

discreture

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# Chapter 1

## Discreture

This is a modern C++ 11 (and 14) library designed to facilitate combinatorial research by providing fast and easy iterators to a few combinatorial objects, such as combinations, permutations, partitions, and others. The idea is to have them resemble the STL containers as much as possible, without actually storing the whole set of objects in memory.

Discreture is designed to follow the STL containers as closely as possible, by providing the standard ways of iterating. In addition, many of the algorithm described in the standard `<algorithm>` work as-is in these containers, but they should be treated as const containers.

### Example use:

““c++ #include <iostream> #include "discreture.hpp" using namespace std; using namespace dscr; int main() { combinations X(5,3); for (const auto& x : X) cout << x << endl; return 0; } “” The above code would produce the following output:

```
[ 0 1 2 ]
[ 0 1 3 ]
[ 0 2 3 ]
[ 1 2 3 ]
[ 0 1 4 ]
[ 0 2 4 ]
[ 1 2 4 ]
[ 0 3 4 ]
[ 1 3 4 ]
[ 2 3 4 ]
```

Of course, you need to link with the discreture library: `g++ -O3 -ldiscreture main.cpp`

Some tests show discreture is usually faster when compiled with clang++ instead of g++.

### Installation

To download and install, run the following commands:

```
“sh git clone https://github.com/mraggi/discreture.git cd discreture mkdir build cd build cmake
.. make sudo make install #optional “
```

You can run tests like this: `./testdiscreture`

### Combinatorial Objects

There are a few combinatorial objects, such as:

- Combinations
- Permutations
- Subsets
- Multisets
- Partitions
- Dyck Paths
- Range
- Motzkin Paths

These all follow the same design principle: The templated class is called `basic_SOMETHING<class T>`, and the most reasonable type for `T` is instantiated as `SOMETHING`. For example, `combinations` is a typedef of `basic_combinations<int>`, and `partitions` is a typedef of `basic_partitions<int>`.



## Chapter 2

## Todo List

Member `dscr::basic_combinations< IntType >::find_all` (`PartialPredicate pred`)

Perhaps one should be able to iterate over all such permutations without constructing a vector of them!



## Chapter 3

# Namespace Index

### 3.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

<a href="#">dscr</a>	Namespace under which all the discreture library resides . . . . .	<a href="#">11</a>
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## Chapter 4

# Hierarchical Index

### 4.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

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dscr::basic_dyck_paths< IntType > . . . . .	22
dscr::basic_motzkin_paths< IntType > . . . . .	24
dscr::basic_multisets< IntType > . . . . .	25
dscr::basic_partitions< IntType > . . . . .	26
dscr::basic_permutations< IntType > . . . . .	28
dscr::basic_subsets< BoolType > . . . . .	30
iterator	
dscr::basic_combinations< IntType >::iterator . . . . .	35
dscr::basic_combinations< IntType >::reverse_iterator . . . . .	44
dscr::basic_dyck_paths< IntType >::iterator . . . . .	33
dscr::basic_dyck_paths< IntType >::reverse_iterator . . . . .	45
dscr::basic_motzkin_paths< IntType >::iterator . . . . .	33
dscr::basic_multisets< IntType >::iterator . . . . .	34
dscr::basic_partitions< IntType >::iterator . . . . .	35
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dscr::basic_permutations< IntType >::iterator . . . . .	39
dscr::basic_permutations< IntType >::reverse_iterator . . . . .	42
dscr::basic_subsets< BoolType >::iterator . . . . .	37
dscr::basic_subsets< BoolType >::reverse_iterator . . . . .	41
dscr::range< IntType >::iterator . . . . .	36
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dscr::RClock . . . . .	41
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## Chapter 5

# Class Index

### 5.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

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Class of all $n$ choose $k$ combinations of size $k$ of the set $\{0,1,\dots,n-1\}$	
<a href="#">dscr::basic_dyck_paths&lt; IntType &gt;</a>	22
Class for iterating through all dyck (dyck) paths	
<a href="#">dscr::basic_motzkin_paths&lt; IntType &gt;</a>	24
Class for iterating through all motzkin paths	
<a href="#">dscr::basic_multisets&lt; IntType &gt;</a>	25
<a href="#">dscr::basic_partitions&lt; IntType &gt;</a>	26
Class of partitions of the number $n$	
<a href="#">dscr::basic_permutations&lt; IntType &gt;</a>	28
Class of all $n!$ permutation of size $n$ of the set $\{0,1,\dots,n-1\}$	
<a href="#">dscr::basic_subsets&lt; BoolType &gt;</a>	30
Class of all $2^n$ subsets of the set $\{0,1,\dots,n-1\}$ , expressed as incidence vectors	
<a href="#">dscr::basic_dyck_paths&lt; IntType &gt;::iterator</a>	33
Forward iterator class	
<a href="#">dscr::basic_motzkin_paths&lt; IntType &gt;::iterator</a>	33
Forward iterator class	
<a href="#">dscr::basic_multisets&lt; IntType &gt;::iterator</a>	34
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Forward iterator class	
<a href="#">dscr::basic_combinations&lt; IntType &gt;::iterator</a>	35
Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access	
<a href="#">dscr::range&lt; IntType &gt;::iterator</a>	36
Random access iterator class	
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Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access	
<a href="#">dscr::basic_permutations&lt; IntType &gt;::iterator</a>	39
Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access	
<a href="#">dscr::range&lt; IntType &gt;</a>	40
Similar to python <code>range(n)</code> or <code>range(n,m)</code> or <code>range(n,m,step)</code>	
<a href="#">dscr::RClock</a>	41
<a href="#">dscr::basic_subsets&lt; BoolType &gt;::reverse_iterator</a>	41
Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access	

<a href="#">dscr::basic_permutations&lt; IntType &gt;::reverse_iterator</a>	
Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access . . . . .	42
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Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access . . . . .	45
<a href="#">dscr::Sequence</a>	
A class to help store known and constant sequences, such as the factorial sequence . . . . .	46



## Chapter 6

# Namespace Documentation

### 6.1 dscr Namespace Reference

Namespace under which all the discreture library resides.

#### Classes

- class [basic\\_combinations](#)  
*class of all  $n$  choose  $k$  combinations of size  $k$  of the set  $\{0, 1, \dots, n-1\}$ .*
- class [basic\\_dyck\\_paths](#)  
*Class for iterating through all dyck (dyck) paths.*
- class [basic\\_motzkin\\_paths](#)  
*Class for iterating through all motzkin paths.*
- class [basic\\_multisets](#)
- class [basic\\_partitions](#)  
*class of partitions of the number  $n$ .*
- class [basic\\_permutations](#)  
*class of all  $n!$  permutation of size  $n$  of the set  $\{0, 1, \dots, n-1\}$ .*
- class [range](#)  
*Similar to python `range(n)` or `range(n,m)` or `range(n,m,step)`.*
- class [Sequence](#)  
*A class to help store known and constant sequences, such as the factorial sequence.*
- class [basic\\_subsets](#)  
*class of all  $2^n$  subsets of the set  $\{0, 1, \dots, n-1\}$ , expressed as incidence vectors*
- class [RClock](#)

#### Typedefs

- typedef short int **sint**
- typedef long int **lint**
- typedef long long int **llint**
- typedef unsigned char **uchar**
- typedef short unsigned int **suint**
- typedef unsigned int **nuint**
- typedef long unsigned int **luint**
- typedef long long unsigned int **lluint**
- using **combinations** = [basic\\_combinations](#)< int >

- using **dyck\_paths** = [basic\\_dyck\\_paths](#)< int >
- using **motzkin\_paths** = [basic\\_motzkin\\_paths](#)< int >
- typedef [basic\\_multisets](#)< int > **multisets**
- using **partitions** = [basic\\_partitions](#)< int >
- typedef [basic\\_permutations](#)< int > **permutations**
- typedef [basic\\_subsets](#)< bool > **subsets**
- typedef [basic\\_subsets](#)  
    < uint\_fast8\_t > **subsets\_fast**
- typedef  
    std::chrono::time\_point  
    < std::chrono::high\_resolution\_clock > **clockt**
- typedef vector< bool > **VB**
- typedef vector< char > **VC**
- typedef vector< sint > **VSI**
- typedef vector< int > **VI**
- typedef vector< lint > **VLI**
- typedef vector< nuint > **VUI**
- typedef vector< suint > **VSUI**
- typedef vector< size\_t > **VLUI**
- typedef vector< uchar > **VUC**
- typedef vector< double > **VR**

