5

APPLYING NEWTON'S LAWS

VP5.5.1. IDENTIFY: The cart and bucket move with constant speed, so their acceleration is zero, which means that the forces on each of them must balance.

SET UP: Apply $\sum F_x = 0$ and $\sum F_y = 0$ to the cart and the bucket. For the cart, take the +x-axis parallel to the surface of the incline pointing upward. For the bucket, take the +y-axis vertically upward.

EXECUTE: (a) Isolate the bucket and apply $\sum F_v = 0$. $T - w = 0 \rightarrow T = w = 255$ N.

Now apply $\sum F_x = 0$ to the cart. $T - w \sin 36.9^\circ = 0$. 255 N $- w \sin 36.9^\circ = 0$. w = 425 N.

(b) From above, T = 255 N.

EVALUATE: The bucket can balance a much heavier cart because it only needs to balance the component of the cart's weight that is parallel to the surface of the incline.

VP5.5.2. IDENTIFY: The cart and bucket are at rest, which means that the forces on each of them must balance. **SET UP:** Apply $\sum F_x = 0$ and $\sum F_y = 0$ to the cart and the bucket. For the cart, take the +x-axis parallel to the surface of the incline pointing upward. For the bucket, take the +y-axis vertically upward.

EXECUTE: (a) Apply $\sum F_x = 0$ to the cart, giving $T - w_C \sin 25.0^\circ = 0$.

155 N – $w_C \sin 25.0^\circ$, so $w_C = 367$ N.

(b) Isolate the bucket and apply $\sum F_v = 0$. $T - w_B = 0$, so $w_B = T = 367$ N.

The total weight is 367 N + 155 N = 522 N.

EVALUATE: A light bucket can balance a heavy cart because it must balance only the weight component of the cart that is parallel to the surface of the incline.

VP5.5.3. IDENTIFY: The cart and bucket move with constant speed, so their acceleration is zero, which means that the forces on each of them must balance.

SET UP: Apply $\sum F_x = 0$ and $\sum F_y = 0$ to the cart and the bucket. For the cart, take the +x-axis parallel to the surface of the incline pointing upward. For the bucket, take the +y-axis vertically upward. We want to find the angle θ of the slope. Call T the tension in the cable.

EXECUTE: (a) Applying $\sum F_y = 0$ to the bucket gives $T = w_B$. Applying $\sum F_x = 0$ to the cart gives $T = w_C \sin \theta$. Equating the two expressions for T gives $w_B = w_C \sin \theta$, which tells us

$$\sin \theta = \frac{w_B}{w_C} = \frac{m_B g}{m_C g} = \frac{65.0 \text{ kg}}{175 \text{ kg}} = 0.371 \text{, so } \theta = 21.8^\circ.$$

(b) From part (a), $T = w_B = (65.0 \text{ kg})(9.80 \text{ m/s}^2) = 637 \text{ N}.$

EVALUATE: It must also be true that $T = w_C \sin \theta$. $T = (175 \text{ kg})(9.80 \text{ m/s}^2) \sin 21.8^\circ = 637 \text{ N}$, which agrees with our answer in (b).

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VP5.5.4. IDENTIFY: The cart and bucket remain at rest, so the forces on each of them must balance. **SET UP:** Apply $\sum F_x = 0$ and $\sum F_y = 0$ to the cart and the bucket. For the cart, take the +x-axis parallel

to the surface of the incline pointing upward. For the bucket, take the +y-axis vertically upward. We want to find the angle θ of the slope. Call T the tension in the cable and f the friction force. If there were no friction, the cart would slide up the incline because $w > w \sin \theta$. Since friction opposes motion, it must act down the incline.

EXECUTE: Applying $\sum F_y = 0$ to the bucket gives $T = w_B = w$. Applying $\sum F_x = 0$ to the cart gives $T - w_C \sin \theta - f = 0$, which becomes $T - w_C \sin \theta - f = 0$. Combining the results gives $f = w(1 - \sin \theta)$. Since $\sin \theta < 1$, we know that f < w.

EVALUATE: The weight of the bucket must now balance *two* forces: the weight of the cart acting down the incline and the friction force down the incline.

VP5.15.1. IDENTIFY: The crate moves at constant velocity, so the forces on it must balance. **SET UP:** Apply $\sum F_x = 0$ and $\sum F_y = 0$ to the crate. Take the *x*-axis horizontal and the *y*-axis vertical. Make a free-body diagram as in Fig. VP5.15.1.

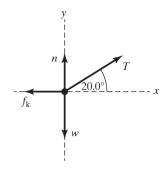


Figure VP5.15.1

EXECUTE: (a) Using the notation in Fig. VP5.15.1, $\sum F_x = 0$ gives $T \cos 20.0^{\circ} - f_k = 0$ and $\sum F_y = 0$ gives $T \sin 20.0^{\circ} + n - w = 0$, so $n = w - T \sin 20.0^{\circ}$. For sliding friction $f_k = \mu_k n$. Combining these results gives $T \cos 20.0^{\circ} - \mu_k (w - T \sin 20.0^{\circ}) = 0$. Putting in the numbers:

 $T \cos 20.0^{\circ} - (0.250)(325 \text{ N}) + (0.250)T \sin 20.0^{\circ} = 0$ \rightarrow T=79.3 N

(b) $n = w - T \sin 20.0^{\circ} = 325 \text{ N} - (79.3 \text{ N}) \sin 20.0^{\circ} = 298 \text{ N}.$

EVALUATE: We find that $n \le w$. This is reasonable because the upward component of the tension balances part of the weight of the crate.

VP5.15.2. IDENTIFY: The crate moves at constant velocity, so the forces on it must balance. **SET UP:** Apply $\sum F_x = 0$ and $\sum F_y = 0$ to the crate. Take the *x*-axis horizontal and the *y*-axis vertical. Make a free-body diagram as in Fig. 5.15.2.

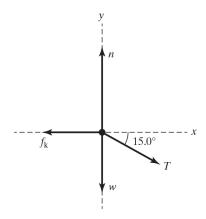


Figure VP5.15.2

EXECUTE: The procedure is exactly the same as for VP5.15.1 *except* that the tension is now directed at 15.0° *below* the horizontal.

(a)
$$\sum F_x = 0$$
 gives $n - w - T \sin 15.0^\circ = 0$, so $n = w + T \sin 15.0^\circ$.

$$\sum F_v = 0$$
 gives $T \cos 15.0^{\circ} - f_k = T \cos 15.0^{\circ} - \mu_k n = 0.$

Combining these equations and solving for T gives T = 90.2 N.

(b)
$$n = w + T \sin 15.0^{\circ} = 325 \text{ N} + (90.2 \text{ N}) \sin 15.0^{\circ} = 348 \text{ N}.$$

EVALUATE: The normal force must balance the downward component of the tension in addition to the weight of the crate, so it is greater than the weight.

VP5.15.3. IDENTIFY: The sled is accelerated horizontally, so Newton's second law applies to it.

SET UP: $\sum F_x = ma_x$ applies to the horizontal motion and $\sum F_y = 0$ applies to the vertical motion. Use $\sum F_y = 0$ to find the normal force n. The kinetic friction force is $f_k = \mu_k n$. Call P the magnitude of the pull and w the weight of the sled. Take the +x-axis to be horizontal in the direction of the horizontal component of the pull.

EXECUTE: (a) $\sum F_{v} = 0$: $T \sin 12.0^{\circ} + n - w = 0$.

$$n = w - T \sin 12.0^{\circ} = 475 \text{ N} - (125 \text{ N}) \sin 12.0^{\circ} = 449 \text{ N}.$$

(b)
$$\sum F_x = ma_x : P \cos 12.0^\circ - f_k = ma_x = P \cos 12.0^\circ - \mu_k n$$

(125 N) cos 12.0° – (0.200)(449 N = [(475 N)/(9.80 m/s²)] $a_x \rightarrow a_x = 0.670$ m/s². We have chosen the +x-axis in the same direction as the horizontal component of the pull. Since a_x is positive, the acceleration is in the same direction as that pull, so the sled is *speeding up*.

EVALUATE: If the sled were slowing down, that would mean that friction was greater than the horizontal component of the pull. In that case, the sled could never have started moving in the first place, so our answer is reasonable.

VP5.15.4. IDENTIFY: Before it slides, the forces on the box must balance.

SET UP: For the minimum pull, the box is just ready to slide, so static friction is at its maximum, which is $f_s = \mu_s n$. Apply $\sum F_x = 0$ and $\sum F_y = 0$ to the box just as it is ready to slide.

EXECUTE:
$$\sum F_x = 0$$
: $T_{\min} \cos \theta - f_s = 0 \rightarrow T_{\min} \cos \theta - \mu_s n = 0$.

$$\sum F_v = 0 : T_{\min} \sin \theta + n - mg = 0$$
 \rightarrow $n = mg - T_{\min} \sin \theta$.

Combine these results and solve for $\mu_{\rm s}$.

$$T_{\min}\cos\theta - \mu_{\rm s} (mg - T_{\min}\sin\theta) = 0$$
 \rightarrow $\mu_{\rm s} = \frac{T_{\min}\cos\theta}{mg - T_{\min}\sin\theta}$.

EVALUATE: If the box is *not* just ready to slide, our analysis is not valid. The forces still balance, but $f_s \neq \mu_s n$ in that case.

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VP5.22.1. IDENTIFY: The pendulum bob is moving in a horizontal circle at constant speed. Therefore it has horizontal acceleration toward the center of the circle, but it has no vertical acceleration. The vertical forces on it must balance, but we need to use Newton's second law for the horizontal motion.

SET UP: Vertically $\sum F_y = 0$ and horizontally $\sum F_x = ma_x$, where a_x is the radial acceleration $a_{\text{rad}} = ma_x$

 v^2/R . Therefore horizontally we use $\sum F = m \frac{v^2}{R}$. The speed is $v = 2\pi R/t$, where t is the time for one

cycle (do not use T for the period to avoid confusion with the tension T). Make a free-body diagram like Fig. 5.32b in the text.

EXECUTE: (a) $R = L \sin \beta = (0.800 \text{ m}) \sin 20.0^{\circ} = 0.274 \text{ m}.$

(b)
$$\sum F = m \frac{v^2}{R}$$
 gives $T \sin \beta = m \frac{v^2}{R}$. Using $v = 2\pi R/t$, this becomes $T \sin \beta = \frac{m}{R} \left(\frac{2\pi R}{t} \right)^2$. Solving for t

we get $t = \sqrt{\frac{4\pi^2 Rm}{T \sin \beta}}$, so we need to find T.

(c) $\Sigma F_v = 0$ gives $T \cos \beta = W = mg \rightarrow T = (0.250 \text{ kg})(9.80 \text{ m/s}^2)/(\cos 20.0^\circ) = 2.61 \text{ N}$. Now

return to part (b) to find the time $t = \sqrt{\frac{4\pi^2 Rm}{T \sin \beta}}$. Putting in the numbers gives

Ita
$$t = 2\pi \sqrt{\frac{(0.274 \text{ m})(0.250 \text{ kg})}{(2.61 \text{ N})(\sin 20.0^\circ)}} = 1.74 \text{ s}.$$

EVALUATE: Even though the bob has constant speed, the horizontal forces do not balance because its *velocity* is changing direction, so it has acceleration.

VP5.22.2. IDENTIFY: The cyclist is moving in a horizontal circle at constant speed. Therefore she has horizontal acceleration toward the center of the circle, but no vertical acceleration. The vertical forces on her must balance, but we need to use Newton's second law for her horizontal motion.

SET UP: Vertically $\sum F_v = 0$ and horizontally $\sum F_x = ma_x$, where a_x is the radial acceleration $a_{\text{rad}} = 0$

 v^2/R . Therefore horizontally we use $\sum F = m \frac{v^2}{R}$. Make a free-body diagram as shown in Fig. VP5.22.2.

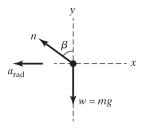


Figure VP5.22.2

EXECUTE: (a) $\sum F_x = ma_x = n \sin \beta = mv^2/R$

$$\sum F_{v} = 0 = n \cos \beta - mg$$
.

Combining these two equations gives $\tan \beta = v^2/Rg$, which gives

 $R = v^2/(g \tan \beta) = (12.5 \text{ m/s})^2/[(9.80 \text{ m/s}^2)(\tan 40.0^\circ)] = 19.0 \text{ m}.$

(b) $a_{\text{rad}} = v^2/R = (12.5 \text{ m/s})^2/(19.0 \text{ m}) = 8.22 \text{ m/s}^2.$

(c) Using $n \cos \beta - mg = 0$, we get $n = mg/\cos \beta = (64.0 \text{ kg})(9.80 \text{ m/s}^2)/(\cos 40.0^\circ) = 819 \text{ N}$.

EVALUATE: We found that n > w. This is reasonable since only the vertical component of n balances her weight, which means that n has to be greater then w.

VP5.22.3. IDENTIFY: The plane is moving in a horizontal circle at constant speed. Therefore it has horizontal acceleration toward the center of the circle, but no vertical acceleration. The vertical forces on it must balance, but we need to use Newton's second law for its horizontal motion.

SET UP: Vertically $\sum F_y = 0$ and horizontally $\sum F_x = ma_x$, where a_x is the radial acceleration $a_{\text{rad}} = ma_x$

 v^2/R . Therefore horizontally we use $\sum F = m \frac{v^2}{R}$. Make a free-body diagram like Fig. 5.35 in the text.

EXECUTE: (a)
$$\sum F_x = ma_x = n \sin \beta = mv^2/R$$

$$\sum F_v = 0 = n \cos \beta - mg$$
.

Combining these two equations gives $\tan \beta = v^2/Rg = (80.0 \text{ m/s})^2/[(175 \text{ m})(9.80 \text{ m/s}^2)]$, which gives $\beta = 75.0^\circ$.

(b) The pilot's apparent weight will be the force n due to the seat. Using $\sum F_{y} = 0$ gives

$$w = n \cos \beta$$
, so $n = w/\cos \beta = (80.0 \text{ kg})(9.80 \text{ m/s}^2)/(\cos 75.0^\circ) = 3.03 \times 10^3 \text{ N}.$

 $w_{\text{apparent}}/w_{\text{actual}} = (3.03 \times 10^3 \text{ N})/[(80.0 \text{ kg})(9.80 \text{ m/s}^2)] = 3.86$, which means that is apparent weight is 3.86 times great than his actual weight.

EVALUATE: Notice that $\tan \beta \propto v^2$, so a large speed means a large bank angle. We also saw that $n = w/\cos \beta$, so as v gets larger and larger, β gets closer and closer to 90° , and $\cos \beta$ gets closer and closer to zero. Therefore n gets larger and larger. This can be dangerous for pilots in high speed turns. The effects from such turns can cause a pilot to black out if the speed is great enough.

VP5.22.4. IDENTIFY: The driver is moving in a horizontal circle at constant speed. Therefore she has horizontal acceleration toward the center of the circle, but no vertical acceleration. The vertical forces on her must balance, but we need to use Newton's second law for her horizontal motion.

SET UP: Vertically $\sum F_y = 0$ and horizontally $\sum F_x = ma_x$, where a_x is the radial acceleration $a_{\text{rad}} = ma_x$

 v^2/R . Therefore horizontally we use $\sum F = m \frac{v^2}{R}$. Make a free-body diagram like Fig. 5.34b in the

textbook. Her apparent weight x times her actual weight, which means that the normal force n on her due to the seat is n = xmg.

EXECUTE: (a) Using $\sum F = m \frac{v^2}{R}$, we see that the net force on her is $F_{\text{net}} = ma_x = mv^2/R$. From the free-

body diagram, we see that $F_{\text{rad}} = n \sin \beta$. So $F_{\text{net}} = F_{\text{rad}} = n \sin \beta = xmg \sin \beta$. Use $\sum F_{y} = 0$ to find

$$\beta: n\cos\beta - mg = 0 \rightarrow \cos\beta = mg/n = mg/xmg = 1/x$$
. This means that $\sin\beta = \frac{\sqrt{x^2 - 1}}{x}$.

We showed that $F_{\text{net}} = xmg \sin \beta$, so $F_{\text{net}} = xmg \frac{\sqrt{x^2 - 1}}{x} = mg\sqrt{x^2 - 1}$.

(b) $F_{\text{rad}} = F_{\text{net}} = mv^2/R$. Use the result from (a) for F_{net} .

$$mg\sqrt{x^2-1} = mv^2/R$$
 \rightarrow $R = \frac{v^2}{g\sqrt{x^2-1}}$.

EVALUATE: Our result in (b) says that as x gets larger and larger, R gets smaller and smaller. This is reasonable, since the larger x is, the greater the apparent weight of the driver. So for a given speed, a sharper turn will produce a greater apparent weight than a wide turn.

5.1. IDENTIFY: a = 0 for each object. Apply $\Sigma F_v = ma_v$ to each weight and to the pulley.

SET UP: Take +y upward. The pulley has negligible mass. Let T_r be the tension in the rope and let T_c be the tension in the chain.

EXECUTE: (a) The free-body diagram for each weight is the same and is given in Figure 5.1a. $\Sigma F_v = ma_v$ gives $T_r = w = 25.0 \text{ N}$.

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(b) The free-body diagram for the pulley is given in Figure 5.1b. $T_c = 2T_r = 50.0 \text{ N}.$

EVALUATE: The tension is the same at all points along the rope.

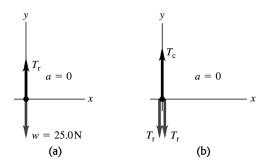


Figure 5.1

5.2. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each weight.

SET UP: Two forces act on each mass: w down and T(=w) up.

EXECUTE: In all cases, each string is supporting a weight w against gravity, and the tension in each string is w

EVALUATE: The tension is the same in all three cases.

5.3. IDENTIFY: Both objects are at rest and a = 0. Apply Newton's first law to the appropriate object. The maximum tension T_{max} is at the top of the chain and the minimum tension is at the bottom of the chain. **SET UP:** Let +y be upward. For the maximum tension take the object to be the chain plus the ball. For the minimum tension take the object to be the ball. For the tension T three-fourths of the way up from the bottom of the chain, take the chain below this point plus the ball to be the object. The free-body diagrams in each of these three cases are sketched in Figure 5.3. $m_{b+c} = 75.0 \text{ kg} + 26.0 \text{ kg} = 101.0 \text{ kg}$.

 $m_b = 75.0$ kg. m is the mass of three-fourths of the chain: $m = \frac{3}{4}(26.0 \text{ kg}) = 19.5 \text{ kg}$.

EXECUTE: (a) From Figure 5.3a, $\Sigma F_v = 0$ gives $T_{\text{max}} - m_{\text{b+c}}g = 0$ and

 $T_{\text{max}} = (101.0 \text{ kg})(9.80 \text{ m/s}^2) = 990 \text{ N}$. From Figure 5.3b, $\Sigma F_y = 0$ gives $T_{\text{min}} - m_b g = 0$ and

$$T_{\text{min}} = (75.0 \text{ kg})(9.80 \text{ m/s}^2) = 735 \text{ N}.$$

(b) From Figure 5.3c, $\Sigma F_y = 0$ gives $T - (m + m_b)g = 0$ and

$$T = (19.5 \text{ kg} + 75.0 \text{ kg})(9.80 \text{ m/s}^2) = 926 \text{ N}.$$

EVALUATE: The tension in the chain increases linearly from the bottom to the top of the chain.

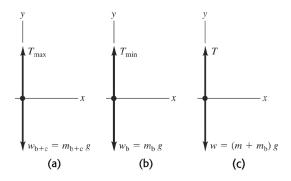


Figure 5.3

5.4. IDENTIFY: For the maximum tension, the patient is just ready to slide so static friction is at its maximum and the forces on him add to zero.

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SET UP: (a) The free-body diagram for the person is given in Figure 5.4a. F is magnitude of the traction force along the spinal column and w = mg is the person's weight. At maximum static friction, $f_s = \mu_s n$.

(b) The free-body diagram for the collar where the cables are attached is given in Figure 5.4b. The tension in each cable has been resolved into its *x*- and *y*-components.

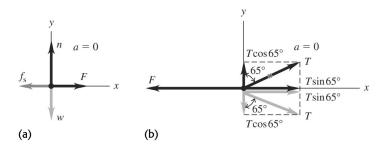


Figure 5.4

EXECUTE: (a) n = w and $F = f_s = \mu_s n = 0.75w = 0.75(9.80 \text{ m/s}^2)(78.5 \text{ kg}) = 577 \text{ N}.$

(b)
$$2T \sin 65^{\circ} - F = 0$$
 so $T = \frac{F}{2 \sin 65^{\circ}} = \frac{0.75w}{2 \sin 65^{\circ}} = 0.41w = (0.41)(9.80 \text{ m/s}^2)(78.5 \text{ kg}) = 315 \text{ N}.$

EVALUATE: The two tensions add up to 630 N, which is more than the traction force, because the cables do not pull directly along the spinal column.

5.5. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the frame.

SET UP: Let w be the weight of the frame. Since the two wires make the same angle with the vertical, the tension is the same in each wire. T = 0.75w.

EXECUTE: The vertical component of the force due to the tension in each wire must be half of the weight, and this in turn is the tension multiplied by the cosine of the angle each wire makes with the

vertical.
$$\frac{w}{2} = \frac{3w}{4} \cos \theta$$
 and $\theta = \arccos \frac{2}{3} = 48^\circ$.

EVALUATE: If $\theta = 0^{\circ}$, T = w/2 and $T \to \infty$ as $\theta \to 90^{\circ}$. Therefore, there must be an angle where T = 3w/4.

5.6. IDENTIFY: Apply Newton's first law to the wrecking ball. Each cable exerts a force on the ball, directed along the cable.

SET UP: The force diagram for the wrecking ball is sketched in Figure 5.6.

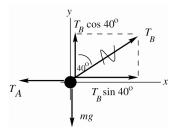


Figure 5.6

EXECUTE: (a)
$$\Sigma F_y = ma_y$$

$$T_R \cos 40^\circ - mg = 0$$

$$T_B = \frac{mg}{\cos 40^\circ} = \frac{(3620 \text{ kg})(9.80 \text{ m/s}^2)}{\cos 40^\circ} = 4.63 \times 10^4 \text{ N} = 46.3 \text{ kN}$$

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(b)
$$\Sigma F_x = ma_x$$

 $T_B \sin 40^\circ - T_A = 0$
 $T_A = T_B \sin 40^\circ = 2.98 \times 10^4 \text{ N} = 29.8 \text{ kN}$

EVALUATE: If the angle 40° is replaced by 0° (cable B is vertical), then $T_B = mg$ and $T_A = 0$.

5.7. **IDENTIFY:** Apply $\Sigma \vec{F} = m\vec{a}$ to the object and to the knot where the cords are joined. **SET UP:** Let +y be upward and +x be to the right.

EXECUTE: (a) $T_C = w$, $T_A \sin 30^\circ + T_B \sin 45^\circ = T_C = w$, and $T_A \cos 30^\circ - T_B \cos 45^\circ = 0$. Since $\sin 45^\circ = \cos 45^\circ$, adding the last two equations gives $T_A(\cos 30^\circ + \sin 30^\circ) = w$, and so

$$T_A = \frac{w}{1.366} = 0.732w$$
. Then, $T_B = T_A \frac{\cos 30^\circ}{\cos 45^\circ} = 0.897w$.

(b) Similar to part (a), $T_C = w$, $-T_A \cos 60^\circ + T_B \sin 45^\circ = w$, and $T_A \sin 60^\circ - T_B \cos 45^\circ = 0$.

Adding these two equations, $T_A = \frac{w}{(\sin 60^\circ - \cos 60^\circ)} = 2.73w$, and $T_B = T_A \frac{\sin 60^\circ}{\cos 45^\circ} = 3.35w$.

EVALUATE: In part (a), $T_A + T_B > w$ since only the vertical components of T_A and T_B hold the object against gravity. In part (b), since T_A has a downward component T_B is greater than w.

- **5.8. IDENTIFY:** Apply Newton's first law to the hanging weight and to each knot. The tension force at each end of a string is the same.
 - (a) Let the tensions in the three strings be T, T', and T'', as shown in Figure 5.8a.

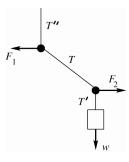


Figure 5.8a

SET UP: The free-body diagram for the block is given in Figure 5.8b.

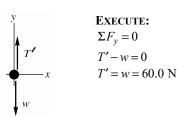
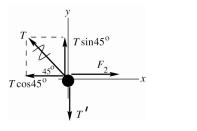


Figure 5.8b

SET UP: The free-body diagram for the lower knot is given in Figure 5.8c.



EXECUTE:

$$\Sigma F_y = 0$$

 $T \sin 45^\circ - T' = 0$
 $T = \frac{T'}{\sin 45^\circ} = \frac{60.0 \text{ N}}{\sin 45^\circ} = 84.9 \text{ N}$

Figure 5.8c

(b) Apply $\Sigma F_x = 0$ to the force diagram for the lower knot:

$$\Sigma F_{\rm r} = 0$$

$$F_2 = T\cos 45^\circ = (84.9 \text{ N})\cos 45^\circ = 60.0 \text{ N}$$

SET UP: The free-body diagram for the upper knot is given in Figure 5.8d.

