

!date

Fri Feb 25 05:37:04 UTC 2022

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## ▼ CSCI-SHU 210 Data Structures

### ▼ Recitation 3 Recursion

You have a series of tasks in front of you. Complete them! Everyone should code on their own computer, but you are encouraged to talk to others, and seek help from each other and from the TA/LA.

Important:

1. Analyzing the output for recursive programs;
2. Determining the big O complexity for recursive programs;
3. Understand “Break large problem into smaller problems + induction”;
4. Understand what type of problem branching can solve.

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- For students who have recitation on Wednesday, you should submit your solutions by **Feb 25th** Friday 11:59pm.
- For students who have recitation on Thursday, you should submit your solutions by **Feb 26th** Saturday 11:59pm.
- For students who have recitation on Friday, you should submit your solutions by **Feb 27th** Sunday 11:59pm.

### ▼ Problem 1

#### ▼ Recursion output analysis

What is the output for the following recursive program? Don't run it, first try to guess.

def f(n):

```
if n > 0:
    f(n-1)
    print(n, end = " ")
    f(n-1)
```

f(4)

Your Answer: 1 2 3 4 3 2 1

## ▼ Problem 2

双击（或按回车键）即可修改

## ▼ Determine big-O complexity for the following code snippets:

def func1(N):

```
if n < 1:
    return
else:
    for i in range(5*N):
        print("hi")
    func1(N - 5)
```

## ▼ Your Answer: $O(n^2)$

def func2(N):

```
if n < 1:
    return
else:
    func2(N - 1)
    func2(N - 1)
    for i in range(N):
        print("*")
```

Your Answer:  $O(2^n)$

### ▼ Problem 3

Palindrome (Recursive version)

Implement function `palindrome()`: this function assesses whether an input String is indeed a palindrome.

Important:

1. Check the string letter by letter, no `string.reverse()`
2. Use recursion to break large problem into smaller problem.

```
def palindrome_recursive(string, index):
    """
    # Complete the palindrome algorithm --- with recursion
    # Think about how to break a large problem into smaller sub p
    What is our base case in this problem?

    # Another way to ask: what is our smallest problem?
    How to get to this smallest problem?

    :param string: String -- the string to check whether it is a
    :param index: Int -- additional parameter for recursion track

    :return: True if @string is palindrome, False otherwise
    """
    if index==len(string)//2+1:
        return True
    return string[index]==string[len(string)-index-1] and palindr

def main():
    s1 = "nodevilllivedon"
    s2 = "livenoevil!liveonevil"
    s3 = "beliveivileb"
    r1 = palindrome_recursive(s1, 0)
    r2 = palindrome_recursive(s2, 0)
    r3 = palindrome_recursive(s3, 0)
    print("s1 is", r1) # Should be True
    print("s2 is", r2) # Should be True
    print("s3 is", r3) # Should be False
```

```
main()

s1 is True
s2 is True
s3 is False
```

## ▼ Problem 4

### Tower of Hanoi

Your task is to code the famous Tower of Hanoi problem. Complete function `hanoi()`, so the disks move correctly when you run the program.

Important:

