NATIONAL RESEARCH UNIVERSITY HIGHER SCHOOL OF ECONOMICS

The Faculty of Economics Science

Department of Applied Economics

DIPLOMA

FACTOR-AUGMENTED VECTOR AUTOREGRESSION FOR FORECASTING RUSSIAN MACROECONOMIC TIME SERIES.

Petr Garmider, BEC 165

Advisor:

 ${ \mbox{Boris Demeshev},}$ Senior Lecturer, ${ \mbox{Department of Applied Economics} }$

Moscow

17 April 2020

Abstract

There are several models used for time series forecasts that focus on incorporating a huge set of information. Conventional VAR fails to employ such an approach because of the "degrees of freedom" problem. The focus of this paper is to test factor-augmented VAR's ability to forecast main Russian macroeconomic indicators. Results will be presented in a table of RMSEs for different horizons using time series cross-validation procedure for each one. There are reasons to believe, that FAVAR will show better results than univariate models in long- term forecasts.

1 Introduction

1.1 Overview

Forecasting of macroeconomic time series is an important task for different economic institutions. Accurate forecasts for main macro indicators allow central banks to timely react to possible dangers for the economy. Proper actions conducted by the central bank may prevent a possible recession or the same way, wrong actions may result in initiating one. Since some of its instruments have a delay time after its decision will have an impact on the economy, central banks especially interested in forecasts to be able to influence a situation while it is possible.

Macro indicators forecasts are useful for commercial companies as well. There are many scenarios in which corporations are particularly interested in understanding possible future macro factor outcomes, such as: choosing the right price policy, signing long-term contracts with counterparties, making decisions on the possibility of entering a new market, etc. One cannot deny that a huge amount of financial instruments heavily dependent on macroeconomic situation within the country. Investors in attempts to value

a particular financial asset always build a forecast of its determinants. In this way, almost everything to some extent shows comovement with one or another macro factor. This demonstrates that forecasting macroeconomic time series is an extremely crucial part of quite a huge range of spheres.

There are a number of models used for time series prediction. Each model uses a different approach to dealing with time series. Some approaches do not require any assumptions about data and aimed to minimize proper loss function in a specific manner. The other includes restrictions on data, assuming, for example, the presence of the data-generating process with parameters that are to be estimated. State-of-the-art models, usually employ mixed approaches such as forecast is based on results of the two mentioned methods. Models of the first type show high accuracy of prediction, however, they fail to interpret its results and prone to outliers. Models of the second type, on the contrary, show moderate accuracy, though, give information about moving forces and produce quite robust results. The last approach, as one can understand tries to balance between advantages and disadvantages of such approaches. Of course, there are plenty of other models with different views on data.

One can divide the second type of model onto two subcategories: univariate and multivariate. To make a forecast for the considering time series more accurate, the last method tries to use additional data, while first assumes the data generating process of a particular series to be a function of past realizations of itself and only. This paper mostly deals with multivariate models: vector autoregression (VAR) suggested by Sims (1980) and its variation factor-augmented VAR that aimed to eliminate drawbacks of classical version.

In this paper I will consider factor-augmented vector autoregression (FAVAR): method of estimation, its application for forecasting purposes, and

accuracy evaluation of produced forecast. There is no academic literature that uses FAVAR model for Russian macroeconomic time series prediction. The goal is to understand, whether the factor model outperform univariate approach. One also may be interested in comparing classical VAR with its augmented version. It will be shown, that VAR is a restricted model of FAVAR, therefore it is possible to test whether the difference between the two is statistically significant.

1.2 Literature review

Several studies discuss FAVAR model and employ its potential for particular purposes. Bernanke et al. (2005) were first to introduce a model to incorporate a huge set of information to assess structural shocks effect on monetary policy. They discuss Sims (1992) and his interpretation of the "price puzzle" when several papers showed that VAR models predict that contractionary monetary policy shock is followed by a rise in a price level, rather than decrease as traditional macroeconomic theory suggests. Authors believe that the explanation proposed by the inventor of VAR yet had weak points, therefore suggest their way to deal with "price puzzle". In the paper authors used 120 monthly time series pointing out that central banks while making decisions on interest rate act in a "data-rich environment", considering a larger set of time series than standard VAR approach allows to include. Therefore, econometrician, ignoring this fact, faces a problem of biased estimates. They suggested two ways of how FAVAR can be estimated and one of them will be presented as pseudo-code in this work. The main goal of model inventors was to obtain correct impulse responses for variables of interest rather than producing forecasts for them.

Nevertheless, there are some works focused on applying considering

model for prediction task as well, for example, Mönch (2008) in his work uses FAVAR to forecast yield curve. The author mentions that state-of-the-art models in this sphere have a large number of parameters to estimate, which means that users cannot simply include as many explanatory variables as one wishes, so there is a risk to lose important information. Therefore, the author used the approach of latent factor extraction described in Bernanke et al. (2005) and mixed it with traditional models for yield curve prediction.

What for the time series prediction, most of the papers agree, that factor-augmented VAR shows better performance for long-term forecasts. In Figueiredo and Guillén (2013) FAVAR is used for time series forecasting of Brazilian consumer inflation (IPCA). Authors found that factor-based models outperform those of traditional AR ones on long horizons. They also considered estimation methods pointing out that ML approach strictly outperforms two-step PCA method, that is the focus of study in this paper. Pang (2010) employed a factor model for predicting GDP growth rate, unemployment, and inflation rates of the Hong Kong economy. Author's results are in line with those obtained in Figueiredo and Guillén (2013) – FAVAR performs better than simple VAR and AR models especially for long horizons. The author used 76 monthly variables that are believed to reflect the economic situation in Hong Kong. Transforming original data, the author followed the methodology suggested in Stock and Watson (2005).

Berggren and Lodenius (2016) in their paper computed Diebold-Mariano test of equal predictive accuracy, comparing FAVAR with benchmark models. The authors found, that the forecast performance of FAVAR was not statistically better than traditional VAR or AR models. Nonetheless, they claim that further research should be done towards an optimal number of lags for the factors, since they found that FAVAR with only one lag for factors performed statistically better than with twelve.

Overall, the literature suggests that the potential of FAVAR model for time series prediction task still is not fully unlocked. There is still space for improvements and experiments, for example, employing FAVAR for noneconomic time series.

1.3 Methods

There are several approaches to measure the quality of time series prediction models. Each method, however, captures one side of the model. Traditional train test split is quite sensitive to split proportion and also to structural changes that occurred after the end of a training set. For this reason, it is not fully accurate to perform this method in their traditional form.

Nonetheless, it is possible to account for h-horizon prediction power performing time-series cross-validation and treat a forecast for each horizon separately. Still results of such procedure may be argued, since a robust estimate of a model's accuracy requires a large number of observations that is problematic for Russian data available. For this reason, I will measure models' performance using time series cross-validation with expanding window.