## Functions

- luint **factorial** (luint n)
- luint **binomial** (nuint n, nuint r)
- double [linear\\_convert](#) (double x, double a, double b, double u, double v)  
    *This function of x is just the linear function from [a,b] to [u,v].*
- long [abs](#) (long a)  
    *For those who hate typing fabs, labs, llabs instead of abs.*
- long long **abs** (long long a)
- template<class NumType >  
    NumType **abs** (NumType a)
- template<class IntType >  
    IntType [modulo](#) (IntType a, IntType b)  
    *This is what operator % should be but isn't (!).*
- size\_t [twoD\\_to\\_oneD](#) (nuint x, nuint y, nuint width, nuint height)  
    *Helper function to linearize tables.*
- template<class T >  
    T [Clamped](#) (T x, T a, T b)  
    *Clamps x to be in the interval [a,b].*
- template<typename T >  
    int [signof](#) (T val)  
    *Equivalent to x/|x| when x != 0, and 0 when x = 0.*
- std::default\_random\_engine & **random\_engine** ()
- bool **probability\_of\_true** (double p)
- void **randomize** ()
- double **random\_real** (double from, double upto)
- void **set\_seed\_with\_time** ()
- template<class IntType >  
    IntType **random\_int** (IntType from, IntType thru)
- double **random\_real** ()
- template<class IntType >  
    [range](#)< IntType >::iterator **operator+** (typename [range](#)< IntType >::iterator it, long int n)

- `template<class IntType >`  
`range< IntType >::iterator operator-` (typename `range< IntType >::iterator` it, long int n)
- `template<class T >`  
`void overwrite` (vector< T > &lhs, `range< T >` rhs)
- `lluint factorial` (suint n)  

$$n!$$
- `lluint binomial` (lluint n, lluint r)  
*The number of subsets of size r chosen from a set of size n.*
- `lluint catalan` (suint n)  
*The n-th catalan number.*
- `lluint motzkin` (suint n)  
*The n-th motzkin number.*
- `lluint partition_number` (suint n)
- `double diffclock` (clock\_t a, clock\_t b)
- `double diffclockt` (clockt a, clockt b)
- `double TimeFromStart` ()
- `double Chronometer` ()
- `VB operator&` (const VB &A, const VB &B)  
*Bitwise and for vector<bool>*
- `VB operator|` (const VB &A, const VB &B)  
*Bitwise or for vector<bool>*
- `std::ostream & operator<<` (std::ostream &os, const VUI &rhs)
- `std::ostream & operator<<` (std::ostream &os, const VUC &rhs)  
*Specialization for vector printouts for vector<unsigned char>*
- `std::ostream & operator<<` (std::ostream &os, const VSUI &rhs)
- `std::ostream & operator<<` (std::ostream &os, const VB &rhs)  
*Specialization for vector printouts for vector<bool> so that it doesn't print out spaces.*
- `std::ostream & operator<<` (std::ostream &os, const vector< VB > &rhs)
- `template<class T , class U >`  
`vector< T > Convert` (const vector< U > &G)  
*Converts a vector<U> into a vector<T>, provided U can be converted to T.*
- `template<class numType >`  
`double Sum` (const vector< numType > &vi)  
*Finds the sum of all elements of vector. Returns a double because it's easier.*
- `template<class T >`  
`std::ostream & operator<<` (std::ostream &os, const vector< T > &rhs)  
*prints out a space separated vector.*
- `template<class T >`  
`std::ostream & operator<<` (std::ostream &os, const std::list< T > &rhs)  
*prints out a space separated list.*
- `template<class T >`  
`T min` (const vector< T > &v)  
*Find the minimum value of a vector.*
- `template<class T >`  
`T max` (const vector< T > &v)  
*Find the max value of a vector.*
- `template<class T >`  
`size_t argmin` (const vector< T > &v)  
*Find the minimum index of a vector.*
- `template<class T >`  
`size_t argmax` (const vector< T > &v)  
*Find the maximum index of a vector.*

- `template<class T >`  
`vector< T > operator+ (const vector< T > &U, const vector< T > &V)`  
*vector coordinate-wise addition.*
- `template<class T >`  
`void operator+= (vector< T > &U, const vector< T > &V)`  
*inplace vector coordinate-wise addition.*
- `template<class T , class NumType >`  
`void operator/= (vector< T > &U, NumType t)`  
*inplace vector coordinate-wise division by a number.*
- `template<class T , class NumType >`  
`void operator*= (vector< T > &U, NumType t)`  
*inplace vector coordinate-wise multiplication by a number.*
- `template<class T , class NumType >`  
`vector< T > operator* (vector< T > U, NumType t)`  
*coordinate-wise multiplication by a number.*
- `template<class T , class NumType >`  
`vector< T > operator/ (vector< T > U, NumType t)`  
*coordinate-wise division by a number.*
- `template<class T >`  
`vector< T > mincac (const vector< T > &U, const vector< T > &V)`  
*returns a vector W such that for each coordinate i,  $W[i] = \min(V[i], U[i])$*
- `template<class T >`  
`vector< T > maxcac (const vector< T > &U, const vector< T > &V)`  
*returns a vector W such that for each coordinate i,  $W[i] = \max(V[i], U[i])$*
- `template<class T >`  
`bool operator<= (const vector< T > &A, const vector< T > &B)`  
*Lexicographic compare vector A and B.*
- `template<class T >`  
`bool operator== (const vector< T > &A, const vector< T > &B)`  
*Equality comparison of vectors.*
- `template<class T >`  
`VB CombinationToSubset (const vector< T > &C, size_t size)`  
*Given a subset S, written in combination form (1,2,4), returns the same subset written in subset form (01101)*
- `template<class vecT , class UIntType >`  
`vecT compose (const vecT &f, const vector< UIntType > &g)`  
*Function composition.*
- `template<class T >`  
`bool AreTheyAllDifferent (const vector< T > &G)`

## Variables

- `constexpr double pi = 3.1415926535897932384626433832795`
- `constexpr double e = 2.718281828459045`
- `constexpr double phi = 1.618033988749895`

### 6.1.1 Detailed Description

Namespace under which all the discreture library resides.

### 6.1.2 Function Documentation

#### 6.1.2.1 `lluint dscr::binomial ( lluint n, lluint r )`

The number of subsets of size r chosen from a set of size n.

## Parameters

$n$	is a (small) nonnegative integer
$r$	is a small integer between 0 and $n$ (inclusive)

## Returns

$$n!/(r!(n-r)!)$$
6.1.2.2 `lluint dscr::catalan ( suint  $n$  )`

The  $n$ -th catalan number.

## Parameters

$n$	is a (small) nonnegative integer
-----	----------------------------------

## Returns

$$\text{binomial}(2n,n)/(n+1)$$
6.1.2.3 `template<class vecT , class UIntType > vecT dscr::compose ( const vecT &  $f$ , const vector< UIntType > &  $g$  )`

Function composition.

## Returns

$$f \circ g$$
6.1.2.4 `lluint dscr::factorial ( suint  $n$  )`

$$n!$$

## Parameters

$n$	is a (small) nonnegative integer.
-----	-----------------------------------

## Returns

$$n!$$
6.1.2.5 `double dscr::linear_convert ( double  $x$ , double  $a$ , double  $b$ , double  $u$ , double  $v$  ) [inline]`

This function of  $x$  is just the linear function from  $[a,b]$  to  $[u,v]$ .

## Returns

$$f(x), \text{ where } f:[a,b] \rightarrow [u,v] \text{ is the only linear, monotone, bijective function.}$$
6.1.2.6 `template<class IntType > IntType dscr::modulo ( IntType  $a$ , IntType  $b$  ) [inline]`

This is what operator `%` should be but isn't (!).

C++ modulo operator `%` is dumb for negative integers:  $(-7)\%3$  returns -1, instead of 2. This fixes it.

## Returns

$$\text{an integer in } [0,b)$$

#### 6.1.2.7 `lluint dscr::motzkin ( suint n )`

The *n*-th motzkin number.

Parameters

<i>n</i>	is a (small) nonnegative integer
----------	----------------------------------

Returns

`Mn`

#### 6.1.2.8 `template<class T> bool dscr::operator<= ( const vector< T > &A, const vector< T > &B )`

Lexicographic compare vector A and B.

Returns

A <= B in lexicographic order.

#### 6.1.2.9 `template<class T> bool dscr::operator== ( const vector< T > &A, const vector< T > &B )`

Equality comparison of vectors.