1. We have graphical demo for this question. (Only works in your local IDE)
2. Start, goal, mid parameters represent three poles.
3. To move a disk, call function `game.move(num_disks, start, goal)`
4. Use recursion to break large problem into smaller problem.

```
from tkinter import Tk, Canvas

def hanoi(num_disks, start, goal, mid):
    """
    Implement the tower of hanoi algorithm.
    If implemented correctly, a window should pop up, and disks v
    to move a disk, you can call
    game.move(num_disks, start, goal)

    :param num_disks: number of disks in this function call.
    :param start: Int -- start moving from this pole
    :param goal: Int -- move to this pole
    :param mid: Int -- Intermediate (useless) pole for this move.

    :return: nothing to return
    """

    if num_disks==1:
        game.move(1, start, goal)
        return None
    hanoi(num_disks-1, start, mid, goal)
    game.move(num_disks, start, goal)
    hanoi(num_disks-1, mid, goal, start)

# The graphical interface
```

```
class Tkhanoi:
```

```
    # Create our objects
```

```
    def __init__(self, n, bitmap = None):
```

```
        self.n = n
```

```
        self.tk = tk = Tk()
```

```
        self.canvas = c = Canvas(tk)
```

```
        c.pack()
```

```
        width, height = tk.getint(c['width']), tk.getint(c['height'])
```

```
    # Add background
```

```
    if bitmap:
```

```
        self.bitmap = c.create_bitmap(width//2, height//2,
                                       bitmap=bitmap,
                                       foreground='blue')
```

```
    # Generate pegs
```

```
    pegwidth = 10
```

```
    pegheight = height//2
```

```
    pegdist = width//3
```

```
    x1, y1 = (pegdist-pegwidth)//2, height*1//3
```

```
    x2, y2 = x1+pegwidth, y1+pegheight
```

```
    self.pegs = []
```

```
    p = c.create_rectangle(x1, y1, x2, y2, fill='black')
```

```
    self.pegs.append(p)
```

```
    x1, x2 = x1+pegdist, x2+pegdist
```

```
    p = c.create_rectangle(x1, y1, x2, y2, fill='black')
```

```
    self.pegs.append(p)
```

```
    x1, x2 = x1+pegdist, x2+pegdist
```

```
    p = c.create_rectangle(x1, y1, x2, y2, fill='black')
```

```
    self.pegs.append(p)
```

```
    self.tk.update()
```

```
    # Generate pieces
```

```
    pieceheight = pegheight//16
```

```
    maxpiecewidth = pegdist*2//3
```

```
    minpiecewidth = 2*pegwidth
```

```
    self.pegstate = [[], [], []]
```

```
    self.pieces = {}
```

```
    x1, y1 = (pegdist-maxpiecewidth)//2, y2-pieceheight-2
```

```
    x2, y2 = x1+maxpiecewidth, y1+pieceheight
```

```
    dx = (maxpiecewidth-minpiecewidth) // (2*max(1, n-1))
```

```
    for i in range(n, 0, -1):
```

```
        p = c.create_rectangle(x1, y1, x2, y2, fill='red')
```

```
        self.pieces[i] = p
```

```

        self.pegstate[0].append(i)
        x1, x2 = x1 + dx, x2-dx
        y1, y2 = y1 - pieceheight-2, y2-pieceheight-2
        self.tk.update()
        self.tk.after(25)

def run(self):
    hanoi(self.n, 0, 2, 1)

# Reporting callback for the actual hanoi function
def move(self, i, a, b):
    if self.pegstate[a][-1] != i: raise RuntimeError # Assert
    del self.pegstate[a][-1]
    p = self.pieces[i]
    c = self.canvas

    # Lift the piece above peg a
    ax1, ay1, ax2, ay2 = c.bbox(self.pegs[a])
    while 1:
        x1, y1, x2, y2 = c.bbox(p)
        if y2 < ay1: break
        c.move(p, 0, -1)
        self.tk.update()

    # Move it towards peg b
    bx1, by1, bx2, by2 = c.bbox(self.pegs[b])
    newcenter = (bx1+bx2)//2
    while 1:
        x1, y1, x2, y2 = c.bbox(p)
        center = (x1+x2)//2
        if center == newcenter: break
        if center > newcenter: c.move(p, -1, 0)
        else: c.move(p, 1, 0)
        self.tk.update()

    # Move it down on top of the previous piece
    pieceheight = y2-y1
    newbottom = by2 - pieceheight*len(self.pegstate[b]) - 2
    while 1:
        x1, y1, x2, y2 = c.bbox(p)
        if y2 >= newbottom: break
        c.move(p, 0, 1)
        self.tk.update()

    # Update peg state

```

```
self.pegstate[b].append(i)
```

```
bitmap = None
game = Tkhanoi(6, bitmap)
game.run()
```

```
-----
TclError                                Traceback (most recent call last)
<ipython-input-9-484467f546e9> in <module>()
    118
    119 bitmap = None
--> 120 game = Tkhanoi(6, bitmap)
    121 game.run()

----- 1 frames -----
/usr/lib/python3.7/tkinter/__init__.py in __init__(self, screenName, baseName,
    2021             baseName = baseName + ext
    2022             interactive = 0
--> 2023             self.tk = _tkinter.create(screenName, baseName, className, int
    2024             if useTk:
    2025                 self._loadtk()

TclError: no display name and no $DISPLAY environment variable
```

SEARCH STACK OVERFLOW

## ▼ Problem 5

### All Possible Combinations problem

Implement a recursive approach to show all the teams that can be created from a group (out of n things choose k at a time). Implement the recursive showTeams(), given a group of players, and the size of the team, display all the possible combinations of players.

Important:

1. Combination is different from permutation. This is a combination problem.
2. There are  $\frac{n!}{k!(n-k)!}$  combinations (Choose k out of n) [1, 2], [2, 1] are the same combinations.
3. There are  $\frac{n!}{(n-k)!}$  permutations (Choose k out of n) [1, 2], [2, 1] are different permutations.
4. Understand what is a help function.