Forecasts are measured on RMSE (root of mean square error) metric as it is quite interpretable. The chosen measure will be evaluated for different horizons separately. The formula for h-th horizon as follows:

$$RMSE = \sqrt{\frac{1}{n} \sum_{t=T+h-ts}^{T} \left[y_t - \widehat{y_{t|t-h}} \right]^2}$$

where ts – hold-out set size, $\widehat{y_{t|t-h}}$ – forecast for period t having available information up to the moment t-h.

There are several ways to estimate FAVAR model. Bernanke et al. (2005) in their work consider two, which are two-step estimation using principal components analysis to recover latent factors and one-step Bayesian

likelihood approach estimation. Authors stated that they found no obvious evidence of one method being superior to another and whether the computational cost of the first one worths it. Since cross-validation requires multiple reestimation, I simply choose the approach that is less time-consuming.

Particular properties of the two-step approach estimation make unclear distribution of estimated coefficients, therefore building right confident intervals becomes a separate task. Bernanke et al. (2005) use a bootstrap procedure for obtaining impulse response function intervals, the same is possible to apply for predictive confident intervals, however that is out of the scope of this paper. One needs a large dataset to test statistical correctness of build intervals, which is not the case in the dataset available.

2 Model

2.1 VAR

Lets Y_t be $M \times 1$ vector of variables under consideration. It is said that Y_t is a VAR(d) process if it has the following dynamic equation:

$$Y_t = A_0 + A_1 Y_{t-1} + A_2 Y_{t-2} + \dots + A_d Y_{t-d} + \varepsilon_t, \tag{1}$$

where $A_0 - M \times 1$ vector; $\forall i \neq 0$ $A_i - M \times M$ matrix; $\varepsilon_t - M \times 1$ error vector with zero mean. \hat{A}_i can be obtained by equation-by-equation least squares. One can easily check that number of parameters to be estimated equals $M(Md+1) = O(M^2)$, $M \to \infty$. For example, an econometrician should estimate 57 coefficients if one wants to use VAR(6) model with 3 variables for forecasting purposes. This means, that M is strictly limited to the number of periods. In practice, it is uncommon to see more than 6 variables included in a VAR equation. This problem particularly relevant while deal-

ing with short time series, which is the case with Russian economic data. It is hard to believe that econometrician is able to select six variables without missing an important one. Consequently, researcher generally gets biased estimates which may result, for example, in popular VAR issue that is called "price puzzle". In Bernanke et al. (2005) authors propose an explanation to this problem which completely relies on omitted equation assumption. Thus, ignoring one variable may result in incorrect economic dynamics modeling that may lead to weak forecasting performance. In order to address this issue, one can estimate FAVAR model, which allows incorporating a huge set of economic indicators without losing degrees of freedom¹.

2.2 FAVAR

This section will be based on II.A part in Bernanke et al. (2005). Let Y_t be $M \times 1$ vector of observable economic variables that are believed to reflect the dynamics of the economy. Standard VAR approach implies that Y_t contains price indicator, observable variable reflecting the economy's real output and policy instrument. Such a specification of Y_t is mainly used for structural analysis. As discussed earlier, one may argue that barely information captured by Y_t reflects the dynamics of the whole economy. Let F_t be $K \times 1$ vector of unobservable variables, where in some way K is a small number, that are assumed to summarise all the information that is not captured by Y_t . These factors are said to reflect the situation of theoretical variables, such as: "economic activity", "investment environment", "price pressure" and etc.

Assume also that dynamics of vector (F'_t, Y'_t) follows the equation:

$$\begin{bmatrix} F_t \\ Y_t \end{bmatrix} = \Phi(L) \begin{bmatrix} F_{t-1} \\ Y_{t-1} \end{bmatrix} + v_t, \tag{2}$$

¹Number of observations - number of model's parameters

where $\Phi(L) = (\Phi_0 + \Phi_1 L + \Phi_2 L^2 + ... + \Phi_d L^d)$; d – finite number; $\Phi_i - (K + M) \times (K + M)$ matrix; v_t – error term vector, such that: $\mathbb{E}(v_t) = 0$, $\mathbb{E}(v_t v_t') = Q$; Q is symmetric positive semi-definite $(K + M) \times (K + M)$ matrix; L – lag operator: $LY_t = Y_{t-1}$.

One may see, that if components of $\Phi(L)$ that relate Y_t to F_{t-1} are zeros, then Y_t is simply VAR process. Otherwise, equation (2) is VAR in (F'_t, Y'_t) . The fact, that econometrician may obtain VAR in Y_t from (2) by putting restrictions on some coefficients makes model (2) unrestricted to VAR in Y_t . This makes it possible to perform statistical tests, for instance, the likelihood ratio, that allows to check whether an unrestricted model is statistically different from a restricted one. If so, (2) is commonly called factor-augmented vector autoregression, or simply FAVAR. In the paper Bernanke et al. (2005) authors correctly note that if the true model is FAVAR, but instead VAR in Y_t is estimated, then econometrician generally gets biased estimates, therefore observes poor forecasting power of an estimated model.

Coefficients of $\Phi(L)$ cannot be estimated directly since vector F_t is unobservable. If one was provided with real values of F_t , he could apply conventional techniques of VAR estimation, equation-by-equation least squares, for example, in order to estimate (2).

It is obvious, that real dynamics of Y_t is affected by a huge number of time series, such as exchange rate, price indices, investment climate situation, import/export shocks, and many more. Let us introduce $N \times 1$ vector X_t – set of "informational" variables, where N is in some way a "large" number, specifically such that K+M << N. Unlike F_t , vector X_t is assumed to be observable. It is also believed that X_t is a linear function of observable Y_t and unobservable F_t :

$$X_t = \Lambda^f F_t + \Lambda^y Y_t + e_t, \tag{3}$$

where $\Lambda^f - N \times K$ matrix; $\Lambda^y - N \times M$; e_t - error term vector, such that: $\mathbb{E}(e_t) = 0$, $\mathbb{E}(e_{ti}e_{tj}) \approx 0 \ \forall i \neq j$. Equation (3) reflects the idea that economy can be precisely described by just K + M main indicators. All the other variables that we may observe are generated from those key ones. The main point in (3) is that F_t is still vector of unobservable variables and the idea is to exploit the fact that (F'_t, X'_t) is observed to get estimates of F_t vector. Having in some sense accurate \hat{F}_t , econometrician is able to estimate (2) in (\hat{F}'_t, Y'_t) . It is important to note, that X_t depends only on F_t and Y_t , not from lags of these vectors. Though X_t itself may contain one step ahead series.