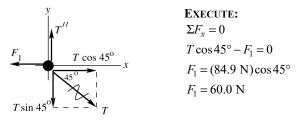
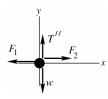


Figure 5.8d

Note that $F_1 = F_2$.

EVALUATE: Applying $\Sigma F_y = 0$ to the upper knot gives $T'' = T \sin 45^\circ = 60.0 \text{ N} = w$. If we treat the whole system as a single object, the force diagram is given in Figure 5.8e.



$$\Sigma F_x = 0$$
 gives $F_2 = F_1$, which checks $\Sigma F_y = 0$ gives $T'' = w$, which checks

Figure 5.8e

5.9. IDENTIFY: Since the velocity is constant, apply Newton's first law to the piano. The push applied by the man must oppose the component of gravity down the incline.

SET UP: The free-body diagrams for the two cases are shown in Figure 5.9. \vec{F} is the force applied by the man. Use the coordinates shown in the figure.

EXECUTE: (a) $\Sigma F_x = 0$ gives $F - w \sin 19.0^\circ = 0$ and $F = (180 \text{ kg})(9.80 \text{ m/s}^2) \sin 19.0^\circ = 574 \text{ N}.$

(b)
$$\Sigma F_y = 0$$
 gives $n \cos 19.0^\circ - w = 0$ and $n = \frac{w}{\cos 19.0^\circ}$. $\Sigma F_x = 0$ gives $F - n \sin 19.0^\circ = 0$ and $F = \left(\frac{w}{\cos 19.0^\circ}\right) \sin 19.0^\circ = w \tan 19.0^\circ = 607 \text{ N}.$

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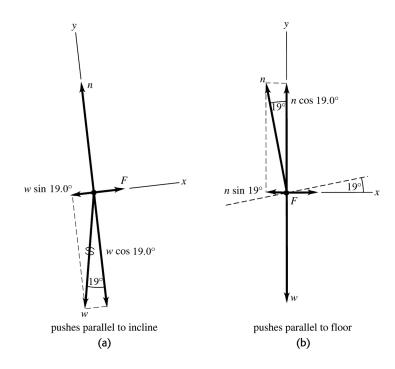


Figure 5.9

EVALUATE: When pushing parallel to the floor only part of the push is up the ramp to balance the weight of the piano, so you need a larger push in this case than if you push parallel to the ramp.

5.10. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the composite object of elevator plus student $(m_{\text{tot}} = 850 \text{ kg})$ and also to the student (w = 550 N). The elevator and the student have the same acceleration.

SET UP: Let +y be upward. The free-body diagrams for the composite object and for the student are given in Figure 5.10. T is the tension in the cable and n is the scale reading, the normal force the scale exerts on the student. The mass of the student is m = w/g = 56.1 kg.

EXECUTE: (a) $\Sigma F_v = ma_v$, applied to the student gives $n - mg = ma_v$.

 $a_y = \frac{n - mg}{m} = \frac{450 \text{ N} - 550 \text{ N}}{56.1 \text{ kg}} = -1.78 \text{ m/s}^2. \text{ The elevator has a downward acceleration of } 1.78 \text{ m/s}^2.$

(b)
$$a_y = \frac{670 \text{ N} - 550 \text{ N}}{56.1 \text{ kg}} = 2.14 \text{ m/s}^2.$$

(c) n = 0 means $a_y = -g$. The student should worry; the elevator is in free fall.

(d) $\Sigma F_y = ma_y$ applied to the composite object gives $T - m_{\text{tot}}g = m_{\text{tot}}a_y$. $T = m_{\text{tot}}(a_y + g)$. In part (a), $T = (850 \text{ kg})(-1.78 \text{ m/s}^2 + 9.80 \text{ m/s}^2) = 6820 \text{ N}$. In part (c), $a_y = -g$ and T = 0.

EVALUATE: In part (b), $T = (850 \text{ kg})(2.14 \text{ m/s}^2 + 9.80 \text{ m/s}^2) = 10,150 \text{ N}$. The weight of the composite object is 8330 N. When the acceleration is upward the tension is greater than the weight and when the acceleration is downward the tension is less than the weight.

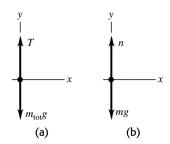


Figure 5.10

5.11. IDENTIFY: We apply Newton's second law to the rocket and the astronaut in the rocket. A constant force means we have constant acceleration, so we can use the standard kinematics equations. **SET UP:** The free-body diagrams for the rocket (weight w_r) and astronaut (weight w) are given in Figure 5.11. F_T is the thrust and n is the normal force the rocket exerts on the astronaut. The speed of sound is 331 m/s. We use $\Sigma F_v = ma_v$ and $v = v_0 + at$.

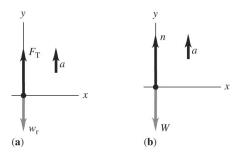


Figure 5.11

EXECUTE: (a) Apply $\Sigma F_y = ma_y$ to the rocket: $F_T - w_r = ma$. a = 4g and $w_r = mg$, so $F = m(5g) = (2.25 \times 10^6 \text{ kg}) (5) (9.80 \text{ m/s}^2) = 1.10 \times 10^8 \text{ N}$.

(b) Apply
$$\Sigma F_y = ma_y$$
 to the astronaut: $n - w = ma$. $a = 4g$ and $m = \frac{w}{g}$, so $n = w + \left(\frac{w}{g}\right)(4g) = 5w$.

(c)
$$v_0 = 0$$
, $v = 331$ m/s and $a = 4g = 39.2$ m/s². $v = v_0 + at$ gives $t = \frac{v - v_0}{a} = \frac{331 \text{ m/s}}{39.2 \text{ m/s}^2} = 8.4 \text{ s}.$

EVALUATE: The 8.4 s is probably an unrealistically short time to reach the speed of sound because you would not want your astronauts at the brink of blackout during a launch.

5.12. IDENTIFY: Apply Newton's second law to the rocket plus its contents and to the power supply. Both the rocket and the power supply have the same acceleration.

SET UP: The free-body diagrams for the rocket and for the power supply are given in Figure 5.12. Since the highest altitude of the rocket is 120 m, it is near to the surface of the earth and there is a downward gravity force on each object. Let +y be upward, since that is the direction of the

acceleration. The power supply has mass $m_{ps} = (15.5 \text{ N})/(9.80 \text{ m/s}^2) = 1.58 \text{ kg}.$

EXECUTE: (a) $\Sigma F_y = ma_y$ applied to the rocket gives $F - m_r g = m_r a$.

$$a = \frac{F - m_{\rm r}g}{m_{\rm r}} = \frac{1720 \text{ N} - (125 \text{ kg})(9.80 \text{ m/s}^2)}{125 \text{ kg}} = 3.96 \text{ m/s}^2.$$

(b) $\Sigma F_y = ma_y$ applied to the power supply gives $n - m_{ps}g = m_{ps}a$.

$$n = m_{\rm ps}(g+a) = (1.58 \text{ kg})(9.80 \text{ m/s}^2 + 3.96 \text{ m/s}^2) = 21.7 \text{ N}.$$

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EVALUATE: The acceleration is constant while the thrust is constant, and the normal force is constant while the acceleration is constant. The altitude of 120 m is not used in the calculation.

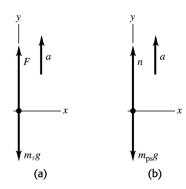


Figure 5.12

5.13. IDENTIFY: Use the kinematic information to find the acceleration of the capsule and the stopping time. Use Newton's second law to find the force F that the ground exerted on the capsule during the crash.
SET UP: Let +y be upward. 311 km/h = 86.4 m/s. The free-body diagram for the capsule is given in Figure 5.13.

EXECUTE:
$$y - y_0 = -0.810 \text{ m}, \ v_{0y} = -86.4 \text{ m/s}, \ v_y = 0. \ v_y^2 = v_{0y}^2 + 2a_y(y - y_0) \text{ gives}$$

$$a_y = \frac{v_y^2 - v_{0y}^2}{2(y - y_0)} = \frac{0 - (-86.4 \text{ m/s})^2}{2(-0.810) \text{ m}} = 4610 \text{ m/s}^2 = 470g.$$

(b) $\Sigma F_v = ma_v$ applied to the capsule gives F - mg = ma and

 $F = m(g + a) = (210 \text{ kg})(9.80 \text{ m/s}^2 + 4610 \text{ m/s}^2) = 9.70 \times 10^5 \text{ N} = 471 \text{w}.$

(c)
$$y - y_0 = \left(\frac{v_{0y} + v_y}{2}\right)t$$
 gives $t = \frac{2(y - y_0)}{v_{0y} + v_y} = \frac{2(-0.810 \text{ m})}{-86.4 \text{ m/s} + 0} = 0.0187 \text{ s}$

EVALUATE: The upward force exerted by the ground is much larger than the weight of the capsule and stops the capsule in a short amount of time. After the capsule has come to rest, the ground still exerts a force mg on the capsule, but the large 9.70×10^5 N force is exerted only for 0.0187 s.

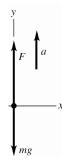


Figure 5.13

5.14. IDENTIFY: Apply Newton's second law to the three sleds taken together as a composite object and to each individual sled. All three sleds have the same horizontal acceleration a.

SET UP: The free-body diagram for the three sleds taken as a composite object is given in Figure 5.14a and for each individual sled in Figures 5.14b–d. Let +x be to the right, in the direction of the acceleration. $m_{\text{tot}} = 60.0 \text{ kg}$.

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EXECUTE: (a) $\Sigma F_x = ma_x$ for the three sleds as a composite object gives $P = m_{\text{tot}}a$ and $a = \frac{P}{m_{\text{tot}}} = \frac{190 \text{ N}}{60.0 \text{ kg}} = 3.17 \text{ m/s}^2$.

(b) $\Sigma F_x = ma_x$ applied to the 10.0 kg sled gives $P - T_A = m_{10}a$ and $T_A = P - m_{10}a = 190 \text{ N} - (10.0 \text{ kg})(3.17 \text{ m/s}^2) = 158 \text{ N}.$ $\Sigma F_x = ma_x$ applied to the 30.0 kg sled gives

$$T_R = m_{30}a = (30.0 \text{ kg})(3.17 \text{ m/s}^2) = 95.1 \text{ N}.$$

EVALUATE: If we apply $\Sigma F_x = ma_x$ to the 20.0 kg sled and calculate a from T_A and T_B found in part

(b), we get
$$T_A - T_B = m_{20}a$$
. $a = \frac{T_A - T_B}{m_{20}} = \frac{158 \text{ N} - 95.1 \text{ N}}{20.0 \text{ kg}} = 3.15 \text{ m/s}^2$, which agrees closely with the

value we calculated in part (a), the difference being due to rounding.

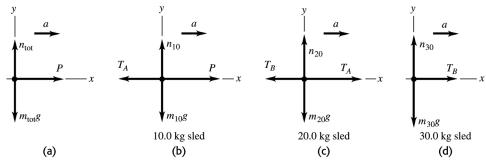


Figure 5.14

- **5.15. IDENTIFY:** Apply $\Sigma \vec{F} = m\vec{a}$ to the load of bricks and to the counterweight. The tension is the same at each end of the rope. The rope pulls up with the same force (T) on the bricks and on the counterweight. The counterweight accelerates downward and the bricks accelerate upward; these accelerations have the same magnitude.
 - (a) SET UP: The free-body diagrams for the bricks and counterweight are given in Figure 5.15.

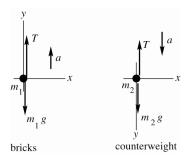


Figure 5.15

(b) EXECUTE: Apply $\Sigma F_y = ma_y$ to each object. The acceleration magnitude is the same for the two objects. For the bricks take +y to be upward since \vec{a} for the bricks is upward. For the counterweight take +y to be downward since \vec{a} is downward.

bricks:
$$\Sigma F_y = ma_y$$

 $T - m_1 g = m_1 a$
counterweight: $\Sigma F_y = ma_y$
 $m_2 g - T = m_2 a$

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Add these two equations to eliminate *T*:

$$(m_2 - m_1)g = (m_1 + m_2)a$$

$$a = \left(\frac{m_2 - m_1}{m_1 + m_2}\right) g = \left(\frac{28.0 \text{ kg} - 15.0 \text{ kg}}{15.0 \text{ kg} + 28.0 \text{ kg}}\right) (9.80 \text{ m/s}^2) = 2.96 \text{ m/s}^2$$

(c)
$$T - m_1 g = m_1 a$$
 gives $T = m_1 (a + g) = (15.0 \text{ kg})(2.96 \text{ m/s}^2 + 9.80 \text{ m/s}^2) = 191 \text{ N}$

As a check, calculate T using the other equation.

$$m_2g - T = m_2a$$
 gives $T = m_2(g - a) = 28.0 \text{ kg}(9.80 \text{ m/s}^2 - 2.96 \text{ m/s}^2) = 191 \text{ N}$, which checks.

EVALUATE: The tension is 1.30 times the weight of the bricks; this causes the bricks to accelerate upward. The tension is 0.696 times the weight of the counterweight; this causes the counterweight to accelerate downward. If $m_1 = m_2$, a = 0 and $T = m_1 g = m_2 g$. In this special case the objects don't move. If $m_1 = 0$, a = g and T = 0; in this special case the counterweight is in free fall. Our general result is correct in these two special cases.

5.16. IDENTIFY: In part (a) use the kinematic information and the constant acceleration equations to calculate the acceleration of the ice. Then apply $\Sigma \vec{F} = m\vec{a}$. In part (b) use $\Sigma \vec{F} = m\vec{a}$ to find the acceleration and use this in the constant acceleration equations to find the final speed.

SET UP: Figure 5.16 gives the free-body diagrams for the ice both with and without friction. Let +x be directed down the ramp, so +y is perpendicular to the ramp surface. Let ϕ be the angle between the ramp and the horizontal. The gravity force has been replaced by its x- and y-components.

EXECUTE: (a)
$$x - x_0 = 1.50 \text{ m}$$
, $v_{0x} = 0$. $v_x = 2.50 \text{ m/s}$. $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ gives

$$a_x = \frac{v_x^2 - v_{0x}^2}{2(x - x_0)} = \frac{(2.50 \text{ m/s})^2 - 0}{2(1.50 \text{ m})} = 2.08 \text{ m/s}^2$$
. $\Sigma F_x = ma_x$ gives $mg \sin \phi = ma$ and

$$\sin \phi = \frac{a}{g} = \frac{2.08 \text{ m/s}^2}{9.80 \text{ m/s}^2}. \ \phi = 12.3^\circ.$$

(b)
$$\Sigma F_x = ma_x$$
 gives $mg\sin\phi - f = ma$ and

$$a = \frac{mg\sin\phi - f}{m} = \frac{(8.00 \text{ kg})(9.80 \text{ m/s}^2)\sin 12.3^\circ - 10.0 \text{ N}}{8.00 \text{ kg}} = 0.838 \text{ m/s}^2.$$

Then
$$x - x_0 = 1.50$$
 m, $v_{0x} = 0$. $a_x = 0.838$ m/s² and $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ gives

$$v_r = \sqrt{2a_r(x - x_0)} = \sqrt{2(0.838 \text{ m/s}^2)(1.50 \text{ m})} = 1.59 \text{ m/s}$$

EVALUATE: With friction present the speed at the bottom of the ramp is less.

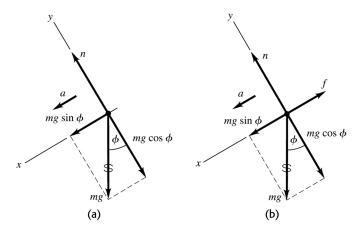


Figure 5.16

5.17. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each block. Each block has the same magnitude of acceleration a.

SET UP: Assume the pulley is to the right of the 4.00 kg block. There is no friction force on the 4.00 kg block; the only force on it is the tension in the rope. The 4.00 kg block therefore accelerates to the right and the suspended block accelerates downward. Let +x be to the right for the 4.00 kg block, so for it $a_x = a$, and let +y be downward for the suspended block, so for it $a_y = a$.

EXECUTE: (a) The free-body diagrams for each block are given in Figures 5.17a and b.

(b) $\Sigma F_x = ma_x$ applied to the 4.00 kg block gives T = (4.00 kg)a and

$$a = \frac{T}{4.00 \text{ kg}} = \frac{15.0 \text{ N}}{4.00 \text{ kg}} = 3.75 \text{ m/s}^2.$$

(c) $\Sigma F_v = ma_v$, applied to the suspended block gives mg - T = ma and

$$m = \frac{T}{g - a} = \frac{15.0 \text{ N}}{9.80 \text{ m/s}^2 - 3.75 \text{ m/s}^2} = 2.48 \text{ kg}.$$

(d) The weight of the hanging block is $mg = (2.48 \text{ kg})(9.80 \text{ m/s}^2) = 24.3 \text{ N}$. This is greater than the tension in the rope; T = 0.617mg.

EVALUATE: Since the hanging block accelerates downward, the net force on this block must be downward and the weight of the hanging block must be greater than the tension in the rope. Note that the blocks accelerate no matter how small m is. It is not necessary to have m > 4.00 kg, and in fact in this problem m is less than 4.00 kg.

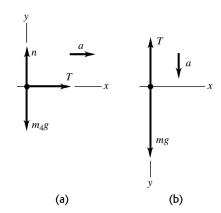


Figure 5.17

- **5.18. IDENTIFY:** (a) Consider both gliders together as a single object, apply $\Sigma \vec{F} = m\vec{a}$, and solve for a. Use a in a constant acceleration equation to find the required runway length.
 - **(b)** Apply $\Sigma \vec{F} = m\vec{a}$ to the second glider and solve for the tension T_g in the towrope that connects the two gliders.

SET UP: In part (a), set the tension T_t in the towrope between the plane and the first glider equal to its maximum value, $T_t = 12,000 \text{ N}$.

EXECUTE: (a) The free-body diagram for both gliders as a single object of mass 2m = 1400 kg is given in Figure 5.18a. $\Sigma F_x = ma_x$ gives $T_t - 2f = (2m)a$ and

$$a = \frac{T_{\rm t} - 2f}{2m} = \frac{12,000 \text{ N} - 5000 \text{ N}}{1400 \text{ kg}} = 5.00 \text{ m/s}^2$$
. Then $a_x = 5.00 \text{ m/s}^2$, $v_{0x} = 0$ and $v_x = 40 \text{ m/s}$ in

$$v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$$
 gives $(x - x_0) = \frac{v_x^2 - v_{0x}^2}{2a_x} = 160$ m.

(b) The free-body diagram for the second glider is given in Figure 5.18b.

 $\Sigma F_x = ma_x$ gives $T_g - f = ma$ and $T_g = f + ma = 2500 \text{ N} + (700 \text{ kg})(5.00 \text{ m/s}^2) = 6000 \text{ N}$.

EVALUATE: We can verify that $\Sigma F_x = ma_x$ is also satisfied for the first glider.

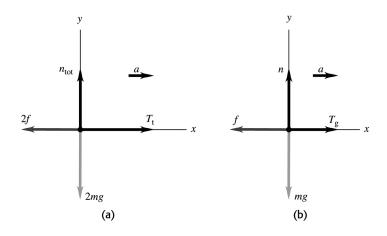


Figure 5.18

5.19. IDENTIFY: While the person is in contact with the ground, he is accelerating upward and experiences two forces: gravity downward and the upward force of the ground. Once he is in the air, only gravity acts on him so he accelerates downward. Newton's second law applies during the jump (and at all other times).

SET UP: Take +y to be upward. After he leaves the ground the person travels upward 60 cm and his acceleration is $g = 9.80 \text{ m/s}^2$, downward. His weight is w so his mass is w/g. $\Sigma F_y = ma_y$ and $v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$ apply to the jumper.

EXECUTE: (a) $v_y = 0$ (at the maximum height), $y - y_0 = 0.60$ m, $a_y = -9.80$ m/s². $v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$ gives $v_{0y} = \sqrt{-2a_y(y - y_0)} = \sqrt{-2(-9.80 \text{ m/s}^2)(0.60 \text{ m})} = 3.4 \text{ m/s}.$

- **(b)** The free-body diagram for the person while he is pushing up against the ground is given in Figure 5.19.
- (c) For the jump, $v_{0y} = 0$, $v_y = 3.4$ m/s (from part (a)), and $y y_0 = 0.50$ m. $v_y^2 = v_{0y}^2 + 2a_y(y y_0)$ gives $a_y = \frac{v_y^2 v_{0y}^2}{2(y y_0)} = \frac{(3.4 \text{ m/s})^2 0}{2(0.50 \text{ m})} = 11.6 \text{ m/s}^2$. $\Sigma F_y = ma_y$ gives n w = ma.

$$n = w + ma = w \left(1 + \frac{a}{g} \right) = 2.2w.$$

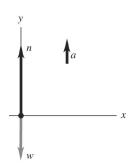


Figure 5.19

EVALUATE: To accelerate the person upward during the jump, the upward force from the ground must exceed the downward pull of gravity. The ground pushes up on him because he pushes down on the ground.

5.20. IDENTIFY: Acceleration and velocity are related by $a_y = \frac{dv_y}{dt}$. Apply $\Sigma \vec{F} = m\vec{a}$ to the rocket.

SET UP: Let +y be upward. The free-body diagram for the rocket is sketched in Figure 5.20. \vec{F} is the thrust force.

EXECUTE: (a) $v_y = At + Bt^2$. $a_y = A + 2Bt$. At t = 0, $a_y = 1.50 \text{ m/s}^2$ so $A = 1.50 \text{ m/s}^2$. Then $v_y = 2.00 \text{ m/s}$ at t = 1.00 s gives $2.00 \text{ m/s} = (1.50 \text{ m/s}^2)(1.00 \text{ s}) + B(1.00 \text{ s})^2$ and $B = 0.50 \text{ m/s}^3$.

- **(b)** At t = 4.00 s, $a_y = 1.50 \text{ m/s}^2 + 2(0.50 \text{ m/s}^3)(4.00 \text{ s}) = 5.50 \text{ m/s}^2$.
- (c) $\Sigma F_y = ma_y$ applied to the rocket gives T mg = ma and $T = m(a+g) = (2540 \text{ kg})(9.80 \text{ m/s}^2 + 5.50 \text{ m/s}^2) = 3.89 \times 10^4 \text{ N}. \ T = 1.56w.$
- (d) When $a = 1.50 \text{ m/s}^2$, $T = (2540 \text{ kg})(9.80 \text{ m/s}^2 + 1.50 \text{ m/s}^2) = 2.87 \times 10^4 \text{ N}$.

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EVALUATE: During the time interval when $v(t) = At + Bt^2$ applies the magnitude of the acceleration is increasing, and the thrust is increasing.

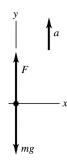


Figure 5.20

5.21. IDENTIFY: We know the external forces on the box and want to find the distance it moves and its speed. The force is not constant, so the acceleration will not be constant, so we cannot use the standard constant-acceleration kinematics formulas. But Newton's second law will apply.

SET UP: First use Newton's second law to find the acceleration as a function of time: $a_x(t) = \frac{F_x}{m}$. Then integrate the acceleration to find the velocity as a function of time, and next integrate the velocity to find the position as a function of time.

EXECUTE: Let +x be to the right. $a_x(t) = \frac{F_x}{m} = \frac{(-6.00 \text{ N/s}^2)t^2}{2.00 \text{ kg}} = -(3.00 \text{ m/s}^4)t^2$. Integrate the

acceleration to find the velocity as a function of time: $v_x(t) = -(1.00 \text{ m/s}^4)t^3 + 9.00 \text{ m/s}$. Next integrate the velocity to find the position as a function of time: $x(t) = -(0.250 \text{ m/s}^4)t^4 + (9.00 \text{ m/s})t$. Now use the given values of time.

- (a) $v_x = 0$ when $(1.00 \text{ m/s}^4)t^3 = 9.00 \text{ m/s}$. This gives t = 2.08 s. At t = 2.08 s, $x = (9.00 \text{ m/s})(2.08 \text{ s}) (0.250 \text{ m/s}^4)(2.08 \text{ s})^4 = 18.72 \text{ m} 4.68 \text{ m} = 14.0 \text{ m}$.
- **(b)** At t = 3.00 s, $v_r(t) = -(1.00 \text{ m/s}^4)(3.00 \text{ s})^3 + 9.00 \text{ m/s} = -18.0 \text{ m/s}$, so the speed is 18.0 m/s.

EVALUATE: The box starts out moving to the right. But because the acceleration is to the left, it reverses direction and v_x is negative in part (b).

5.22. IDENTIFY: We know the position of the crate as a function of time, so we can differentiate to find its acceleration. Then we can apply Newton's second law to find the upward force.

SET UP: $v_y(t) = dy/dt$, $a_y(t) = dv_y/dt$, and $\Sigma F_y = ma_y$.