Example Input:

```
players = ["Dey", "Ruowen", "Josh", "Kinder", "Mario", "Rock", "LOL"] # 7 players
```

```
show_team_driver(players, 2) # Choose 2 from 7
```

Should output:

```
['Rock', 'LOL'] ['Mario', 'LOL'] ['Mario', 'Rock'] ['Kinder', 'LOL'] ['Kinder', 'Rock'] ['Kinder', 'Mario'] ['Josh', 'LOL'] ['Josh', 'Rock'] ['Josh', 'Mario'] ['Josh', 'Kinder'] ['Ruowen', 'LOL'] ['Ruowen', 'Rock'] ['Ruowen', 'Mario'] ['Ruowen', 'Kinder'] ['Ruowen', 'Josh'] ['Dey', 'LOL'] ['Dey', 'Rock'] ['Dey', 'Mario'] ['Dey', 'Kinder'] ['Dey', 'Josh'] ['Dey', 'Ruowen']
```

Another example Input:

```
players = ["Dey", "Ruowen", "Josh", "Kinder", "Mario", "Rock", "LOL"] # 7 players
```

```
show_team_driver(players, 4) # Choose 4 from 7
```

▼ Should output:

```
['Kinder', 'Mario', 'Rock', 'LOL'] ['Josh', 'Mario', 'Rock', 'LOL'] ['Josh', 'Kinder', 'Rock', 'LOL'] ['Josh', 'Kinder', 'Mario', 'LOL'] ['Josh', 'Kinder', 'Mario', 'Rock'] ['Ruowen', 'Mario', 'Rock', 'LOL'] ['Ruowen', 'Kinder', 'Rock', 'LOL'] ['Ruowen', 'Kinder', 'Mario', 'LOL'] ['Ruowen', 'Kinder', 'Mario', 'Rock'] ['Ruowen', 'Josh', 'Rock', 'LOL'] ['Ruowen', 'Josh', 'Mario', 'LOL'] ['Ruowen', 'Josh', 'Mario', 'Rock'] ['Ruowen', 'Josh', 'Kinder', 'LOL'] ['Ruowen', 'Josh', 'Kinder', 'Rock'] ['Ruowen', 'Josh', 'Kinder', 'Mario'] ['Professor Day', 'Mario', 'Rock', 'LOL'] ['Professor Day', 'Kinder', 'Rock', 'LOL'] ['Professor Day', 'Kinder', 'Mario', 'LOL'] ['Professor Day', 'Kinder', 'Mario', 'Rock'] ['Professor Day', 'Josh', 'Rock', 'LOL'] ['Professor Day', 'Josh', 'Mario', 'LOL'] ['Professor Day', 'Josh', 'Mario', 'Rock'] ['Professor Day', 'Josh', 'Kinder', 'LOL'] ['Professor Day', 'Josh', 'Kinder', 'Rock'] ['Professor Day', 'Josh', 'Kinder', 'Mario'] ['Professor Day', 'Ruowen', 'Rock', 'LOL'] ['Professor Day', 'Ruowen', 'Mario', 'LOL'] ['Professor Day', 'Ruowen', 'Mario', 'Rock'] ['Professor Day', 'Ruowen', 'Kinder', 'LOL'] ['Professor Day', 'Ruowen', 'Kinder', 'Rock'] ['Professor Day', 'Ruowen', 'Kinder', 'Mario'] ['Professor Day', 'Ruowen', 'Josh', 'LOL'] ['Professor Day', 'Ruowen', 'Josh', 'Rock'] ['Professor Day', 'Ruowen', 'Josh', 'Mario'] ['Professor Day', 'Ruowen', 'Josh', 'Kinder']
```

```
import copy
```

```
def show_team(names, team_size):
```

```
    help_show_team(names, team_size, [], 0)
```

```
def help_show_team(names, team_size, result_list, position):
```

```
    """
```

```
    # Base case 1: we get enough person in the result_list.
```

```
    # Base case 2: we have checked all the players.
```



```

# Create two branches
# Branch 1 add current person to result_list
# Branch 2 does not add current person to result_list(copy)
# Move on to the next person

:param names: List[String] -- list of players
:param team_size: Int -- choose how many players
:param result_list: List[String] -- Additional list parameter
:param position: Int -- Additional index parameter for recursion

:return: Nothing to return
:print: All the combinations players
"""
if len(result_list)==team_size:
    print(result_list)
    return
elif position==len(names):
    return
temp=names[position]
new=copy.deepcopy(result_list)
position+=1
help_show_team(names, team_size, new, position)
new.append(temp)
help_show_team(names, team_size, new, position)

```

```

players = ["Dey", "Ruowen", "Josh", "Kinder", "Mario", "Rock", "I"]
show_team(players, 2)