If N is a small number, it is possible to include X_t directly in (2) and estimate VAR in (X'_t, Y'_t) . However, barely it is the truth, that central bank, for example, monitor only three or four variables, setting the key rate. Though, if a researcher wants to incorporate an additional variable in a model, it is quite unlikely that he would have enough observations to get coefficients' estimates.

There are several possible FAVAR models may be constructed depending on what a researcher initially assume. For example, it is possible to include in Y_t variables such as CPI, GDP growth, and central bank key rate, which means that researcher is uncertain about the rest structure of the economy and believe in the presence of a finite number of latent factors that fill possible model misspecification. One may also argue, that in reality we don't observe truth GDP growth and CPI. Instead, we are provided with these series estimations by some federal institutions, that are still noisy measures for true variables. Such model specification is in line with the fact, that GDP growth and CPI series are subjects for several corrections, even in a year. However, for sure, we observer the truth central bank key rate.

 $^{^2\}mathrm{One}$ can find formal requirements on e_t in Stock and Watson (2002)

2.3 Estimation

Authors in Bernanke et al. (2005) propose two ways of FAVAR estimation. The first is based on Gibbs sampling approach, which is not applicable if one desires to obtain a cross-validation model's error, since such an approach is enormously time-costly. Estimation of one model may take even an hour. The second approach is referred in Bernanke et al. (2005) as two-step principal component method, that is much more computationally efficient in time and easy in implementation. Moreover, the last approach does not require special assumptions on error-terms distributions, as well as allows some cross-correlation in it, which is more likely the truth dealing with real data.

Two-stage estimation approach includes:

- 1. Extraction of factors F_t from X_t , purifying it from the influence of Y_t .
- 2. Estimation of (2), using obtained \hat{F}_t by standard VAR methods.

In order to perform stage 1 one should use the equation (3) and exploit the fact that (X'_t, Y'_t) is observable vector for each period t. Let us remind once again equation (3):

$$X_t = \Lambda^f F_t + \Lambda^y Y_t + e_t$$

We can rewrite (3) as:

$$X_t = \left[\Lambda^f \Lambda^y\right] \begin{bmatrix} F_t \\ Y_t \end{bmatrix} + e_t \tag{4}$$

$$X_{t} = \Lambda \alpha_{t} + e_{t}, \tag{5}$$
where $\Lambda_{N \times (K+M)} \stackrel{\text{def}}{=} \left[\Lambda^{f} \Lambda^{y} \right]$ and $\alpha_{t(K+M) \times 1} \stackrel{\text{def}}{=} \begin{bmatrix} F_{t} \\ Y_{t} \end{bmatrix}$.

 $^{^3\}mathrm{To}$ get only additional information about ecnomy dynamics, that is not captured by Y_t

The idea is if econometrician came up with such $\hat{\Lambda}$ and $\hat{\alpha}_t$ that \hat{e}_t is a small number for all t, then such estimates of (3) are "good". Assume X_t is normalized to have zero mean: $\sum_{t=1}^T X_t = \left(0 \dots 0\right)_{N \times 1}'$. Then, let us then set the following minimization task:

$$\sum_{t=1}^{T} (X_t - \Lambda \alpha_t)'(X_t - \Lambda \alpha_t) \to \min_{\Lambda, \alpha_1, \alpha_2 \dots \alpha_T}$$
 (6)

It is worth noting that (6) has in total (K+M)N + (K+M)T number of parameters for estimation. It is also important to note, that there are infinite number of solutions for such optimization task. If we came up with a solution to (6) in form $(\tilde{\Lambda}, \tilde{\alpha})$ then for any $Z: Z'Z = I \Longrightarrow (\tilde{\Lambda}Z', Z\tilde{\alpha})$ is also solution of (6). Thus let us impose restriction on $\Lambda: \Lambda'\Lambda = I$, which basically means we are trying to obtain orthogonal and normalised unit-scale vectors. Problem (6) transforms to:

$$\begin{cases} \sum_{t=1}^{T} (X_t - \Lambda \alpha_t)'(X_t - \Lambda \alpha_t) \to \min_{\Lambda, \ \alpha_1, \alpha_2 \dots \alpha_T} \\ s.t. \ \Lambda' \Lambda = I \end{cases}$$
 (7)

Assuming solution $\hat{\Lambda}$ being known, optimal $\hat{\alpha}_t = (\Lambda' \Lambda)^{-1} \Lambda' X_t$. Since α_t does not affect other periods error, then we can treat (6) as T independent minimization problems, such for fixed period t:

$$(X_t - \Lambda \alpha_t)'(X_t - \Lambda \alpha_t) \to \min_{\alpha_t}$$
 (8)

With known Λ , problem (8) becomes nothing but a simple least-squares task with know analytic solution. Thus, (7) transforms to:

$$\begin{cases} \sum_{t=1}^{T} (X_t - \Lambda(\Lambda'\Lambda)^{-1} \Lambda' X_t)' (X_t - \Lambda(\Lambda'\Lambda)^{-1} \Lambda' X_t) \to \min_{\Lambda} \\ s.t. \ \Lambda'\Lambda = I \end{cases}$$
(9)

$$\begin{cases} \sum_{t=1}^{T} (X_t - \Lambda \Lambda' X_t)' (X_t - \Lambda \Lambda' X_t) \to \min_{\Lambda} \\ s.t. \ \Lambda' \Lambda = I \end{cases}$$
 (10)

Let $L = \sum_{t=1}^{T} (X_t - \Lambda \Lambda' X_t)' (X_t - \Lambda \Lambda' X_t)$, then:

$$L = \sum_{t=1}^{T} \left[(I - \Lambda \Lambda') X_t \right]' \left[(I - \Lambda \Lambda') X_t \right] =$$

$$= \sum_{t=1}^{T} X'_t (I - \Lambda \Lambda')' (I - \Lambda \Lambda') X_t =$$

$$= \sum_{t=1}^{T} X_t' (I - \Lambda \Lambda') X_t = \sum_{t=1}^{T} X_t' X_t - \sum_{t=1}^{T} X_t' \Lambda \Lambda' X_t$$

Thus, problem (10) is equivalent to:

$$\begin{cases} \sum_{t=1}^{T} X_t' \Lambda \Lambda' X_t \to \max_{\Lambda} \\ s.t. \ \Lambda' \Lambda = I \end{cases}$$
 (11)

Let $\tilde{L} = \sum_{t=1}^{T} X_t \Lambda \Lambda' X_t$, then:

$$\tilde{L} = tr(\sum_{t=1}^{T} X_t' \Lambda \Lambda' X_t) = \sum_{t=1}^{T} tr(X_t' \Lambda \Lambda' X_t)) =$$

$$= \sum_{t=1}^{T} tr(\Lambda \Lambda' X_t X_t') = tr(\sum_{t=1}^{T} \Lambda \Lambda' X_t X_t') = tr(\Lambda \Lambda' \sum_{t=1}^{T} X_t X_t'),$$

where (*) follows from the trace property: tr(AB) = tr(BA), if A and B are matrices of suitable sizes.