EXECUTE: Let +y be upward. $dy/dt = v_y(t) = 2.80 \text{ m/s} + (1.83 \text{ m/s}^3)t^2$ and

 $dv_y/dt = a_y(t) = (3.66 \text{ m/s}^3)t$. At t = 4.00 s, $a_y = 14.64 \text{ m/s}^2$. Newton's second law in the y direction

gives F - mg = ma. Solving for F gives $F = 49 \text{ N} + (5.00 \text{ kg})(14.64 \text{ m/s}^2) = 122 \text{ N}$.

EVALUATE: The force is greater than the weight since it is accelerating the crate upward.

5.23. IDENTIFY: At the maximum tilt angle, the patient is just ready to slide down, so static friction is at its maximum and the forces on the patient balance.

SET UP: Take +x to be down the incline. At the maximum angle $f_s = \mu_s n$ and $\Sigma F_x = ma_x = 0$.

EXECUTE: The free-body diagram for the patient is given in Figure 5.23. $\Sigma F_v = ma_v$ gives

 $n = mg\cos\theta$. $\Sigma F_x = 0$ gives $mg\sin\theta - \mu_s n = 0$. $mg\sin\theta - \mu_s mg\cos\theta = 0$. $\tan\theta = \mu_s$ so $\theta = 50^\circ$.

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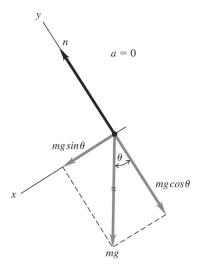


Figure 5.23

EVALUATE: A larger angle of tilt would cause more blood to flow to the brain, but it would also cause the patient to slide down the bed.

5.24. IDENTIFY: $f_s \le \mu_s n$ and $f_k = \mu_k n$. The normal force n is determined by applying $\Sigma \vec{F} = m\vec{a}$ to the block. Normally, $\mu_k \le \mu_s$. f_s is only as large as it needs to be to prevent relative motion between the two surfaces

SET UP: Since the table is horizontal, with only the block present n = 135 N. With the brick on the block,

n = 270 N.

EXECUTE: (a) The friction is static for P = 0 to P = 75.0 N. The friction is kinetic for P > 75.0 N.

(b) The maximum value of f_s is $\mu_s n$. From the graph the maximum f_s is $f_s = 75.0$ N, so

$$\mu_{\rm s} = \frac{\max f_{\rm s}}{n} = \frac{75.0 \; \rm N}{135 \; \rm N} = 0.556. \quad f_{\rm k} = \mu_{\rm k} n. \; \text{From the graph}, \; f_{\rm k} = 50.0 \; \rm N \; \; \text{and} \; \; \mu_{\rm k} = \frac{f_{\rm k}}{n} = \frac{50.0 \; \rm N}{135 \; \rm N} = 0.370.$$

- (c) When the block is moving the friction is kinetic and has the constant value $f_k = \mu_k n$, independent of P. This is why the graph is horizontal for P > 75.0 N. When the block is at rest, $f_s = P$ since this prevents relative motion. This is why the graph for P < 75.0 N has slope +1.
- (d) max f_s and f_k would double. The values of f on the vertical axis would double but the shape of the graph would be unchanged.

EVALUATE: The coefficients of friction are independent of the normal force.

5.25. (a) IDENTIFY: Constant speed implies a = 0. Apply Newton's first law to the box. The friction force is directed opposite to the motion of the box.

SET UP: Consider the free-body diagram for the box, given in Figure 5.25a. Let \vec{F} be the horizontal force applied by the worker. The friction is kinetic friction since the box is sliding along the surface.

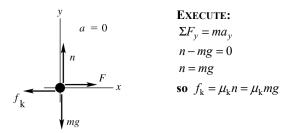


Figure 5.25a

$$\Sigma F_x = ma_x$$

 $F - f_k = 0$
 $F = f_k = \mu_k mg = (0.20)(16.8 \text{ kg})(9.80 \text{ m/s}^2) = 33 \text{ N}$

(b) IDENTIFY: Now the only horizontal force on the box is the kinetic friction force. Apply Newton's second law to the box to calculate its acceleration. Once we have the acceleration, we can find the distance using a constant acceleration equation. The friction force is $f_k = \mu_k mg$, just as in part (a).

SET UP: The free-body diagram is sketched in Figure 5.25b.

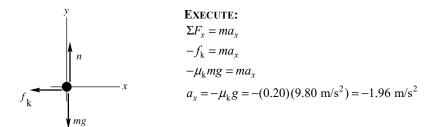


Figure 5.25b

Use the constant acceleration equations to find the distance the box travels:

$$v_x = 0$$
, $v_{0x} = 3.50 \text{ m/s}$, $a_x = -1.96 \text{ m/s}^2$, $x - x_0 = ?$
 $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$
 $x - x_0 = \frac{v_x^2 - v_{0x}^2}{2a_x} = \frac{0 - (3.50 \text{ m/s})^2}{2(-1.96 \text{ m/s}^2)} = 3.1 \text{ m}$

EVALUATE: The normal force is the component of force exerted by a surface perpendicular to the surface. Its magnitude is determined by $\Sigma \vec{F} = m\vec{a}$. In this case n and mg are the only vertical forces and $a_y = 0$, so n = mg. Also note that f_k and n are proportional in magnitude but perpendicular in direction.

5.26. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the box.

SET UP: Since the only vertical forces are n and w, the normal force on the box equals its weight. Static friction is as large as it needs to be to prevent relative motion between the box and the surface, up to its maximum possible value of $f_s^{\text{max}} = \mu_s n$. If the box is sliding then the friction force is $f_k = \mu_k n$.

EXECUTE: (a) If there is no applied force, no friction force is needed to keep the box at rest. (b) $f_s^{\text{max}} = \mu_s n = (0.40)(40.0 \text{ N}) = 16.0 \text{ N}$. If a horizontal force of 6.0 N is applied to the box, then $f_s = 6.0 \text{ N}$ in the opposite direction.

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- (c) The monkey must apply a force equal to f_s^{max} , 16.0 N.
- (d) Once the box has started moving, a force equal to $f_k = \mu_k n = 8.0 \text{ N}$ is required to keep it moving at constant velocity.

(e)
$$f_k = 8.0 \text{ N}$$
. $a = (18.0 \text{ N} - 8.0 \text{ N}) / (40.0 \text{ N} / 9.80 \text{ m} / \text{s}^2) = 2.45 \text{ m} / \text{s}^2$

EVALUATE: $\mu_k < \mu_s$ and less force must be applied to the box to maintain its motion than to start it moving.

5.27. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the crate. $f_s \le \mu_s n$ and $f_k = \mu_k n$.

SET UP: Let +y be upward and let +x be in the direction of the push. Since the floor is horizontal and the push is horizontal, the normal force equals the weight of the crate: n = mg = 441 N. The force it takes to start the crate moving equals max f_s and the force required to keep it moving equals f_k .

EXECUTE: (a) max
$$f_s = 313 \text{ N}$$
, so $\mu_s = \frac{313 \text{ N}}{441 \text{ N}} = 0.710$. $f_k = 208 \text{ N}$, so $\mu_k = \frac{208 \text{ N}}{441 \text{ N}} = 0.472$.

(b) The friction is kinetic. $\Sigma F_x = ma_x$ gives $F - f_k = ma$ and

$$F = f_k + ma = 208 \text{ N} + (45.0 \text{ kg})(1.10 \text{ m/s}^2) = 258 \text{ N}.$$

(c) (i) The normal force now is mg = 72.9 N. To cause it to move,

$$F = \max f_s = \mu_s n = (0.710)(72.9 \text{ N}) = 51.8 \text{ N}.$$

(ii)
$$F = f_k + ma$$
 and $a = \frac{F - f_k}{m} = \frac{258 \text{ N} - (0.472)(72.9 \text{ N})}{45.0 \text{ kg}} = 4.97 \text{ m/s}^2$

EVALUATE: The kinetic friction force is independent of the speed of the object. On the moon, the mass of the crate is the same as on earth, but the weight and normal force are less.

5.28. IDENTIFY: On the level floor and on the ramp the box moves with constant velocity, so its acceleration is zero. Therefore the forces on it must balance. In addition to your push, kinetic friction and gravity act on the box.

SET UP: Estimate: Heaviest box is about 150 lb with sustained effort. $\sum F_x = 0$, $\sum F_y = 0$, and the kinetic friction force is $f_k = \mu_k n$.

EXECUTE: To push a 150-lb box on a horizontal surface, the force needed would be equal to the kinetic friction force, which is $f_k = \mu_k n = (0.50)(150 \text{ lb}) = 75 \text{ lb}$. We now exert this push on a box on a ramp and want to know the weight of the heaviest box we can push up the ramp at constant speed. μ_k is the same on the ramp as it is on the level floor. Fig. 5.28 shows a free-body diagram of the box on the ramp. Take the *x*-axis parallel to the ramp surface pointing up the ramp, and call β the angle the ramp makes above the horizontal.

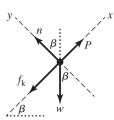


Figure 5.28

Using the notation in Fig. 5.28, $\sum F_y = 0$ gives $n - w \cos \beta = 0$, so $n = w \cos \beta$. $\sum F_x = 0$ gives $P - f_k - w \sin \beta = 0$. We also have $f_k = \mu_k n$, so the last equation becomes

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$$P - \mu_k w \cos \beta - w \sin \beta = 0$$
. Solve for $w: w = \frac{P}{\mu_k \cos \beta + \sin \beta} = \frac{75 \text{ lb}}{(0.50) \cos 60^\circ + \sin 60^\circ}$, so $w = 67 \text{ lb}$.

EVALUATE: This weight is less than you can push on a level surface because you need to balance the weight component down the ramp in addition to the friction force.

5.29. IDENTIFY: The children are accelerated as they move down the slide, so Newton's second law applies. The acceleration is constant, so the constant-acceleration formulas apply.

SET UP: Estimations: The height of the slide is about 6 ft or 2.0 m, and it rises at an angle of 30° above the horizontal. The forces on the child are gravity, the normal force due to the slide, and friction. Apply $\sum F_x = ma_x$ with the x-axis is along the surface of the slide pointing downward, and $\sum F_y = 0$ with the y-axis perpendicular to the slide surface. Fig. 5.29 shows free-body diagrams of the child with and without friction.

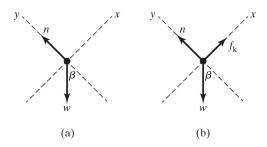


Figure 5.29

EXECUTE: (a) First find the acceleration and then use it to find the velocity at the bottom of the slide. Use $\sum F_x = ma_x$ with the notation in Fig. 5.29a. $mg \sin \beta = ma_x$, so $a_x = g \sin \beta = g \sin 30^\circ = g/2$. Now use $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ to find v_x at the bottom. The distance $x - x_0 = (2.0 \text{ m})/(\sin \beta) = (2.0 \text{ m})/(\sin 30^\circ) = 4.0 \text{ m}$. This gives $v_x^2 = 0 + 2(g/2)(4.0 \text{ m})$, so $v_x = 6.3 \text{ m/s}$.

(b) Now friction is acting up the slide, as shown in Fig. 5.29b, and we want to find μ_k . In this case, v_x is half of what it was without friction, so $v_x = (0.50)(6.3 \text{ m/s}) = 3.13 \text{ m/s}$. Now use $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ to find the acceleration. $(3.13 \text{ m/s})^2 = 2a_x(4.0 \text{ m}) \rightarrow a_x = 1.225 \text{ m/s}^2$. Using $\sum F_x = ma_x$ gives $mg \sin \beta - f_k = mg \sin \beta - \mu_k n = ma_x$. Now use $\sum F_y = 0$ to find the normal force. $n - mg \cos \beta = 0$, so $n = mg \cos \beta$. Combining these two results gives

 $mg \sin \beta - \mu_k mg \cos \beta = ma_x$. Solving for μ_k gives $\mu_k = \frac{g \sin \beta - a_x}{g \cos \beta}$. Using $a_x = 1.225$ m/s² and $\beta = 30^\circ$, we get $\mu_k = 0.43$.

(c) We now have static friction. For μ_s to have its minimum value, the child must be just ready to slide, so static friction is at its maximum value, which is $f_s = \mu_s n$. As before, $n = mg \cos \beta$. Now we have $\sum F_x = 0$, giving $\mu_s mg \cos \beta - mg \sin \beta = 0$, so $\mu_s = \tan \beta = \tan 30^\circ = 0.58$.

EVALUATE: Table 5.1 shows that 0.58 is a reasonable value for μ_s , and it is larger than the value for μ_k we used in part (b).

5.30. IDENTIFY: Newton's second law applies to the rocks on the hill. When they are moving, kinetic friction acts on them, but when they are at rest, static friction acts.

SET UP: Use coordinates with axes parallel and perpendicular to the incline, with +x in the direction of the acceleration. $\Sigma F_x = ma_x$ and $\Sigma F_y = ma_y = 0$.

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EXECUTE: With the rock sliding up the hill, the friction force is down the hill. The free-body diagram is given in Figure 5.30a.

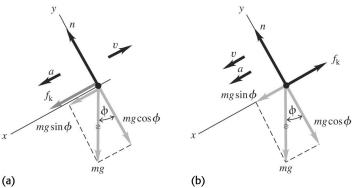


Figure 5.30

 $\Sigma F_y = ma_y = 0$ gives $n = mg\cos\phi$ and $f_k = \mu_k n = \mu_k mg\cos\phi$. $\Sigma F_x = ma_x$ gives $mg\sin\phi + \mu_k mg\cos\phi = ma$.

 $a = g(\sin \phi + \mu_k \cos \phi) = (9.80 \text{ m/s}^2)[\sin 36^\circ + (0.45)\cos 36^\circ].$ $a = 9.33 \text{ m/s}^2$, down the incline.

(b) The component of gravity down the incline is $mg \sin \phi = 0.588mg$. The maximum possible static friction force is $f_s = \mu_s n = \mu_s mg \cos \phi = 0.526mg$. f_s can't be as large as $mg \sin \phi$ and the rock slides back down. As the rock slides down, f_k is up the incline. The free-body diagram is given in Figure 5.30b. $\Sigma F_y = ma_y = 0$ gives $n = mg \cos \phi$ and $f_k = \mu_k n = \mu_k mg \cos \phi$. $\Sigma F_x = ma_x$ gives $mg \sin \phi - \mu_k mg \cos \phi = ma$, so $a = g(\sin \phi - \mu_k \cos \phi) = 2.19 \text{ m/s}^2$, down the incline.

EVALUATE: The acceleration down the incline in (a) is greater than that in (b) because in (a) the static friction and gravity are both acting down the incline, whereas in (b) friction is up the incline, opposing gravity which still acts down the incline.

5.31. IDENTIFY: A 10.0-kg box is pushed on a ramp, causing it to accelerate. Newton's second law applies. **SET UP:** Choose the *x*-axis along the surface of the ramp and the *y*-axis perpendicular to the surface. The only acceleration of the box is in the *x*-direction, so $\Sigma F_x = ma_x$ and $\Sigma F_y = 0$. The external forces acting on the box are the push *P* along the surface of the ramp, friction f_k , gravity mg, and the normal force *n*. The ramp rises at 55.0° above the horizontal, and $f_k = \mu_k n$. The friction force opposes the sliding, so it is directed up the ramp in part (a) and down the ramp in part (b).

EXECUTE: (a) Applying $\Sigma F_y = 0$ gives $n = mg \cos(55.0^\circ)$, so the force of kinetic friction is $f_k = \mu_k n = (0.300)(10.0 \text{ kg})(9.80 \text{ m/s}^2)(\cos 55.0^\circ) = 16.86 \text{ N}$. Call the +x-direction down the ramp since that is the direction of the acceleration of the box. Applying $\Sigma F_x = ma_x$ gives $P + mg \sin(55.0^\circ) - f_k = ma$. Putting in the numbers gives $(10.0 \text{ kg})a = 120 \text{ N} + (98.0 \text{ N})(\sin 55.0^\circ) - 16.86 \text{ N}$; $a = 18.3 \text{ m/s}^2$.

(b) Now *P* is up the up the ramp and f_k is down the ramp, but the other force components are unchanged, so $f_k = 16.86$ N as before. We now choose +x to be up the ramp, so $\Sigma F_x = ma_x$ gives

 $P - mg \sin(55.0^{\circ}) - f_k = ma$. Putting in the same numbers as before gives $a = 2.29 \text{ m/s}^2$.

EVALUATE: Pushing up the ramp produces a much smaller acceleration than pushing down the ramp because gravity helps the downward push but opposes the upward push.

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5.32. IDENTIFY: For the shortest time, the acceleration is a maximum, so the toolbox is just ready to slide relative to the bed of the truck. The box is at rest relative to the truck, but it is accelerating relative to the ground because the truck is accelerating. Therefore Newton's second law will be useful.

SET UP: If the truck accelerates to the right the static friction force on the box is to the right, to try to prevent the box from sliding relative to the truck. The free-body diagram for the box is given in Figure 5.32. The maximum acceleration of the box occurs when f_s has its maximum value, so $f_s = \mu_s n$. If the box doesn't slide, its acceleration equals the acceleration of the truck. The constant-acceleration equation $v_x = v_{0x} + a_x t$ applies.

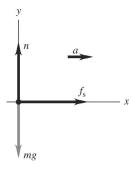


Figure 5.32

EXECUTE: n = mg. $\Sigma F_x = ma_x$ gives $f_s = ma$ so $\mu_s mg = ma$ and $a = \mu_s g = 6.37 \text{ m/s}^2$. $v_{0x} = 0$, $v_x = 30.0 \text{ m/s}$. $v_x = v_{0x} + a_x t$ gives $t = \frac{v_x - v_{0x}}{a_x} = \frac{30.0 \text{ m/s} - 0}{6.37 \text{ m/s}^2} = 4.71 \text{ s}$.

EVALUATE: If the truck has a smaller acceleration it is still true that $f_s = ma$, but now $f_s < \mu_s n$.

5.33. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the composite object consisting of the two boxes and to the top box. The friction the ramp exerts on the lower box is kinetic friction. The upper box doesn't slip relative to the lower box, so the friction between the two boxes is static. Since the speed is constant the acceleration is zero.

SET UP: Let +x be up the incline. The free-body diagrams for the composite object and for the upper box are given in Figure 5.33. The slope angle ϕ of the ramp is given by $\tan \phi = \frac{2.50 \text{ m}}{4.75 \text{ m}}$, so $\phi = 27.76^{\circ}$.

Since the boxes move down the ramp, the kinetic friction force exerted on the lower box by the ramp is directed up the incline. To prevent slipping relative to the lower box the static friction force on the upper box is directed up the incline. $m_{\text{tot}} = 32.0 \text{ kg} + 48.0 \text{ kg} = 80.0 \text{ kg}$.

EXECUTE: (a) $\Sigma F_y = ma_y$ applied to the composite object gives $n_{\text{tot}} = m_{\text{tot}}g\cos\phi$ and $f_k = \mu_k m_{\text{tot}}g\cos\phi$. $\Sigma F_x = ma_x$ gives $f_k + T - m_{\text{tot}}g\sin\phi = 0$ and $T = (\sin\phi - \mu_k\cos\phi)m_{\text{tot}}g = (\sin 27.76^\circ - [0.444]\cos 27.76^\circ)(80.0 \text{ kg})(9.80 \text{ m/s}^2) = 57.1 \text{ N}.$

The person must apply a force of 57.1 N, directed up the ramp.

(b) $\Sigma F_x = ma_x$ applied to the upper box gives $f_s = mg \sin \phi = (32.0 \text{ kg})(9.80 \text{ m/s}^2) \sin 27.76^\circ = 146 \text{ N}$, directed up the ramp.

EVALUATE: For each object the net force is zero.

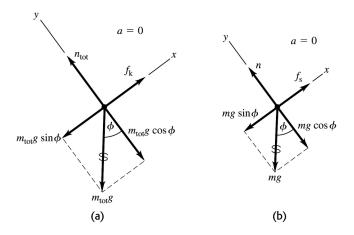


Figure 5.33

5.34. IDENTIFY: Constant speed means zero acceleration for each block. If the block is moving, the friction force the tabletop exerts on it is kinetic friction. Apply $\Sigma \vec{F} = m\vec{a}$ to each block.

SET UP: The free-body diagrams and choice of coordinates for each block are given by Figure 5.34. $m_A = 4.59 \text{ kg}$ and $m_B = 2.55 \text{ kg}$.

EXECUTE: (a) $\Sigma F_y = ma_y$ with $a_y = 0$ applied to block B gives $m_B g - T = 0$ and T = 25.0 N. $\Sigma F_x = ma_x$ with $a_x = 0$ applied to block A gives $T - f_k = 0$ and $f_k = 25.0 \text{ N}$. $n_A = m_A g = 45.0 \text{ N}$ and $\mu_k = \frac{f_k}{n_A} = \frac{25.0 \text{ N}}{45.0 \text{ N}} = 0.556$.

(b) Now let A be block A plus the cat, so $m_A = 9.18$ kg. $n_A = 90.0$ N and $f_k = \mu_k n = (0.556)(90.0 \text{ N}) = 50.0$ N. $\sum F_x = ma_x$ for A gives $T - f_k = m_A a_x$. $\sum F_y = ma_y$ for block B gives $m_B g - T = m_B a_y$. a_x for A equals a_y for B, so adding the two equations gives

$$m_B g - f_k = (m_A + m_B) a_y$$
 and $a_y = \frac{m_B g - f_k}{m_A + m_B} = \frac{25.0 \text{ N} - 50.0 \text{ N}}{9.18 \text{ kg} + 2.55 \text{ kg}} = -2.13 \text{ m/s}^2$. The acceleration is upward and block *B* slows down.

EVALUATE: The equation $m_B g - f_k = (m_A + m_B) a_y$ has a simple interpretation. If both blocks are considered together then there are two external forces: $m_B g$ that acts to move the system one way and f_k that acts oppositely. The net force of $m_B g - f_k$ must accelerate a total mass of $m_A + m_B$.

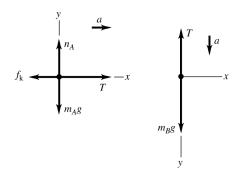


Figure 5.34

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5.35. IDENTIFY: Use $\Sigma \vec{F} = m\vec{a}$ to find the acceleration that can be given to the car by the kinetic friction force. Then use a constant acceleration equation.

SET UP: Take +x in the direction the car is moving.

EXECUTE: (a) The free-body diagram for the car is shown in Figure 5.35. $\Sigma F_v = ma_v$ gives n = mg.

$$\Sigma F_x = ma_x \text{ gives } -\mu_k n = ma_x. \quad -\mu_k mg = ma_x \text{ and } a_x = -\mu_k g. \text{ Then } v_x = 0 \text{ and } v_x^2 = v_{0x}^2 + 2a_x (x - x_0)$$
 gives $(x - x_0) = -\frac{v_{0x}^2}{2a_x} = +\frac{v_{0x}^2}{2\mu_k g} = \frac{(28.7 \text{ m/s})^2}{2(0.80)(9.80 \text{ m/s}^2)} = 52.5 \text{ m}.$

$$2a_x 2\mu_k g 2(0.80)(9.80 \text{ m/s}^2)$$
(b) $v_{0x} = \sqrt{2\mu_k g(x - x_0)} = \sqrt{2(0.25)(9.80 \text{ m/s}^2)52.5 \text{ m}} = 16.0 \text{ m/s}$

EVALUATE: For constant stopping distance $\frac{v_{0x}^2}{\mu_k}$ is constant and v_{0x} is proportional to $\sqrt{\mu_k}$. The

answer to part (b) can be calculated as $(28.7 \text{ m/s})\sqrt{0.25/0.80} = 16.0 \text{ m/s}$.

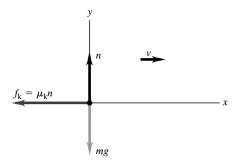


Figure 5.35

5.36. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the box. When the box is ready to slip the static friction force has its maximum possible value, $f_s = \mu_s n$.

SET UP: Use coordinates parallel and perpendicular to the ramp.

EXECUTE: (a) The normal force will be $w \cos \alpha$ and the component of the gravitational force along the ramp is $w \sin \alpha$. The box begins to slip when $w \sin \alpha > \mu_s w \cos \alpha$, or $\tan \alpha > \mu_s = 0.35$, so slipping occurs at $\alpha = \arctan(0.35) = 19.3^\circ$.

(b) When moving, the friction force along the ramp is $\mu_k w \cos \alpha$, the component of the gravitational force along the ramp is $w \sin \alpha$, so the acceleration is

$$(w\sin\alpha - w\mu_k\cos\alpha)/m = g(\sin\alpha - \mu_k\cos\alpha) = 0.92 \text{ m/s}^2.$$

(c) Since $v_{0x} = 0$, $2ax = v^2$, so $v = (2ax)^{1/2}$, or $v = [(2)(0.92 \text{ m/s}^2)(5 \text{ m})]^{1/2} = 3 \text{ m/s}$.

EVALUATE: When the box starts to move, friction changes from static to kinetic and the friction force becomes smaller.