```

```

['Rock', 'LOL']
['Mario', 'LOL']
['Mario', 'Rock']
['Kinder', 'LOL']
['Kinder', 'Rock']
['Kinder', 'Mario']
['Josh', 'LOL']
['Josh', 'Rock']
['Josh', 'Mario']
['Josh', 'Kinder']
['Ruowen', 'LOL']
['Ruowen', 'Rock']
['Ruowen', 'Mario']
['Ruowen', 'Kinder']

```

```
['Ruowen', 'Josh']
['Dey', 'LOL']
['Dey', 'Rock']
['Dey', 'Mario']
['Dey', 'Kinder']
['Dey', 'Josh']
['Dey', 'Ruowen']
```

## ▼ Problem 6

### Binary Search

Complete function `binary_search()`: this function uses a binary search to determine whether an ordered list contains a specified value. We will implement two versions of binary search:

1. Recursive
2. Iterative

```
import random

def binary_search_rec(x, sorted_list):
    # this function uses binary search to determine whether an ordered list
    # contains a specified value.
    # return True if value x is in the list
    # return False if value x is not in the list
    # If you need, you can use a helper function.
    # TO DO
    n=len(sorted_list)
    mid=sorted_list[n//2]
    if x==mid:
        return True
    elif x<mid:
        return binary_search_rec(x, sorted_list[:n//2])
    else:
        return binary_search_iter(x, sorted_list[n//2+1:])

def binary_search_iter(x, sorted_list):
    # TO DO
    # return True if value x is in the list
    # return False if value x is not in the list
    low=0
    high=len(sorted_list)
    mid=(low+high)//2
    while low<=high:
        if sorted_list[mid]==x:
            return True
        elif sorted_list[mid]<x:
```

```

        low=mid+1
        mid=(low+high)//2
    else:
        high=mid-1
        mid=(low+high)//2

def main():
    sorted_list = []
    for i in range(100):
        sorted_list.append(random.randint(0, 100))
    sorted_list.sort()

    print("Testing recursive binary search ...")
    for i in range(5):
        value = random.randint(0, 100)
        answer = binary_search_rec(value, sorted_list)
        answer2 = binary_search_iter(value, sorted_list)
        if(answer!=answer2):
            print('your code is shit')
        if (answer ==answer2== True):
            print("List contains value", value)

    else:
        print("List does not contain value", value)

    print("Testing iterative binary search ...")
    for i in range(5):
        value = random.randint(0, 100)
        answer = binary_search_iter(value, sorted_list)
        if (answer == True):
            print("List contains value", value)
        else:
            print("List does not contain value", value)

main()

```

```

Testing recursive binary search ...
List does not contain value 34
List does not contain value 86
List contains value 9
List contains value 61
List contains value 92
Testing iterative binary search ...
List contains value 75
List contains value 41
List contains value 22

```

```
List does not contain value 86
List does not contain value 31
```

## ▼ Problem 7 (Optional)

Use Turtle module draw a Tree (**Use recursion**)

Turtle module is a python built in module. Turtle module draws lines by moving the cursor.

**For example (the following works only in your IDE)**

```
import turtle

t = turtle.Turtle() # Initialize the turtle

t.left(30) # The turtle turns left 30 degrees

t.right(30) # The turtle turns right 30 degrees

t.forward(20) # The turtle moves forward 20 pixels, leave a line on the path.

t.backward(30) # The turtle moves backward 30 pixels, leave a line on the path.

... and more! In this recitation, that's all we need.'''
```

With the mind set of recursion, let's break down this problem.

1. Move forward
2. Make a turn, aim to the direction for the first branch
3. Recursion for a smaller problem
4. Make a turn, aim to the direction for the second branch
5. Recursion for a smaller problem
6. Make a turn, aim to the direction for coming back
7. Come back

Base case: If the branch is too small, stop.