Returns

A <= B in lexicographic order.

#### 6.1.2.10 `template<typename T> int dscr::signof ( T val )`

Equivalent to  $x/|x|$  when  $x \neq 0$ , and 0 when  $x = 0$ .

Returns

1 if val is positive, -1 if it's negative, and 0 if it's 0

## Chapter 7

# Class Documentation

### 7.1 `dscr::basic_combinations< IntType >` Class Template Reference

class of all  $n$  choose  $k$  combinations of size  $k$  of the set  $\{0,1,\dots,n-1\}$ .

```
#include <Combinations.hpp>
```

#### Classes

- class `iterator`  
*Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.*
- class `reverse_iterator`  
*Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.*

#### Public Types

- typedef long long int **difference\_type**
- typedef unsigned long long int **size\_type**
- typedef vector< IntType > **value\_type**
- typedef vector< IntType > **combination**

#### Public Member Functions

- `basic_combinations` (IntType n, IntType k)  
*Constructor.*
- `size_type size` () const  
*The total number of combinations.*
- `size_type get_index` (const combination &comb) const  
*Returns the ID of the iterator whose value is comb. That is, the index of combination comb in the lexicographic order.*
- IntType `get_n` () const
- IntType `get_k` () const
- `iterator get_iterator` (const combination &comb)
- const `iterator` & `begin` () const
- const `iterator` & `end` () const
- const `reverse_iterator` & `rbegin` () const
- const `reverse_iterator` & `rend` () const
- combination `operator[]` (size\_type m) const  
*Access to the m-th combination (slow for iteration)*

- `template<class PartialPredicate >`  
`iterator find_if` (PartialPredicate pred)

*This is an efficient way to construct a combination of size k which fully satisfies a predicate.*

- `template<class PartialPredicate >`  
`vector< combination > find_all` (PartialPredicate pred)

*This is an efficient way to construct all combination of size k which fully satisfy a predicate.*

## Static Public Member Functions

- static `IntType next_combination` (combination &data, IntType hint=0)
- static void `prev_combination` (combination &data)
- static void `construct_combination` (combination &data, size\_type m)
- static bool `compare` (const combination &lhs, const combination &rhs)

*Combination comparison "less than" operator. Assumes lhs and rhs have the same size.*

### 7.1.1 Detailed Description

`template<class IntType>class dscr::basic_combinations< IntType >`

class of all n choose k combinations of size k of the set {0,1,...,n-1}.

#### Parameters

<i>IntType</i>	should be an integral type with enough space to store n and k. It can be signed or unsigned.
<i>n</i>	the size of the set
<i>k</i>	the size of the combination (subset). Should be an integer such that n choose k is not bigger than the largest unsigned long int there is. For example, typically 50 choose 25 is already larger than the largest long unsigned int.
	<b>Example:</b>

```
combinations X(6,3);
for (const auto& x : X)
    cout << x << " ";
```

Prints out:

```
[ 0 1 2 ] [ 0 1 3 ] [ 0 2 3 ] [ 1 2 3 ] [ 0 1 4 ] [ 0 2 4 ] [ 1 2 4 ] [ 0 3 4 ] [ 1 3 4 ] [ 2 3 4 ] [ 0 1 5 ]
```

#### Example 2:

```
basic_combinations<short int> X(5,1);
for (const auto& x : X)
    cout << x << " ";
```

Prints out:

```
[0] [1] [2] [3] [4]
```

#### Example 3:

```
string A = "helloworld";
combinations X(A.size(),2);
for (const auto& x : X)
{
    auto b = compose(A,x);
    cout << b << "-";
}
```



Prints out:

```
he-hl-el-hl-el-ll-ho-eo-lo-lo-hw-ew-lw-lw-ow-ho-eo-lo-lo-oo-wo-hr-er-lr-lr-or-wr-or-hl-el-ll-ll-ol-wl-ol-r
```

## 7.1.2 Constructor & Destructor Documentation

**7.1.2.1** `template<class IntType > dscr::basic_combinations< IntType >::basic_combinations ( IntType n, IntType k ) [inline]`

Constructor.

Parameters

<i>n</i>	is an integer $\geq 0$
<i>k</i>	is an integer with $0 \leq k \leq n$

## 7.1.3 Member Function Documentation

**7.1.3.1** `template<class IntType > static bool dscr::basic_combinations< IntType >::compare ( const combination & lhs, const combination & rhs ) [inline], [static]`

Combination comparison "less than" operator. Assumes lhs and rhs have the same size.

Returns

true if lhs would appear before rhs in the normal iteration order, false otherwise

**7.1.3.2** `template<class IntType > template<class PartialPredicate > vector<combination> dscr::basic_combinations< IntType >::find_all ( PartialPredicate pred ) [inline]`

This is an efficient way to construct all combination of size k which fully satisfy a predicate.

This function is similar to find\_if, but it returns a vector with all combinations which satisfy pred,

### Example:

```
combinations X(12,6);
auto vall = X.find_all([](const vector<int>& comb) -> bool
{
    for (int i = 0; i < comb.size()-1; ++i)
    {
        if (comb[i]+1 == comb[i+1])
            return false;
    }
    return true;
});
for (const auto& v : vall)
    cout << v << endl;
```

Prints out: [0 2 4 6 8][0 2 4 6 9][0 2 4 7 9][0 2 5 7 9][0 3 5 7 9][1 3 5 7 9] which are all combinations which don't contain two consecutive elements

Parameters

<i>Pred</i>	should be what we call a <i>partial predicate</i> : It takes a combination as a parameter and returns either true or false.
-------------	---

**Returns**

An vector<combination> filled with all permutations which fully satisfy the predicate.

**Todo** Perhaps one should be able to iterate over all such permutations without constructing a vector of them!

**7.1.3.3** `template<class IntType > template<class PartialPredicate > iterator dscr::basic_combinations< IntType >::find_if ( PartialPredicate pred ) [inline]`

This is an efficient way to construct a combination of size k which fully satisfies a predicate.

This function is conceptually equivalent to `std::find_if(begin(), end(), Pred)`, but much faster if the predicate can be evaluated on a partial combination (so as to prune the search tree)

**Example:**

```
combinations X(40,6);
auto it = X.find_if([](const vector<int>& comb) -> bool
{
    for (int i = 0; i < comb.size()-1; ++i)
    {
        if (2*comb[i] + 1 > comb[i+1])
            return false;
    }
    return true;
});
cout << *it << endl;
```

Prints out: [ 0 1 3 7 15 31 ]

**Parameters**

<i>Pred</i>	should be what we call a <i>partial predicate</i> : It takes a combination as a parameter and returns either true or false.
-------------	---

**Returns**

An iterator to a combination which fully satisfies the predicate.

**7.1.3.4** `template<class IntType > size_type dscr::basic_combinations< IntType >::get_index ( const combination & comb ) const [inline]`

Returns the ID of the iterator whose value is *comb*. That is, the index of combination *comb* in the lexicographic order.

Inverse of operator[]. If combination *x* is the *m*-th combination, then `get_index(x)` is *m*. If one has a `combinations::iterator`, then the member function `ID()` should return the same value.

**Returns**

the index of combination *comb*, as if `basic_combinations` was a proper data structure

**Note**

This constructs the proper index from scratch. If an iterator is already known, calling `ID` on the iterator is much more efficient.

7.1.3.5 `template<class IntType > combination dscr::basic_combinations< IntType >::operator[] ( size_type m ) const`  
`[inline]`

Access to the *m*-th combination (slow for iteration)

This is equivalent to calling `*(begin()+m)`

## Parameters

<i>m</i>	should be an integer between 0 and <a href="#">size()</a> . Undefined behavior otherwise.
----------	---

## Returns

The *m*-th combination, as defined in the order of iteration (lexicographic)

7.1.3.6 `template<class IntType > size_type dscr::basic_combinations< IntType >::size ( ) const [inline]`

The total number of combinations.