5.37. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each crate. The rope exerts force *T* to the right on crate *A* and force *T* to the left on crate *B*. The target variables are the forces *T* and *F*. Constant *v* implies a = 0.

SET UP: The free-body diagram for *A* is sketched in Figure 5.37a.

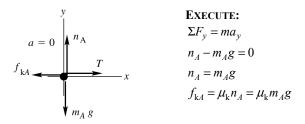


Figure 5.37a

$$\Sigma F_x = ma_x$$
$$T - f_{kA} = 0$$

$$T = \mu_k m_A g$$

SET UP: The free-body diagram for *B* is sketched in Figure 5.37b.

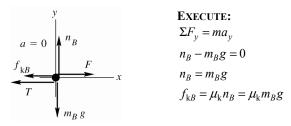


Figure 5.37b

$$\Sigma F_x = ma_x$$

$$F - T - f_{kB} = 0$$

$$F = T + \mu_k m_B g$$

Use the first equation to replace T in the second:

 $F = \mu_k m_A g + \mu_k m_B g.$

(a)
$$F = \mu_k (m_A + m_B) g$$

(b)
$$T = \mu_k m_4 g$$

EVALUATE: We can also consider both crates together as a single object of mass $(m_A + m_B)$.

 $\Sigma F_x = ma_x$ for this combined object gives $F = f_k = \mu_k (m_A + m_B)g$, in agreement with our answer in part (a).

5.38. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the box.

SET UP: Let +y be upward and +x be horizontal, in the direction of the acceleration. Constant speed means a = 0.

EXECUTE: (a) There is no net force in the vertical direction, so $n + F \sin \theta - w = 0$, or $n = w - F \sin \theta = mg - F \sin \theta$. The friction force is $f_k = \mu_k n = \mu_k (mg - F \sin \theta)$. The net horizontal force is $F \cos \theta - f_k = F \cos \theta - \mu_k (mg - F \sin \theta)$, and so at constant speed,

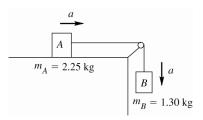
$$F = \frac{\mu_{\rm k} mg}{\cos \theta + \mu_{\rm k} \sin \theta}$$

(b) Using the given values,
$$F = \frac{(0.35)(90 \text{ kg})(9.80 \text{ m/s}^2)}{(\cos 25^\circ + (0.35) \sin 25^\circ)} = 290 \text{ N}.$$

EVALUATE: If $\theta = 0^{\circ}$, $F = \mu_k mg$.

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- **5.39. IDENTIFY:** Apply $\Sigma \vec{F} = m\vec{a}$ to each block. The target variables are the tension T in the cord and the acceleration a of the blocks. Then a can be used in a constant acceleration equation to find the speed of each block. The magnitude of the acceleration is the same for both blocks.
 - **SET UP:** The system is sketched in Figure 5.39a.



For each block take a positive coordinate direction to be the direction of the block's acceleration.

Figure 5.39a

Block on the table: The free-body is sketched in Figure 5.39b (next page).

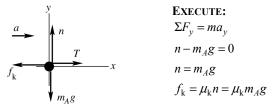


Figure 5.39b

$$\Sigma F_x = ma_x$$

$$T - f_k = m_A a$$

$$T - \mu_k m_A g = m_A a$$

SET UP: Hanging block: The free-body is sketched in Figure 5.39c.

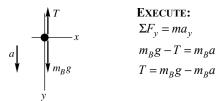


Figure 5.39c

(a) Use the second equation in the first

$$m_B g - m_B a - \mu_k m_A g = m_A a$$

$$(m_A + m_B) a = (m_B - \mu_k m_A) g$$

$$a = \frac{(m_B - \mu_k m_A) g}{m_A + m_B} = \frac{(1.30 \text{ kg} - (0.45)(2.25 \text{ kg}))(9.80 \text{ m/s}^2)}{2.25 \text{ kg} + 1.30 \text{ kg}} = 0.7937 \text{ m/s}^2$$

SET UP: Now use the constant acceleration equations to find the final speed. Note that the blocks have the same speeds. $x - x_0 = 0.0300 \text{ m}$, $a_x = 0.7937 \text{ m/s}^2$, $v_{0x} = 0$, $v_x = ?$

$$v_r^2 = v_{0r}^2 + 2a_r(x - x_0)$$

EXECUTE: $v_x = \sqrt{2a_x(x - x_0)} = \sqrt{2(0.7937 \text{ m/s}^2)(0.0300 \text{ m})} = 0.218 \text{ m/s} = 21.8 \text{ cm/s}.$

(b)
$$T = m_B g - m_B a = m_B (g - a) = 1.30 \text{ kg} (9.80 \text{ m/s}^2 - 0.7937 \text{ m/s}^2) = 11.7 \text{ N}$$

Or, to check, $T - \mu_k m_A g = m_A a$.

 $T = m_A(a + \mu_k g) = 2.25 \text{ kg}(0.7937 \text{ m/s}^2 + (0.45)(9.80 \text{ m/s}^2)) = 11.7 \text{ N}$, which checks.

EVALUATE: The force T exerted by the cord has the same value for each block. $T < m_B g$ since the hanging block accelerates downward. Also, $f_k = \mu_k m_A g = 9.92 \text{ N}$. $T > f_k$ and the block on the table accelerates in the direction of T.

5.40. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the ball. At the terminal speed, f = mg.

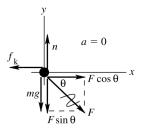
SET UP: The fluid resistance is directed opposite to the velocity of the object. At half the terminal speed, the magnitude of the frictional force is one-fourth the weight.

EXECUTE: (a) If the ball is moving up, the frictional force is down, so the magnitude of the net force is (5/4)w and the acceleration is (5/4)g, down.

(b) While moving down, the frictional force is up, and the magnitude of the net force is (3/4)w and the acceleration is (3/4)g, down.

EVALUATE: The frictional force is less than mg in each case and in each case the net force is downward and the acceleration is downward.

5.41. (a) IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the crate. Constant v implies a = 0. Crate moving says that the friction is kinetic friction. The target variable is the magnitude of the force applied by the woman. **SET UP:** The free-body diagram for the crate is sketched in Figure 5.41.



$\Sigma F_{y} = ma_{y}$ $n - mg - F \sin \theta = 0$ $n = mg + F \sin \theta$ $f_{k} = \mu_{k} n = \mu_{k} mg + \mu_{k} F \sin \theta$

Figure 5.41

$$\Sigma F_x = ma_x$$

$$F\cos\theta - f_k = 0$$

$$F\cos\theta - \mu_k mg - \mu_k F\sin\theta = 0$$

$$F(\cos\theta - \mu_k \sin\theta) = \mu_k mg$$

$$F = \frac{\mu_k mg}{\cos\theta - \mu_k \sin\theta}$$

(b) IDENTIFY and SET UP: "Start the crate moving" means the same force diagram as in part (a), except that μ_k is replaced by μ_s . Thus $F = \frac{\mu_s mg}{\cos \theta - \mu_s \sin \theta}$.

EXECUTE:
$$F \to \infty$$
 if $\cos \theta - \mu_s \sin \theta = 0$. This gives $\mu_s = \frac{\cos \theta}{\sin \theta} = \frac{1}{\tan \theta}$.

EVALUATE: \vec{F} has a downward component so n > mg. If $\theta = 0$ (woman pushes horizontally), n = mg and $F = f_k = \mu_k mg$.

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5.42. IDENTIFY: You are accelerated toward the center of the circle, so Newton's second law applies. Static friction is the force preventing you from sliding off the disk.

SET UP: $\sum F = m \frac{v^2}{R}$ applies to circular motion. Static friction is at its maximum in this case, so we can use $f_S = \mu_S n$, with n = mg. Our target variable is the time for one revolution.

EXECUTE: (a) The speed is $v = 2\pi R/T$, so $\sum F = m \frac{v^2}{R}$ becomes $f_S = m(2\pi R/T)^2/R$, which becomes

$$\mu_{\rm s} \, mg = m(4\pi^2 R/T^2)$$
. Solving for T gives $T = \sqrt{\frac{4\pi^2 R}{g\mu_{\rm s}}} = \sqrt{\frac{4\pi^2 (3.00 \text{ m})}{(9.80 \text{ m/s}^2)(0.400)}} = 5.50 \text{ s}.$

(b) Since $T = \sqrt{\frac{4\pi^2 R}{g\mu_s}}$, the period does not depend on the mass (or weight) of the person, so the answer

is the same: T = 5.50 s.

EVALUATE: In part (a) we could use the formula $a_{\text{rad}} = \frac{4\pi^2 R}{T^2}$ which leads to the same result.

5.43. IDENTIFY: Since the stone travels in a circular path, its acceleration is $a_{\text{rad}} = v^2/R$, directed toward the center of the circle. The only horizontal force on the stone is the tension of the string. Set the tension in the string equal to its maximum value.

SET UP:
$$\sum F_x = ma_x$$
 gives $T = m\frac{v^2}{R}$.

EXECUTE: (a) The free-body diagram for the stone is given in Figure 5.43 (next page). In the diagram the stone is at a point to the right of the center of the path.

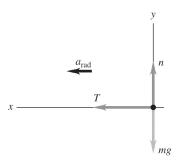


Figure 5.43

(b) Solving for *v* gives
$$v = \sqrt{\frac{TR}{m}} = \sqrt{\frac{(60.0 \text{ N})(0.90 \text{ m})}{0.80 \text{ kg}}} = 8.2 \text{ m/s}.$$

EVALUATE: The tension is directed toward the center of the circular path of the stone. Gravity plays no role in this case because it is a vertical force and the acceleration is horizontal.

5.44. IDENTIFY: The wrist exerts a force on the hand causing the hand to move in a horizontal circle. Newton's second law applies to the hand.

SET UP: Each hand travels in a circle of radius 0.750 m and has mass (0.0125)(52 kg) = 0.65 kg and weight 6.4 N. The period for each hand is T = (1.0 s)/(2.0) = 0.50 s. Let +x be toward the center of the

circular path. The speed of the hand is $v = 2\pi R/T$, the radial acceleration is $a_{\rm rad} = \frac{v^2}{R} = \frac{4\pi^2 R}{T^2}$, and

 $\sum F_x = ma_x = ma_{\rm rad}$.

EXECUTE: (a) The free-body diagram for one hand is given in Figure 5.44. \vec{F} is the force exerted on the hand by the wrist. This force has both horizontal and vertical components.

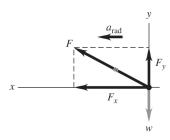


Figure 5.44

(b)
$$a_{\text{rad}} = \frac{4\pi^2 R}{T^2} = \frac{4\pi^2 (0.750 \text{ m})}{(0.50 \text{ s})^2} = 118 \text{ m/s}^2$$
, so $F_x = ma_{\text{rad}} = (0.65 \text{ kg})(118 \text{ m/s}^2) = 77 \text{ N}$.

(c)
$$\frac{F}{w} = \frac{77 \text{ N}}{6.4 \text{ N}} = 12$$
, so the horizontal force from the wrist is 12 times the weight of the hand.

EVALUATE: The wrist must also exert a vertical force on the hand equal to the weight of the hand.

5.45. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the car. It has acceleration \vec{a}_{rad} , directed toward the center of the circular path.

SET UP: The analysis is the same as in Example 5.23.

EXECUTE: **(a)**
$$F_A = m \left(g + \frac{v^2}{R} \right) = (1.60 \text{ kg}) \left(9.80 \text{ m/s}^2 + \frac{(12.0 \text{ m/s})^2}{5.00 \text{ m}} \right) = 61.8 \text{ N}.$$

(b)
$$F_B = m \left(g - \frac{v^2}{R} \right) = (1.60 \text{ kg}) \left(9.80 \text{ m/s}^2 - \frac{(12.0 \text{ m/s})^2}{5.00 \text{ m}} \right) = -30.4 \text{ N}, \text{ where the minus sign indicates}$$

that the track pushes down on the car. The magnitude of this force is 30.4 N.

EVALUATE:
$$|F_A| > |F_B|$$
. $|F_A| - 2mg = |F_B|$.

5.46. IDENTIFY: The acceleration of the car at the top and bottom is toward the center of the circle, and Newton's second law applies to it.

SET UP: Two forces are acting on the car, gravity and the normal force. At point B (the top), both forces are toward the center of the circle, so Newton's second law gives $mg + n_B = ma$. At point A (the bottom), gravity is downward but the normal force is upward, so $n_A - mg = ma$.

EXECUTE: Solving the equation at *B* for the acceleration gives

$$a = \frac{mg + n_B}{m} = \frac{(0.800 \text{ kg})(9.8 \text{ m/s}^2) + 6.00 \text{ N}}{0.800 \text{ kg}} = 17.3 \text{ m/s}^2.$$
 Solving the equation at A for the normal

force gives
$$n_A = m(g + a) = (0.800 \text{ kg})(9.8 \text{ m/s}^2 + 17.3 \text{ m/s}^2) = 21.7 \text{ N}.$$

EVALUATE: The normal force at the bottom is greater than at the top because it must balance the weight in addition to accelerating the car toward the center of its track.

5.47. IDENTIFY: A model car travels in a circle so it has radial acceleration, and Newton's second law applies to it.

SET UP: We use $\Sigma \vec{F} = m\vec{a}$, where the acceleration is $a_{\rm rad} = \frac{v^2}{R}$ and the time T for one revolution is $T = 2\pi R/v$.

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EXECUTE: At the bottom of the track, taking +y upward, $\Sigma \vec{F} = m\vec{a}$ gives n - mg = ma, where n is the normal force. This gives 2.50mg - mg = ma, so a = 1.50g. The acceleration is $a_{\text{rad}} = \frac{v^2}{R}$, so

$$v = \sqrt{aR} = \sqrt{(1.50)(9.80 \text{ m/s}^2)(5.00 \text{ m})} = 8.573 \text{ m/s}, \text{ so } T = 2\pi R/v = 2\pi (5.00 \text{ m})/(8.573 \text{ m}) = 3.66 \text{ s}.$$

EVALUATE: We never need the mass of the car because we know the acceleration as a fraction of g and the force as a fraction of mg.

5.48. IDENTIFY: Since the car travels in an arc of a circle, it has acceleration $a_{\rm rad} = v^2/R$, directed toward the center of the arc. The only horizontal force on the car is the static friction force exerted by the roadway. To calculate the minimum coefficient of friction that is required, set the static friction force equal to its maximum value, $f_{\rm s} = \mu_{\rm s} n$. Friction is static friction because the car is not sliding in the radial direction.

SET UP: The free-body diagram for the car is given in Figure 5.48 (next page). The diagram assumes the center of the curve is to the left of the car.

EXECUTE: (a) $\Sigma F_y = ma_y$ gives n = mg. $\Sigma F_x = ma_x$ gives $\mu_s n = m \frac{v^2}{R}$. $\mu_s mg = m \frac{v^2}{R}$ and

$$\mu_{\rm s} = \frac{v^2}{gR} = \frac{(25.0 \text{ m/s})^2}{(9.80 \text{ m/s}^2)(170 \text{ m})} = 0.375$$

(b)
$$\frac{v^2}{\mu_s} = Rg = \text{constant}$$
, so $\frac{v_1^2}{\mu_{s1}} = \frac{v_2^2}{\mu_{s2}}$. $v_2 = v_1 \sqrt{\frac{\mu_{s2}}{\mu_{s1}}} = (25.0 \text{ m/s}) \sqrt{\frac{\mu_{s1}/3}{\mu_{s1}}} = 14.4 \text{ m/s}$.

EVALUATE: A smaller coefficient of friction means a smaller maximum friction force, a smaller possible acceleration and therefore a smaller speed.

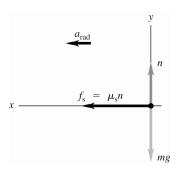


Figure 5.48

5.49. IDENTIFY: Apply Newton's second law to the car in circular motion, assume friction is negligible. **SET UP:** The acceleration of the car is $a_{\text{rad}} = v^2/R$. As shown in the text, the banking angle β is given by $\tan \beta = \frac{v^2}{gR}$. Also, $n = mg/\cos \beta$. 65.0 mi/h = 29.1 m/s.

EXECUTE: (a) $\tan \beta = \frac{(29.1 \text{ m/s})^2}{(9.80 \text{ m/s}^2)(225 \text{ m})}$ and $\beta = 21.0^\circ$. The expression for $\tan \beta$ does not involve

the mass of the vehicle, so the truck and car should travel at the same speed.

(b) For the car,
$$n_{\text{car}} = \frac{(1125 \text{ kg})(9.80 \text{ m/s}^2)}{\cos 21.0^{\circ}} = 1.18 \times 10^4 \text{ N}$$
 and $n_{\text{truck}} = 2n_{\text{car}} = 2.36 \times 10^4 \text{ N}$, since $m_{\text{truck}} = 2m_{\text{car}}$.

EVALUATE: The vertical component of the normal force must equal the weight of the vehicle, so the normal force is proportional to *m*.

5.50. IDENTIFY: The acceleration of the person is $a_{\text{rad}} = v^2/R$, directed horizontally to the left in the figure in the problem. The time for one revolution is the period $T = \frac{2\pi R}{v}$. Apply $\Sigma \vec{F} = m\vec{a}$ to the person.

SET UP: The person moves in a circle of radius $R = 3.00 \text{ m} + (5.00 \text{ m}) \sin 30.0^{\circ} = 5.50 \text{ m}$. The free-body diagram is given in Figure 5.50. \vec{F} is the force applied to the seat by the rod.

EXECUTE: (a)
$$\Sigma F_y = ma_y$$
 gives $F \cos 30.0^\circ = mg$ and $F = \frac{mg}{\cos 30.0^\circ}$. $\Sigma F_x = ma_x$ gives

 $F \sin 30.0^{\circ} = m \frac{v^2}{R}$. Combining these two equations gives

$$v = \sqrt{Rg \tan \theta} = \sqrt{(5.50 \text{ m})(9.80 \text{ m/s}^2) \tan 30.0^\circ} = 5.58 \text{ m/s}$$
. Then the period is

$$T = \frac{2\pi R}{v} = \frac{2\pi (5.50 \text{ m})}{5.58 \text{ m/s}} = 6.19 \text{ s}.$$

(b) The net force is proportional to m so in $\Sigma \vec{F} = m\vec{a}$ the mass divides out and the angle for a given rate of rotation is independent of the mass of the passengers.

EVALUATE: The person moves in a horizontal circle so the acceleration is horizontal. The net inward force required for circular motion is produced by a component of the force exerted on the seat by the rod.

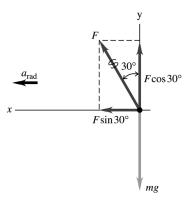


Figure 5.50

5.51. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the composite object of the person plus seat. This object moves in a horizontal circle and has acceleration $a_{\rm rad}$, directed toward the center of the circle.

SET UP: The free-body diagram for the composite object is given in Figure 5.51. Let +x be to the right, in the direction of $\vec{a}_{\rm rad}$. Let +y be upward. The radius of the circular path is R = 7.50 m. The total mass is $(255 \text{ N} + 825 \text{ N})/(9.80 \text{ m/s}^2) = 110.2 \text{ kg}$. Since the rotation rate is

28.0 rev/min = 0.4667 rev/s, the period *T* is
$$\frac{1}{0.4667 \text{ rev/s}} = 2.143 \text{ s.}$$

EXECUTE:
$$\Sigma F_y = ma_y$$
 gives $T_A \cos 40.0^\circ - mg = 0$ and $T_A = \frac{mg}{\cos 40.0^\circ} = \frac{255 \text{ N} + 825 \text{ N}}{\cos 40.0^\circ} = 1410 \text{ N}.$

 $\Sigma F_x = ma_x$ gives $T_A \sin 40.0^\circ + T_B = ma_{\text{rad}}$ and

$$T_B = m \frac{4\pi^2 R}{T^2} - T_A \sin 40.0^\circ = (110.2 \text{ kg}) \frac{4\pi^2 (7.50 \text{ m})}{(2.143 \text{ s})^2} - (1410 \text{ N}) \sin 40.0^\circ = 6200 \text{ N}$$

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The tension in the horizontal cable is 6200 N and the tension in the other cable is 1410 N.

EVALUATE: The weight of the composite object is 1080 N. The tension in cable A is larger than this since its vertical component must equal the weight. The tension in cable B is less than $ma_{\rm rad}$ because part of the required inward force comes from a component of the tension in cable A.

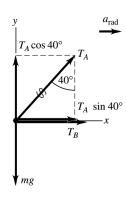


Figure 5.51

5.52. IDENTIFY: Newton's second law applies to the steel ball. Gravity and the tension in the rope are the forces acting on it.

SET UP:
$$\sum F = m \frac{v^2}{R}$$

EXECUTE: (a) At the lowest point, the tension T is upward and the weight w = mg is downward.

$$\sum F = m \frac{v^2}{R}$$
 gives $T - mg = ma$, which becomes $3mg - mg = \frac{mv^2}{R}$. Solving for v gives $v = \sqrt{2Rg} = \sqrt{2(15.0 \text{ m})(9.80 \text{ m/s}^2)} = 17.1 \text{ m/s}.$

(b) If
$$T = mg$$
, the vertical forces balance, so $\sum F = m \frac{v^2}{R} = 0$, which tells us that the speed is zero.

EVALUATE: If T = mg, the ball is just hanging by the rope.

5.53. IDENTIFY: The acceleration due to circular motion is $a_{\text{rad}} = \frac{4\pi^2 R}{T^2}$.

SET UP: R = 400 m. 1/T is the number of revolutions per second.

EXECUTE: (a) Setting $a_{\text{rad}} = g$ and solving for the period T gives

$$T = 2\pi \sqrt{\frac{R}{g}} = 2\pi \sqrt{\frac{400 \text{ m}}{9.80 \text{ m/s}^2}} = 40.1 \text{ s},$$

so the number of revolutions per minute is (60 s/min)/(40.1 s) = 1.5 rev/min.

(b) The lower acceleration corresponds to a longer period, and hence a lower rotation rate, by a factor of the square root of the ratio of the accelerations, $T' = (1.5 \text{ rev/min}) \times \sqrt{3.70/9.8} = 0.92 \text{ rev/min}$.

EVALUATE: In part (a) the tangential speed of a point at the rim is given by $a_{\text{rad}} = \frac{v^2}{R}$, so

 $v = \sqrt{Ra_{\text{rad}}} = \sqrt{Rg} = 62.6 \text{ m/s}$; the space station is rotating rapidly.

5.54. IDENTIFY: $T = \frac{2\pi R}{v}$. The apparent weight of a person is the normal force exerted on him by the seat

he is sitting on. His acceleration is $a_{rad} = v^2/R$, directed toward the center of the circle.

SET UP: The period is T = 60.0 s. The passenger has mass m = w/g = 90.0 kg.

EXECUTE: (a)
$$v = \frac{2\pi R}{T} = \frac{2\pi (50.0 \text{ m})}{60.0 \text{ s}} = 5.24 \text{ m/s}. \text{ Note that } a_{\text{rad}} = \frac{v^2}{R} = \frac{(5.24 \text{ m/s})^2}{50.0 \text{ m}} = 0.549 \text{ m/s}^2.$$

(b) The free-body diagram for the person at the top of his path is given in Figure 5.54a. The acceleration is downward, so take +y downward. $\Sigma F_v = ma_v$ gives $mg - n = ma_{rad}$.

$$n = m(g - a_{rad}) = (90.0 \text{ kg})(9.80 \text{ m/s}^2 - 0.549 \text{ m/s}^2) = 833 \text{ N}.$$

The free-body diagram for the person at the bottom of his path is given in Figure 5.54b. The acceleration is upward, so take +y upward. $\Sigma F_y = ma_y$ gives $n - mg = ma_{\rm rad}$ and $n = m(g + a_{\rm rad}) = 931$ N.

- (c) Apparent weight = 0 means n = 0 and $mg = ma_{rad}$. $g = \frac{v^2}{R}$ and $v = \sqrt{gR} = 22.1$ m/s. The time for one revolution would be $T = \frac{2\pi R}{v} = \frac{2\pi (50.0 \text{ m})}{22.1 \text{ m/s}} = 14.2 \text{ s.}$ Note that $a_{rad} = g$.
- (d) $n = m(g + a_{rad}) = 2mg = 2(882 \text{ N}) = 1760 \text{ N}$, twice his true weight.

EVALUATE: At the top of his path his apparent weight is less than his true weight and at the bottom of his path his apparent weight is greater than his true weight.

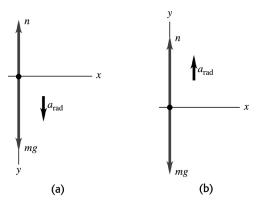


Figure 5.54

5.55. IDENTIFY: Newton's second law applies to the rock moving in a vertical circle of radius *L*. Gravity and the tension in the string are the forces acting on it.

SET UP:
$$\sum F = m \frac{v^2}{R}$$
, where $R = L$ in this case.