Let us remind that if $X_{T\times N} = \left(X_1X_2...X_T\right)'$ is matrix that have zero mean by columns, then $S_X = \frac{1}{T}\sum_{t=1}^T X_t X_t'$ – is empirical covariance matrix of X_t vector.

$$\tilde{L} = tr(\sum_{t=1}^{T} \Lambda \Lambda' X_{t} X_{t}') = tr(\Lambda \Lambda' T S_{X}) = Ttr(\Lambda' S_{X} \Lambda)$$

Thus (10) problem becomes equivalent to:

$$\begin{cases} tr(\Lambda' S_X \Lambda) \to \max_{\Lambda} \\ s.t. \ \Lambda' \Lambda = I \end{cases}$$
 (12)

Still (12) has N(K+M) parameters along which econometrician should implement optimization procedure. Though, such an optimization task has an exact analytical solution. One should compute the first K+M eigenvectors of S_X corresponding to the largest eigenvalues. These vectors are columns of $\hat{\Lambda}$ that solves maximization task (12) The fact that S_X is a symmetrical positive semi-definite matrix guarantees that it has real-valued eigenvector and eigenvalues. Columns of $\hat{\Lambda}$ are nothing but the first K+M principal components of X. Knowing solution to (12) one can easily find $\hat{\alpha}_t$ from (8). Stock and Watson (2002) showed that under certain conditions on N, that should be "large", econometrician may use only first K principle components and obtain consistent estimator of space spanned by Y_t and F_t . It is important to note, that at this moment we did not rely on the fact that Y_t is observable. For now we got K linear combinations of F_t and Y_t . In Bernanke et al. (2005) authors then perform purification procedure, which is removing Y_t from the space spanned by the first K principal component of X_t .

For stage 2 authors divide variables into two groups: fast-moving and slow-moving. The first group assumed to contemporaneously react on unexpected shocks in Y_t , whereas the second one does not respond to unanticipated fluctuations in Y_t at period t. Such variables' separation is necessary for obtaining purified factors F_t , that contains all the information apart from that in Y_t . Since impulse response functions is the main focus in Bernanke et al. (2005), absence of immediate response in F_t to shocks in Y_t is one of the requirements in some SVAR identification schemes, such as recursive identification including Choleski decomposition of residuals covariance matrix. However, there is a place for experiments if one tries to employ FAVAR methodology for forecasting purposes. In literature, there are several ways to remove dependence of obtained in stage 1 factors from Y_t . The one used in Bernanke et al. (2005) will be described below.

Let $\hat{C}(F_t, Y_t) \stackrel{\text{def}}{=} \hat{\Lambda} \hat{\alpha}_t \stackrel{(8)}{=} (\hat{\Lambda}' \hat{\Lambda})^{-1} \hat{\Lambda}' X_t \stackrel{(12)}{=} \hat{\Lambda}' X_t$, then authors estimate following model:

$$\hat{C}(F_t, Y_t) = \beta_0 + \beta_{-0} \hat{C}^{slow}(F_t) + \gamma Y_t + \nu_t, \tag{13}$$

where $\hat{C}(F_t, Y_t)$ – the first K principle components of X_t ; $\hat{C}^{slow}(F_t)$ – the first K principle components of X_t^{slow} ; $b_0 - K \times 1$ vector; $b_{-0} - K \times K$ matrix; $\gamma - K \times M$ vector, though one may include subset of Y_t variables; $v_t - K \times 1$ error vector. One can obtain $\hat{\beta}$ and $\hat{\gamma}$ using simple OLS method by rows, then:

$$\hat{F}_t = \hat{\beta}_{-0}\hat{C}^{slow}(F_t) - \hat{\gamma}Y_t$$

Presence of F_t estimates allows one to substitute F_t by \hat{F}_t in (2), which result in:

$$\begin{bmatrix} \hat{F}_t \\ Y_t \end{bmatrix} = \Phi(L) \begin{bmatrix} \hat{F}_{t-1} \\ Y_{t-1} \end{bmatrix} + \nu_t \tag{14}$$

Note once again that (14) in nothing but standard VAR model in (\hat{F}_t, Y_t) , therefore $\Phi(L)$ can be estimated using traditional VAR techniques. Summarising all, we finally get:

Algorithm 1 FAVAR estimation

 $\overline{C(F_t,Y_t)} \leftarrow \text{ the first K components of } X_t$

 $C^{slow}(F_t) \leftarrow \text{ the first K components of } X_t^{slow}$

OLS estimation results $\leftarrow \hat{C}(F_t, Y_t) = \hat{\beta}_0 + \hat{\beta}_{-0}\hat{C}^{slow}(F_t) + \hat{\gamma}Y_t$

 $\hat{F}_t \leftarrow \hat{\beta}_{-0}\hat{C}^{slow}(F_t) - \hat{\gamma}Y_t$

 $d \leftarrow \mathrm{VAR}(\hat{F}_t, Y_t)$ lag selection according to AIC

 $\underline{\text{FAVAR estimation results}} \leftarrow \underline{\text{VAR}}(d) \text{ in } (\hat{F}_t', Y_t')$

Explained procedure was used in Bernanke et al. (2005) for producing impulse response functions to policy shock. Purification is necessary for producing factors that has not respond contemporaneously to policy shock,

since authors used recursive identification with FFR (Federal Funds Rate) ordering last. For forecasting purposes, one may try to remove impact of another variables (from X_t) or skip factor purification procedure at all. Using variables in Y_t at (13) will not change result of reduced form VAR (14) that is finally used for series prediction.

2.4 Model's specifications

Once econometrician has estimated $\hat{\Phi}(L)$ in (14), h-horizon forecast for (\hat{F}_{t-1}, Y_{t-1}) is nothing but:

 $\begin{bmatrix} \hat{F}_{t+h-1} \\ \hat{Y}_{t+h-1} \end{bmatrix} = \hat{\Phi}(L)^h \begin{bmatrix} \hat{F}_{t-1} \\ Y_{t-1} \end{bmatrix}$

For a particular variable forecast, researcher takes corresponding component of \hat{Y}_{t+h-1} vector. One should also specify parameter K representing number of latent factors. I find, that K=1 is sufficient in most cases. However, K=2 sometimes helps to obtain more accurate results in short-term prediction, Interesting that $K \geq 3$ generally increases model's error for almost all horizons. There is a space for experiments still, one may receive more accurate results at some horizons selecting proper variables for Y_t .

Another approach, is to treat variable of interest z_t as "informational" (included in X_t), but I found no clear evidence that such method is more preferable than assuming z_t being observed. Such different FAVARs produce quite similar results, however there is a still place for experiments in choice of Y_t vector components.