## Returns

`binomial(n,r)`

The documentation for this class was generated from the following file:

- `Combinations.hpp`

## 7.2 `dscr::basic_dyck_paths< IntType >` Class Template Reference

Class for iterating through all dyck (dyck) paths.

```
#include <DyckPaths.hpp>
```

## Classes

- class [iterator](#)  
*Forward iterator class.*
- class [reverse\\_iterator](#)  
*Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.*

## Public Types

- `typedef long long int difference_type`
- `typedef unsigned long long int size_type`
- `typedef vector< IntType > value_type`
- `typedef vector< IntType > dyck_path`

## Public Member Functions

- [basic\\_dyck\\_paths](#) (IntType n)  
*Constructor.*
- `size_type size () const`  
*The total number of dyck\_paths.*
- `IntType get_n () const`
- `const iterator & begin () const`
- `const iterator & end () const`
- `const reverse_iterator & rbegin () const`
- `const reverse_iterator & rend () const`

## Static Public Member Functions

- static void **next\_dyck\_path** (dyck\_path &data)
- static void **prev\_dyck\_path** (dyck\_path &data, IntType n)
- static std::string **to\_string** (const dyck\_path &data, const string &delim="()")

### 7.2.1 Detailed Description

template<class IntType>class dscr::basic\_dyck\_paths< IntType >

Class for iterating through all dyck (dyck) paths.

#### Parameters

<i>IntType</i>	must be a SIGNED integer type.
----------------	--------------------------------

Dyck paths, also called Catalan Paths, are paths that go from  $(0,0)$  to  $(0,2n)$ , which never go below the  $y = 0$  line, in which each step is from  $(x,y)$  to either  $(x+1,y+1)$  or  $(x+1,y-1)$  #Example Usage:

```
dyck_paths X(3)
for (const auto& x : X)
    cout << x << endl;
```

Prints out: [ 1 1 1 -1 -1 -1 ] [ 1 1 -1 1 -1 -1 ] [ 1 -1 1 1 -1 -1 ] [ 1 1 -1 -1 1 -1 ] [ 1 -1 1 -1 1 -1 ]

#### Example: Parenthesis

```
dyck_paths X(3)
for (const auto& x : X)
    cout << dyck_paths::to_string(x, "()") << endl;
```

Prints out: ((( ))) (( )) ()( ) ()( ) ()( )

### 7.2.2 Constructor & Destructor Documentation

7.2.2.1 template<class IntType > dscr::basic\_dyck\_paths< IntType >::basic\_dyck\_paths ( IntType n )  
[inline]

Constructor.

#### Parameters

<i>n</i>	is an integer $\geq 0$
----------	------------------------

### 7.2.3 Member Function Documentation

7.2.3.1 template<class IntType > size\_type dscr::basic\_dyck\_paths< IntType >::size ( ) const [inline]

The total number of dyck\_paths.

#### Returns

$\text{binomial}(2n,n)/(n+1)$

The documentation for this class was generated from the following file:

- DyckPaths.hpp

## 7.3 dscr::basic\_motzkin\_paths< IntType > Class Template Reference

Class for iterating through all motzkin paths.

```
#include <Motzkin.hpp>
```

### Classes

- class [iterator](#)

*Forward iterator class.*

### Public Types

- typedef long long int **difference\_type**
- typedef unsigned long long int **size\_type**
- typedef vector< IntType > **value\_type**
- typedef vector< IntType > **motzkin\_path**
- typedef [basic\\_combinations](#)  
< IntType >::iterator **comb\_i**
- typedef [basic\\_dyck\\_paths](#)  
< IntType >::iterator **dyck\_i**

### Public Member Functions

- [basic\\_motzkin\\_paths](#) (IntType n)  
*Constructor.*
- size\_type [size](#) () const  
*The total number of motzkin\_paths.*
- IntType [get\\_n](#) () const
- const [iterator](#) & [begin](#) () const
- const [iterator](#) & [end](#) () const

### Static Public Member Functions

- static std::string [to\\_string](#) (const motzkin\_path &data, const string &delim="(-)")

#### 7.3.1 Detailed Description

```
template<class IntType>class dscr::basic_motzkin_paths< IntType >
```

Class for iterating through all motzkin paths.

#### Parameters

<i>IntType</i>	must be a SIGNED integer type.
----------------	--------------------------------

Motzkin paths are paths that go from  $(0,0)$  to  $(0,2n)$ , which never go below the  $y = 0$  line, in which each step is from  $(x,y)$  to either  $(x+1,y+1)$  or  $(x+1,y-1)$  or  $(x+1,y)$  #Example Usage:

```
motzkin_paths X(4)
for (const auto& x : X)
    cout << x << endl;
```

Prints out: [ 0 0 0 0 ] [ 1 -1 0 0 ] [ 1 0 -1 0 ] [ 0 1 -1 0 ] [ 1 0 0 -1 ] [ 0 1 0 -1 ] [ 0 0 1 -1 ] [ 1 1 -1 -1 ] [ 1 -1 1 -1 ]

### Example: Parenthesis

```
motzkin_paths X(4)
for (const auto& x : X)
    cout << motzkin_paths::to_string(x, "(-)") << endl;
```

Prints out:

()- (-)- -()- (-) -(-) -() (()) (())

## 7.3.2 Constructor & Destructor Documentation

**7.3.2.1** `template<class IntType > dscr::basic_motzkin_paths< IntType >::basic_motzkin_paths ( IntType n )`  
`[inline]`

Constructor.

Parameters

<i>n</i>	is an integer $\geq 0$
----------	------------------------

## 7.3.3 Member Function Documentation

**7.3.3.1** `template<class IntType > size_type dscr::basic_motzkin_paths< IntType >::size ( ) const` `[inline]`

The total number of motzkin\_paths.

Returns

M\_n

The documentation for this class was generated from the following file:

- Motzkin.hpp

## 7.4 dscr::basic\_multisets< IntType > Class Template Reference

### Classes

- class [iterator](#)

### Public Types

- typedef long long int **difference\_type**
- typedef unsigned long long int **size\_type**
- typedef vector< IntType > **value\_type**
- typedef vector< IntType > **multiset**

### Public Member Functions

- [basic\\_multisets](#) (const vector< IntType > &set)  
*class of all submultiset of a given set, expressed as incidence vectors with multiplicities*
- **basic\_multisets** (IntType size, IntType n=1)

- `size_type size () const`
- `const iterator & begin () const`
- `const iterator & end () const`

### 7.4.1 Constructor & Destructor Documentation

**7.4.1.1** `template<class IntType > dscr::basic_multisets< IntType >::basic_multisets ( const vector< IntType > & set ) [inline]`

class of all submultiset of a given set, expressed as incidence vectors with multiplicities

#### Parameters

<i>IntType</i>	can be an int, uint, etc. It can be signed or unsigned (the negatives are not used)
	<b>Example:</b>

```
multisets X({1,0,3,1});
for (const auto& x : X)
    cout << x << " ";
```

Prints out:

```
[ 0 0 0 0 ]
[ 1 0 0 0 ]
[ 0 0 1 0 ]
[ 1 0 1 0 ]
[ 0 0 2 0 ]
[ 1 0 2 0 ]
[ 0 0 3 0 ]
[ 1 0 3 0 ]
[ 0 0 0 1 ]
[ 1 0 0 1 ]
[ 0 0 1 1 ]
[ 1 0 1 1 ]
[ 0 0 2 1 ]
[ 1 0 2 1 ]
[ 0 0 3 1 ]
[ 1 0 3 1 ]
```

TODO: Make it a random-access class and more like the others. It's not hard.

The documentation for this class was generated from the following file:

- Multisets.hpp

## 7.5 dscr::basic\_partitions< IntType > Class Template Reference

class of partitions of the number n.

```
#include <Partitions.hpp>
```

### Classes

- class `iterator`  
*Forward iterator class.*
- class `reverse_iterator`  
*Forward Iterator class.*



## Public Types

- typedef long long int **difference\_type**
- typedef unsigned long long int **size\_type**
- typedef vector< IntType > **value\_type**
- typedef vector< IntType > **partition**

## Public Member Functions

- [basic\\_partitions](#) (IntType n)  
*Constructor.*
- size\_type [size](#) () const  
*The total number of partitions.*
- IntType [get\\_n](#) () const
- const [iterator](#) & [begin](#) () const
- const [iterator](#) & [end](#) () const
- const [reverse\\_iterator](#) & [rbegin](#) () const
- const [reverse\\_iterator](#) & [rend](#) () const

## Static Public Member Functions

- static void [next\\_partition](#) (partition &data, IntType n)
- static void [prev\\_partition](#) (partition &data, IntType n)
- static partition [conjugate](#) (const partition &P)

### 7.5.1 Detailed Description

template<class IntType>class dscr::basic\_partitions< IntType >

class of partitions of the number n.