EXECUTE: (a) Apply $\sum F = m \frac{v^2}{R}$ at the top of the circle. Both gravity and the tension act downward, so $T + mg = mv^2/L$. The smallest that T can be is zero, in which case $mg = mv^2/L$, so $v = \sqrt{Lg}$.

(b) In this case,
$$v = 2\sqrt{Lg}$$
. $\sum F = m\frac{v^2}{R}$ gives $T - mg = \frac{mv^2}{L} = \frac{m(2\sqrt{Lg})^2}{L} = 4mg$, so $T = 5mg$.

EVALUATE: Note in (a) that the rock does *not stop* at the top of the circle. If it did, it would just fall down and not complete the rest of the circle.

5.56. IDENTIFY: $a_{\text{rad}} = v^2/R$, directed toward the center of the circular path. At the bottom of the dive, \vec{a}_{rad} is upward. The apparent weight of the pilot is the normal force exerted on her by the seat on which she is sitting.

SET UP: The free-body diagram for the pilot is given in Figure 5.56.

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EXECUTE: **(a)**
$$a_{\text{rad}} = \frac{v^2}{R}$$
 gives $R = \frac{v^2}{a_{\text{rad}}} = \frac{(95.0 \text{ m/s})^2}{4.00(9.80 \text{ m/s}^2)} = 230 \text{ m}.$

(b)
$$\Sigma F_v = ma_v$$
 gives $n - mg = ma_{\text{rad}}$.

$$n = m(g + a_{rad}) = m(g + 4.00g) = 5.00mg = (5.00)(50.0 \text{ kg})(9.80 \text{ m/s}^2) = 2450 \text{ N}$$

EVALUATE: Her apparent weight is five times her true weight, the force of gravity the earth exerts on her

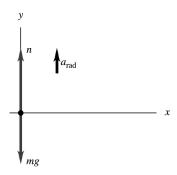
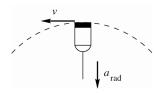


Figure 5.56

5.57. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the water. The water moves in a vertical circle. The target variable is the speed v; we will calculate $a_{\rm rad}$ and then get v from $a_{\rm rad} = v^2/R$.

SET UP: Consider the free-body diagram for the water when the pail is at the top of its circular path, as shown in Figures 5.57a and b.



The radial acceleration is in toward the center of the circle so at this point is downward. *n* is the downward normal force exerted on the water by the bottom of the pail.

Figure 5.57a

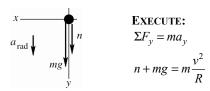


Figure 5.57b

At the minimum speed the water is just ready to lose contact with the bottom of the pail, so at this speed, $n \to 0$. (Note that the force *n* cannot be upward.)

With
$$n \to 0$$
 the equation becomes $mg = m\frac{v^2}{R}$. $v = \sqrt{gR} = \sqrt{(9.80 \text{ m/s}^2)(0.600 \text{ m})} = 2.42 \text{ m/s}$.

EVALUATE: At the minimum speed $a_{\text{rad}} = g$. If v is less than this minimum speed, gravity pulls the water (and bucket) out of the circular path.

- **5.58. IDENTIFY:** The ball has acceleration $a_{\text{rad}} = v^2 / R$, directed toward the center of the circular path. When the ball is at the bottom of the swing, its acceleration is upward.
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SET UP: Take +y upward, in the direction of the acceleration. The bowling ball has mass m = w/g = 7.27 kg.

EXECUTE: **(a)**
$$a_{\text{rad}} = \frac{v^2}{R} = \frac{(4.20 \text{ m/s})^2}{3.80 \text{ m}} = 4.64 \text{ m/s}, \text{ upward.}$$

(b) The free-body diagram is given in Figure 5.58. $\Sigma F_y = ma_y$ gives $T - mg = ma_{\rm rad}$.

$$T = m(g + a_{\text{rad}}) = (7.27 \text{ kg})(9.80 \text{ m/s}^2 + 4.64 \text{ m/s}^2) = 105 \text{ N}$$

EVALUATE: The acceleration is upward, so the net force is upward and the tension is greater than the weight.

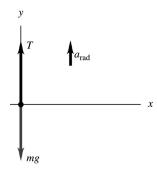


Figure 5.58

5.59. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the knot.

SET UP: a = 0. Use coordinates with axes that are horizontal and vertical.

EXECUTE: (a) The free-body diagram for the knot is sketched in Figure 5.59.

 T_1 is more vertical so supports more of the weight and is larger. You can also see this from $\Sigma F_x = ma_x$: $T_2 \cos 40^\circ - T_1 \cos 60^\circ = 0$. $T_2 \cos 40^\circ - T_1 \cos 60^\circ = 0$.

(b)
$$T_1$$
 is larger so set $T_1 = 5000$ N. Then $T_2 = T_1/1.532 = 3263.5$ N. $\Sigma F_y = ma_y$ gives $T_1 \sin 60^\circ + T_2 \sin 40^\circ = w$ and $w = 6400$ N.

EVALUATE: The sum of the vertical components of the two tensions equals the weight of the suspended object. The sum of the tensions is greater than the weight.

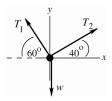
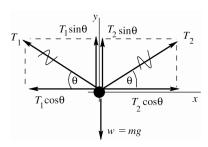


Figure 5.59

5.60. IDENTIFY: Apply Newton's first law to the person. Each half of the rope exerts a force on him, directed along the rope and equal to the tension *T* in the rope.

SET UP: (a) The force diagram for the person is given in Figure 5.60.

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 T_1 and T_2 are the tensions in each half of the rope.

Figure 5.60

EXECUTE: $\Sigma F_x = 0$

 $T_2 \cos \theta - T_1 \cos \theta = 0$

This says that $T_1 = T_2 = T$ (The tension is the same on both sides of the person.)

 $\Sigma F_v = 0$

 $T_1 \sin \theta + T_2 \sin \theta - mg = 0$

But $T_1 = T_2 = T$, so $2T \sin \theta = mg$

$$T = \frac{mg}{2\sin\theta} = \frac{(90.0 \text{ kg})(9.80 \text{ m/s}^2)}{2\sin 10.0^\circ} = 2540 \text{ N}$$

(b) The relation $2T \sin \theta = mg$ still applies but now we are given that $T = 2.50 \times 10^4$ N (the breaking strength) and are asked to find θ .

$$\sin \theta = \frac{mg}{2T} = \frac{(90.0 \text{ kg})(9.80 \text{ m/s}^2)}{2(2.50 \times 10^4 \text{ N})} = 0.01764, \ \theta = 1.01^\circ.$$

EVALUATE: $T = mg/(2\sin\theta)$ says that T = mg/2 when $\theta = 90^{\circ}$ (rope is vertical).

 $T \to \infty$ when $\theta \to 0$ since the upward component of the tension becomes a smaller fraction of the tension.

5.61. IDENTIFY: The engine is hanging at rest, so its acceleration is zero which means that the forces on it must balance. We balance horizontal components and vertical components.

SET UP: In addition to the tensions in the four cables shown in the text, gravity also acts on the engine. Call +x horizontally to the right and +y vertically upward, and call θ the angle that cable C makes with cable D. The mass of the engine is 409 kg and the tension T_A in cable A is 722 N.

EXECUTE: The tension in cable *D* is the only force balancing gravity on the engine, so $T_D = mg$. In the *x*-direction, we have $T_A = T_C \sin \theta$, which gives $T_C = T_A/\sin \theta = (722 \text{ N})/(\sin 37.1^\circ) = 1197 \text{ N}$. In the *y*-direction, we have $T_B - T_D - T_C \cos \theta = 0$, which gives $T_B = (409 \text{ kg})(9.80 \text{ m/s}^2) + (1197 \text{ N})\cos(37.1^\circ) = 4963 \text{ N}$. Rounding to 3 significant figures gives $T_B = 4960 \text{ N}$ and $T_C = 1200 \text{ N}$.

EVALUATE: The tension in cable B is greater than the weight of the engine because cable C has a downward component that B must also balance.

5.62. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each object. Constant speed means a = 0.

SET UP: The free-body diagrams are sketched in Figure 5.62. T_1 is the tension in the lower chain, T_2 is the tension in the upper chain and T = F is the tension in the rope.

EXECUTE: The tension in the lower chain balances the weight and so is equal to w. The lower pulley must have no net force on it, so twice the tension in the rope must be equal to w and the tension in the rope, which equals F, is w/2. Then, the downward force on the upper pulley due to the rope is also w, and so the upper chain exerts a force w on the upper pulley, and the tension in the upper chain is also w. **EVALUATE:** The pulley combination allows the worker to lift a weight w by applying a force of only w/2.

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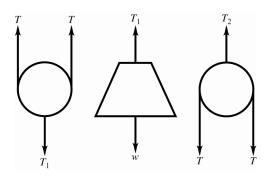


Figure 5.62

5.63. IDENTIFY: Newton's second law applies to the block. Gravity, kinetic friction, and the normal force due to the board act upon it.

SET UP: Apply $\sum F_x = ma_x$ and $\sum F_y = 0$ to the block. Choose the +x-axis along the surface of the board pointing downward. At the maximum angle α_0 just before slipping, $\tan \alpha_0 = \mu_s = 0.600$, so $\alpha_0 = 30.96^\circ$. Fig. 5.63 shows a free-body diagram of the block after it has slipped.

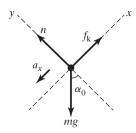


Figure 5.63

EXECUTE: First find the acceleration using Newton's laws. $\sum F_y = 0$ gives $n = mg \cos \alpha_0$ $\sum F_x = ma_x$ gives

 $mg \sin \alpha_0 - f_k = ma_x$

 $mg \sin \alpha_0 - \mu_k mg \cos \alpha_0 = ma_x$

 $a_x = g(\sin \alpha_0 - \mu_k \cos \alpha_0) = (9.80 \text{ m/s}^2)[\sin 30.96^\circ - (0.400) \cos 30.96^\circ] = 1.681 \text{ m/s}^2$. Now use $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ to find the speed at the bottom of the board.

$$v_x^2 = 0 + 2(1.681 \text{ m/s}^2)(3.00 \text{ m}) \rightarrow v_x = 3.18 \text{ m/s}.$$

EVALUATE: We chose the $\pm x$ -axis to be downward because that is the direction of the acceleration. In most cases, it is easiest to make that choice if the direction of the acceleration is known.

5.64. IDENTIFY: Apply Newton's first law to the ball. Treat the ball as a particle.

SET UP: The forces on the ball are gravity, the tension in the wire and the normal force exerted by the surface. The normal force is perpendicular to the surface of the ramp. Use *x*- and *y*-axes that are horizontal and vertical.

EXECUTE: (a) The free-body diagram for the ball is given in Figure 5.64 (next page). The normal force has been replaced by its x and y components.

(b)
$$\Sigma F_y = 0$$
 gives $n \cos 35.0^\circ - w = 0$ and $n = \frac{mg}{\cos 35.0^\circ} = 1.22 mg$.

(c)
$$\Sigma F_x = 0$$
 gives $T - n\sin 35.0^\circ = 0$ and $T = (1.22mg)\sin 35.0^\circ = 0.700mg$.

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EVALUATE: Note that the normal force is greater than the weight, and increases without limit as the angle of the ramp increases toward 90°. The tension in the wire is $w \tan \phi$, where ϕ is the angle of the ramp and T also increases without limit as $\phi \to 90^\circ$.

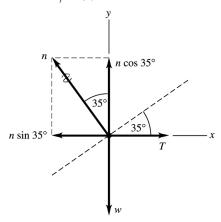


Figure 5.64

5.65. IDENTIFY: Newton's second law applies to the accelerating box. The forces acting on it are the force F, gravity, the normal force due to the surface, and kinetic friction.

SET UP: Apply $\sum F_y = 0$ and $\sum F_x = ma_x$. Fig. 5.65 shows a free-body diagram of the box. Choose the +x-axis in the direction of the acceleration.

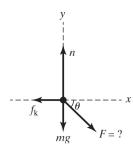


Figure 5.65

EXECUTE: (a) We want to find the magnitude of the force F. First use $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ to find a_x .

$$(6.00 \text{ m/s})^2 = 0 + 2a_x(8.00 \text{ m}) \rightarrow a_x = 2.250 \text{ m/s}^2.$$

Now apply $\sum F_x = ma_x$: $F \cos \theta - f_k = ma_x$

We also have $f_k = \mu_k n$

Apply $\sum F_v = 0 : n - mg - F \sin \theta = 0$

Combine these three results and solve for F: $F = \frac{m(a_x + \mu_k g)}{\cos \theta - \mu_k \sin \theta}$. Using m = 12.0 kg, $a_x = 2.250$ m/s²,

 $\mu_{\rm k} = 0.300$, and $\theta = 37.0^{\circ}$, we get F = 101 N.

- **(b)** If $f_k = 0$, we have $F \cos \theta = ma_x \rightarrow F \cos 37.0^\circ = (12.0 \text{ kg})(2.250 \text{ m/s}^2) \rightarrow F = 33.8 \text{ N}.$
- (c) If F is horizontal, $\theta = 0^{\circ}$, n = mg, and $f_k = \mu_k mg$, so $F = m(a_x + \mu_k g) = 62.3 \text{ N}$.

EVALUATE: We see that *F* is least when there is no friction and greatest when it has a downward component. These results are reasonable since a downward component increases the normal force which increases friction. And the fact that it has a downward component means that there is less horizontal component to cause acceleration.

5.66. IDENTIFY: In each rough patch, the kinetic friction (and hence the acceleration) is constant, but the constants are different in the two patches. Newton's second law applies, as well as the constant-acceleration kinematics formulas in each patch.

SET UP: Choose the +y-axis upward and the +x-axis in the direction of the velocity.

EXECUTE: (a) Find the velocity and time when the box is at x = 2.00 m. Newton's second law tells us that n = mg and $-f_k = ma_x$ which gives $-\mu_k mg = ma_x$; $a_x = -\mu_k g = -(0.200)(9.80 \text{ m/s}^2) = -1.96 \text{ m/s}^2$. Now use the kinematics equations involving v_x . Using $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ we get

$$v_x = \sqrt{(4.00 \text{ m/s})^2 + 2(-1.96 \text{ m/s}^2)(2.00 \text{ m})} = 2.857 \text{ m/s}$$
. Now solve the equation $v_x = v_{0x} + a_x t$ for t to get $t = (2.857 \text{ m/s} - 4.00 \text{ m/s})/(-1.96 \text{ m/s}^2) = 0.5834 \text{ s}$.

Now look at the motion in the section for which $\mu_k = 0.400$: $a_x = -(0.400)(9.80 \text{ m/s}^2) = -3.92 \text{ m/s}^2$, $v_x = 0$, $v_{0x} = 2.857 \text{ m/s}$. Solving $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ for $x - x_0$ gives $x - x_0 = -(2.857 \text{ m/s})^2/[2(-3.92 \text{ m/s}^2)] = 1.041 \text{ m}$.

The box is at the point x = 2.00 m + 1.041 m = 3.04 m.

Solving $v_x = v_{0x} + a_x t$ for t gives $t = (-2.857 \text{ m/s})/(-3.92 \text{ m/s}^2) = 0.7288 \text{ s}$. The total time is 0.5834 s + 0.7288 s = 1.31 s.

EVALUATE: We cannot do this problem in a single process because the acceleration, although constant in each patch, is different in the two patches.

5.67. IDENTIFY: Kinematics will give us the acceleration of the person, and Newton's second law will give us the force (the target variable) that his arms exert on the rest of his body.

SET UP: Let the person's weight be W, so W = 680 N. Assume constant acceleration during the speeding up motion and assume that the body moves upward 15 cm in 0.50 s while speeding up. The constant-acceleration kinematics formula $y - y_0 = v_{0y}t + \frac{1}{2}a_yt^2$ and $\Sigma F_y = ma_y$ apply. The free-body diagram for the person is given in Figure 5.67. F is the force exerted on him by his arms.

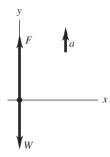


Figure 5.67

EXECUTE:
$$v_{0y} = 0$$
, $y - y_0 = 0.15$ m, $t = 0.50$ s. $y - y_0 = v_{0y}t + \frac{1}{2}a_yt^2$ gives $a_y = \frac{2(y - y_0)}{t^2} = \frac{2(0.15 \text{ m})}{(0.50 \text{ s})^2} = 1.2 \text{ m/s}^2$. $\Sigma F_y = ma_y$ gives $F - W = ma$. $m = \frac{W}{g}$, so $F = W \left(1 + \frac{a}{g} \right) = 1.12W = 762 \text{ N}$.

EVALUATE: The force is greater than his weight, which it must be if he is to accelerate upward.

5.68. IDENTIFY: The force is time-dependent, so the acceleration is not constant. Therefore we must use calculus instead of the standard kinematics formulas. Newton's second law applies.

SET UP: The acceleration is the time derivative of the velocity and $\Sigma F_v = ma_v$.

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EXECUTE: Differentiating the velocity gives $a_y = dv_y/dt = 2.00 \text{ m/s}^2 + (1.20 \text{ m/s}^3)t$. Find the time when $v_y = 9.00 \text{ m/s}$: $9.00 \text{ m/s} = (2.00 \text{ m/s}^2)t + (0.600 \text{ m/s}^3)t^2$. Solving this quadratic for t and taking the positive value gives t = 2.549 s. At this time the acceleration is $a = 2.00 \text{ m/s}^2 + (1.20 \text{ m/s}^3)(2.549 \text{ s}) = 5.059 \text{ m/s}^2$.

Now apply Newton's second law to the box, calling T the tension in the rope: T - mg = ma, which gives $T = m(g + a) = (2.00 \text{ kg})(9.80 \text{ m/s}^2 + 5.059 \text{ m/s}^2) = 29.7 \text{ N}.$

EVALUATE: The tension is greater than the weight of the box, which it must be to accelerate the box upward. As time goes on, the acceleration, and hence the tension, would increase.

5.69. IDENTIFY: We know the forces on the box and want to find information about its position and velocity. Newton's second law will give us the box's acceleration.

SET UP: $a_y(t) = \frac{\sum F_y}{m}$. We can integrate the acceleration to find the velocity and the velocity to find the

position. At an altitude of several hundred meters, the acceleration due to gravity is essentially the same as it is at the earth's surface.

EXECUTE: Let +y be upward. Newton's second law gives $T - mg = ma_y$, so

 $a_v(t) = (12.0 \text{ m/s}^3)t - 9.8 \text{ m/s}^2$. Integrating the acceleration gives $v_v(t) = (6.00 \text{ m/s}^3)t^2 - (9.8 \text{ m/s}^2)t$.

- (a) (i) At t = 1.00 s, $v_v = -3.80$ m/s. (ii) At t = 3.00 s, $v_v = 24.6$ m/s.
- **(b)** Integrating the velocity gives $y y_0 = (2.00 \text{ m/s}^3)t^3 (4.9 \text{ m/s}^2)t^2$. $v_y = 0$ at t = 1.63 s. At t = 1.63 s, $y y_0 = 8.71 \text{ m} 13.07 \text{ m} = -4.36 \text{ m}$.
- (c) Setting $y y_0 = 0$ and solving for t gives t = 2.45 s.

EVALUATE: The box accelerates and initially moves downward until the tension exceeds the weight of the box. Once the tension exceeds the weight, the box will begin to accelerate upward and will eventually move upward, as we saw in part (b).

5.70. IDENTIFY: We can use the standard kinematics formulas because the force (and hence the acceleration) is constant, and we can use Newton's second law to find the force needed to cause that acceleration. Kinetic friction, not static friction, is acting.

SET UP: From kinematics, we have $x - x_0 = v_{0x}t + \frac{1}{2}a_xt^2$ and $\Sigma F_x = ma_x$ applies. Forces perpendicular to the ramp balance. The force of kinetic friction is $f_k = \mu_k mg \cos \theta$.

EXECUTE: Call $\pm x$ upward along the surface of the ramp. Kinematics gives

$$a_x = \frac{2(x - x_0)}{t^2} = \frac{2(8.00 \text{ m})}{(6.00 \text{ s})^2} = 0.4444 \text{ m/s}^2$$
. $\Sigma F_x = ma_x$ gives $F - mg\sin\theta - \mu_k mg\cos\theta = ma_x$. Solving

for F and putting in the numbers for this problem gives

$$F = m(a_x + g\sin\theta + \mu_k mg\cos\theta) = (5.00 \text{ kg})(0.4444 \text{ m/s}^2 + 4.9 \text{ m/s}^2 + 3.395 \text{ m/s}^2) = 43.7 \text{ N}.$$

EVALUTE: As long as the box is moving, only kinetic friction, not static friction, acts on it. The force is less than the weight of the box because only part of the box's weight acts down the ramp. We should also investigate if the force is great enough to start the box moving in the first place. In that case, static friction would have it maximum value, so $f_s = \mu_s n$. The force F in this would be $F = \mu_s mg\cos(30^\circ) + mg\sin(30^\circ) = mg(\mu_s\cos30^\circ + \sin30^\circ) = (5.00 \text{ kg})(9.80 \text{ m/s}^2)[(0.43)(\cos30^\circ) + \sin30^\circ] = 42.7 \text{ N}$. Since the force we found is 43.7 N, it is great enough to overcome static friction and cause the box to move.

5.71. IDENTIFY: Newton's second law applies to the accelerating crate. The forces acting on it are the vertical force \vec{F} , gravity, the normal force due to the surface, and kinetic friction. SET UP: Apply $\sum F_x = ma_x$. Fig. 5.71 shows a free-body diagram of the crate. Choose the +x-axis in the direction of the acceleration, which is down the surface of the ramp. Call α the angle the ramp makes above the horizontal. We want to find the magnitude of \vec{F} that will give the crate an acceleration of 9.8 m/s² down the ramp.

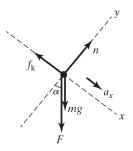


Figure 5.71

EXECUTE: First apply $\sum F_x = ma_x$ without the force \vec{F} and then apply it with \vec{F} . Without \vec{F} the normal force is $n = mg \cos \alpha$ and with \vec{F} it is $n = (mg + F)\cos \alpha$.

Without the force: $mg \sin \alpha - \mu_k mg \cos \alpha = ma_1$.

With the force: $(mg + F)\sin \alpha - \mu_k (mg + F)\cos \alpha = ma_2$.

We know that $a_2/a_1 = (9.80 \text{ m/s}^2)/(4.9 \text{ m/s}^2) = 2$, so take the ratio of the equations, giving $\frac{a_2}{a_1} = \frac{(mg+F)\sin\alpha - \mu_k(mg+F)\cos\alpha}{mg\sin\alpha - \mu_k mg\cos\alpha} = \frac{(mg+F)(\sin\alpha - \mu_k\cos\alpha)}{mg(\sin\alpha - \mu_k\cos\alpha)} = \frac{mg+F}{mg} = 2$. Solving for F

gives $F = mg = (25.0 \text{ kg})(9.80 \text{ m/s}^2) = 245 \text{ N}$. The force F is equal to the weight of the crate.

EVALUATE: The addition of the force F doubles the acceleration of the crate. Since F and mg are both downward, we need twice the force to double the acceleration, which tells us that F must be equal to the weight. So our result is reasonable. The addition of F = mg effectively doubles the weight without changing the mass, so it doubles the acceleration.

5.72. IDENTIFY: The forces acting on the crate are the force *F*, gravity, the normal force due to the floor, and static friction. The crate is at rest, so the forces on it must balance. The crate is just ready to slide, so static friction force is a maximum.

SET UP: Apply $\sum F_x = 0$ and $\sum F_y = 0$. Fig. 5.72 shows a free-body diagram of the box. Choose the +x-axis horizontally to the right. At its maximum, $f_S = \mu_S n$. We want to find the mass m of the crate.

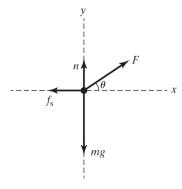


Figure 5.72

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EXECUTE:
$$\sum F_x = 0$$
: $F \cos \theta - f_S = F \cos \theta - \mu_S n = 0$

$$\sum F_{v} = 0: F \sin \theta + n - mg = 0$$

Combine these two equations and solve for m: $m = \frac{F(\cos\theta + \mu_s \sin\theta)}{\mu_s g}$. Using $F = 380 \text{ N}, \ \theta = 30.0^\circ$,

and $\mu_{\rm s} = 0.400$ gives m = 103 kg.

EVALUATE: If the crate were not just ready to slide, we could *not* use $f_S = \mu_S n$.

5.73. IDENTIFY: Newton's second law applies to the box.

SET UP: $f_k = \mu_k n$, $\Sigma F_x = ma_x$, and $\Sigma F_y = ma_y$ apply to the box. Take the +x-axis down the surface of the ramp and the +y-axis perpendicular to the surface upward.

EXECUTE: $\Sigma F_y = ma_y$ gives $n + F\sin(33.0^\circ) - mg\cos(33.0^\circ) = 0$, which gives n = 51.59 N. The friction force is $f_k = \mu_k n = (0.300)(51.59 \text{ N}) = 15.48$ N. Parallel to the surface we have $\Sigma F_x = ma_x$ which gives $F\cos(33.0^\circ) + mg\sin(33.0^\circ) - f_k = ma$, which gives $a = 6.129 \text{ m/s}^2$. Finally the velocity formula gives us $v_x = v_{0x} + a_x t = 0 + (6.129 \text{ m/s}^2)(2.00 \text{ s}) = 12.3 \text{ m/s}$.

