Prim's aporithm Let (V, E) Le a connected proph of an associated cost function 1. Itent by choosing some vertex $v \in V$. Our starting subject is (iv), p).

2. List all edges in E in a greene so that the cost of the edges is non-decreasing in the greene, i.e. if $e, e' \in E$ and if c(e) < c(e'), then e precedes e' in the greene. C: E-> R.

3. We identify the first edge in the grove, which has one (51) vertex included in the current this josph and the other vertex mot included in the subgraph. We add that edge to the unvert subgraph as well as the vertex not already included. Since the subgraph with which we started was a true, the resultance subgraph is a true (we added one vertex and one edge). Continue this process until it is not possible to proceed any further, i.e. we have added all writes in V.

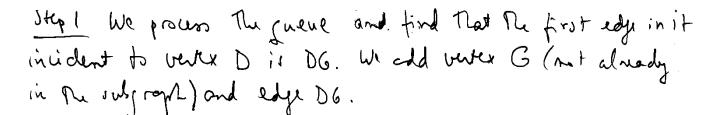
The fact at each stage we have a tree, and at the end that true contains all vertices in V justantees that Prim's Aljorithm yields a spanning true. The fact that we choose what edge to add next by following the greene of edges ordered by cast justantees that the true we obtain is a minimal spanning true of the original connected graph (V, E).

Let us illustrate Prim's Algorithm on The same growth we und for Kruskal's algorithm.

Example Consider B 3 C 4 F 5 F 6 4 H

We use The same greene as sefere AB, EH, FH, AC, EF, BC, DG, DE, CF, GH, BE, BD, CE.

We have a choice which vertex we take to start the algorithm. Let us choose vertex D. So of step O, we have (ID3, \$)



D

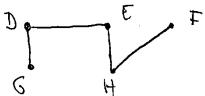
Ity 2 We process the jueue looking for the first edge incident to either vertex D or vertex G and find DE. We add vertex E and edge DE.

D

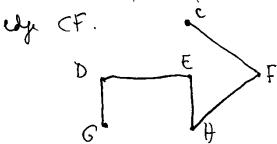
almosty in the subgraph

Sty 3 We prouse the gueve from the beginning again booking for the first edge incident to D, E or G and find EH. We add vertex E (not already in the subgroups) and edge EH.

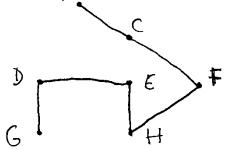
Stupy we prouse the juene from the seginning again looking for the first edge incident to D, E, G on H with an endpoint mot in the M ED, E, G, H) and that FH. We add vertex F and edge FH.



Sty 5 We prous the judice from the Seginning looking for the first edge incident to D, E, F, G or H with the other endpoint mot in 2D, E, F, G, H) and find CF. We add vertex C and



Sty 6 We prison The Jineue from The Syinning looking (52) for The first edge incident to C,D,E, F, G or H: W The other endpoint not in {C,D,E,F,G,H} and find AC. We add renter A and edge AC.



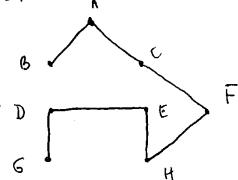
Step 7 We prouse the grower from The Seyinning looking for Re

First edge in ident to A, C, D, E, F, G or H wy the other endpoint

Not in {A, C, D, E, F, G, H} and find AB. We add vertix B and

edge AB.

A



We have recovered all verbies of the original graph so the algorithm ends here. Frim's Algorithm produced the same true or Kruskal's in this case sites the same suerce.

Remarks

I) just eike Kruskel', Alporithm, Prim's Alporithm produces a unique minimal spanning true if no two edges have the same cost. If there are edges of the same cost, runhiffing them yields different grows that in turn yield different minimal spanning trus.

2) We make a choice as to which vertex kickstarts Prints Alporithm. Different choices yield different trees at The inthrmediate steps of the appointm. by the minimal spanning true Gilded by Prim's Algorithm is called the Prim spanning true.

Prim's Algorithm. All ventions in Vi an called visited vertices.

If (V,E) is the original connected graph on which Prim's Algorithm is seing applicat, all ventions in VIVI are called the unvisited ventions.