#### Parameters

<i>IntType</i>	should be an integral type with enough space to store n and k. It can be signed or unsigned.
	<b>Example:</b>

```
partitions X(6);
for (auto& x : X)
    cout << x << " ";
```

Prints out:

```
[ 1 1 1 1 1 1 ] [ 2 1 1 1 1 ] [ 3 1 1 1 ] [ 2 2 1 1 ] [ 4 1 1 ] [ 3 2 1 ] [ 2 2 2 ] [ 5 1 ] [ 4 2 ] [ 3 3 ] [
```

### 7.5.2 Constructor & Destructor Documentation

7.5.2.1 template<class IntType > dscr::basic\_partitions< IntType >::basic\_partitions ( IntType n ) [inline]

Constructor.

## Parameters

$n$	is an integer $\geq 0$
-----	------------------------

### 7.5.3 Member Function Documentation

7.5.3.1 `template<class IntType > size_type dscr::basic_partitions< IntType >::size ( ) const` `[inline]`

The total number of partitions.

## Returns

`p_n`

The documentation for this class was generated from the following file:

- Partitions.hpp

## 7.6 dscr::basic\_permutations< IntType > Class Template Reference

class of all  $n!$  permutation of size  $n$  of the set  $\{0,1,...,n-1\}$ .

```
#include <Permutations.hpp>
```

## Classes

- class [iterator](#)  
*Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.*
- class [reverse\\_iterator](#)  
*Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.*

## Public Types

- typedef long long int **difference\_type**
- typedef unsigned long long int **size\_type**
- typedef vector< IntType > **value\_type**
- typedef vector< IntType > **permutation**

## Public Member Functions

- [basic\\_permutations](#) (IntType n)  
*Constructor.*
- size\_type [size](#) () const  
*The total number of permutations.*
- permutation [identity](#) () const  
*Returns the identity permutation: [1, 2, 3, ... , (n-1)].*
- permutation [random](#) () const  
*Constructs a random permutation of {0,1,2,...,n-1}.*
- size\_type [get\\_index](#) (const permutation &perm, size\_t start=0)  
*Returns the ID of the iterator whose value is perm. That is, the index of permutation perm in the lexicographic order.*
- const [iterator](#) & **begin** () const
- const [iterator](#) & **end** () const

- const [reverse\\_iterator](#) & **rbegin** () const
- const [reverse\\_iterator](#) & **rend** () const
- permutation [operator\[\]](#) (size\_type m) const

*Access to the m-th permutation (slow for iteration)*

## Static Public Member Functions

- static void **construct\_permutation** (permutation &data, size\_type m)

### 7.6.1 Detailed Description

template<class IntType>class dscr::basic\_permutations< IntType >

class of all n! permutation of size n of the set {0,1,...,n-1}.

#### Parameters

<i>IntType</i>	should be an integral type with enough space to store n and k. It can be signed or unsigned.
<i>n</i>	should be an integer <= 20, since 20! already exceeds the numeric limits of a long unsigned int C++
	<b>Example:</b>

```
permutations X(3);
for (const auto& x : X)
    cout << x << " ";
```

Prints out:

```
[ 0 1 2 ] [ 0 2 1 ] [ 1 0 2 ] [ 1 2 0 ] [ 2 0 1 ] [ 2 1 0 ]
```

#### Example 3:

```
string A = "abc";
permutations X(A.size());
for (const auto& x : X)
{
    auto b = compose(A,x);
    cout << b << "-";
}
```

Prints out: abc-acb-bac-bca-cab-cba-

### 7.6.2 Constructor & Destructor Documentation

7.6.2.1 template<class IntType > dscr::basic\_permutations< IntType >::basic\_permutations ( IntType *n* )  
[inline]

Constructor.

#### Parameters

<i>n</i>	is an integer >= 0
----------	--------------------

### 7.6.3 Member Function Documentation

**7.6.3.1** `template<class IntType > size_type dscr::basic_permutations< IntType >::get_index ( const permutation & perm, size_t start = 0 ) [inline]`

Returns the ID of the iterator whose value is perm. That is, the index of permutation perm in the lexicographic order. Inverse of operator[]. If permutation x is the m-th permutation, then get\_index(x) is m. If one has a permutations-iterator, then the member function ID() should return the same value.

#### Returns

the index of permutation comb, as if [basic\\_permutations](#) was a proper data structure

#### Note

This constructs the proper index from scratch. If an iterator is already known, calling ID() on the iterator is much more efficient.

**7.6.3.2** `template<class IntType > permutation dscr::basic_permutations< IntType >::identity ( ) const [inline]`

Returns the identity permutation: [1, 2, 3, ... , (n-1)].

#### Parameters

<i>n</i>	is an integer $\geq 0$
----------	------------------------

**7.6.3.3** `template<class IntType > permutation dscr::basic_permutations< IntType >::operator[] ( size_type m ) const [inline]`

Access to the m-th permutation (slow for iteration)

This is equivalent to calling `*(begin()+m)`

#### Parameters

<i>m</i>	should be an integer between 0 and <a href="#">size()</a> . Undefined behavior otherwise.
----------	---

#### Returns

The m-th permutation, as defined in the order of iteration (lexicographic)

**7.6.3.4** `template<class IntType > size_type dscr::basic_permutations< IntType >::size ( ) const [inline]`

The total number of permutations.

#### Returns

$n!$

The documentation for this class was generated from the following file:

- Permutations.hpp

## 7.7 dscr::basic\_subsets< BoolType > Class Template Reference

class of all  $2^n$  subsets of the set  $\{0, 1, \dots, n-1\}$ , expressed as incidence vectors

```
#include <Subsets.hpp>
```

## Classes

- class [iterator](#)  
*Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.*
- class [reverse\\_iterator](#)  
*Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.*

## Public Types

- typedef long long int **difference\_type**
- typedef unsigned long long int **size\_type**
- typedef vector< BoolType > **value\_type**
- typedef vector< BoolType > **subset**

## Public Member Functions

- [basic\\_subsets](#) (size\_t n)  
*Constructor.*
- size\_type [size](#) () const  
*The total number of subsets.*
- size\_type [get\\_index](#) (const subset &set) const  
*Returns the ID of the iterator whose value is set. That is, the index of subset sub in the lexicographic order.*
- const [iterator](#) & **begin** () const
- const [iterator](#) & **end** () const
- const [reverse\\_iterator](#) & **rbegin** () const
- const [reverse\\_iterator](#) & **rend** () const
- subset [operator\[\]](#) (size\_type m) const  
*Access to the m-th subset (slow for iteration)*

## Static Public Member Functions

- static void **next\_subset** (subset &data)
- static void **prev\_subset** (subset &data)
- static void **construct\_subset** (subset &data, size\_type m)

### 7.7.1 Detailed Description

template<class BoolType>class dscr::basic\_subsets< BoolType >

class of all  $2^n$  subsets of the set  $\{0,1,\dots,n-1\}$ , expressed as incidence vectors

#### Parameters

<i>BoolType</i>	is at least a bool, but it can be an int, uint, etc. It can be signed or unsigned.
	<b>Example:</b>

```
subsets X(4);
for (const auto& x : X)
    cout << x << " ";
```

Prints out:

```
[0000] [1000] [0100] [1100] [0010] [1010] [0110] [1110] [0001] [1001] [0101] [1101] [0011] [1011] [0111] [1111]
```

## 7.7.2 Constructor & Destructor Documentation

7.7.2.1 `template<class BoolType > dscr::basic_subsets< BoolType >::basic_subsets ( size_t n ) [inline]`

Constructor.

Parameters

<i>n</i>	is an integer $\geq 0$
----------	------------------------

## 7.7.3 Member Function Documentation

7.7.3.1 `template<class BoolType > size_type dscr::basic_subsets< BoolType >::get_index ( const subset & set ) const [inline]`

Returns the ID of the iterator whose value is set. That is, the index of subset *sub* in the lexicographic order.

Inverse of operator[]. If subset *x* is the *m*-th subset, then `get_index(x)` is *m*. If one has a `subsets::iterator`, then the member function `ID()` should return the same value.

Returns

the index of subset *sub*, as if `basic_subsets` was a proper data structure

Note

This constructs the proper index from scratch. If an iterator is already known, calling `ID` on the iterator is much more efficient.

7.7.3.2 `template<class BoolType > subset dscr::basic_subsets< BoolType >::operator[] ( size_type m ) const [inline]`

Access to the *m*-th subset (slow for iteration)

This is equivalent to calling `*(begin()+m)`

Parameters

<i>m</i>	should be an integer between 0 and <code>size()</code> . Undefined behavior otherwise.
----------	--

Returns

The *m*-th subset, as defined in the order of iteration (lexicographic)

7.7.3.3 `template<class BoolType > size_type dscr::basic_subsets< BoolType >::size ( ) const [inline]`

The total number of subsets.