3 Data

Data was collected from Thomson Reuters database. Dataset includes 199 monthly variables, that are assumed to represent economic situation in Rus-

sia, starting from 01/01/2000 and contains 240 observations maximum. Original data involved missings, such variables were dropped before the estimation procedure. To be in line with Bernanke et al. (2005) original time series were transformed (one or two times differencing) to induce stationarity⁴. In addition, for convenience original time series were standardised to have zero mean and unit standard deviation. Though, in order to obtain fair results, seasonal component in considered time series was not removed, since benchmark models are capable of handling seasonality in data. One can still decompose original time series on seasonal and trend components, though FAVAR methodology cannot be applied to produce seasonal component forecasts, so it becomes mix of FAVAR and other model for seasonal component. Probably such an approach will yield more accurate forecasts, but the goal of this paper to check pure FAVAR model prediction power.

Depending on variable being forecasted different number of observations was used: 238 in case of CPI and unemployment rate, 138 in case of GDP Y/Y % change forecasts.

4 Results

In order to understand FAVAR model's predictive power I decided to compare its results on cross-validation with popular univariate models, such as: ETS, ARIMA and simple random walk with drift; and restricted to FAVAR model – standard VAR (K=0). I treat variable of interest as being observed, so include it directly in Y_t vector. For ARIMA and ETS optimal model selection I used auto-ARIMA and auto-ETS funcions in "forecast" R package, that select best model specification according to AIC. Optimal lag of resulting VAR models is also selected using AIC.

⁴According to KPSS test

	FAVAR	ARIMA	ETS	VAR	RWD
h=1	0.70*	0.86	0.76	0.83	0.93
h=2	0.95*	1.09	1.02	1.07	1.37
h=3	1.01*	1.07	1.06	1.12	1.54
$h{=}4$	0.96*	1.03	1.10	1.13	1.58
h=5	0.91*	1.03	1.05	1.13	1.49
h=6	0.95*	1.07	1.07	1.15	1.47
h=7	1.00*	1.05	1.19	1.17	1.65
h=8	1.06	0.96*	1.24	1.19	1.78
h=9	1.05	0.99*	1.26	1.18	1.75
h=10	0.94*	0.98	1.21	1.02	1.57
h=11	0.90*	0.99	1.23	0.97	1.35
h=12	0.90*	1.04	1.16	0.98	1.08

Table 1: RMSE \times 100 for CPI forecasts

Table 1 shows cross-validation results for CPI forecasting. FAVAR specification includes two variables in $Y_t = (aRUCPI_t, RUCBIR = ECI_t)'$ and one latent factor K = 1. Interesting that increasing number of factors deteriorates model's quality. One can see, that such FAVAR specification completely outperform other models almost at each horizon.

	FAVAR	ARIMA	ETS	VAR	RWD
h=1	10.31	6.97*	9.90	7.13	11.39
h=2	10.25	6.95	9.75	6.74*	10.97
h=3	8.68	6.56	9.90	6.52*	10.06
h=4	8.04	6.60	9.86	6.36*	12.06
h=5	6.88	5.86	10.02	6.22*	12.00

h=6	6.10	5.94*	9.70	6.44	11.36
h=7	5.74*	6.00	9.27	6.56	12.64
h=8	5.71*	6.09	9.57	6.44	10.90
h=9	6.15*	6.15	9.66	6.17	10.40
h=10	5.90*	5.96	9.21	6.42	10.10
h=11	5.86*	5.89	9.67	6.52	9.32
h=12	6.43	5.70*	9.51	6.43	9.09

Table 2: RMSE \times 100 for unemployment rate forecasts

Table 2 shows models' cross-validation errors in attempts to forecast unemployment rate in Russia. FAVAR specification is such that $Y_t = (aRUCPI_t, RUUNR =$ $ECI_t)'$ and K = 1. As with CPI, increasing of K leads to weak performance. As one can see, for such variable, FAVAR produces best forecasts only on long horizons. Yet one can experiment with proper Y_t selection to obtain lower error at short-term forecasts.

	FAVAR	ARIMA	ETS	VAR	RWD
h=1	19.88*	22.34	21.67	20.10	38.56
h=2	20.44*	23.22	22.07	20.79	25.65
h=3	21.92*	23.79	22.59	22.37	35.73
h=4	22.40	23.13	22.35	22.31*	31.02
h=5	22.96	23.49	22.94	22.90*	34.74
h=6	22.75	22.98	22.82	22.68*	30.00
h=7	23.06*	23.66	23.15	23.17	35.66
h=8	23.46*	24.45	23.53	23.51	34.69
h=9	24.52	25.21	24.29	24.25*	33.81
h=10	22.74	25.06	22.72*	22.75	33.99

h=11	22.98	24.59	22.74	22.70*	33.43
h=12	23.09*	24.29	23.15	23.17	25.37

Table 3: RMSE \times 100 for GDP forecasts

At table 3 one can find cross-validation error for corresponding models, that are used for GDP growth rate forecasts. It is important to mention again, that for this variable only 168 observations were used, because of missings for interested time series. That might one reason explaining model's performance. Surprisingly, FAVAR produces best forecasts mostly for short-term, rather than for long-term points as was expected. FAVAR in $Y_t = (RUGDP = ECI_t, RUCBIR = ECI_t)'$ with K = 2 shows best performance on 6 out of 12 horizons, though difference is significant only for $h = \overline{1,3}$.

5 Conclusion

Results showed that FAVAR is quite competitive model in a forecasting task, even though it was initially developed as the solution for "price puzzle", that is more about impulse response functions, rather than predictions. For some series FAVAR can completely outperform traditional univariate models as well as multivariate VAR. In addition, FAVAR allows incorporating as much variables as one wants and there are reasons to believe that this will improve model's performance. Nevertheless, it still remains a question whether cost of data collection outweigh potential forecast improvement for standard VAR.

Appendixes

A Data Description

Table bellow provides information about used dataset. An asterisk *, after mnemonic of some series shows that such variables were assumed to be slow-moving. Each time series is provided with transformation applied to the original data: l – no transformations, Δ – first difference and Δ^2 – second difference.

