, "(":1, ")":1}
    tokens = string.split()
    for token in tokens:
        if token not in table.keys(): # operand
            operand_stack.push(int(token))

        elif token == '(':
            operator_stack.push(token)

        elif token == ')':
            operator = operator_stack.pop()
            while operator != '(':
                operand1 = operand_stack.pop()
                operand2 = operand_stack.pop()
                operand_stack.push(compute(operand2, operand1, operator))
                operator = operator_stack.pop()

        else: # operator
            while (not operator_stack.is_empty()) and \
                (table[operator_stack.top()] >= table[token]):
                operand1 = operand_stack.pop()
                operand2 = operand_stack.pop()
                operator = operator_stack.pop()
                operand_stack.push(compute(operand2, operand1, operator))
            operator_stack.push(token)

    while (not operator_stack.is_empty()):
        operand1 = operand_stack.pop()
        operand2 = operand_stack.pop()
        operator = operator_stack.pop()

```

```
        operand_stack.push(compute(operand2, operand1, operator))

    return operand_stack.pop()

if __name__ == '__main__':
    print(evaluate("9 + 8 * ( 7 - 6 ) / ( 2 / 8 )"))    #41
    print(evaluate("9 + 8 * 7 / ( 6 + 5 ) - ( 4 + 3 ) * 2"))    # 0.09090909
    print(evaluate("9 + 8 * 7 / ( ( 6 + 5 ) - ( 4 + 3 ) * 2 )"))    # -9.666

41.0
0.0909090909090908994
-9.6666666666666668
```