Returns

$2^n$

The documentation for this class was generated from the following file:

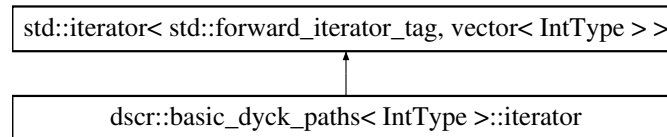
- Subsets.hpp

## 7.8 dscr::basic\_dyck\_paths< IntType >::iterator Class Reference

Forward iterator class.

```
#include <DyckPaths.hpp>
```

Inheritance diagram for dscr::basic\_dyck\_paths< IntType >::iterator:



### Public Member Functions

- **iterator** (IntType n)
- **iterator** & **operator++** ()
- **iterator** & **operator--** ()
- const vector< IntType > & **operator\*** () const
- const dyck\_path \* **operator->** () const
- size\_type **ID** () const
- bool **operator==** (const **iterator** &it) const
- bool **operator!=** (const **iterator** &it) const
- bool **is\_at\_end** (IntType n) const
- void **reset** (IntType r)

### Friends

- class **basic\_dyck\_paths**
- difference\_type **operator-** (const **iterator** &lhs, const **iterator** &rhs)

### 7.8.1 Detailed Description

```
template<class IntType>class dscr::basic_dyck_paths< IntType >::iterator
```

Forward iterator class.

The documentation for this class was generated from the following file:

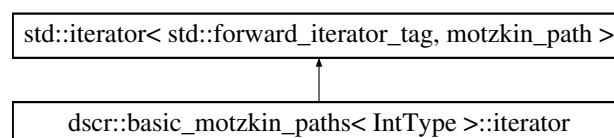
- DyckPaths.hpp

## 7.9 dscr::basic\_motzkin\_paths< IntType >::iterator Class Reference

Forward iterator class.

```
#include <Motzkin.hpp>
```

Inheritance diagram for dscr::basic\_motzkin\_paths< IntType >::iterator:



## Public Member Functions

- **iterator** (IntType n)
- **iterator** & **operator++** ()
- **iterator** & **operator--** ()
- const vector< IntType > & **operator\*** () const
- const motzkin\_path \* **operator->** () const
- size\_type **ID** () const
- bool **operator==** (const **iterator** &it) const
- bool **operator!=** (const **iterator** &it) const
- void **reset** (IntType n)

## Friends

- class **basic\_motzkin\_paths**
- difference\_type **operator-** (const **iterator** &lhs, const **iterator** &rhs)

### 7.9.1 Detailed Description

template<class IntType>class dscr::basic\_motzkin\_paths< IntType >::iterator

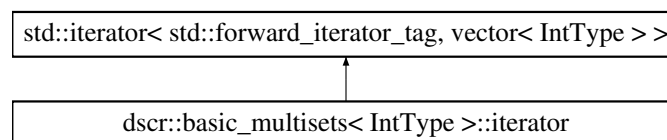
Forward iterator class.

The documentation for this class was generated from the following file:

- Motzkin.hpp

### 7.10 dscr::basic\_multisets< IntType >::iterator Class Reference

Inheritance diagram for dscr::basic\_multisets< IntType >::iterator:



## Public Member Functions

- **iterator** (const vector< IntType > &total)
- **iterator** & **operator++** ()
- const vector< IntType > & **operator\*** () const
- vector< IntType > & **operator\*** ()
- bool **operator==** (const **iterator** &it) const
- bool **operator!=** (const **iterator** &it) const

## Friends

- class **basic\_multisets**

The documentation for this class was generated from the following file:

- Multisets.hpp

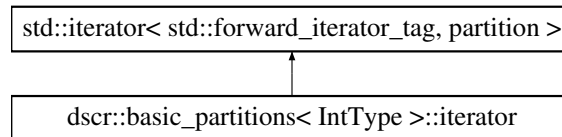


## 7.11 dscr::basic\_partitions< IntType >::iterator Class Reference

Forward iterator class.

```
#include <Partitions.hpp>
```

Inheritance diagram for dscr::basic\_partitions< IntType >::iterator:



### Public Member Functions

- **iterator** (IntType n)
- **iterator** & **operator++** ()
- **iterator** & **operator--** ()
- const vector< IntType > & **operator\*** () const
- const partition \* **operator->** () const
- size\_type **ID** () const
- bool **operator==** (const **iterator** &it) const
- bool **operator!=** (const **iterator** &it) const
- bool **is\_at\_end** (IntType n) const
- void **reset** (IntType r)

### Friends

- class **basic\_partitions**
- difference\_type **operator-** (const **iterator** &lhs, const **iterator** &rhs)

### 7.11.1 Detailed Description

```
template<class IntType>class dscr::basic_partitions< IntType >::iterator
```

Forward iterator class.

The documentation for this class was generated from the following file:

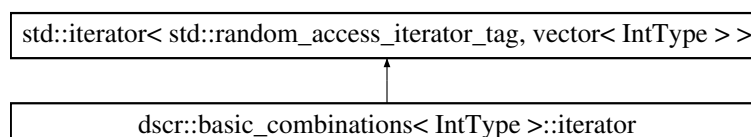
- Partitions.hpp

## 7.12 dscr::basic\_combinations< IntType >::iterator Class Reference

Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

```
#include <Combinations.hpp>
```

Inheritance diagram for dscr::basic\_combinations< IntType >::iterator:



## Public Member Functions

- **iterator** (IntType n, IntType r)
- **iterator** & **operator++** ()
- **iterator** & **operator--** ()
- const vector< IntType > & **operator\*** () const
- const combination \* **operator->** () const
- **iterator** & **operator+=** (difference\_type n)  
*Random access capabilities to the iterators.*
- **iterator** & **operator-=** (difference\_type n)
- size\_type **ID** () const
- bool **operator==** (const **iterator** &it) const
- bool **operator!=** (const **iterator** &it) const
- bool **is\_at\_end** (IntType n) const
- void **reset** (IntType n, IntType r)

## Friends

- class **basic\_combinations**
- **iterator operator+** (**iterator** lhs, difference\_type n)
- **iterator operator-** (**iterator** lhs, difference\_type n)
- difference\_type **operator-** (const **iterator** &lhs, const **iterator** &rhs)

### 7.12.1 Detailed Description

template<class IntType>class dscr::basic\_combinations< IntType >::iterator

Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

### 7.12.2 Member Function Documentation

7.12.2.1 template<class IntType > **iterator& dscr::basic\_combinations< IntType >::iterator::operator+=** ( difference\_type *n* ) [inline]

Random access capabilities to the iterators.

#### Parameters

<i>n</i>	-> This assumes $0 \leq n + ID \leq \text{size}(n, k)$
----------	--

The documentation for this class was generated from the following file:

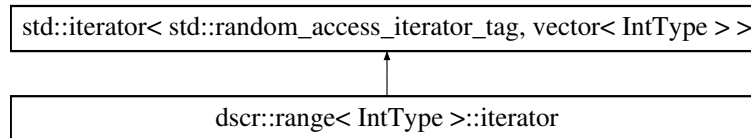
- Combinations.hpp

## 7.13 dscr::range< IntType >::iterator Class Reference

Random access iterator class.

```
#include <Range.hpp>
```

Inheritance diagram for dscr::range< IntType >::iterator:



## Public Member Functions

- **iterator** (size\_type t\_from)
- **iterator** (size\_type t\_from, size\_type t\_step)
- **iterator** & **operator++** ()
- **iterator** & **operator--** ()
- const IntType & **operator\*** () const
- **iterator** & **operator+=** (long int n)  
*Random access capabilities to the iterators.*
- **iterator** & **operator-=** (long int n)
- bool **operator==** (const **iterator** &it)
- bool **operator!=** (const **iterator** &it)
- difference\_type **operator-** (const **iterator** &it)
- size\_type **step** () const

## Friends

- class **range**

### 7.13.1 Detailed Description

template<class IntType>class dscr::range< IntType >::iterator

Random access iterator class.

### 7.13.2 Member Function Documentation

7.13.2.1 template<class IntType > iterator& dscr::range< IntType >::iterator::operator+=( long int n ) [inline]

Random access capabilities to the iterators.