Mnemonic	Description	
1. aRUPTTTT/C*	Passenger Transport Turnover, Price Index	\overline{l}
2. $aRUFTTCTT/C*$	Freight Transport Turnover, Cargo transport,	l
	Volume Index	
3. aRUCEXBA*	Exports of Goods, Balance of Payments Basis,	Δ
	Standardized, Current Prices	
4. aRUCIMBA*	Imports of Goods, Balance of Payments Basis,	Δ
	Standardized, Current Prices	
5. aRUCBOPA*	Visible Trade Balance, Balance of Payments Ba-	l
	sis, Standardized, Current Prices	
6. aRUCEXBPA*	Exports of Goods, Balance of Payments Basis,	l
	% month on month, Standardized, Chg P/P,	
	Current Prices	
7. aRUCIMBPA*	Imports of Goods, Balance of Payments Basis,	l
	% month on month, Standardized, Chg P/P,	
	Current Prices	
8. aRUCBOPPA*	Visible Trade Balance, Balance of Payments Ba-	l
	sis, month on month, Standardized, Absolute	
	change, Current Prices	

9. aRUCEXBYA*	Exports of Goods, Balance of Payments Basis, % year on year, Standardized, Chg Y/Y, Current Prices	Δ
10. aRUCIMBYA*	Imports of Goods, Balance of Payments Basis, % year on year, Standardized, Chg Y/Y, Current Prices	Δ
11. aRUCBOPYA*	Visible Trade Balance, Balance of Payments Basis, year on year, Standardized, Absolute change, Current Prices	l
12. RUCBIR=ECI	Central bank key rate	Δ
13. aRUBCFBNKA	Bank Lending: Loans to banks (in frgn. cur.), Current Prices	Δ
14. aRUDOMDET	Domestic Debt, Current Prices	Δ^2
15. aRUBCDBNKA	Bank Lending: Loans to banks (in rubles), Current Prices	Δ
16. RUCPIY=ECI*	$\mathrm{CPI},\ \mathrm{Chg}\ \mathrm{Y/Y}$	Δ
17. aRUCPI*	CPI, Price Index	Δ
18. aRUCCPIYF*	CPI, $\%$ year on year, Standardized, Chg Y/Y, Price Index	Δ
19. $aRUCCPIF/C*$	CPI, Standardized, Price Index	Δ
20. aRUCPFYYF*	CPI, Food products, Chg Y/Y	Δ
21. aRUCPCORIF*	CPI, Core inflation, Chg Y/Y	Δ
22. aRUCCPIYE/A*	CPI, % year on year, Standardized, Chg Y/Y, Price Index, SA	Δ
23. aRUCCPIPF*	CPI, % month on month, Standardized, Chg P/P, Price Index	Δ

24. aRUCCORYE/A*	Core CPI, Standardized, Chg Y/Y, Price Index,	Δ
	SA	
25. aRUCCPIPE/A*	CPI, % month on month, Standardized, Chg	Δ
	P/P, Price Index, SA	
26. aRUCPNYYF*	CPI, Non-food products, Chg Y/Y	l
27. aRUCPIF*	CPI, Food and beverages, Price Index	l
28. aRUCPISERV*	CPI, Services, Price Index	Δ
29. aRUCPIXF*	CPI, Non-food goods, Price Index	l
30. aRUCPGOODF/C*	CPI, Goods, Price Index	l
31. aRUGOODSF*	CPI, Goods, Chg Y/Y	Δ
32. aRUCPFPFVF/ C^*	CPI, Food products without fruits and vegeta-	Δ
	bles, Price Index	
33. $aRUCCPIE/CA*$	CPI, Standardized, Price Index, SA	Δ
34. $aRUCCORF/C*$	Core CPI, Standardized, Price Index	Δ
35. $aRUCCORE/CA*$	Core CPI, Standardized, Price Index, SA	Δ
36. aRUCCORPF*	Core CPI, Standardized, Chg P/P, Price Index	Δ
37. $aRUCCORPE/A^*$	Core CPI, Standardized, Chg P/P, Price Index,	Δ
	SA	
38. aRUCCORYF*	Core CPI, Standardized, Chg Y/Y, Price Index	Δ
39. RUCPIY=ECIX*	CPI, Chg Y/Y	Δ
40. aRUCPFWFVF*	CPI, Food products without fruits .and vegeta-	Δ
	bles, Chg Y/Y	
41. aRUCPICORY/C*	CPI, Core CPI, Price Index	Δ
42. aRUCPNPSVF*	CPI, Paid services, Chg Y/Y	Δ
43. aRUCPICOR/ C^*	CPI, Core CPI, Price Index	Δ
44. aRUCLEAD	Composite leading indicators, Trend restored,	Δ
	SA	

45. aRUEMPLMT*	Employment, Volume	Δ
46. aRUBISRXBR	BIS, Real Broad Effective Exchange Rate Index	Δ
47. aRUCXTWF/C	Trade Weighted nominal exchange rate, Stan-	Δ
	dardized, Price Index	
48. aRUCXTWPF	Trade Weighted nominal exchange rate, %	l
	month on month, Standardized, Chg P/P, Price	
	Index	
49. aRUCXTWYF	Trade Weighted nominal exchange rate, % year	l
	on year, Standardized, Chg Y/Y, Price Index	
50. aRUCXTRF/C	Trade Weighted real exchange rate, Standard-	Δ
	ized, Price Index	
51. aRUCXTRPF	Trade Weighted real exchange rate, % month on	l
	month, Standardized, Chg P/P, Price Index	
52. aRUCXTRYF	Trade Weighted real exchange rate, % year on	l
	year, Standardized, Chg Y/Y, Price Index	
53. aRUIRECE/C	Real effective exchange rate (REER) based on	Δ
	consumer price index, 2010=100, Not SA, Price	
	Index	
54. aRUINECE/C	Nominal effective exchange rate (NEER) based	Δ
	on consumer price index, 2010=100, Not SA,	
	Price Index	
55. aRUBISNXBR	BIS, Nominal Broad Effective Exchange Rate	Δ
	Index	
56. aRUXRUSD	Russian roubles to US \$	Δ
57. RUGDP=ECI*	GDP, Chg Y/Y	Δ
58. aRUTREV*	Revenue, Federal budget, Current Prices	Δ
59. aRUPFEXP*	Expenditure, Current Prices	Δ

60. aRUCBUDIC*	Revenue, Consolidated budget, incomes total,	Δ
	Current Prices	
61. aRUEXPDT*	Expenditure, Current Prices	Δ
62. aRUGDEF*	Deficit/Surplus, Federal budget, Current Prices	l
63. aRUCGOVA*	Central government Deficit/Surplus, Standard-	l
	ized, Current Prices	
64. aRUCGOVPA*	Central government Deficit/Surplus, month on	l
	month, Standardized, Absolute change, Current	
	Prices	
65. aRUCGOVYA*	Central government Deficit/Surplus, year on	l
	year, Standardized, Absolute change, Current	
	Prices	
66. aRSCGOVBLA*	Public Finances, Central Government, Budget,	l
	Balance, Deficit/Surplus, Current Prices	
67. aRUDSCBUD*	Deficit/Surplus, Consolidated budget, Current	l
	Prices	
68. aRUDCTDA	Dwellings Commenced, Total dwellings area,	Δ
	Volume	
69. aRUDCTI	Dwellings Commenced, Total dwellings area,	Δ
	Price Index	
70. aRUPPICONS*	Producer Prices, Investment products, Chg P/P	Δ
71. RUTRD=ECI*	Trade Balance, Total, Free On Board, Current	l
	Prices	
72. aRUEXP*	Exports, FOB, Current Prices	Δ
73. aRUIMP*	Imports, FOB, Current Prices	Δ
74. aRUTBAL*	Trade Balance, FOB, Current Prices	l
75. aRUEXPNGC*	Exports, Natural gas, Current Prices	l

