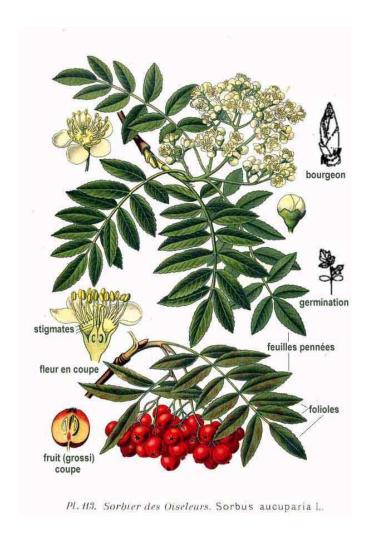
Can machine Learning be used to identify species of

Sorbus

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6 0. Abstract.

Machine learning was used to separate seven species of Sorbus within the subgenus Soraria based on morphological measurements of fruit and leaves. Box plots show that there is considerable overlap of characteristics between the species, but that some species were sufficiently differentiated in one or two characteristics. This was reflected in the modelling where unsupervised clustering algorithms gave inaccurate results but decision tree methods were successful. Accuracy of the decision tree was 0.68, for hierarchical clustering 0.41 and for kmeans the highest value obtained was 0.22. Although hierarchical clustering showed sensitivity for S. arrensis of 0.87, for the remaining species sensitivities were below 0.32. For the decision tree the lowest sensitivity was 0.17 for S. intermedia but for five of the species the value was above 0.6. The decision tree had precision of 1 for one cluster and five remain values above 0.5, whereas for hierarchical clustering, the highest value was 0.81 and five remaining value were below 0.43.

18 1. Introduction - The genus Sorbus.

- Sorbus is a member of the Rosaceae family, perhaps the best known species being Sorbus aucuparia,
 the Rowan or Mountain Ash. However, there are over 50 species of Sorbus in the UK, 38 of these
 are vulnerable or critically endangered and most are endemic or native. There are four diploid
 species, but, as with many Rosaceae, Sorbus produce new apomictic polyploid species. These can
 also produce viable pollen and can therefore backcross with other diploid or polyploid species. This
 results in the large number of genetically unique, stable, clonal communities, which can look very
 similar to each other. This presents a problem with recording and many Sorbus require expert
 knowledge to correctly identify to species level because much of the identification depends on
 comparative knowledge. This tends to dissuade recorders, or encourages records at aggregate level.
 This is a problem for such an important genus with many endangered plants that could benefit
 from identification.
- Sorbus are grouped into six subgenera, each of which are reasonably easy to identify by recorders
- with some knowledge, more difficulty arises when identifying plants within these subgenera, and

- this is where this work has concentrated. In this modelling only the subgenus Soraria has been
- trialled. This subgenus consists of eight species all similar in appearance to Sorbus intermedia,
- 34 although only seven species are considered based on the availability of data. These plants are
- 35 distinguished from other subgenera by having leaves with rounded lobes which are tomentose
- beneath and the fruits having fewer lenticles. Perhaps the most noticeable difference between plants
- 37 within the subgenus, are the larger fruits on S intermedia, the smaller leaves of S minima and the
- 38 small fruits of S mougeotii.

$_{39}$ 2. Data and data preparation

- 40 The data was provided by Dr T Rich, the Botanical Society of Britain and Ireland expert on Sorbus
- and consists of leaf and fruit measurements. For the leaves, the length, width, widest point on the
- leaf, base angle, number of veins, depth of the lobes, and vein angle have been recorded. For the
- 43 fruit, the length and the width are used. Due to the variability in leaf size across one plant, the
- 44 measurements were all carried out in a specific manner described by Rich []. Essentially, repeated
- 45 measurements of leaves on sterile spurs on the sunlight side of the tree are recorded and averaged
- over at least ten leaves.
- 47 The nature of collection means that the data was sparse. Every plant of every species did not have
- 48 have complete set of measurements or the same number of measurements. For example, S
- 49 intermedia had 126 observations but S leyana only had 39. This is due to the rarity S. leyana. S.
- 50 intermedia is a common plant found throughout the UK in easily accessible places, whilst S leyana
- 51 is only found in two sites in South Wales, sometimes on the sides of cliffs. In addition,
- 52 measurements cannot all be collected at the same time. Leaves must be measured when mature,
- 53 around flowering time, and therefore cannot be measured in conjunction with fruit. Separate trips
- to re-measure fruit on the same trees may not be possible. This has lead to a sparse dataset in
- ⁵⁵ which not all morphological characteristics were available for every plant. S intermedia records are
- an example. Of 122 records, 72 are purely for fruit measurements and the remaining 50 purely for
- ⁵⁷ leaf measurements, and these occur on different plants If imputation was carried out, 59% of the
- be leaf measurements would be imputed. This would reduce the effectiveness of some algorithms. For