EVALUATE: Even though F is horizontal and mg is vertical, it is best to choose the axes as we have done, rather than horizontal-vertical, because the acceleration is then in the x-direction. Taking x and y to be horizontal-vertical would give the acceleration x- and y-components, which would complicate the solution.

5.74. IDENTIFY: This is a system having constant acceleration, so we can use the standard kinematics formulas as well as Newton's second law to find the unknown mass m_2 .

SET UP: Newton's second law applies to each block. The standard kinematics formulas can be used to find the acceleration because the acceleration is constant. The normal force on m_1 is $m_1 g \cos \alpha$, so the force of friction on it is $f_k = \mu_k m_1 g \cos \alpha$.

EXECUTE: Standard kinematics gives the acceleration of the system to be

$$a_y = \frac{2(y - y_0)}{t^2} = \frac{2(12.0 \text{ m})}{(3.00 \text{ s})^2} = 2.667 \text{ m/s}^2$$
. For m_1 , $n = m_1 g \cos \alpha = 117.7 \text{ N}$, so the friction force on m_1

is $f_k = (0.40)(117.7 \text{ N}) = 47.08 \text{ N}$. Applying Newton's second law to m_1 gives

 $T - f_k - m_1 g \sin \alpha = m_1 a$, where T is the tension in the cord. Solving for T gives

 $T = f_k + m_1 g \sin \alpha + m_1 a = 47.08 \text{ N} + 156.7 \text{ N} + 53.34 \text{ N} = 257.1 \text{ N}$. Newton's second law for m_2 gives

$$m_2g - T = m_2a$$
, so $m_2 = \frac{T}{g - a} = \frac{257.1 \text{ N}}{9.8 \text{ m/s}^2 - 2.667 \text{ m/s}^2} = 36.0 \text{ kg}.$

EVALUATE: We could treat these blocks as a two-block system. Newton's second law would then give $m_2g - m_1g \sin \alpha - \mu_k m_1g \cos \alpha = (m_1 + m_2)a$, which gives the same result as above.

5.75. IDENTIFY: Newton's second law applies, as do the constant-acceleration kinematics equations.

SET UP: Call the +x-axis horizontal and to the right and the +y-axis vertically upward. $\Sigma F_y = ma_y$ and $\Sigma F_x = ma_x$ both apply to the book.

EXECUTE: The book has no horizontal motion, so $\Sigma F_x = ma_x = 0$, which gives us the normal force n: $n = F\cos(60.0^\circ)$. The kinetic friction force is $f_k = \mu_k n = (0.300)(96.0 \text{ N})(\cos 60.0^\circ) = 14.4 \text{ N}$. In the vertical direction, we have $\Sigma F_y = ma_y$, which gives $F\sin(60.0^\circ) - mg - f_k = ma$. Solving for a gives us $a = [(96.0 \text{ N})(\sin 60.0^\circ) - 49.0 \text{ N} - 14.4 \text{ N}]/(5.00 \text{ kg}) = 3.948 \text{ m/s}^2 \text{ upward}$. Now the velocity formula $v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$ gives $v_y = \sqrt{2(3.948 \text{ m/s}^2)(0.400 \text{ m})} = 1.78 \text{ m/s}$.

EVALUATE: Only the upward component of the force F makes the book accelerate upward, while the horizontal component of T is the magnitude of the normal force.

- **5.76. IDENTIFY:** The system is in equilibrium. Apply Newton's first law to block *A*, to the hanging weight and to the knot where the cords meet. Target variables are the two forces.
 - (a) **SET UP:** The free-body diagram for the hanging block is given in Figure 5.76a.

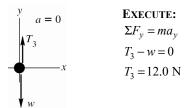


Figure 5.76a

SET UP: The free-body diagram for the knot is given in Figure 5.76b.

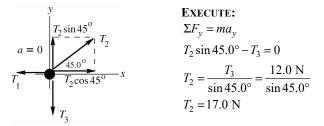


Figure 5.76b

$$\Sigma F_x = ma_x$$

 $T_2 \cos 45.0^{\circ} - T_1 = 0$
 $T_1 = T_2 \cos 45.0^{\circ} = 12.0 \text{ N}$

SET UP: The free-body diagram for block A is given in Figure 5.76c.

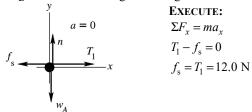


Figure 5.76c

EVALUATE: Also can apply $\Sigma F_y = ma_y$ to this block:

$$n - w_A = 0$$
$$n = w_A = 60.0 \text{ N}$$

Then $\mu_s n = (0.25)(60.0 \text{ N}) = 15.0 \text{ N}$; this is the maximum possible value for the static friction force. We see that $f_s < \mu_s n$; for this value of w the static friction force can hold the blocks in place.

(b) SET UP: We have all the same free-body diagrams and force equations as in part (a) but now the static friction force has its largest possible value, $f_s = \mu_s n = 15.0 \text{ N}$. Then $T_1 = f_s = 15.0 \text{ N}$.

EXECUTE: From the equations for the forces on the knot

$$T_2 \cos 45.0^\circ - T_1 = 0$$
 implies $T_2 = T_1 / \cos 45.0^\circ = \frac{15.0 \text{ N}}{\cos 45.0^\circ} = 21.2 \text{ N}$

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 $T_2 \sin 45.0^\circ - T_3 = 0$ implies $T_3 = T_2 \sin 45.0^\circ = (21.2 \text{ N}) \sin 45.0^\circ = 15.0 \text{ N}$

And finally $T_3 - w = 0$ implies $w = T_3 = 15.0$ N.

EVALUATE: Compared to part (a), the friction is larger in part (b) by a factor of (15.0/12.0) and w is larger by this same ratio.

5.77. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each block.

SET UP: Constant speed means a = 0. When the blocks are moving, the friction force is f_k and when they are at rest, the friction force is f_s .

EXECUTE: (a) The tension in the cord must be m_2g in order that the hanging block move at constant speed. This tension must overcome friction and the component of the gravitational force along the incline, so $m_2g = (m_1g\sin\alpha + \mu_km_1g\cos\alpha)$ and $m_2 = m_1(\sin\alpha + \mu_k\cos\alpha)$.

- (b) In this case, the friction force acts in the same direction as the tension on the block of mass m_1 , so $m_2 g = (m_1 g \sin \alpha \mu_k m_1 g \cos \alpha)$, or $m_2 = m_1 (\sin \alpha \mu_k \cos \alpha)$.
- (c) Similar to the analysis of parts (a) and (b), the largest m_2 could be is $m_1(\sin\alpha + \mu_s\cos\alpha)$ and the smallest m_2 could be is $m_1(\sin\alpha \mu_s\cos\alpha)$.

EVALUATE: In parts (a) and (b) the friction force changes direction when the direction of the motion of m_1 changes. In part (c), for the largest m_2 the static friction force on m_1 is directed down the incline and for the smallest m_2 the static friction force on m_1 is directed up the incline.

5.78. IDENTIFY: The net force at any time is $F_{\text{net}} = ma$.

SET UP: At t = 0, a = 62g. The maximum acceleration is 140g at t = 1.2 ms.

EXECUTE: (a) $F_{\text{net}} = ma = 62mg = 62(210 \times 10^{-9} \text{ kg})(9.80 \text{ m/s}^2) = 1.3 \times 10^{-4} \text{ N}$. This force is 62 times the flea's weight.

- **(b)** $F_{\text{net}} = 140 mg = 2.9 \times 10^{-4} \text{ N}$, at t = 1.2 ms.
- (c) Since the initial speed is zero, the maximum speed is the area under the $a_x t$ graph. This gives 1.2 m/s.

EVALUATE: a is much larger than g and the net external force is much larger than the flea's weight.

5.79. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each block. Use Newton's third law to relate forces on *A* and on *B*. **SET UP:** Constant speed means a = 0.

EXECUTE: (a) Treat A and B as a single object of weight $w = w_A + w_B = 1.20 \text{ N} + 3.60 \text{ N} = 4.80 \text{ N}$. The free-body diagram for this combined object is given in Figure 5.79a. $\Sigma F_y = ma_y$ gives n = w = 4.80 N. $f_k = \mu_k n = (0.300)(4.80 \text{ N}) = 1.44 \text{ N}$. $\Sigma F_x = ma_x$ gives $F = f_k = 1.44 \text{ N}$.

(b) The free-body force diagrams for blocks A and B are given in Figure 5.79b. n and f_k are the normal and friction forces applied to block B by the tabletop and are the same as in part (a). f_{kB} is the friction force that A applies to B. It is to the right because the force from A opposes the motion of B. n_B is the downward force that A exerts on B. f_{kA} is the friction force that B applies to A. It is to the left because block B wants A to move with it. n_A is the normal force that block B exerts on A. By Newton's third law, $f_{kB} = f_{kA}$ and these forces are in opposite directions. Also, $n_A = n_B$ and these forces are in opposite directions.

 $\Sigma F_v = ma_v$ for block A gives $n_A = w_A = 1.20 \text{ N}$, so $n_B = 1.20 \text{ N}$.

 $f_{kA} = \mu_k n_A = (0.300)(1.20 \text{ N}) = 0.360 \text{ N}$, and $f_{kB} = 0.360 \text{ N}$.

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 $\Sigma F_x = ma_x$ for block A gives $T = f_{kA} = 0.360 \text{ N}.$

 $\Sigma F_r = ma_r$ for block B gives $F = f_{kR} + f_k = 0.360 \text{ N} + 1.44 \text{ N} = 1.80 \text{ N}.$

EVALUATE: In part (a) block A is at rest with respect to B and it has zero acceleration. There is no horizontal force on A besides friction, and the friction force on A is zero. A larger force F is needed in part (b), because of the friction force between the two blocks.

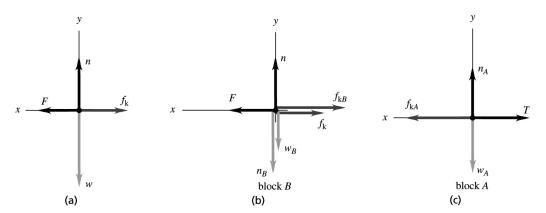


Figure 5.79

5.80. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the passenger to find the maximum allowed acceleration. Then use a constant acceleration equation to find the maximum speed.

SET UP: The free-body diagram for the passenger is given in Figure 5.80.

EXECUTE: $\Sigma F_y = ma_y$ gives n - mg = ma. n = 1.6mg, so $a = 0.60g = 5.88 \text{ m/s}^2$.

$$y - y_0 = 3.0 \text{ m}, a_v = 5.88 \text{ m/s}^2, v_{0v} = 0 \text{ so } v_v^2 = v_{0v}^2 + 2a_v(y - y_0) \text{ gives } v_v = 5.9 \text{ m/s}.$$

EVALUATE: A larger final speed would require a larger value of a_y , which would mean a larger normal force on the person.

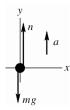


Figure 5.80

5.81. IDENTIFY: a = dv/dt. Apply $\Sigma \vec{F} = m\vec{a}$ to yourself.

SET UP: The reading of the scale is equal to the normal force the scale applies to you.

EXECUTE: The elevator's acceleration is $a = \frac{dv(t)}{dt} = 3.0 \text{ m/s}^2 + 2(0.20 \text{ m/s}^3)t = 3.0 \text{ m/s}^2 + (0.40 \text{ m/s}^3)t.$

At t = 4.0 s, $a = 3.0 \text{ m/s}^2 + (0.40 \text{ m/s}^3)(4.0 \text{ s}) = 4.6 \text{ m/s}^2$. From Newton's second law, the net force on you is $F_{\text{net}} = F_{\text{scale}} - w = ma$ and $F_{\text{scale}} = w + ma = (64 \text{ kg})(9.8 \text{ m/s}^2) + (64 \text{ kg})(4.6 \text{ m/s}^2) = 920 \text{ N}$.

EVALUATE: a increases with time, so the scale reading is increasing.

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5.82. IDENTIFY: The blocks are moving together with the same acceleration, so Newton's second law applies to each of them.

SET UP: For block A take the +x-axis horizontally to the right, and for B take the +y-axis vertically downward. Our choice for B has two advantages: it is in the direction of the acceleration of B and a positive acceleration of A gives a positive acceleration of B. Both blocks have the same acceleration, which we shall simply call a. $\sum F = ma$ applies to both blocks. We want to find the tension T in the rope and the coefficient of kinetic friction μ_k between A and the tabletop.

EXECUTE: (a) We know the speed of A and the distance it moved, so use $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ to find its horizontal acceleration. $(3.30 \text{ m/s})^2 = 0 + 2a(2.00 \text{ m})$, so $a = 2.7225 \text{ m/s}^2$. Now look at B to find the

tension.
$$\sum F_y = ma_y$$
 gives $w_B - T = m_B a = (w_B/g)a$. Solving for T gives $T = w_B \left(1 - \frac{a}{g}\right) = ma_B a$

$$(25.0 \text{ N}) \left(1 - \frac{2.7225 \text{ m/s}^2}{9.80 \text{ m/s}^2} \right) = 18.1 \text{ N}.$$

Now look at block A. Balancing vertical forces tells us that $n = w_A$. The friction force is $f_k = \mu_k n = \mu_k w_A$. $\sum F_x = ma_x$ gives $T - f_k = m_A a \rightarrow T - \mu_k w_A = (w_A/g)a$. Solving for μ_k gives $\mu_k = \frac{T - (w_A/g)a}{w_A}$. Using $w_A = 45.0$ N, a = 2.7225 m/s², and T = 18.1 N gives $\mu_k = 0.123$.

EVALUATE: According to Table 5.1 in the text, 0.123 is not an unreasonable coefficient of kinetic friction.

5.83. IDENTIFY: The blocks move together with the same acceleration. Newton's second law applies to each of them. The forces acting on each block are gravity downward the upward tension in the rope. **SET UP:** $\sum F_y = ma_y$ applies to each block. The heavier block accelerates downward while the lighter one accelerates upward, both with acceleration a. Call the +y-axis downward for the heavier block and upward for the lighter block. We want to find the mass of each block.

EXECUTE: Heavier block: First find the acceleration using $y = y_0 + v_{0y}t + \frac{1}{2}a_yt^2$, which gives us $y = v_0 + v_{0y}t + \frac{1}{2}a_yt^2$

$$\frac{1}{2}at^2$$
, so 5.00 m = $\frac{1}{2}a(2.00 \text{ s})^2$ \rightarrow $a = 2.50 \text{ m/s}^2$. Now apply $\sum F_y = ma_y$ to this block, which

gives
$$m_2g - T = m_2a$$
. Now olve for m_2 : $m_2 = \frac{T}{g - a} = \frac{16.0 \text{ N}}{9.80 \text{ m/s}^2 - 2.50 \text{ m/s}^2} = 2.19 \text{ kg}.$

Lighter block:
$$\sum F_y = ma_y$$
 gives $T - m_1g = m_1a$, so $m_1 = \frac{T}{a+g} = 1.30$ kg.

EVALUATE: As a check, consider the two blocks as a singe system The only external force causing the acceleration is $m_2g - m_1g$, so $\sum F_y = ma_y$ gives $m_2g - m_1g = (m_1 + m_2)a$. Solving for a using our results for the two masses gives a = 2.50 m/s², which agrees with our result.

5.84. IDENTIFY: Apply Newton's first law to the rope. Let m_1 be the mass of that part of the rope that is on the table, and let m_2 be the mass of that part of the rope that is hanging over the edge. $(m_1 + m_2 = m,$ the total mass of the rope). Since the mass of the rope is not being neglected, the tension in the rope varies along the length of the rope. Let T be the tension in the rope at that point that is at the edge of the table.

SET UP: The free-body diagram for the hanging section of the rope is given in Figure 5.84a.

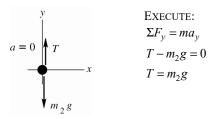


Figure 5.84a

SET UP: The free-body diagram for that part of the rope that is on the table is given in Figure 5.84b.

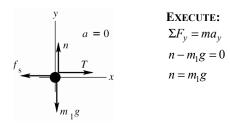


Figure 5.84b

When the maximum amount of rope hangs over the edge the static friction has its maximum value:

$$f_s = \mu_s n = \mu_s m_1 g$$

a
$$\Sigma F_x = ma_x$$

$$T - f_s = 0$$

$$T = \mu_{\rm s} m_1 g$$

Use the first equation to replace *T*:

$$m_2g = \mu_s m_1g$$

$$m_2 = \mu_s m_1$$

The fraction that hangs over is $\frac{m_2}{m} = \frac{\mu_s m_1}{m_1 + \mu_s m_1} = \frac{\mu_s}{1 + \mu_s}$.

EVALUATE: As $\mu_s \to 0$, the fraction goes to zero and as $\mu_s \to \infty$, the fraction goes to unity.

5.85. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the point where the three wires join and also to one of the balls. By symmetry the tension in each of the 35.0 cm wires is the same.

SET UP: The geometry of the situation is sketched in Figure 5.85a. The angle ϕ that each wire makes with the vertical is given by $\sin \phi = \frac{12.5 \text{ cm}}{47.5 \text{ cm}}$ and $\phi = 15.26^{\circ}$. Let T_A be the tension in the vertical wire and let T_B be the tension in each of the other two wires. Neglect the weight of the wires. The free-body diagram for the left-hand ball is given in Figure 5.85b and for the point where the wires join in Figure

5.85c. *n* is the force one ball exerts on the other. **EXECUTE:** (a) $\Sigma F_v = ma_v$ applied to the ball gives $T_B \cos \phi - mg = 0$.

$$T_B = \frac{mg}{\cos \phi} = \frac{(15.0 \text{ kg})(9.80 \text{ m/s}^2)}{\cos 15.26^\circ} = 152 \text{ N}. \text{ Then } \Sigma F_y = ma_y \text{ applied in Figure 5.85c gives}$$

$$T_A - 2T_B \cos \phi = 0$$
 and $T_A = 2(152 \text{ N}) \cos \phi = 249 \text{ N}.$

(b) $\Sigma F_x = ma_x$ applied to the ball gives $n - T_B \sin \phi = 0$ and $n = (152 \text{ N}) \sin 15.26^\circ = 40.0 \text{ N}$.

EVALUATE: T_A equals the total weight of the two balls.

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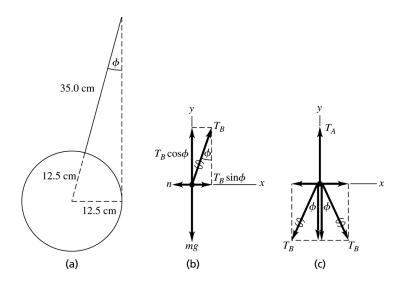


Figure 5.85

5.86. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the car to calculate its acceleration. Then use a constant acceleration equation to find the initial speed.

SET UP: Let +x be in the direction of the car's initial velocity. The friction force f_k is then in the -x-direction. 192 ft = 58.52 m.

EXECUTE: n = mg and $f_k = \mu_k mg$. $\Sigma F_x = ma_x$ gives $-\mu_k mg = ma_x$ and $a_x = -\mu_k g = -(0.750)(9.80 \text{ m/s}^2) = -7.35 \text{ m/s}^2$. $v_x = 0$ (stops), $x - x_0 = 58.52 \text{ m}$. $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ gives $v_{0x} = \sqrt{-2a_x(x - x_0)} = \sqrt{-2(-7.35 \text{ m/s}^2)(58.52 \text{ m})} = 29.3 \text{ m/s} = 65.5 \text{ mi/h}$. He was guilty.

EVALUATE: $x - x_0 = \frac{v_x^2 - v_{0x}^2}{2a_x} = -\frac{v_{0x}^2}{2a_x}$. If his initial speed had been 45 mi/h he would have stopped in $\left(\frac{45 \text{ mi/h}}{65.5 \text{ mi/h}}\right)^2 (192 \text{ ft}) = 91 \text{ ft.}$

5.87. IDENTIFY: Apply $-\left(\frac{M+m}{M}\right)\tan\alpha$ to each block. Forces between the blocks are related by Newton's

third law. The target variable is the force F. Block B is pulled to the left at constant speed, so block A moves to the right at constant speed and a = 0 for each block.

SET UP: The free-body diagram for block A is given in Figure 5.87a. n_{BA} is the normal force that B exerts on A. $f_{BA} = \mu_k n_{BA}$ is the kinetic friction force that B exerts on A. Block A moves to the right relative to B, and f_{BA} opposes this motion, so f_{BA} is to the left. Note also that F acts just on B, not on A.

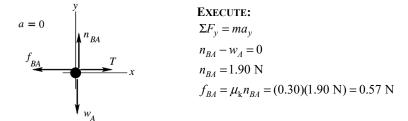


Figure 5.87a

$$\Sigma F_x = ma_x$$
. $T - f_{BA} = 0$. $T = f_{BA} = 0.57$ N.

SET UP: The free-body diagram for block *B* is given in Figure 5.87b.

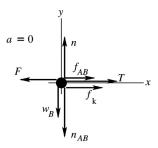


Figure 5.87b

EXECUTE: n_{AB} is the normal force that block A exerts on block B. By Newton's third law n_{AB} and n_{BA} are equal in magnitude and opposite in direction, so $n_{AB} = 1.90$ N. f_{AB} is the kinetic friction force that A exerts on B. Block B moves to the left relative to A and f_{AB} opposes this motion, so f_{AB} is to the right. $f_{AB} = \mu_k n_{AB} = (0.30)(1.90 \text{ N}) = 0.57 \text{ N}$. n and f_k are the normal and friction force exerted by the floor on block B; $f_k = \mu_k n$. Note that block B moves to the left relative to the floor and f_k opposes this motion, so f_k is to the right.

$$\Sigma F_y = ma_y$$
: $n - w_B - n_{AB} = 0$. $n = w_B + n_{AB} = 4.20 \text{ N} + 1.90 \text{ N} = 6.10 \text{ N}$. Then $f_k = \mu_k n = (0.30)(6.10 \text{ N}) = 1.83 \text{ N}$. $\Sigma F_x = ma_x$: $f_{AB} + T + f_k - F = 0$. $F = T + f_{AB} + f_k = 0.57 \text{ N} + 0.57 \text{ N} + 1.83 \text{ N} = 3.0 \text{ N}$.

EVALUATE: Note that f_{AB} and f_{BA} are a third law action-reaction pair, so they must be equal in magnitude and opposite in direction and this is indeed what our calculation gives.

5.88. IDENTIFY: Both blocks accelerate together. The force *P* accelerates the two-block system, but only static friction accelerates block *B*. Newton's second law applies to each block as well as the entire system.

SET UP: When P is the largest, block A is just ready to slide over block B so static friction is at its maximum, which is $f_S = \mu_s n$. Apply $\sum F_x = ma_x$. We want the largest value of P for which the blocks move together.

EXECUTE: <u>Isolate A</u>: $n = m_A g$ and $f_S = \mu_S m_A g$. $\sum F_x = m a_x$ gives $P - \mu_S m_A g = m_A a_x$. We need a_x . <u>Treat the two blocks as a single system</u>: $\sum F_x = m a_x$ gives $P = (m_A + m_B)a_x$. Now solve for a_x to get $a_x = P/(m_A + m_B)$.

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Now use this value of a_x in the equation for block A, giving $P - \mu_s m_A g = m_A \left(\frac{P}{m_A + m_B} \right)$. Solving for P

and using $m_A = 2.00$ kg, $m_B = 5.00$ kg, and $\mu_s = 0.400$ gives P = 11.0 N.

EVALUATE: If *P* were to exceed 11.0 N, slipping would occur, the friction force would be kinetic friction, and the blocks would not have the same acceleration.

5.89. IDENTIFY: Apply $-\left(\frac{M+m}{M}\right)\tan\alpha$ to each block. Parts (a) and (b) will be done together.

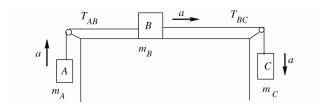


Figure 5.89a

Note that each block has the same magnitude of acceleration, but in different directions. For each block let the direction of \vec{a} be a positive coordinate direction.

SET UP: The free-body diagram for block *A* is given in Figure 5.89b.

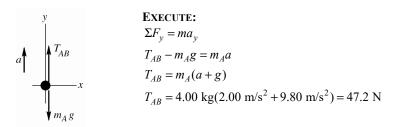


Figure 5.89b

SET UP: The free-body diagram for block *B* is given in Figure 5.89c.

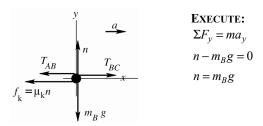


Figure 5.89c

$$f_k = \mu_k n = \mu_k m_B g = (0.25)(12.0 \text{ kg})(9.80 \text{ m/s}^2) = 29.4 \text{ N}$$

$$\Sigma F_x = ma_x$$

$$T_{BC} - T_{AB} - f_k = m_B a$$

$$T_{BC} = T_{AB} + f_k + m_B a = 47.2 \text{ N} + 29.4 \text{ N} + (12.0 \text{ kg})(2.00 \text{ m/s}^2)$$

$$T_{BC} = 100.6 \text{ N}$$

SET UP: The free-body diagram for block *C* is sketched in Figure 5.89d (next page).