76. aRUEXPCRD*	Exports, Crude oil, Current Prices	l
77. aRUEXPDIESL*	Exports, Diesel fuel, Current Prices	l
78. aRUIMPPRO*	Exports, Petroleum products, Current Prices	l
79. aRUIMPMED*	Imports, Medicines, Current Prices	l
80. aRUIMPMNEQ*	Imports, Machinery and equipment, Current	l
	Prices	
81. aRUIMPCLOTH*	Imports, Clothing, Current Prices	Δ
82. aRUEXPMOM*	Exports, Ferrous metals, Current Prices	l
83. aRUCEXPB/A*	Merchandise Exports, Standardized, Current	Δ
	Prices, SA	
84. aRUCIMPB/A*	Merchandise Imports, Standardized, Current	Δ
	Prices, SA	
85. aRUCEXPPB/A*	Merchandise Exports, $\%$ month on month, Stan-	l
	dardized, Chg P/P, Current Prices, SA	
86. aRUCEXPYB/A*	Merchandise Exports, % year on year, Standard-	Δ
	ized, Chg Y/Y, Current Prices, SA	
87. aRUCIMPPB/A*	Merchandise Imports, $\%$ month on month, Stan-	l
	dardized, Chg P/P, Current Prices, SA	
88. aRUCIMPYB/A*	Merchandise Imports, $\%$ year on year, Standard-	Δ
	ized, Chg Y/Y, Current Prices, SA	
89. aRUCVISB/A*	Visible Trade Balance, Standardized, Current	l
	Prices, SA	
90. aRUCVISPB/A*	Visible Trade Balance, month on month, Stan-	l
	dardized, Absolute change, Current Prices, SA	
91. aRUCVISYB/A*	Visible Trade Balance, year on year, Standard-	l
	ized, Absolute change, Current Prices, SA	
92. RUTRD=ECIX*	Trade Balance, Total, Free On Board	l

93. RUIP=ECI*	Production, IP Total , Chg Y/Y	l
94. aRUIP*	Production, Chg Y/Y	l
95. aRUIPOIL*	Production, Oil output, including gas conden-	Δ
	sate, Volume	
96. $aRUCINDG/A*$	Industrial Production Index, Standardized, Vol-	Δ
	ume Index, SA	
97. aRUIPNAG*	Production, Natural gas output, Volume	l
98. $aRUIPMANH/C*$	Production, Manufacturing, Volume Index	l
99. aRUIPMANG*	Production, Manufacturing, Chg Y/Y	l
100. aRUINP/ C^*	Production, Industry, Volume Index	Δ
101. aRUCINDPG/A*	Industrial Production Index, Standardized, Chg	l
	P/P, Volume Index, SA	
102. aRUCINDYG/CA*	Industrial Production Index, % year on year,	l
	Standardized, Chg Y/Y, Volume Index, SA	
103. RUIP=ECIX*	Production, IP Total, Chg Y/Y	l
104. aRUPRATE	Policy Rates, Minimum Rate on 7 Day Repo	Δ
105. aRUINTRES	Reserves, Gross international, Current Prices	Δ
106. aRUFXRES	Reserves, Foreign currency reserves, Current	Δ
	Prices	
107. aRUFCRES	Reserves, Foreign currency, Current Prices	Δ
108. aRUCRESA	Official international reserves, Standardized,	Δ
	Current Prices	
109. aRURESGLD	Reserves, Gold, Current Prices	Δ
110. aRUCRESPA	Official international reserves, % month on	Δ
	month, Standardized, Chg P/P, Current Prices	
111. aRUCRESYA	Official international reserves, $\%$ year on year,	Δ
	Standardized, Chg Y/Y, Current Prices	

112. aRURTM1A1A	Official reserve assets, Foreign currency, Current	Δ^2
113. aRURESSDR	Prices Reserves, Special Drawing Rights, Current Prices	Δ
114. aRURTM1AA	Official reserve assets, Overall, Current Prices	Δ
115. aRURESIMF	Reserves, Reserve position in the IMF, Current Prices	Δ
116. aRUM2	Money supply M2 by national definition, Current Prices	Δ
117. aRUM0	Money supply M0, Current Prices	Δ
118. aRUNM1	Money Supply - M1, Current Prices	Δ
119. aRUMNBAS	Monetary base (narrow definition), Current	Δ
	Prices	
120. aRUMBASMOC	Monetary base (broad definition), Current	Δ
	Prices	
121. aRUMSMBBRA	Broad money liabilities, Current Prices	Δ
$122.~\mathrm{aRUCMS2B/A}$	Money Supply M2, Standardized, Current	Δ
	Prices, SA	
123. $aRUCMS2PB/A$	Money Supply M2, % month on month, Stan-	l
	dardized, Chg P/P, Current Prices, SA	
124.~aRUCMS2YB/A	Money Supply M2, % year on year, Standard-	Δ
	ized, Chg Y/Y, Current Prices, SA	
125. $aRUCMS1B/A$	Money Supply M1, Standardized, Current	Δ
	Prices, SA	
126. $aRUCMS0B/A$	Money Supply M0, Standardized, Current	Δ
	Prices, SA	

127. $aRUCMS1PB/A$	Money Supply M1, Standardized, Chg P/P,	l
	Current Prices, SA	
128. $aRUCMS0PB/A$	Money Supply M0, Standardized, Chg P/P,	l
	Current Prices, SA	
129. $aRUCMS1YB/A$	Money Supply M1, Standardized, Chg Y/Y ,	Δ
	Current Prices, SA	
$130.~\mathrm{aRUCMS0YB/A}$	Money Supply M0, Standardized, Chg Y/Y ,	Δ
	Current Prices, SA	
131. RUPPI=ECI*	Producer Prices, Chg P/P	l
132. RUPPIY=ECI*	Producer Prices, Chg Y/Y	l
133. $aRUPPI/C*$	Producer Prices, Price Index	Δ
134. aRUPPITCP*	Producer Prices, Chg P/P	l
135. aRUPPIF*	Producer Prices, Chg Y/Y	l
136. aRUCPPIE/CA*	Producer Prices, PPI, Standardized, Price In-	Δ
	dex, SA	
137. aRUPPIAR*	Producer Prices, Chg P/P	l
138. $aRUCPPIF/C*$	Producer Prices, PPI, Standardized, Price Index	Δ
139. $aRUCPPIPE/A*$	Producer Prices, PPI, % month on month, Stan-	l
	dardized, Chg P/P, Price Index, SA	
140. aRUCPPIPF*	Producer Prices, PPI, $\%$ month on month, Stan-	l
	dardized, Chg P/P, Price Index	
141. $aRUCPPIYE/A*$	Producer Prices, PPI, $\%$ year on year, Standard-	Δ
	ized, Chg Y/Y, Price Index, SA	
142. aRUCPPIYF*	Producer Prices, PPI, $\%$ year on year, Standard-	Δ
	ized, Chg Y/Y, Price Index	
143. RUPPI=ECIX*	Producer Prices, Chg P/P	l
144. RUPPIY=ECIX*	Producer Prices, Chg Y/Y	l