Otherwise, we should create two new branches (two recursions, two smaller problems)

```
!pip3 install ColabTurtle
```

```
Collecting ColabTurtle
  Downloading ColabTurtle-2.1.0.tar.gz (6.8 kB)
Building wheels for collected packages: ColabTurtle
  Building wheel for ColabTurtle (setup.py) ... done
  Created wheel for ColabTurtle: filename=ColabTurtle-2.1.0-py3-none-any.whl s
  Stored in directory: /root/.cache/pip/wheels/0d/ab/65/cc4478508751448dfb4eck
Successfully built ColabTurtle
Installing collected packages: ColabTurtle
Successfully installed ColabTurtle-2.1.0
```

```

from ColabTurtle import Turtle

def draw_tree(branchLen,t):
    """
    Figure out the tree pattern, then display the recursion tree.
    You may have to play/tune with angles/lengths to draw a prett

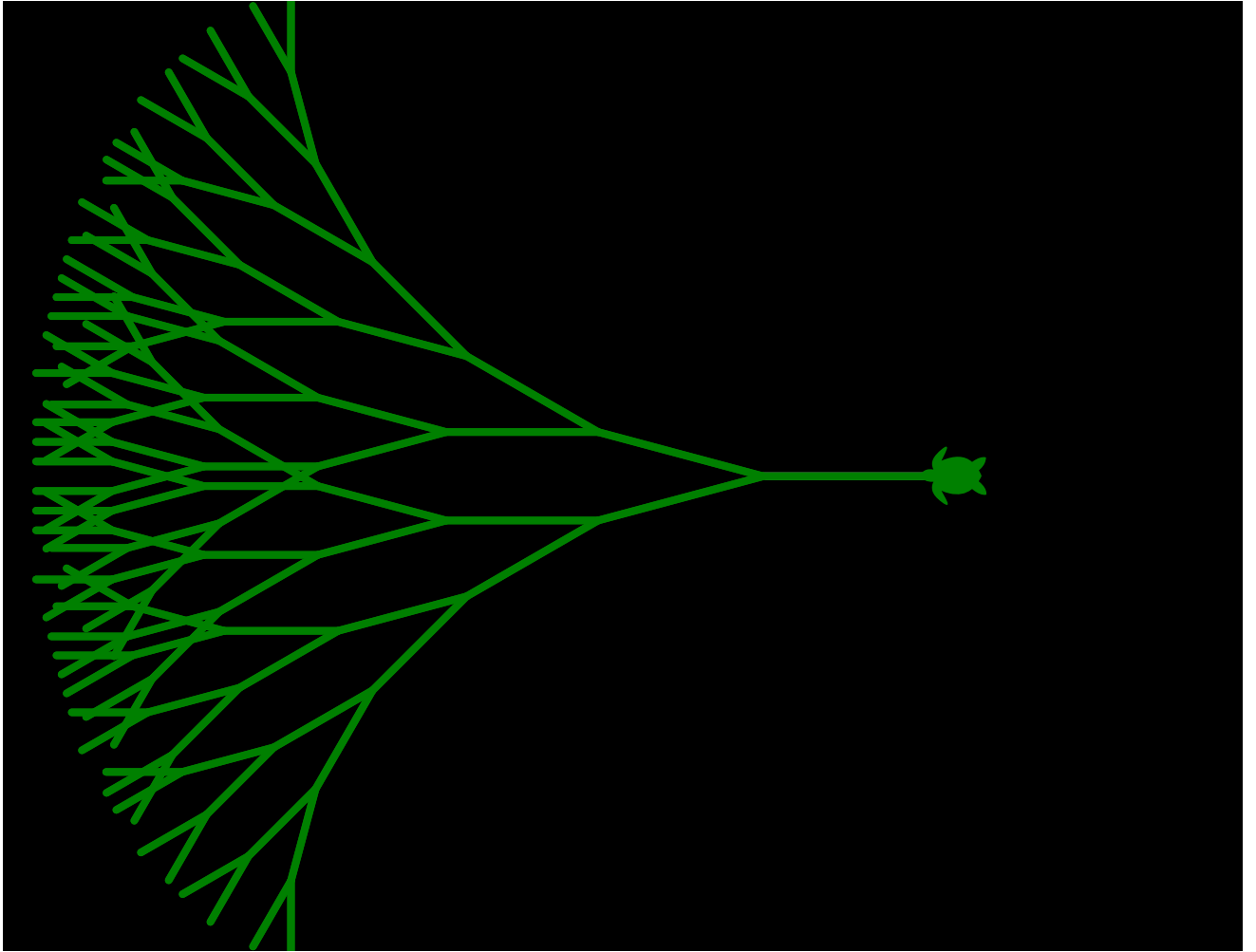
    :param branchLen: Int -- Length of this branch. Should reduce
    :param t: turtle.Turtle -- Instance of turtle module. We can

    :return: Nothing to return
    """
    if branchLen<31:
        return
    t.forward(branchLen)
    t.left(15)
    branchLen-=10
    draw_tree(branchLen, t)
    t.right(30)
    draw_tree(branchLen, t)
    t.left(15)
    branchLen+=10
    t.backward(branchLen)
    return

def main():
    Turtle.initializeTurtle(initial_speed=5)
    Turtle.left(90)
    Turtle.backward(100)
    Turtle.color("green")
    draw_tree(100,Turtle)    # Drawing tree with branchLen = 100

main()

```



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