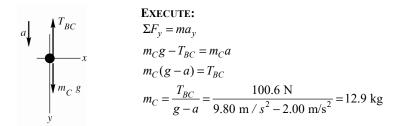


Figure 5.89d

EVALUATE: If all three blocks are considered together as a single object and $-\left(\frac{M+m}{M}\right)\tan\alpha$ is applied to this combined object, $m_Cg-m_Ag-\mu_km_Bg=(m_A+m_B+m_C)a$. Using the values for μ_k , m_A and m_B given in the problem and the mass m_C we calculated, this equation gives a=2.00 m/s², which checks.

5.90. IDENTIFY: Apply $-\left(\frac{M+m}{M}\right)\tan\alpha$ to each block. They have the same magnitude of acceleration, a.

SET UP: Consider positive accelerations to be to the right (up and to the right for the left-hand block, down and to the right for the right-hand block).

EXECUTE: (a) The forces along the inclines and the accelerations are related by $T - (100 \text{ kg})g \sin 30.0^\circ = (100 \text{ kg})a$ and $(50 \text{ kg})g \sin 53.1^\circ - T = (50 \text{ kg})a$, where T is the tension in the cord and a the mutual magnitude of acceleration. Adding these relations, $(50 \text{ kg} \sin 53.1^\circ - 100 \text{ kg} \sin 30.0^\circ)g = (50 \text{ kg} + 100 \text{ kg})a$, or a = -0.067g. Since a comes out negative,

the blocks will slide to the left; the 100-kg block will slide down. Of course, if coordinates had been chosen so that positive accelerations were to the left, a would be +0.067g.

(b)
$$a = 0.067(9.80 \text{ m/s}^2) = 0.658 \text{ m/s}^2$$
.

(c) Substituting the value of a (including the proper sign, depending on choice of coordinates) into either of the above relations involving T yields 424 N.

EVALUATE: For part (a) we could have compared $mg \sin \theta$ for each block to determine which direction the system would move.

5.91. IDENTIFY: Let the tensions in the ropes be T_1 and T_2 .

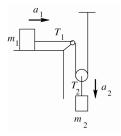


Figure 5.91a

Consider the forces on each block. In each case take a positive coordinate direction in the direction of the acceleration of that block.

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SET UP: The free-body diagram for m_1 is given in Figure 5.91b.

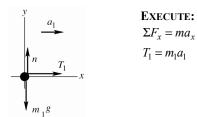


Figure 5.91b

SET UP: The free-body diagram for m_2 is given in Figure 5.91c.

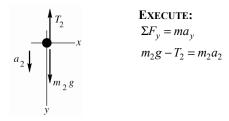


Figure 5.91c

This gives us two equations, but there are four unknowns $(T_1, T_2, a_1 \text{ and } a_2)$ so two more equations are required.

SET UP: The free-body diagram for the moveable pulley (mass *m*) is given in Figure 5.91d.

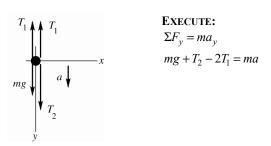


Figure 5.91d

But our pulleys have negligible mass, so mg = ma = 0 and $T_2 = 2T_1$. Combine these three equations to eliminate T_1 and T_2 : $m_2g - T_2 = m_2a_2$ gives $m_2g - 2T_1 = m_2a_2$. And then with $T_1 = m_1a_1$ we have $m_2g - 2m_1a_1 = m_2a_2$.

SET UP: There are still two unknowns, a_1 and a_2 . But the accelerations a_1 and a_2 are related. In any time interval, if m_1 moves to the right a distance d, then in the same time m_2 moves downward a distance d/2. One of the constant acceleration kinematic equations says $x - x_0 = v_{0x}t + \frac{1}{2}a_xt^2$, so if m_2 moves half the distance it must have half the acceleration of m_1 : $a_2 = a_1/2$, or $a_1 = 2a_2$.

EXECUTE: This is the additional equation we need. Use it in the previous equation and get $m_2g - 2m_1(2a_2) = m_2a_2$.

$$a_2(4m_1+m_2)=m_2g$$

$$a_2 = \frac{m_2 g}{4m_1 + m_2}$$
 and $a_1 = 2a_2 = \frac{2m_2 g}{4m_1 + m_2}$.

EVALUATE: If $m_2 \to 0$ or $m_1 \to \infty$, $a_1 = a_2 = 0$. If $m_2 \gg m_1$, $a_2 = g$ and $a_1 = 2g$.

5.92. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to block B, to block A and B as a composite object, and to block C. If A and B slide together all three blocks have the same magnitude of acceleration.

SET UP: If A and B don't slip, the friction between them is static. The free-body diagrams for block B, for blocks A and B, and for C are given in Figure 5.92. Block C accelerates downward and A and B accelerate to the right. In each case take a positive coordinate direction to be in the direction of the acceleration. Since block A moves to the right, the friction force f_s on block B is to the right, to prevent relative motion between the two blocks. When C has its largest mass, f_s has its largest value: $f_s = \mu_s n$.

EXECUTE: $\Sigma F_x = ma_x$ applied to the block B gives $f_s = m_B a$. $n = m_B g$ and $f_s = \mu_s m_B g$. $\mu_s m_B g = m_B a$ and $a = \mu_s g$. $\Sigma F_x = ma_x$ applied to blocks A + B gives $T = m_{AB} a = m_{AB} \mu_s g$. $\Sigma F_y = ma_y$ applied to block C gives $m_C g - T = m_C a$. $m_C g - m_{AB} \mu_s g = m_C \mu_s g$.

$$m_C = \frac{m_{AB}\mu_s}{1 - \mu_s} = (5.00 \text{ kg} + 8.00 \text{ kg}) \left(\frac{0.750}{1 - 0.750}\right) = 39.0 \text{ kg}.$$

EVALUATE: With no friction from the tabletop, the system accelerates no matter how small the mass of C is. If m_C is less than 39.0 kg, the friction force that A exerts on B is less than $\mu_s n$. If m_C is greater than 39.0 kg, blocks C and A have a larger acceleration than friction can give to block B, and A accelerates out from under B.

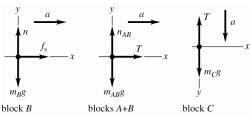


Figure 5.92

5.93. IDENTIFY: Both blocks accelerate together. The force *F* accelerates the two-block system, and the blocks exert kinetic friction forces on each other. Newton's second law applies to each block as well as the entire system.

SET UP: We apply $\sum F_x = ma_x$ and $\sum F_y = 0$ to each block. Block A accelerates to the right and B accelerates to the left. Call the direction of acceleration the +x-direction in each case, and call each acceleration a. Fig. 5.93 shows free-body diagrams of each block. It is important to realize two things immediately: the normal force that A exerts on B is equal and opposite to the normal force that B exerts on A, and the blocks exert equal but opposite friction forces on each other. Both of these points are due to Newton's third law (action-reaction). We want to find the tension in the cord and the coefficient of kinetic friction between A and B.

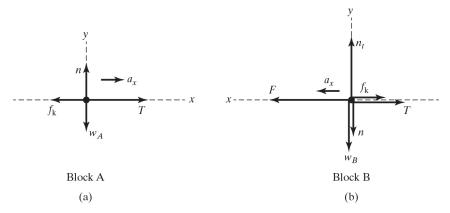


Figure 5.93

EXECUTE: (a) & (b) Isolate block A: Call n the normal force that the blocks exert on each other and f_k the kinetic friction force they exert on each other. From Fig. 5.93a, $\sum F_v = 0$ gives $n = w_A$ and

$$\sum F_x = ma_x$$
 gives $T - f_k = m_A a$, which becomes $T - \mu_k w_A = m_A a$. (Eq. 1)

<u>Isolate block B</u>: Call n_t the normal force due to the table. From Fig. 5.93b wee see that $\sum F_x = ma_x$ gives $T + f_k - F = m_B a$, which becomes $F - T - \mu_k w_A = m_B a$. (Eq. 2)

Combining Eq. 1 and Eq. 2 and solve for μ_k gives $F - 2 \mu_k w_A = (m_A + m_B)a$. Solving for μ_k gives

$$\mu_{\rm k} = \frac{F - (m_A + m_B)a}{2m_A g}$$
. Using the given masses, force, and acceleration gives $\mu_{\rm k} = 0.242$.

Now use Eq. 1 (or Eq. 2) to find T: $T = m_A a + \mu_k m_A g = 7.75 \text{ N}$.

EVALUATE: The tension is less than the force F, which is reasonable because B could never accelerate if T were greater than F. Also, from Table 5.1 we see that 0.242 is a reasonable coefficient of kinetic friction.

5.94. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the box.

SET UP: The box has an upward acceleration of $a = 1.90 \text{ m/s}^2$.

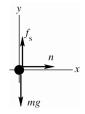
EXECUTE: The floor exerts an upward force n on the box, obtained from n - mg = ma, or n = m(a + g). The friction force that needs to be balanced is

$$\mu_k n = \mu_k m(a+g) = (0.32)(36.0 \text{ kg})(1.90 \text{ m/s}^2 + 9.80 \text{ m/s}^2) = 135 \text{ N}.$$

EVALUATE: If the elevator were not accelerating the normal force would be n = mg and the friction force that would have to be overcome would be 113 N. The upward acceleration increases the normal force and that increases the friction force.

5.95. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the block. The cart and the block have the same acceleration. The normal force exerted by the cart on the block is perpendicular to the front of the cart, so is horizontal and to the right. The friction force on the block is directed so as to hold the block up against the downward pull of gravity. We want to calculate the minimum a required, so take static friction to have its maximum value, $f_s = \mu_s n$.

SET UP: The free-body diagram for the block is given in Figure 5.95.



EXECUTE:

$$\Sigma F_x = ma_x$$

 $n = ma$
 $f_s = \mu_s n = \mu_s ma$

Figure 5.95

$$\Sigma F_y = ma_y: f_s - mg = 0$$

$$\mu_s ma = mg, \text{ so } a = g/\mu_s.$$

EVALUATE: An observer on the cart sees the block pinned there, with no reason for a horizontal force on it because the block is at rest relative to the cart. Therefore, such an observer concludes that n = 0and thus $f_s = 0$, and he doesn't understand what holds the block up against the downward force of gravity. The reason for this difficulty is that $\Sigma \vec{F} = m\vec{a}$ does not apply in a coordinate frame attached to the cart. This reference frame is accelerated, and hence not inertial. The smaller μ_s is, the larger a must be to keep the block pinned against the front of the cart.

5.96. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each block.

SET UP: Use coordinates where +x is directed down the incline.

EXECUTE: (a) Since the larger block (the trailing block) has the larger coefficient of friction, it will need to be pulled down the plane; i.e., the larger block will not move faster than the smaller block, and the blocks will have the same acceleration. For the smaller block, $(4.00 \text{ kg})g(\sin 30^\circ - (0.25)\cos 30^\circ) - T = (4.00 \text{ kg})a$, or 11.11 N - T = (4.00 kg)a, and similarly for the larger, 15.44 N + T = (8.00 kg)a. Adding these two relations, 26.55 N = (12.00 kg)a, $a = 2.21 \text{ m/s}^2$.

- **(b)** Substitution into either of the above relations gives T = 2.27 N.
- (c) The string will be slack. The 4.00-kg block will have $a = 2.78 \text{ m/s}^2$ and the 8.00-kg block will have $a = 1.93 \text{ m/s}^2$, until the 4.00-kg block overtakes the 8.00-kg block and collides with it.

EVALUATE: If the string is cut the acceleration of each block will be independent of the mass of that block and will depend only on the slope angle and the coefficient of kinetic friction. The 8.00-kg block would have a smaller acceleration even though it has a larger mass, since it has a larger μ_k .

5.97. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the block and to the plank.

SET UP: Both objects have a = 0.

EXECUTE: Let n_B be the normal force between the plank and the block and n_A be the normal force between the block and the incline. Then, $n_B = w \cos \theta$ and $n_A = n_B + 3w \cos \theta = 4w \cos \theta$. The net frictional force on the block is $\mu_k(n_A + n_B) = \mu_k 5w\cos\theta$. To move at constant speed, this must balance the component of the block's weight along the incline, so $3w\sin\theta = \mu_k 5w\cos\theta$, and

 $\mu_k = \frac{3}{5} \tan \theta = \frac{3}{5} \tan 37^\circ = 0.452.$

EVALUATE: In the absence of the plank the block slides down at constant speed when the slope angle and coefficient of friction are related by $\tan \theta = \mu_k$. For $\theta = 36.9^\circ$, $\mu_k = 0.75$. A smaller μ_k is needed when the plank is present because the plank provides an additional friction force.

5.98. IDENTIFY: Apply Newton's second law to Jack in the Ferris wheel.

SET UP: $\Sigma \vec{F} = m\vec{a}$ and Jack's acceleration is $a_{\rm rad} = v^2/R$, and $v = 2\pi R/T$. At the highest point, the normal force that the chair exerts on Jack is \(\frac{1}{4} \) of his weight, or 0.25mg. Take +y downward.

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EXECUTE: $\Sigma F_y = ma_y$ gives $mg - n = mv^2/R$. $mg - 0.25mg = mv^2/R$, so $v^2/R = 0.75g$. Using $T = 2\pi R/T$, we get $v^2/R = 4\pi^2 R/T^2$. Therefore $4\pi^2 R/T^2 = 0.750g$. T = 1/(0.100 rev/s) = 10.0 s/rev, so $R = (0.750g)T^2/(4\pi^2) = (0.750)(9.80 \text{ m/s}^2)[(10.0 \text{ s})/(2\pi)]^2 = 18.6 \text{ m}$.

EVALUATE: This Ferris wheel would be about 120 ft in diameter, which is certainly large but not impossible.

5.99. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the person. The person moves in a horizontal circle so his acceleration is $a_{\rm rad} = v^2/R$, directed toward the center of the circle. The target variable is the coefficient of static friction between the person and the surface of the cylinder.

$$v = (0.60 \text{ rev/s}) \left(\frac{2\pi R}{1 \text{ rev}} \right) = (0.60 \text{ rev/s}) \left(\frac{2\pi (2.5 \text{ m})}{1 \text{ rev}} \right) = 9.425 \text{ m/s}$$

(a) SET UP: The problem situation is sketched in Figure 5.99a.

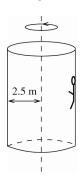
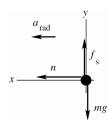


Figure 5.99a



The free-body diagram for the person is sketched in Figure 5.99b.

The person is held up against gravity by the static friction force exerted on him by the wall. The acceleration of the person is $a_{\rm rad}$, directed in toward the axis of rotation.

Figure 5.99b

(b) EXECUTE: To calculate the minimum μ_s required, take f_s to have its maximum value, $f_s = \mu_s n$.

$$\Sigma F_y = ma_y$$
: $f_s - mg = 0$

 $\mu_{\rm s} n = mg$

$$\Sigma F_r = ma_r$$
: $n = mv^2/R$

Combine these two equations to eliminate n: $\mu_s mv^2/R = mg$

$$\mu_{\rm s} = \frac{Rg}{v^2} = \frac{(2.5 \text{ m})(9.80 \text{ m/s}^2)}{(9.425 \text{ m/s})^2} = 0.28$$

(c) EVALUATE: No, the mass of the person divided out of the equation for μ_s . Also, the smaller μ_s is, the larger ν must be to keep the person from sliding down. For smaller μ_s the cylinder must rotate faster to make n large enough.

IDENTIFY: The ice is traveling in a circular arc, so Newton's second law applies to it. The radial acceleration is toward the center of the circle, which is downward at the top of the arc.

SET UP:
$$\sum F = m \frac{v^2}{R}$$
.

EXECUTE: At the top of the arc
$$\sum F = m \frac{v^2}{R}$$
 gives $mg - n = mv^2/R$. Using $n = mg/2$ gives

$$mg - mg/2 = mv^2/R$$
 \rightarrow $v = \sqrt{\frac{Rg}{2}}$.

EVALUATE: The smallest the normal force could be is zero, in which case $v = \sqrt{Rg}$, which is greater than our result. So our answer is reasonable.

5.101. **IDENTIFY:** The race car is accelerated toward the center of the circle of the curve. If the car goes at the proper speed for the banking angle, there will be no friction force on it, and will not tend to slide either up or down the road. In this case, it is going faster than the proper speed, so it will tend to slide up the road, so the friction force will be down the road. Newton's second law applies to the car.

SET UP: At the maximum speed so the car will not slide up the road, static friction from the road on the tires is at its maximum value, so $f_S = \mu_S n$ and its direction is down the road. Fig. 5.101 shows a freebody diagram of the car. Call the +x-axis horizontal pointing toward the center of the circular curve, and the y-axis perpendicular to the road surface. This is one of the few times that it is better not to take the xaxis parallel to the surface of the incline. The reason is that the acceleration is horizontal, not parallel to the surface. Apply $\sum F_x = ma_x$ and $\sum F_y = 0$ letting β be the banking angle.

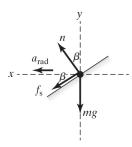


Figure 5.101

EXECUTE: (a) Start with $\sum F_x = ma_{\text{rad}}$. From the free-body diagram, we see that

$$\sum F_x = n \sin \beta + f_S \cos \beta = n \sin \beta + \mu_S n \cos \beta$$
, so

$$ma_{\rm rad} = n(\sin \beta + \mu_{\rm s} \cos \beta)$$
 (Eq. 1)

$$\sum F_v = 0 = n \cos \beta - f_S \sin \beta - mg = n \cos \beta - \mu_S n \sin \beta - mg = 0$$
, which gives

$$mg = n(\cos \beta - \mu_{\rm s} \sin \beta)$$
 (Eq. 2)

$$mg = n(\cos \beta - \mu_s \sin \beta)$$
 (Eq. 2)
Solving for n gives $n = \frac{mg}{\cos \beta - \mu_s \sin \beta} = \frac{(1200 \text{ kg})(9.80 \text{ m/s}^2)}{\cos 18.0^\circ - (0.400) \sin 18.0^\circ} = 1.42 \times 10^4 \text{ N}.$

(b) Divide Eq. 1 by Eq. 2, giving
$$a_{\text{rad}} = \left(\frac{\sin \beta + \mu_{\text{s}} \cos \beta}{\cos \beta - \mu_{\text{s}} \sin \beta}\right) g$$
. Using $\beta = 18.0^{\circ}$ and $\mu_{\text{s}} = 0.400$ gives

$$a_{\rm rad} = 8.17 \text{ m/s}^2$$

(c)
$$a_{\text{rad}} = v^2/R$$
, so $v = \sqrt{Ra_{\text{rad}}} = \sqrt{(90.0 \text{ m})(8.17 \text{ m/s}^2)} = 27.1 \text{ m/s}.$

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EVALUATE: Check our result in (b) for a very smooth road in which $\mu_s = 0$. This gives $a_{rad} = g \tan \beta$,

so
$$\frac{v^2}{R} = g \tan \beta$$
, or $\tan \beta = \frac{v^2}{Rg}$. This result give the familiar angle for a properly banked road for speed

 ν . If there were no friction, a car would have to go at the proper speed to avoid slipping. So our result in this special case checks out. The proper speed for $\beta = 18.0^{\circ}$ should be

$$v = \sqrt{Rg \tan \beta} = \sqrt{(90.0 \text{ m})(9.80 \text{ m/s}^2) \tan 18.0^\circ} = 16.9 \text{ m/s}$$
, so the speed we just found is obviously much greater than the proper speed.

5.102. IDENTIFY: The race car is accelerated toward the center of the circle of the curve. If the car goes at the proper speed for the banking angle, there will be no friction force on it, and will not tend to slide either up or down the road. In this case, it is going slower than the proper speed, so it will tend to slide down the road, so the friction force will be up the road. Newton's second law applies to the car.

SET UP: At the maximum speed so the car will not slide down the road, static friction from the road on the tires is at its maximum value, so $f_S = \mu_S n$ and its direction is up the road. Figure 5.102 shows a free-body diagram of the car. Call the +x-axis horizontal pointing toward the center of the circular curve, and the y-axis perpendicular to the road surface. This is one of the few times that it is better *not* to take the x-axis parallel to the surface of the incline. The reason is that the acceleration is horizontal, not parallel to the surface. Apply $\sum F_x = ma_x$ and $\sum F_y = 0$ letting β be the banking angle.

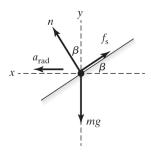


Figure 5.102

EXECUTE: (a) The procedure is the same as for problem 5.101 except that f_S is up the road surface instead of down. Using the same steps as in 5.101 leads to

$$\frac{mv^2}{R} = n(\sin\beta - \mu_{\rm s}\cos\beta) \quad \text{(Eq. 1)}$$

$$n(\cos \beta + \mu_{\rm s} \sin \beta) = mg$$
 (Eq. 2)

Solving for *n* gives
$$n = \frac{mg}{\cos \beta + \mu_s \sin \beta} = \frac{(900 \text{ kg})(9.80 \text{ m/s}^2)}{\cos 18.0^\circ + (0.300) \sin 18.0^\circ} = 8450 \text{ N}.$$

(b) Combining Eq. 1 and Eq. 2 we get
$$v^2 = \left(\frac{\sin \beta - \mu_s \cos \beta}{\cos \beta + \mu_s \sin \beta}\right) Rg$$
. Using $\mu_s = 0.300$, $\beta = 18.0^\circ$, and

R = 120.0 m gives v = 5.17 m/s.

EVALUATE: The proper speed for a banking angle of 18.0° is given by $\tan \beta = \frac{v^2}{Rg}$, so the proper speed

for this angle is $v = \sqrt{Rg \tan \beta} = \sqrt{(120.0 \text{ m})(9.80 \text{ m/s}^2) \tan 18.0^\circ} = 19.5 \text{ m/s}$, so the speed we just found is much slower.

5.103. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each block.

SET UP: For block *B* use coordinates parallel and perpendicular to the incline. Since they are connected by ropes, blocks *A* and *B* also move with constant speed.

EXECUTE: (a) The free-body diagrams are sketched in Figure 5.103.

- **(b)** The blocks move with constant speed, so there is no net force on block A; the tension in the rope connecting A and B must be equal to the frictional force on block A, $T_1 = (0.35)(25.0 \text{ N}) = 8.8 \text{ N}$.
- (c) The weight of block C will be the tension in the rope connecting B and C; this is found by considering the forces on block B. The components of force along the ramp are the tension in the first rope (8.8 N, from part (b)), the component of the weight along the ramp, the friction on block B and the tension in the second rope. Thus, the weight of block C is

$$W_C = 8.8 \text{ N} + W_B (\sin 36.9^\circ + \mu_k \cos 36.9^\circ) = 8.8 \text{ N} + (25.0 \text{ N})(\sin 36.9^\circ + (0.35)\cos 36.9^\circ) = 30.8 \text{ N}$$

The intermediate calculation of the first tension may be avoided to obtain the answer in terms of the common weight w of blocks A and B, $w_C = w(\mu_k + (\sin \theta + \mu_k \cos \theta))$, giving the same result.

(d) Applying Newton's second law to the remaining masses (B and C) gives:

$$a = g(w_C - \mu_k w_B \cos \theta - w_B \sin \theta) / (w_B + w_C) = 1.54 \text{ m/s}^2.$$

EVALUATE: Before the rope between A and B is cut the net external force on the system is zero. When the rope is cut the friction force on A is removed from the system and there is a net force on the system of blocks B and C.

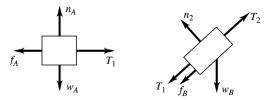


Figure 5.103

5.104. IDENTIFY: The block has acceleration $a_{\text{rad}} = v^2/r$, directed to the left in the figure in the problem. Apply $\Sigma \vec{F} = m\vec{a}$ to the block.

SET UP: The block moves in a horizontal circle of radius $r = \sqrt{(1.25 \text{ m})^2 - (1.00 \text{ m})^2} = 0.75 \text{ m}$. Each string makes an angle θ with the vertical. $\cos \theta = \frac{1.00 \text{ m}}{1.25 \text{ m}}$, so $\theta = 36.9^{\circ}$. The free-body diagram for the block is given in Figure 5.104. Let +x be to the left and let +y be upward.