#### Parameters

<i>n</i>	-> This assumes $0 \leq n+ID \leq \text{size}(n)$
----------	---

The documentation for this class was generated from the following file:

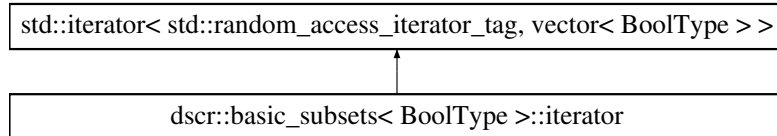
- Range.hpp

## 7.14 dscr::basic\_subsets< BoolType >::iterator Class Reference

Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

```
#include <Subsets.hpp>
```

Inheritance diagram for dscr::basic\_subsets< BoolType >::iterator:



## Public Member Functions

- **iterator** (size\_t n)
- **iterator** & **operator++** ()
- **iterator** & **operator--** ()
- const vector< BoolType > & **operator\*** () const
- **iterator** & **operator+=** (difference\_type n)  
*Random access capabilities to the iterators.*
- **iterator** & **operator-=** (difference\_type n)
- size\_type **ID** () const
- bool **operator==** (const **iterator** &it) const
- bool **operator!=** (const **iterator** &it) const
- bool **is\_at\_end** (size\_t n) const
- void **reset** (size\_t n)

## Friends

- class **basic\_subsets**
- **iterator** **operator+** (**iterator** lhs, difference\_type n)
- **iterator** **operator-** (**iterator** lhs, difference\_type n)
- difference\_type **operator-** (const **iterator** &lhs, const **iterator** &rhs)

### 7.14.1 Detailed Description

template<class BoolType>class dscr::basic\_subsets< BoolType >::iterator

Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

### 7.14.2 Member Function Documentation

7.14.2.1 template<class BoolType > iterator& dscr::basic\_subsets< BoolType >::iterator::operator+= ( difference\_type n ) [inline]

Random access capabilities to the iterators.

Parameters

<i>n</i>	-> This assumes $0 \leq n + ID \leq \text{size}(n, k)$
----------	--

The documentation for this class was generated from the following file:

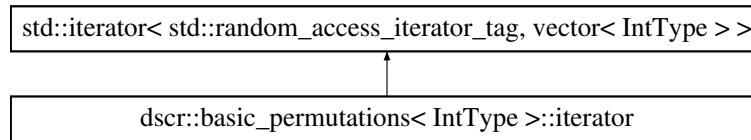
- Subsets.hpp

## 7.15 dscr::basic\_permutations< IntType >::iterator Class Reference

Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

```
#include <Permutations.hpp>
```

Inheritance diagram for dscr::basic\_permutations< IntType >::iterator:



### Public Member Functions

- **iterator** (IntType n)
- **iterator** & **operator++** ()
- **iterator** & **operator--** ()
- const vector< IntType > & **operator\*** () const
- **iterator** & **operator+=** (long int n)
- *Random access capabilities to the iterators.*
- **iterator** & **operator-=** (long int n)
- size\_type **ID** () const
- bool **operator==** (const **iterator** &it) const
- bool **operator!=** (const **iterator** &it) const
- bool **is\_at\_end** (IntType n) const
- void **reset** (IntType r)

### Friends

- class **basic\_permutations**
- **iterator operator+** (**iterator** lhs, difference\_type n)
- **iterator operator-** (**iterator** lhs, difference\_type n)
- difference\_type **operator-** (const **iterator** &lhs, const **iterator** &rhs)

#### 7.15.1 Detailed Description

```
template<class IntType>class dscr::basic_permutations< IntType >::iterator
```

Random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

#### 7.15.2 Member Function Documentation

7.15.2.1 `template<class IntType > iterator& dscr::basic_permutations< IntType >::iterator::operator+=( long int n )`  
`[inline]`

Random access capabilities to the iterators.

## Parameters

<i>n</i>	-> This assumes $0 \leq n+ID \leq \text{size}(n,k)$
----------	---

The documentation for this class was generated from the following file:

- Permutations.hpp

## 7.16 `dscr::range< IntType >` Class Template Reference

Similar to python `range(n)` or `range(n,m)` or `range(n,m,step)`.

```
#include <Range.hpp>
```

## Classes

- class [iterator](#)  
*Random access iterator class.*

## Public Types

- typedef long int **difference\_type**
- typedef IntType **size\_type**
- typedef IntType **value\_type**

## Public Member Functions

- [range](#) (IntType n)  
*Constructor.*
- **range** (IntType t\_from, IntType t\_to, IntType t\_step=1)
- size\_type **size** () const
- **operator vector< IntType >** () const
- const [iterator](#) & **begin** () const
- const [iterator](#) & **end** () const
- IntType **operator[]** (size\_type m) const

### 7.16.1 Detailed Description

```
template<class IntType>class dscr::range< IntType >
```

Similar to python `range(n)` or `range(n,m)` or `range(n,m,step)`.

## Parameters

<i>n</i>	is an integer
----------	---------------

## Returns

an abstract random-access container whose elements are  $\{n, n+1, n+2, \dots, m-1\}$

### 7.16.2 Constructor & Destructor Documentation

7.16.2.1 `template<class IntType > dscr::range< IntType >::range ( IntType n ) [inline]`

Constructor.

## Parameters

$n$	is an integer $\geq 0$
-----	------------------------

The documentation for this class was generated from the following file:

- Range.hpp

## 7.17 dscr::RClock Class Reference

### Static Public Member Functions

- static [RClock](#) & **Instance** ()

### Public Attributes

- std::chrono::time\_point  
  < std::chrono::high\_resolution\_clock > **start\_timer**
- std::chrono::time\_point  
  < std::chrono::high\_resolution\_clock > **running\_timer**

The documentation for this class was generated from the following file:

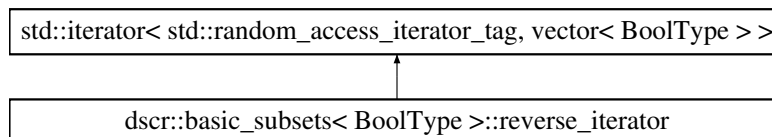
- TimeHelpers.hpp

## 7.18 dscr::basic\_subsets< BoolType >::reverse\_iterator Class Reference

Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

```
#include <Subsets.hpp>
```

Inheritance diagram for dscr::basic\_subsets< BoolType >::reverse\_iterator:



### Public Member Functions

- **reverse\_iterator** (size\_t n)
- [reverse\\_iterator](#) & **operator++** ()
- [reverse\\_iterator](#) & **operator--** ()
- const vector< BoolType > & **operator\*** ()
- const vector< BoolType > & **operator\*** () const
- [reverse\\_iterator](#) & **operator+=** (difference\_type m)  
  *Random access capabilities to the iterators.*
- [reverse\\_iterator](#) & **operator-=** (difference\_type n)
- size\_type **ID** () const
- bool **operator==** (const [reverse\\_iterator](#) &it)
- bool **operator!=** (const [reverse\\_iterator](#) &it)
- bool **is\_at\_end** () const
- void **reset** (BoolType n)

## Friends

- class **basic\_subsets**
- [reverse\\_iterator](#) **operator+** ([reverse\\_iterator](#) lhs, difference\_type n)
- [reverse\\_iterator](#) **operator-** ([reverse\\_iterator](#) lhs, difference\_type n)
- difference\_type **operator-** (const [reverse\\_iterator](#) &lhs, const [reverse\\_iterator](#) &rhs)

### 7.18.1 Detailed Description

```
template<class BoolType>class dscr::basic_subsets< BoolType >::reverse_iterator
```

Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

### 7.18.2 Member Function Documentation

7.18.2.1 `template<class BoolType > reverse_iterator& dscr::basic_subsets< BoolType >::reverse_iterator::operator+=( difference_type m ) [inline]`

Random access capabilities to the iterators.