example, in kNN, if you increase the frequency of the neighbours in the S. Intermedia group, it is more likely that a member of a different group will be close to that neighbour. Therefore, the sparsity was handled by reallocating measurements. For example, the 50 leaf measurements for S. 61 intermedia were assigned to 50 fruit measurements and the excess 22 were not used. In some cases, where there were only a few additional rows of incomplete data, median imputation was carried out. Although it seems dubious to assign records from one plant to another, in this analysis this was felt to be acceptable for two reasons. Firstly, this an exploration of a new technique to aid biological recording; it is not being proposed as a complete and accurate method for species identification. Secondly, the clonal nature of these plants implies that we would expect a great deal of similarity within a species. The variation within the species is more likely to come from the variety of leaf sizes which can be found on one plant, and these are controlled for, although they cannot be eliminated, when the data is collected. However, if these plants are phenotypically very plastic, these assumptions may be invalid. The range of leaf sizes within each plant was not available, but a comparison of the variation within each plant and between all the plants of each species would be useful here. That analysis would demonstrate whether each record needs to be complete or not. This procedure also has the benefit of producing a dataset with no missing values, and some of the machine learning algorithms used here had no method for dealing with these, hence they must be removed before modelling. Some machine learning algorithms are sensitive to scale in the data, for example, k nearest neighbours and k-means, therefore the data was also standardized and models carried out on standardized and non-standardized data. Some machine learning algorithms require train and test sets. The model is fitted to a subset of the data – the training set, and its performance evaluated using new data – the test set. This is to avoid over fitting and to improve the predictive power of the models. The data can be split by selecting a random sample of, for example, 70% of the data. However, this might be problematic with this data because it is unbalanced. Therefore, a random stratified sampling system was carried out. Each species, which has a different number of entries, was split into 70/30 train test sets. This should reduce the bias of the model whilst not over fitting. In addition, cross fold validation was also used to increase accuracy. This technique repeatedly creates train test sets as described above and averages the model performance metrics across all the folds. This gives a more robust estimate of

the model accuracy because it is less dependent on the choice of the data for the train and test sets.

89 3. Modelling

90 3.1 Model performance metrics

- 91 In classification models, the correct and incorrect values assigned to each class are known, and these
- 92 can be used to evaluate the model. For these types of models accuracy, precision and sensitivity are
- used to evaluate the model.
- 94 Accuracy is is the number of correct values divided by total number of items evaluated.
- Precision is the ratio of true positives to false positives in each species, so there will be precision for
- each species. Precision tells you how accurately the algorithm is correctly placing species, a low
- 97 precision tells you that other species are lumped with the correct species.
- 98 Sensitivity is the true positive rate of a class. Sensitivity tells you how good the classes are, low
- number tells you the correct species have been put in other, incorrect, classes,
- For clustering models, well defined clusters represent better models and the ratio of within cluster
- sum of squares to total sum of squares was used. For well defined, compact clusters the ratio will
- be small.
- For all the data, despite using unsupervised learning methods, we do know the identification of the
- species, this means that we can calculate accuracy, precision and sensitivity for all the models and
- 105 compare them using the same metric.
- 106 Confusion matrices, which summarise the the frequencies of the species allocated to different classes
- and clusters can also be produced.

$_{108}$ 3.2 Modelling methods.

- Three machine learning methods were used k-means, hierarchical clustering and a decision tree.
- The first two being unsupervised clustering techniques and the third a supervised classification

algorithm.

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3.2.1. Decision tree.