145. aRUPPIYAR*	Producer Prices, Chg Y/Y	l
146. aRUPPITC*	Producer Prices, Price Index	Δ
147. RURSLY=ECI*	Retail Sales YY, Price Index	Δ
148. aRURSLS*	Retail Trade Turnover, Current Prices	Δ
149. aRURSLSTO*	Retail Trade Turnover, Price Index	Δ
150. aRUCRETF/ C^*	Retail Sales, Standardized, Price Index	Δ
151. $aRUCRETE/CA*$	Retail Sales, Standardized, Price Index, SA	Δ
152. aRUCRETPF*	Retail Sales, Standardized, Chg P/P, Price In-	l
	dex	
153. aRUCRETPE/A*	Retail Sales, Standardized, Chg P/P, Price In-	Δ
	dex, SA	
154. aRUCRETYF*	Retail Sales, Standardized, Chg Y/Y, Price In-	Δ
	dex	
155. aRUCRETYE/A*	Retail Sales, Standardized, Chg Y/Y, Price In-	Δ
	dex, SA	
156. RURSLY=ECIX*	Retail Sales YY	Δ
157. aRURTTNFC*	Retail Trade Turnover, Non-food commodities,	Δ
	Current Prices	
158. aRURSLS/ C^*	Retail Trade Turnover, Volume Index	l
159. aRURTTFC*	Retail Trade Turnover, Food commodities, Cur-	Δ
	rent Prices	
160. aRUGBOND	Bid	Δ
161. aRUSHRPRCF	MICEX, Composite Index, Price Index	Δ
162. aRUWANMAVWG*	Wages, Nominal average monthly per worker,	Δ
	Current Prices	
163. aRUWSAMTCPP*	Wages, Real average monthly, Volume Index	Δ
164. $aRUCWAGF/C*$	Wages, total, Standardized, Price Index	Δ

165. aRUCWAGPF*	Wages, total, $\%$ month on month, Standardized,	l
	Chg P/P, Price Index	
166. aRUCWAGYF*	Wages, total, $\%$ year on year, Standardized, Chg	Δ
	Y/Y, Price Index	
167. aRUAVGMANW*	Average monthly accrued nominal wages, Cur-	Δ
	rent Prices	
168. RUUNR=ECI*	Unemployment, Rate	Δ
169. RURWGE=ECI*	Real Wages YY, Chg Y/Y	Δ
170. aRUUNR*	Unemployment, Rate	Δ
171. aRUUNTOTR*	Uneployment rate, ILO	Δ
172. aRUPOPEA*	Economically active population - Unemployed,	Δ
	Volume	
173. aRUCUNPQ/A*	Unemployment rate, Standardized, SA	Δ
174. aRUUEMPILO*	Unemployment, Total persons (ILO), aged 15	Δ
	and over, Volume	
175. aRUUEMP*	Unemployment, Officially registered, Volume	Δ
176. aRUUNRAR*	Unemployment, Rate	Δ
177. aRUCUNPPQ/ A^*	Unemployment rate, month on month, Stan-	l
	dardized, SA	
178. aRUCUNPYQ/A*	Unemployment rate, year on year, Standard-	l
	ized, SA	
179. aRUCUNPO*	Unemployment Level, Standardized, Volume	Δ
180. aRUCUNPP*	Unemployment Level, Standardized, Volume	Δ
181. aRUCUNPPO/A*	Unemployment Level, $\%$ month on month, Stan-	l
	dardized, Chg P/P, Volume, SA	
182. aRUCUNPPP*	Unemployment Level, $\%$ month on month, Stan-	l
	dardized, Chg P/P, Volume	

183. aRUCUNPYO*	Unemployment Level, $\%$ year on year, Standard-	l
	ized, Chg Y/Y, Volume	
184. aRUCUNPYP*	Unemployment Level, % year on year, Standard-	l
	ized, Chg Y/Y, Volume	
185. RURWGE=ECIX*	Real Wages YY, Chg Y/Y	Δ
186. RUUNR=ECIX*	Unemployment, Rate	Δ
187. aRUUNRRILO*	Unemployment, Rate, Officially registered	Δ
	(ILO)	
188IRTS	RTS Index	Δ
189IMOEX	MOEX Russia Index	Δ
190RTSOG	RTS Oil & Gas Index	Δ
191RTSTL	RTS Telecom Index	Δ
192. BrentP	Brent Price nominal	Δ
193. BrentPP	Brent Price (%)	l
194. WTIP	WTI Price nominal	Δ
195. WTIPP	WTI Price (%)	l
196. RUEURP	Russian roubles to EU €, Close	Δ
197. RUEURMAX	Russian roubles to EsU €, Max	Δ
198. RUEURMIN	Russian roubles to EU €, Min	Δ
199. RUEURPP	Russian roubles to EU €, % change	l

References

- Berggren, E. and Lodenius, E. (2016). Can favar improve swedish inflation forecasting?
- Bernanke, B. S., Boivin, J., and Eliasz, P. (2005). Measuring the effects of monetary policy: a factor-augmented vector autoregressive (favar) approach. The Quarterly journal of economics, 120(1):387–422.
- Figueiredo, F. M. R. and Guillén, O. (2013). Forecasting brazilian consumer inflation with favar models using target variables. Technical report, mimeo.
- Mönch, E. (2008). Forecasting the yield curve in a data-rich environment: A no-arbitrage factor-augmented var approach. Journal of Econometrics, 146(1):26–43.
- Pang, I. A. J. (2010). Forecasting hong kong economy using factor augmented vector autoregression.
- Sims, C. A. (1980). Martingale-like behavior of prices.
- Sims, C. A. (1992). Interpreting the macroeconomic time series facts: The effects of monetary policy. European economic review, 36(5):975–1000.
- Stock, J. H. and Watson, M. W. (2002). Macroeconomic forecasting using diffusion indexes. Journal of Business & Economic Statistics, 20(2):147–162.
- Stock, J. H. and Watson, M. W. (2005). Implications of dynamic factor models for var analysis. Technical report, National Bureau of Economic Research.