#### Parameters

<i>n</i>	-> This assumes $0 \leq n+ID \leq \text{size}(n,k)$
----------	---

The documentation for this class was generated from the following file:

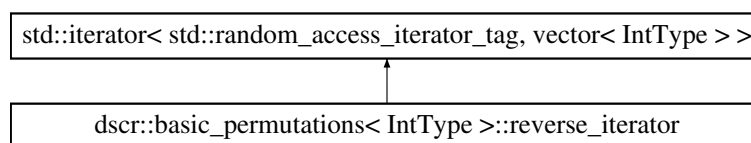
- Subsets.hpp

## 7.19 dscr::basic\_permutations< IntType >::reverse\_iterator Class Reference

Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

```
#include <Permutations.hpp>
```

Inheritance diagram for dscr::basic\_permutations< IntType >::reverse\_iterator:



## Public Member Functions

- **reverse\_iterator** (IntType n)
- [reverse\\_iterator](#) & **operator++** ()
- [reverse\\_iterator](#) & **operator--** ()
- const permutation & **operator\*** () const
- [reverse\\_iterator](#) & **operator+=** (long int m)  
*Random access capabilities to the iterators.*
- [reverse\\_iterator](#) & **operator-=** (long int n)
- size\_type **ID** () const
- bool **operator==** (const [reverse\\_iterator](#) &it) const
- bool **operator!=** (const [reverse\\_iterator](#) &it) const
- void **reset** (IntType n)



## Friends

- class **basic\_permutations**
- [reverse\\_iterator](#) **operator+** ([reverse\\_iterator](#) lhs, difference\_type n)
- [reverse\\_iterator](#) **operator-** ([reverse\\_iterator](#) lhs, difference\_type n)
- difference\_type **operator-** (const [reverse\\_iterator](#) &lhs, const [reverse\\_iterator](#) &rhs)

### 7.19.1 Detailed Description

```
template<class IntType>class dscr::basic_permutations< IntType >::reverse_iterator
```

Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

### 7.19.2 Member Function Documentation

7.19.2.1 `template<class IntType > reverse_iterator& dscr::basic_permutations< IntType >::reverse_iterator::operator+=( long int m ) [inline]`

Random access capabilities to the iterators.

#### Parameters

<i>n</i>	-> This assumes 0 <= n+ID <= size(n,k)
----------	--

The documentation for this class was generated from the following file:

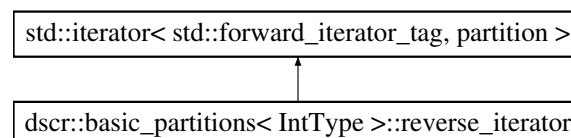
- Permutations.hpp

## 7.20 dscr::basic\_partitions< IntType >::reverse\_iterator Class Reference

Forward Iterator class.

```
#include <Partitions.hpp>
```

Inheritance diagram for dscr::basic\_partitions< IntType >::reverse\_iterator:



## Public Member Functions

- **reverse\_iterator** (IntType n)
- [reverse\\_iterator](#) & **operator++** ()
- [reverse\\_iterator](#) & **operator--** ()
- const partition & **operator\*** ()
- const partition & **operator\*** () const
- const partition \* **operator->** () const
- size\_type **ID** () const
- bool **operator==** (const [reverse\\_iterator](#) &it)
- bool **operator!=** (const [reverse\\_iterator](#) &it)

## Friends

- class **basic\_partitions**
- difference\_type **operator-** (const [reverse\\_iterator](#) &lhs, const [reverse\\_iterator](#) &rhs)

### 7.20.1 Detailed Description

template<class IntType>class dscr::basic\_partitions< IntType >::reverse\_iterator

Forward Iterator class.

The documentation for this class was generated from the following file:

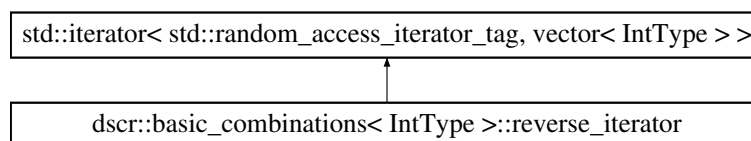
- Partitions.hpp

## 7.21 dscr::basic\_combinations< IntType >::reverse\_iterator Class Reference

Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

```
#include <Combinations.hpp>
```

Inheritance diagram for dscr::basic\_combinations< IntType >::reverse\_iterator:



## Public Member Functions

- **reverse\_iterator** (IntType n, IntType r)
- [reverse\\_iterator](#) & **operator++** ()
- [reverse\\_iterator](#) & **operator--** ()
- const combination & **operator\*** ()
- const combination & **operator\*** () const
- const combination \* **operator->** () const
- [reverse\\_iterator](#) & **operator+=** (difference\_type m)

*Random access capabilities to the iterators.*

- [reverse\\_iterator](#) & **operator-=** (difference\_type n)
- size\_type **ID** () const
- bool **operator==** (const [reverse\\_iterator](#) &it)
- bool **operator!=** (const [reverse\\_iterator](#) &it)
- bool **is\_at\_end** () const
- void **reset** (IntType n, IntType r)

## Friends

- class **basic\_combinations**
- [reverse\\_iterator](#) **operator+** ([reverse\\_iterator](#) lhs, difference\_type n)
- [reverse\\_iterator](#) **operator-** ([reverse\\_iterator](#) lhs, difference\_type n)
- difference\_type **operator-** (const [reverse\\_iterator](#) &lhs, const [reverse\\_iterator](#) &rhs)

### 7.21.1 Detailed Description

```
template<class IntType>class dscr::basic_combinations< IntType >::reverse_iterator
```

Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

### 7.21.2 Member Function Documentation

```
7.21.2.1 template<class IntType > reverse_iterator& dscr::basic_combinations< IntType
>::reverse_iterator::operator+=( difference_type m ) [inline]
```

Random access capabilities to the iterators.

Parameters

<i>n</i>	-> This assumes $0 \leq n+ID \leq \text{size}(n,k)$
----------	---

The documentation for this class was generated from the following file:

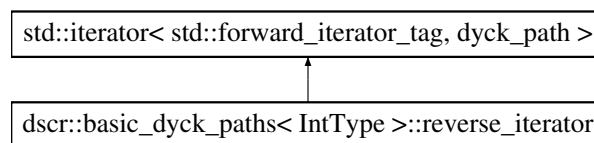
- Combinations.hpp

## 7.22 dscr::basic\_dyck\_paths< IntType >::reverse\_iterator Class Reference

Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

```
#include <DyckPaths.hpp>
```

Inheritance diagram for dscr::basic\_dyck\_paths< IntType >::reverse\_iterator:



### Public Member Functions

- **reverse\_iterator** (IntType n)
- **reverse\_iterator** & **operator++** ()
- **reverse\_iterator** & **operator--** ()
- const dyck\_path & **operator\*** ()
- const dyck\_path & **operator\*** () const
- const dyck\_path \* **operator->** () const
- size\_type **ID** () const
- bool **operator==** (const **reverse\_iterator** &it)
- bool **operator!=** (const **reverse\_iterator** &it)

### Friends

- class **basic\_dyck\_paths**
- difference\_type **operator-** (const **reverse\_iterator** &lhs, const **reverse\_iterator** &rhs)

### 7.22.1 Detailed Description

```
template<class IntType>class dscr::basic_dyck_paths< IntType >::reverse_iterator
```

Reverse random access iterator class. It's much more efficient as a bidirectional iterator than purely random access.

The documentation for this class was generated from the following file:

- DyckPaths.hpp

## 7.23 dscr::Sequence Class Reference

A class to help store known and constant sequences, such as the factorial sequence.

```
#include <Sequences.hpp>
```

### Friends

- `lluint factorial` (`suint n`)  
 *$n!$*
- `lluint binomial` (`lluint n`, `lluint r`)  
*The number of subsets of size  $r$  chosen from a set of size  $n$ .*
- `lluint catalan` (`suint n`)  
*The  $n$ -th catalan number.*
- `lluint motzkin` (`suint n`)  
*The  $n$ -th motzkin number.*
- `lluint partition_number` (`suint n`)

### 7.23.1 Detailed Description

A class to help store known and constant sequences, such as the factorial sequence.

### 7.23.2 Friends And Related Function Documentation

#### 7.23.2.1 `lluint binomial ( lluint $n$ , lluint $r$ )` `[friend]`

The number of subsets of size  $r$  chosen from a set of size  $n$ .

##### Parameters

$n$	is a (small) nonnegative integer
$r$	is a small integer between 0 and $n$ (inclusive)

##### Returns

$n!/(r!*(n-r)!)$

#### 7.23.2.2 `lluint catalan ( suint $n$ )` `[friend]`

The  $n$ -th catalan number.

## Parameters

$n$	is a (small) nonnegative integer
-----	----------------------------------

## Returns

$\text{binomial}(2n,n)/(n+1)$

7.23.2.3 lluint factorial ( suint  $n$  ) [friend]

$n!$

## Parameters

$n$	is a (small) nonnegative integer.
-----	-----------------------------------

## Returns

$n!$

7.23.2.4 lluint motzkin ( suint  $n$  ) [friend]

The  $n$ -th motzkin number.

## Parameters

$n$	is a (small) nonnegative integer
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## Returns

$M_n$

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