Decisions are made based on whether the information after the decision, i.e., the separation of the 114 groups, is increased or decreased. The final classes would ideally contain only the items of a single 115 species, this will not be the case due to noise within the data. The model here is be represented by 116 the logical processes followed to reach the final classes. The rpart package was used for the decision 117 tree. 118 Accuracy, precision, sensitivity and a confusion matrix were used to evaluate the decision tree, as 119 well as a decision tree plot which summarises the binary choices used at each node. since 120 standardization should not effect a decision tree, only the unstandardized data was modelled.

Variables are used to make binary decisions as whether data points are part of a group or not.

3.2.2. K-means

Kmeans is an unsupervised clustering technique. Even though we do know the identity of the instances in the data, this is not used in the model. Instead, the data is grouped into clusters where 124 the aim is to make the items within each cluster similar, whilst each cluster is as dissimilar as 125 possible from other clusters. This is similar to a classification technique except the classes to which 126 the items belong is to specified. In clustering, no information is needed about the objects and there 127 is no right or wrong, so in that sense, this problem is not strictly a clustering problem. We know 128 what species a sample belongs to and we do not want it allocated to another cluster. However, it is 129 a useful technique for examining the data and revealing patterns within the data. The k in k means 130 refers to the number of clusters to be used, which we specified as seven – the number of species. 131 In k-means k centroids are randomly assigned to the data. The data points are then assigned to the 132 closest centroid, resulting in k clusters. The centroid is then moved to the average location of the 133 data-points in its cluster. This process is repeated until the centroid position is stable, or the maximum number of iterations has occurred. If repeating the k-means function results in different 135 clusters, which can be seen in differences in accuracy, precision and the numbers of true positives, it 136

- can be assumed that the algorithm is not efficient at separating clusters. Since the number of 137 clusters is known, repeating the algorithm and examining the true positives will indicate the success of the model. 139
- In order to explore different k-means models the algorithm was also repeated on imputed 140 standardised and non-standarized data. The standardize function in R was used to subtract the 141 means and divide by the standard deviation. The MacQueen method gave the highest accuracy and was used for all the calculations.
- Accuracy, precision and sensitity were used to evaluate the algorithm, as well as between cluster to within cluster ratio. The consistency of the algorithm over ten was was examined and the 145 percentage of true positives on each run calcualted. Since there were repeated runs, displaying a 146 confusion matrix in each case would be visually difficult to examine, so they were not used in this case.

3.2.3. Hierarchical Clustering.

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- Instead of randomly assigning k centroids, hierarchical clustering assigns each data-point to a single 150 cluster. The distance between the clusters is calculated and the closest two points are aggregated 151 into a new cluster, so the clusters decrease by one. The process is repeated until all items are 152 clustered into one cluster. The clusters can be cut at k and the members can be examined. 153 Hierarchical clustering was explored using different distance calculation methods.
- Hierarchical clustering is again unsupervised, but since we know the members of each cluster, we 155 can compare the clusters to the original data and calculate accuracy, precision and sensitivity. The 156
- hclust function is part of the stats package [] which is usually included in base R.
- Accuracy, precision, sensitivity and a confusion matrix were used to evaluate the hierarchical clustering technique. 150

3.4 Computing languages

R was the main language used in this project, although there is no reason, in terms of functionality, 161 why Python could not be used, especially at the more simplistic level of modelling carried out here. 162 A large benefit in R was that it can easily be used in conjunction with R markdown which then 163 provide a mechanism for easily producing pdf documents with an interactive document. In addition, 164 the data was provided by, and the results prepared for, members of the ecological community, 165 where R is the most common package being used. Python was used for some data preparation in 166 order to full fill the criteria of the project, but R would have been equally suitable. R markdown 167 was used as it provides the same functionality as Latex, allowing the use of latex commands directly 168 within the document, but with the added benefit of being a dynamic document that is commonly 160 used by other researchers in ecology.

171 4.Data exploration.