EXECUTE: (a) $\Sigma F_v = ma_v$ gives $T_u \cos \theta - T_1 \cos \theta - mg = 0$.

$$T_1 = T_u - \frac{mg}{\cos \theta} = 80.0 \text{ N} - \frac{(4.00 \text{ kg})(9.80 \text{ m/s}^2)}{\cos 36.9^\circ} = 31.0 \text{ N}.$$

(b)
$$\Sigma F_x = ma_x$$
 gives $(T_u + T_l)\sin\theta = m\frac{v^2}{r}$.

$$v = \sqrt{\frac{r(T_{\rm u} + T_{\rm l})\sin\theta}{m}} = \sqrt{\frac{(0.75 \text{ m})(80.0 \text{ N} + 31.0 \text{ N})\sin 36.9^{\circ}}{4.00 \text{ kg}}} = 3.53 \text{ m/s}. \text{ The number of revolutions per}$$

second is
$$\frac{v}{2\pi r} = \frac{3.53 \text{ m/s}}{2\pi (0.75 \text{ m})} = 0.749 \text{ rev/s} = 44.9 \text{ rev/min.}$$

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(c) If
$$T_1 \to 0$$
, $T_u \cos \theta = mg$ and $T_u = \frac{mg}{\cos \theta} = \frac{(4.00 \text{ kg})(9.80 \text{ m/s}^2)}{\cos 36.9^\circ} = 49.0 \text{ N}$. $T_u \sin \theta = m \frac{v^2}{r}$.
$$v = \sqrt{\frac{rT_u \sin \theta}{m}} = \sqrt{\frac{(0.75 \text{ m})(49.0 \text{ N})\sin 36.9^\circ}{4.00 \text{ kg}}} = 2.35 \text{ m/s}$$
. The number of revolutions per minute is
$$(44.9 \text{ rev/min}) \left(\frac{2.35 \text{ m/s}}{3.53 \text{ m/s}}\right) = 29.9 \text{ rev/min}$$
.

EVALUATE: The tension in the upper string must be greater than the tension in the lower string so that together they produce an upward component of force that balances the weight of the block.

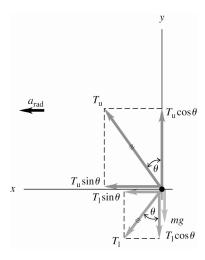


Figure 5.104

5.105. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$, with f = kv.

SET UP: Follow the analysis that leads to the equation $v_y = v_t[1 - e^{-(k/m)t}]$, except now the initial speed is $v_{0y} = 3mg/k = 3v_t$ rather than zero.

EXECUTE: The separated equation of motion has a lower limit of $3v_t$ instead of zero; specifically,

$$\int_{3v_{t}}^{v} \frac{dv}{v - v_{t}} = \ln \frac{v_{t} - v}{-2v_{t}} = \ln \left(\frac{v}{2v_{t}} - \frac{1}{2}\right) = -\frac{k}{m}t, \text{ or } v = 2v_{t} \left[\frac{1}{2} + e^{-(k/m)t}\right]$$

where $v_t = mg/k$.

EVALUATE: As $t \to \infty$ the speed approaches v_t . The speed is always greater than v_t and this limit is approached from above.

5.106. IDENTIFY: The box on the ramp slows down on the way up and speeds up on the way down. Newton's second law applies to both the upward and downward motion, but the acceleration will not be the same for both parts of the motion.

SET UP: On the way up, kinetic friction acts down the ramp, but on the way down it acts up the ramp. Yet gravity acts down the ramp in both cases. Therefore the acceleration will not be the same in both on the upward motion as on the downward motion. We must break this problem up into two segments: motion up the ramp and motion down the ramp. Fig. 5.106(a) shows a free-body diagram for the upward part of the motion. The free-body diagram for the downward segment is shown in Fig. 5.106(b). It is the same as for the upward motion except that friction acts up the ramp. We appy $\sum F_x = ma_x$ in both segments and use the constant-acceleration equations as needed. In both segments, the acceleration is

down the ramp, so we call that the +x-axis in both parts. We use $\sum F_y = 0$ and $f_k = \mu_k n$ in both segments. At its highest point, the speed of the box is zero. We want to find μ_k in terms of α .

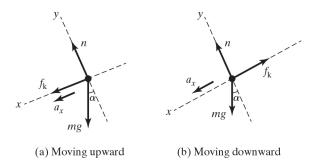


Figure 5.106

EXECUTE: First find the acceleration of the box on both segments of the motion. Call a_{up} the magnitude of the acceleration on the upward segment and a_{down} the magnitude of the acceleration on the downward segment.

<u>Upward segment</u>: Use $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ with v = 0 at the highest point. This gives $0 = v_0^2 + 2a_{\rm up}(-d)$. Note that we used -d because down the ramp is positive and the displacement d is up the ramp. This gives $a_{\rm up} = v_0^2 / 2d$.

<u>Downward segment</u>: $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ gives $\left(\frac{v_0}{2}\right)^2 = 0 + 2a_{\text{down}}d$. The displacement is down the

ramp so we use +d this time, so we get $a_{\text{down}} = v_0^2 / 8d$.

Now apply $\sum F_x = ma_x$ and $\sum F_y = 0$ for both segments. Referring to Fig. 5.106 shows us the components.

<u>Upward segment</u>: $\sum F_v = 0$ gives $n = mg \cos \alpha$

 $\sum F_x = ma_x$ gives $mg \sin \alpha + f_k = ma_{\rm up}$ $\rightarrow mg \sin \alpha + \mu_k mg \cos \alpha = ma_{\rm up} = mv_0^2 / 2d$. This simplifies to $g(\sin \alpha + \mu_k \cos \alpha) = \frac{v_0^2}{2d}$. (Eq. 1)

<u>Downward segment</u>: The normal force is the same as before, as is the magnitude of the friction force. But now the friction force acts up the ramp and $a_{\text{down}} = v_0^2 / 8d$. $\sum F_x = ma_x$ gives

$$g(\sin \alpha - \mu_k \cos \alpha) = \frac{v_0^2}{8d}$$
. (Eq. 2)

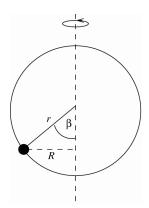
Combining Eq. 1 and Eq. 2 gives $\frac{\sin \alpha - \mu_k \cos \alpha}{\sin \alpha + \mu_k \cos \alpha} = \frac{1}{4}$, from which we get $\mu_k = \frac{3}{5} \tan \alpha$.

EVALUATE: We found the $a_{up} > a_{down}$. This is reasonable because on the upward segment both gravity and friction oppose the motion, whereas on the downward segment, friction still opposes the motion but gravity does not.

5.107. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the circular motion of the bead. Also use $a_{\rm rad} = 4\pi^2 R/T^2$ to relate $a_{\rm rad}$ to the period of rotation T.

SET UP: The bead and hoop are sketched in Figure 5.107a.

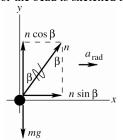
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The bead moves in a circle of radius $R = r \sin \beta$. The normal force exerted on the bead by the hoop is radially inward.

Figure 5.107a

The free-body diagram for the bead is sketched in Figure 5.107b.



EXECUTE:

$$\Sigma F_y = ma_y$$

 $n\cos\beta - mg = 0$
 $n = mg/\cos\beta$
 $\Sigma F_x = ma_x$
 $n\sin\beta = ma_{\rm rad}$

Figure 5.107b

Combine these two equations to eliminate n:

$$\left(\frac{mg}{\cos\beta}\right)\sin\beta = ma_{\text{rad}}$$
$$\frac{\sin\beta}{\beta} = \frac{a_{\text{rad}}}{\beta}$$

 $a_{\rm rad} = v^2/R$ and $v = 2\pi R/T$, so $a_{\rm rad} = 4\pi^2 R/T^2$, where T is the time for one revolution.

$$R = r \sin \beta$$
, so $a_{\text{rad}} = \frac{4\pi^2 r \sin \beta}{T^2}$

Use this in the above equation: $\frac{\sin \beta}{\cos \beta} = \frac{4\pi^2 r \sin \beta}{T^2 g}$

This equation is satisfied by $\sin \beta = 0$, so $\beta = 0$, or by $\frac{1}{\cos \beta} = \frac{4\pi^2 r}{T^2 g}$, which gives $\cos \beta = \frac{T^2 g}{4\pi^2 r}$.

(a) 4.00 rev/s implies T = (1/4.00) s = 0.250 s

Then
$$\cos \beta = \frac{(0.250 \text{ s})^2 (9.80 \text{ m/s}^2)}{4\pi^2 (0.100 \text{ m})}$$
 and $\beta = 81.1^\circ$.

(b) This would mean $\beta = 90^{\circ}$. But $\cos 90^{\circ} = 0$, so this requires $T \to 0$. So β approaches 90° as the hoop rotates very fast, but $\beta = 90^{\circ}$ is not possible.

(c) 1.00 rev/s implies T = 1.00 s

The $\cos \beta = \frac{T^2 g}{4\pi^2 r}$ equation then says $\cos \beta = \frac{(1.00 \text{ s})^2 (9.80 \text{ m/s}^2)}{4\pi^2 (0.100 \text{ m})} = 2.48$, which is not possible. The

only way to have the $\Sigma \vec{F} = m\vec{a}$ equations satisfied is for $\sin \beta = 0$. This means $\beta = 0$; the bead sits at the bottom of the hoop.

EVALUATE: $\beta \to 90^{\circ}$ as $T \to 0$ (hoop moves faster). The largest value T can have is given by $T^2g/(4\pi^2r)=1$ so $T=2\pi\sqrt{r/g}=0.635$ s. This corresponds to a rotation rate of (1/0.635) rev/s = 1.58 rev/s. For a rotation rate less than 1.58 rev/s, $\beta=0$ is the only solution and the bead sits at the bottom of the hoop. Part (c) is an example of this.

5.108. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the combined object of motorcycle plus rider.

SET UP: The object has acceleration $a_{\text{rad}} = v^2/r$, directed toward the center of the circular path.

EXECUTE: (a) For the tires not to lose contact, there must be a downward force on the tires. Thus, the (downward) acceleration at the top of the sphere must exceed mg, so $m\frac{v^2}{R} > mg$, and

$$v > \sqrt{gR} = \sqrt{(9.80 \text{ m/s}^2)(13.0 \text{ m})} = 11.3 \text{ m/s}.$$

(b) The (upward) acceleration will then be 4g, so the upward normal force must be $5mg = 5(110 \text{ kg})(9.80 \text{ m/s}^2) = 5390 \text{ N}.$

EVALUATE: At any nonzero speed the normal force at the bottom of the path exceeds the weight of the object.

5.109. IDENTIFY: The block begins to move when static friction has reached its maximum value. After that, kinetic friction acts and the block accelerates, obeying Newton's second law.

SET UP: $\Sigma F_x = ma_x$ and $f_{s,max} = \mu_s n$, where n is the normal force (the weight of the block in this case).

EXECUTE: (a) & (b) $\Sigma F_x = ma_x$ gives $T - \mu_k mg = ma$. The graph with the problem shows the

acceleration a of the block versus the tension T in the cord. So we solve the equation from Newton's second law for a versus T, giving $a = (1/m)T - \mu_k g$. Therefore the slope of the graph will be 1/m and the intercept with the vertical axis will be $-\mu_k g$. Using the information given in the problem for the best-fit equation, we have $1/m = 0.182 \text{ kg}^{-1}$, so m = 5.4945 kg and $-\mu_k g = -2.842 \text{ m/s}^2$, so $\mu_k = 0.290$.

When the block is just ready to slip, we have $f_{s,max} = \mu_s n$, which gives $\mu_s = (20.0 \text{ N})/[(5.4945 \text{ kg})(9.80 \text{ m/s}^2)] = 0.371$.

(c) On the Moon, g is less than on earth, but the mass m of the block would be the same as would μ_k . Therefore the slope (1/m) would be the same, but the intercept $(-\mu_k g)$ would be less negative.

EVALUATE: Both coefficients of friction are reasonable for ordinary materials, so our results are believable.

5.110. IDENTIFY: Near the top of the hill the car is traveling in a circular arc, so it has radial acceleration and Newton's second law applies. We have measurements for the force the car exerts on the road at various speeds.

SET UP: The acceleration of the car is $a_{\text{rad}} = v^2/R$ and $\Sigma F_y = ma_y$ applies to the car. Let the +y-axis be downward, since that is the direction of the acceleration of the car.

EXECUTE: (a) Apply $\Sigma F_y = ma_y$ to the car at the top of the hill: $mg - n = mv^2/R$, where n is the force the road exerts on the car (which is the same as the force the car exerts on the road). Solving for n gives $n = mg - (m/R)v^2$. So if we plot n versus v^2 , we should get a straight line having slope equal to -m/R and intercept with the vertical axis at mg. We could make a table of v^2 and n using the given numbers given with the problem, or we could use graphing software. The resulting graph is shown in Figure 5.110.

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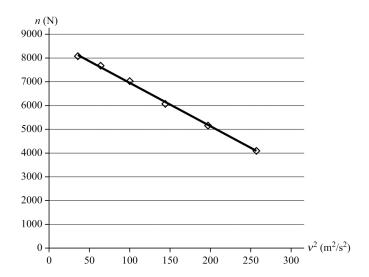


Figure 5.110

(b) The best-fit equation for the graph in Figure 5.110 is $n = [-18.12 \text{ N/(m/s)}^2]v^2 + 8794 \text{ N}$. Therefore mg = 8794 N, which gives $m = (8794 \text{ N})/(9.80 \text{ m/s}^2) = 897 \text{ kg}$.

The slope is equal to -m/R, so $R = -m/\text{slope} = -(897 \text{ kg})/[-18.12 \text{ N/(m/s)}^2] = 49.5 \text{ m}.$

(c) At the maximum speed, n = 0. Using $mg - n = mv^2/R$, this gives $v = \sqrt{gR} = \sqrt{(9.80 \text{ m/s}^2)(49.5 \text{ m})} = 22.0 \text{ m/s}$.

EVALUATE: We can double check (c) using our graph. Putting n = 0 into the best-fit equation, we get $v = \sqrt{(8794 \text{ N})(18.14 \text{ N} \cdot \text{s}^2/\text{m}^2)} = 22.0 \text{ m/s}$, which checks. Also 22 m/s is about 49 mph, which is not an unreasonabled speed on a hill.

5.111. IDENTIFY: A cable pulling parallel to the surface of a ramp accelerates 2170-kg metal blocks up a ramp that rises at 40.0° above the horizontal. Newton's second law applies to the blocks, and the constant-acceleration kinematics formulas can be used.

SET UP: Call the +x-axis parallel to the ramp surface pointing upward because that is the direction of the acceleration of the blocks, and let the y-axis be perpendicular to the surface. There is no acceleration

in the y-direction. $\Sigma F_x = ma_x$, $f_k = \mu_k n$, and $x - x_0 = v_{0x}t + \frac{1}{2}a_xt^2$.

EXECUTE: (a) First use $x - x_0 = v_{0x}t + \frac{1}{2}a_xt^2$ to find the acceleration of a block. Since $v_{0x} = 0$, we have

 $a_x = 2(x - x_0)/t^2 = 2(8.00 \text{ m})/(4.20 \text{ s})^2 = 0.9070 \text{ m/s}^2$. The forces in the y-direction balance, so $n = mg\cos(40.0^\circ)$, so $f_k = (0.350)(2170 \text{ kg})(9.80 \text{ m/s}^2)\cos(40.0^\circ) = 5207 \text{ N}$. Using $\Sigma F_x = ma_x$, we have $T - mg\sin(40.0^\circ) - f_k = ma$. Solving for T gives $T = (2170 \text{ kg})(9.80 \text{ m/s}^2)\sin(40.0^\circ) + 5207 \text{ N} + (2170 \text{ kg})(0.9070 \text{ m/s}^2) = 2.13 \times 10^4 \text{ N} = 21.3 \text{ kN}$.

From the table shown with the problem, this tension is greater than the safe load of a $\frac{1}{2}$ inch diameter cable (which is 19.0 kN), so we need to use a $\frac{5}{8}$ -inch cable.

(b) We assume that the safe load (SL) is proportional to the cross-sectional area of the cable, which means that $SL \propto \pi(D/2)^2 \propto (\pi/4)D^2$, where D is the diameter of the cable. Therefore a graph of SL versus D^2 should give a straight line. We could use the data given in the table with the problem to make the graph by hand, or we could use graphing software. The resulting graph is shown in Figure 5.111 (next page). The best-fit line has a slope of 74.09 kN/in.² and a *y*-intercept of 0.499 kN. For a cable of diameter D = 9/16 in., this equation gives $SL = (74.09 \text{ kN/in.}^2)(9/16 \text{ in.})^2 + 0.499 \text{ kN} = 23.9 \text{ kN}$.

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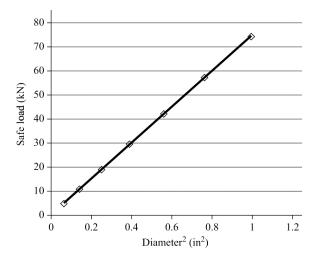


Figure 5.111

(c) The acceleration is now zero, so the forces along the surface balance, giving $T + f_s = mg \sin(40.0^\circ)$. Using the numbers we get T = 3.57 kN.

(d) The tension at the top of the cable must accelerate the block and the cable below it, so the tension at the top would be larger. For a 5/8-inch cable, the mass per meter is 0.98 kg/m, so the 9.00-m long cable would have a mass of (0.98 kg/m)(9.00 m) = 8.8 kg. This is only 0.4% of the mass of the block, so neglecting the cable weight has little effect on accuracy.

EVALUATE: It is reasonable that the safe load of a cable is proportional to its cross-sectional area. If we think of the cable as consisting of many tiny strings each pulling, doubling the area would double the number of strings.

5.112. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the block and to the wedge.

SET UP: For both parts, take the *x*-direction to be horizontal and positive to the right, and the *y*-direction to be vertical and positive upward. The normal force between the block and the wedge is n; the normal force between the wedge and the horizontal surface will not enter, as the wedge is presumed to have zero vertical acceleration. The horizontal acceleration of the wedge is A, and the components of acceleration of the block are a_x and a_y .

EXECUTE: (a) The equations of motion are then $MA = -n\sin\alpha$, $ma_x = n\sin\alpha$ and $ma_y = n\cos\alpha - mg$. Note that the normal force gives the wedge a negative acceleration; the wedge is expected to move to the left. These are three equations in four unknowns, A, a_x , a_y and n. Solution is possible with the imposition of the relation between A, a_x and a_y . An observer on the wedge is not in an inertial frame, and should not apply Newton's laws, but the kinematic relation between the components of acceleration are not so restricted. To such an observer, the vertical acceleration of the block is a_y , but the horizontal acceleration of the block is $a_x - A$. To this observer, the block descends

at an angle α , so the relation needed is $\frac{a_y}{a_x - A} = -\tan \alpha$. At this point, algebra is unavoidable. A

possible approach is to eliminate a_x by noting that $a_x = -\frac{M}{m}A$, using this in the kinematic constraint to eliminate a_y and then eliminating n. The results are:

$$A = \frac{-gm}{(M+m)\tan\alpha + (M/\tan\alpha)}$$

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$$a_x = \frac{gM}{(M+m)\tan\alpha + (M/\tan\alpha)}$$

$$a_y = \frac{-g(M+m) \tan \alpha}{(M+m) \tan \alpha + (M/\tan \alpha)}$$

(b) When $M \gg m$, $A \to 0$, as expected (the large block won't move). Also,

 $a_x \to \frac{g}{\tan \alpha + (1/\tan \alpha)} = g \frac{\tan \alpha}{\tan^2 \alpha + 1} = g \sin \alpha \cos \alpha$ which is the acceleration of the block $(g \sin \alpha)$ in

this case), with the factor of $\cos \alpha$ giving the horizontal component. Similarly, $a_v \rightarrow -g \sin^2 \alpha$.

(c) The trajectory is a straight line with slope $-\left(\frac{M+m}{M}\right)\tan\alpha$.

EVALUATE: If $m \gg M$, our general results give $a_x = 0$ and $a_y = -g$. The massive block accelerates straight downward, as if it were in free fall.

5.113. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the block and to the wedge.

SET UP: From Problem 5.112, $ma_x = n \sin \alpha$ and $ma_y = n \cos \alpha - mg$ for the block. $a_y = 0$ gives $a_x = g \tan \alpha$.

EXECUTE: If the block is not to move vertically, both the block and the wedge have this horizontal acceleration and the applied force must be $F = (M + m)a = (M + m)g\tan\alpha$.

EVALUATE: $F \to 0$ as $\alpha \to 0$ and $F \to \infty$ as $\alpha \to 90^{\circ}$.

5.114. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to each of the three masses and to the pulley B.

SET UP: Take all accelerations to be positive downward. The equations of motion are straightforward, but the kinematic relations between the accelerations, and the resultant algebra, are not immediately obvious. If the acceleration of pulley *B* is a_B , then $a_B = -a_3$, and a_B is the average of the accelerations of masses 1 and 2, or $a_1 + a_2 = 2a_B = -2a_3$.

EXECUTE: (a) There can be no net force on the massless pulley B, so $T_C = 2T_A$. The five equations to be solved are then $m_1g - T_A = m_1a_1$, $m_2g - T_A = m_2a_2$, $m_3g - T_C = m_3a_3$, $a_1 + a_2 + 2a_3 = 0$ and $2T_A - T_C = 0$. These are five equations in five unknowns, and may be solved by standard means. The accelerations a_1 and a_2 may be eliminated using $2a_3 = -(a_1 + a_2) = -[2g - T_A((1/m_1) + (1/m_2))]$. The tension T_A may be eliminated by using $T_A = (1/2)T_C = (1/2)m_3(g - a_3)$.

Combining and solving for a_3 gives $a_3 = g \frac{-4m_1m_2 + m_2m_3 + m_1m_3}{4m_1m_2 + m_2m_3 + m_1m_3}$.

(b) The acceleration of the pulley B has the same magnitude as a_3 and is in the opposite direction.

(c) $a_1 = g - \frac{T_A}{m_1} = g - \frac{T_C}{2m_1} = g - \frac{m_3}{2m_1}(g - a_3)$. Substituting the above expression for a_3 gives

 $a_1 = g \, \frac{4m_1m_2 - 3m_2m_3 + m_1m_3}{4m_1m_2 + m_2m_3 + m_1m_3}.$

(d) A similar analysis (or, interchanging the labels 1 and 2) gives $a_2 = g \frac{4m_1m_2 - 3m_1m_3 + m_2m_3}{4m_1m_2 + m_2m_3 + m_1m_3}$

(e), (f) Once the accelerations are known, the tensions may be found by substitution into the appropriate equation of motion, giving $T_A = g \frac{4m_1m_2m_3}{4m_1m_2 + m_2m_3 + m_1m_3}$, $T_C = g \frac{8m_1m_2m_3}{4m_1m_2 + m_2m_3 + m_1m_3}$.

(g) If $m_1 = m_2 = m$ and $m_3 = 2m$, all of the accelerations are zero, $T_C = 2mg$ and $T_A = mg$. All masses and pulleys are in equilibrium, and the tensions are equal to the weights they support, which is what is expected.

EVALUATE: It is useful to consider special cases. For example, when $m_1 = m_2 \gg m_3$ our general result gives $a_1 = a_2 = +g$ and $a_3 = g$.

5.115. IDENTIFY: Apply $\Sigma \vec{F} = m\vec{a}$ to the ball at each position.

SET UP: When the ball is at rest, a = 0. When the ball is swinging in an arc it has acceleration component $a_{\text{rad}} = \frac{v^2}{R}$, directed inward.

EXECUTE: Before the horizontal string is cut, the ball is in equilibrium, and the vertical component of the tension force must balance the weight, so $T_A \cos \beta = w$ or $T_A = w/\cos \beta$. At point B, the ball is not in equilibrium; its speed is instantaneously 0, so there is no radial acceleration, and the tension force must balance the radial component of the weight, so $T_B = w\cos \beta$ and the ratio $(T_B/T_A) = \cos^2 \beta$.

EVALUATE: At point B the net force on the ball is not zero; the ball has a tangential acceleration.

5.116. IDENTIFY: The forces must balance for the person not to slip.

SET UP and **EXECUTE:** As was done in earlier problems, balancing forces parallel to and perpendicular to the surface of the rock leads to the equation $\mu_s = \tan \theta = 1.2$, so $\theta = 50^\circ$, which is choice (b). **EVALUATE:** The condition $\mu_s = \tan \theta$ applies only when the person is just ready to slip, which would be the case at the maximum angle.

5.117. IDENTIFY: Friction changes from static friction to kinetic friction.

SET UP and **EXECUTE:** When she slipped, static friction must have been at its maximum value, and that was enough to support her weight just before she slipped. But the kinetic friction will be less than the maximum static friction, so the kinetic friction force will not be enough to balance her weight down the incline. Therefore she will slide down the surface and continue to accelerate downward, making (b) the correct choice.

EVALUATE: Shoes with a greater coefficient of static friction would enable her to walk more safely.

5.118. IDENTIFY: The person pushes off horizontally and acclerates herself, so Newton's second law applies. **SET UP** and **EXECUTE:** She runs horizontally, so her vertical acceleration is zero, which makes the normal force n due to the ground equal to her weight mg. In the horizontal direction, static friction accelerates her forward, and it must be its maximum value to achieve her maximum acceleration. Therefore $f_s = ma = \mu_s mg$, which gives $a = \mu_s g = 1.2g$, making (d) the correct choice. **EVALUATE:** Shoes with more friction would allow her to accelerate even faster.

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