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clearly defined clumps with very little overlap. Box plots show the similarity between the variables and how much the variables overlap. 174 The box plots are presented for the imputed, semi-standardised and fully standardised data and 175 show how the scale and overlap could be an issue for the clustering algorithms. The plots also show 176 that despite the overlap, certain features clearly differentiate certain species. For instance, fruit 177 width would separate S. anglica, and then fruit length would subsequently separate S leyana. This 178 suggests that a decision tree algorithm could be successful. The plots also show that more data 170 preparation might need to be employed, for example, scaling some of the variables instead of 180 standardising. 181

In order for machine learning algorithms to work accurately the groups should be separated into

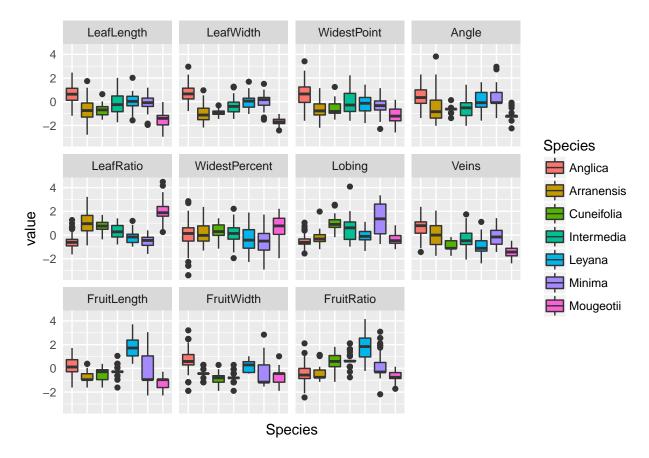


Figure 1: Box plots for standardized data

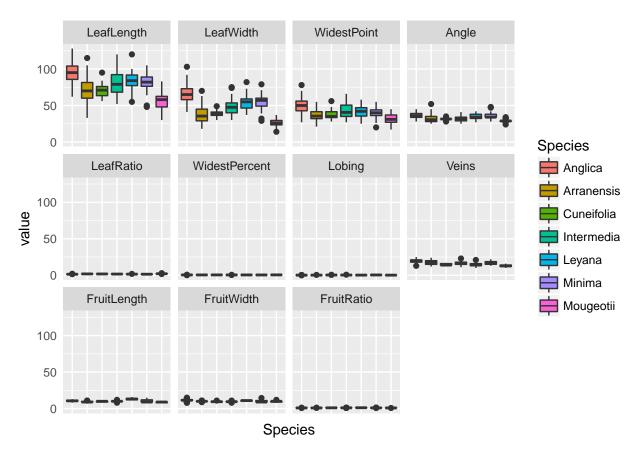


Figure 2: Box plots for un-standardized data

5. Results

$_{3}$ 5.1 Kmeans

Table 1: Within cluster to between cluster ratio

	Run 1	Run 2	Run 3	Run 4	Run 5	Run 6	Run 7	Run 8	Run 9	Run 10
unstandardized	0.14	0.14	0.14	0.14	0.14	0.14	0.14	0.14	0.14	0.14
standardized	0.42	0.42	0.43	0.42	0.42	0.42	0.42	0.42	0.42	0.42

Table 1 shows the within cluster sum of squares to between cluster sum of squares across the 10 repeats. The ratio is better for the unstandardized data.

Table 2: Accuracy

	Run 1	Run 2	Run 3	Run 4	Run 5	Run 6	Run 7	Run 8	Run 9	Run 10
unstandardized	0.07	0.13	0.18	0.21	0.24	0.20	0.15	0.14	0.21	0.09
standardized	0.09	0.19	0.24	0.08	0.06	0.24	0.21	0.18	0.20	0.30

The accuracy shown in table 2 is different on each run which implies that the algorithm is not successfully grouping the data into the same clusters. The mean accuracy is higher for the standardized data, but its low value, its fluctuation and its range imply that the model is not useful. The following tables show the percentage of each species correctly allocated to its cluster on each of the ten repeats for the For example, the top row from left to right, gives the true positive rate for S. anglia on each subsequent run on the kmeans algorithm.

Table 3: Percentage of true positives for non-standarized data

	1	2	3	4	5	6	7	8	9	10
Anglica	0.00	25.62	23.75	18.12	31.25	24.38	24.38	18.75	12.50	0.00
Cuneifolia	22.00	0.00	2.00	34.00	6.00	24.00	6.00	0.00	24.00	6.00
Intermedia	5.26	5.26	0.00	5.26	0.00	0.00	0.00	26.32	63.16	5.26
Leyana	31.25	6.25	20.83	29.17	31.25	29.17	6.25	16.67	16.67	10.42
Minima	3.33	6.67	36.67	3.33	3.33	3.33	33.33	3.33	3.33	3.33
Mougeotii	0.00	4.00	4.00	0.00	42.00	0.00	6.00	4.00	48.00	28.00
Arranensis	0.00	4.35	21.74	73.91	4.35	43.48	0.00	26.09	4.35	43.48

The results again show that the algorithm is not consistently allocating species to the correct cluster. On some runs, it is very accurate for some species, but not necessarily for all the others.

Table 4: Percentage of true positives for standarized data

	1	2	3	4	5	6	7	8	9	10
Anglica	1.88	28.12	54.37	1.88	0.0	49.38	19.38	26.88	26.88	50.62
Cuneifolia	4.00	0.00	6.00	34.00	4.0	16.00	2.00	34.00	0.00	48.00
Intermedia	0.00	0.00	0.00	0.00	0.0	0.00	0.00	0.00	0.00	0.00
Leyana	4.17	20.83	2.08	12.50	12.5	2.08	18.75	2.08	58.33	8.33
Minima	0.00	0.00	0.00	0.00	0.0	6.67	0.00	6.67	0.00	3.33
Mougeotii	6.00	32.00	4.00	6.00	32.0	0.00	32.00	8.00	8.00	6.00
Arranensis	100.00	0.00	0.00	8.70	0.0	0.00	100.00	0.00	0.00	0.00

- Then on other runs its is completely inaccurate. The standardized data shows better results than
- the non standardized data.
- 196 In order to compare this model to hierarchical clustering and decision tree, the precision and
- 197 sensitivity were also calculated.

Table 5: Precision of kmeans with non standardized data

	1	2	3	4	5	6	7	8	9	10
Anglica	0	0.26	0.24	0.18	0.31	0.24	0.24	0.19	0.12	0
Cuneifolia	0.22	0	0.02	0.34	0.06	0.24	0.06	0	0.24	0.06
Intermedia	0.05	0.05	0	0.05	0	0	0	0.26	0.63	0.05
Leyana	0.31	0.06	0.21	0.29	0.31	0.29	0.06	0.17	0.17	0.1
Minima	0.03	0.07	0.37	0.03	0.03	0.03	0.33	0.03	0.03	0.03
Mougeotii	0	0.04	0.04	0	0.42	0	0.06	0.04	0.48	0.28
Arranensis	0	0.04	0.22	0.74	0.04	0.43	0	0.26	0.04	0.43

Table 6: Precision of kmeans with standardized data

	1	2	3	4	5	6	7	8	9	10
Anglica	0.02	0.28	0.54	0.02	0	0.49	0.19	0.27	0.27	0.51
Cuneifolia	0.04	0	0.06	0.34	0.04	0.16	0.02	0.34	0	0.48
Intermedia	0	0	0	0	0	0	0	0	0	0
Leyana	0.04	0.21	0.02	0.12	0.12	0.02	0.19	0.02	0.58	0.08
Minima	0	0	0	0	0	0.07	0	0.07	0	0.03
Mougeotii	0.06	0.32	0.04	0.06	0.32	0	0.32	0.08	0.08	0.06
Arranensis	1	0	0	0.09	0	0	1	0	0	0

- 198 The precision and sensitivity also demonstrate the instability of the model. Although the
- standardized data in both cases sometimes gives very good results, this is not consistent or
- 200 repeatable.

Table 7: Sensitivity of kmeans with non standardized data

	1	2	3	4	5	6	7	8	9	10
Anglica	0	0.26	0.24	0.18	0.31	0.24	0.24	0.19	0.12	0
Cuneifolia	0.22	0	0.02	0.34	0.06	0.24	0.06	0	0.24	0.06
Intermedia	0.05	0.05	0	0.05	0	0	0	0.26	0.63	0.05
Leyana	0.31	0.06	0.21	0.29	0.31	0.29	0.06	0.17	0.17	0.1
Minima	0.03	0.07	0.37	0.03	0.03	0.03	0.33	0.03	0.03	0.03
Mougeotii	0	0.04	0.04	0	0.42	0	0.06	0.04	0.48	0.28
Arranensis	0	0.04	0.22	0.74	0.04	0.43	0	0.26	0.04	0.43

Table 8: Sensitivity of kmeans with standardized data

	1	2	3	4	5	6	7	8	9	10
Anglica	0.02	0.28	0.54	0.02	0	0.49	0.19	0.27	0.27	0.51
Cuneifolia	0.04	0	0.06	0.34	0.04	0.16	0.02	0.34	0	0.48
Intermedia	0	0	0	0	0	0	0	0	0	0
Leyana	0.04	0.21	0.02	0.12	0.12	0.02	0.19	0.02	0.58	0.08
Minima	0	0	0	0	0	0.07	0	0.07	0	0.03
Mougeotii	0.06	0.32	0.04	0.06	0.32	0	0.32	0.08	0.08	0.06
Arranensis	1	0	0	0.09	0	0	1	0	0	0

5.2 Hierarchical Clustering

Table 9: Accuracy obtained in hierarchical clustering using different distance metrics for non standarized data

Distance Method	euclidean	maximum	manhattan	canberra	minkowski
Accuracy	0.3	0.18	0.29	0.42	0.3

Table 10: Accuracy obtained in hierarchical clustering using different distance metrics for standardized data

Distance Method	euclidean	maximum	manhattan	canberra	minkowski
Accuracy	0.41	0.14	0.36	0.25	0.41

The table above shows that the Canberra metric gives the most accurate results in the

203 non-standardized data. The Euclidean and Minkowski methods give slightly worse worse results but

204 the best for the standardized data.

The confusion matrix above shows that the method successful clusters some species, such as S.

Table 11: Confusion matrix for Canberra method using un standardized data

	1	2	3	4	5	6	7
Anglica	108	41	11	0	0	0	0
Arranensis	7	14	0	0	22	0	7
Cuneifolia	0	1	0	8	10	0	0
Intermedia	13	2	2	22	8	1	0
Leyana	4	17	6	0	0	3	0
Minima	1	8	9	29	0	3	0
Mougeotii	0	0	0	0	12	0	11

 $_{\rm 206}$ $\,$ anglica, many other species are dispersed across the cluster.

Table 12: Confusion matrix for Canberra method with standardized data

	1	2	3	4	5	6	7
Anglica	52	17	27	6	10	43	5
Arranensis	5	2	2	12	1	1	27
Cuneifolia	0	0	0	1	0	0	18
Intermedia	6	2	0	10	0	7	23
Leyana	1	2	0	14	8	1	4
Minima	0	2	12	12	13	2	9
Mougeotii	0	0	0	3	0	0	20

The confusion matrix for the standardized data shows worse results than for the non-standardized data.

Table 13: Precision for standardized and non-standardized data

	Standardized	Unstandardized
Class1	0.69	0.81
Class2	0.08	0.17
Class3	0	0
Class4	0.04	0.37
Class5	0.05	0
Class6	0.05	0.43
Class7	0.58	0.61

The precision and sensitivity is not consistent between classes or species. The precision is higher in all cases for the non-standardized data, but the sensitivity is sometimes higher in standardized data.

Table 14: Precision for standardized and non-standardized data

	Standardized	Non-standardized
Anglica	0.68	0.32
Cuneifolia	0.28	0.04
Intermedia	0	0
Leyana	0.46	0.21
Minima	0	0.27
Mougeotii	0.06	0.04
Arranensis	0.48	0.87

5.3 Decision Tree

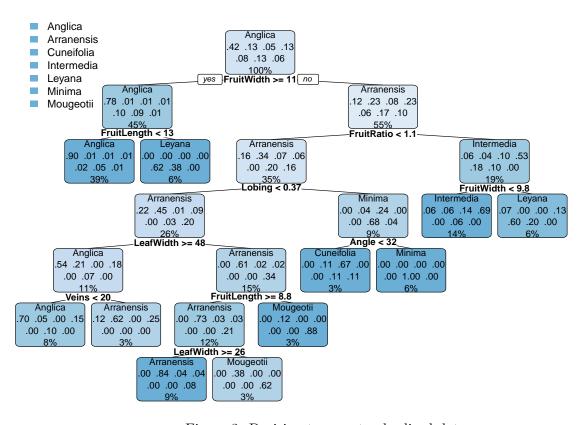


Figure 3: Decision tree unstandardized data

The plot shows the decision tree for the unstandardised data. The decisions at the nodes can be
seen to be based initially on fruit width, which was seen in the box-plots to be an variable which
differentiate S anglica. The leaves of the tree show that by following the splits, many species can be
idendified with a high probability. 100% for S. minima and 90% for S. anglica. S mougeotii and S
arranensis are both about 80% and the remaining species are above 60%.

Table 15: Precision for standardized and non-standardized data

0.68

Table 16: Sensitivity for the decision tree

Species	Sensitivity
Anglica	0.85
Arranensis	0.47
Cuneifolia	0.17
Intermedia	0.71
Leyana	0.67
Minima	0.6
Mougeotii	0.43

The sensitivity for the decision tree is only 0.17 for S cuneifolia but 0.85 for S anglica.

Table 17: Precision for the decision tree

Class	Precision
class_Anglica	0.79
class_Arranensis	0.5
class_Cuneifolia	0.5
class_Intermedia	0.67
class_Leyana	0.4
class_Minima	1
class_Mougeotii	0.43

218 The decision tree achieves high precision.

219 A summary of precision and sensitivity for hierarchical clustering and the decision tree are shown

below. The kmeans has not been included since the inconsistency of the method demonstrates that

it is not suitable for this data.

Table 18: Confusion matrix for the decision tree

	Anglica	Arranensis	Cuneifolia	Intermedia	Leyana	Minima	Mougeotii	
Anglica	41	3	0	0	3	0	1	48
Arranensis	4	7	0	0	1	0	3	15
Cuneifolia	0	1	1	4	0	0	0	6
Intermedia	2	0	1	10	1	0	0	14
Leyana	3	0	0	0	6	0	0	9
Minima	1	0	0	1	4	9	0	15
Mougeotii	1	3	0	0	0	0	3	7

Table 19: Sensitivity for hierarchical clustering and decision tree

	hclust standardised	hclust non-standardized	tree
Anglica	0.68	0.32	0.85
Cuneifolia	0.28	0.04	0.47
Intermedia	0	0	0.17
Leyana	0.46	0.21	0.71
Minima	0	0.27	0.67
Mougeotii	0.06	0.04	0.6
Arranensis	0.48	0.87	0.43

Table 20: Precision for hierarchical clustering and decision tree

	hclust standardised	hclust non-standardized	tree
Class1	0.69	0.81	0.79
Class2	0.08	0.17	0.5
Class3	0	0	0.5
Class4	0.04	0.37	0.67
Class5	0.05	0	0.4
Class6	0.05	0.43	1
Class7	0.58	0.61	0.43

$_{222}$ 6 Conlcusion.

As expected, kmeans was not successful in separating the data into clusters which could be
interpreted as species of Sorbus. The kmeans algorithm was seen to be unrepeatable and although
the ratio of the within cluster sum of squares to between cluster sum of squares was low, the
accuracy was always less 0.3. Sometimes high precision or sensitivity was achieved for a single
species, but this was not reflected in the other species and it was not repeatable. The standardized
data gave slighty better results, as expected.

Hierarchical clustering achieved an accuracy of 0.42 using the Canberra method in standardized data and 0.41 using the Euclidean and Minowski method in non-standardized data. The confusion matrix for the non-standardized data showed better allocation of S Anglica but the confusion matrix for standardized data was better for allocating S mougeotii. The sensitivity and precision also gave inconsistent results for the standardized and non-standardized data. Neither data treatment being better overall for all species.

The decision tree method performed more consistently that hierarchical clustering. Although a

single species might have a higher sensitivity in clustering, across all species the decision tree
performed better, with five of the seven species achieving greater than 0.6 sensitivity and precision
above 0.5 in all but one class. The decision tree also showed high precision and sensitivity for
S.anglica of 0.85 and 0.79 respectively. The overall accuracy was also the highest at 0.68.
The tree plot has the added benefit of providing a key that can be used to assist biological
recording.

7 Further work

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All the variables were used in the decision tree, which may not be the best model. Rpart provides information on the importance of variables which could be used to ascertain which variables could be removed. The model should be repeated with other species of Sorbus to see if the success was due to the specific morphological characteristics of the Soraria subgenus. It would also be interesting to examine the within plant and within species variability in order to ascertain whether the noise in the data can be reduced or has some minimum level which will always be present.