

Homework 5

Peyton Hall

Homework 5

$H_0 : \mu_{\text{Johns Hopkins}} = \mu_{\text{Rancho Los Amigos}} = \mu_{\text{St. Louis}}$ vs. $H_a : \text{At least one } \mu \text{ is different among the three medical centers}$
Question 1

```
johns_hopkins <- c(3.23, 3.47, 1.86, 2.47, 3.01,
                    1.69, 2.10, 2.81, 3.28, 3.36)

rancho_los_amigos <- c(3.22, 2.88, 1.71, 2.89, 3.77,
                        3.29, 3.39, 3.86, 2.64, 2.64)

st_louis <- c(2.79, 3.22, 2.25, 2.98, 2.47,
              2.77, 2.95, 3.56, 2.88, 2.88)

fev_data <- data.frame(
  center = factor(rep(c("Johns Hopkins", "Rancho Los Amigos", "St. Louis"), each = 10)),
  FEV = c(johns_hopkins, rancho_los_amigos, st_louis))

# Fit one-way ANOVA
fit <- aov(FEV ~ center, data = fev_data)
summary(fit)

##           Df Sum Sq Mean Sq F value Pr(>F)
## center      2  0.453  0.2265   0.709  0.501
## Residuals  27  8.621  0.3193

# Extract test statistic and p-value
anova_table <- summary(fit)[[1]]
F_stat <- anova_table$`F value`[1]
p_val <- anova_table$`Pr(>F)`[1]

F_stat

## [1] 0.7094999

p_val

## [1] 0.5008321
```

$f = 0.709$; $p\text{-value} = 0.501$ Fail to reject H_0 . $p\text{-value}$ (0.501) is greater than the significance level (0.05). There is not sufficient evidence to conclude that the mean FEV levels are significantly different among the three medical centers.

$H_{0,1} : \mu_{\text{Low}} = \mu_{\text{Medium}} = \mu_{\text{High}}$ vs. $H_{a,1} : \text{At least one mean is different}$

$H_{0,2} : \mu_{\text{Short}} = \mu_{\text{Long}}$ vs. $H_{a,2} : \mu_{\text{Short}} \neq \mu_{\text{Long}}$

$H_{0,3} : \text{No interaction effect between temperature and presoaking}$ vs. $H_{a,3} : \text{There is an interaction effect between temperature and presoaking}$

Question 2

```
short_low <- c(8, 5, 9)
short_medium <- c(18, 15, 17)
short_high <- c(12, 11, 14)
long_low <- c(11, 13, 15)
long_medium <- c(20, 19, 20)
long_high <- c(15, 16, 12)

taste_data <- data.frame(
  presoaking = factor(rep(c("Short", "Long"), each = 9)),
  temperature = factor(rep(c("Low", "Medium", "High"), each = 3, times = 2)),
  score = c(short_low, short_medium, short_high,
            long_low, long_medium, long_high))
taste_data

##      presoaking temperature score
## 1        Short       Low     8
## 2        Short       Low     5
## 3        Short       Low     9
## 4        Short    Medium    18
## 5        Short    Medium    15
## 6        Short    Medium    17
## 7        Short      High    12
## 8        Short      High    11
## 9        Short      High    14
## 10       Long       Low    11
## 11       Long       Low    13
## 12       Long       Low    15
## 13       Long    Medium    20
## 14       Long    Medium    19
## 15       Long    Medium    20
## 16       Long      High    15
## 17       Long      High    16
## 18       Long      High    12

fit2 <- aov(score~temperature*presoaking, data = taste_data) # Two-way ANOVA
summary(fit2)

##                               Df Sum Sq Mean Sq F value    Pr(>F)
## temperature                  2 194.78   97.39   33.08 1.31e-05 ***
## presoaking                   1  56.89   56.89   19.32 0.000872 ***
## temperature:presoaking     2  10.78    5.39    1.83 0.202430
## Residuals                    12  35.33    2.94
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

anova_table <- summary(fit2)[[1]] # extract test statistics and p-values
```

```

# test statistic and p-value for temperature effect
F_temp <- anova_table$`F value`[1]
p_temp <- anova_table$`Pr(>F)`[1]

# test statistic and p-value for presoaking effect
F_presoak <- anova_table$`F value`[2]
p_presoak <- anova_table$`Pr(>F)`[2]

# test statistic and p-value for interaction
F_interaction <- anova_table$`F value`[3]
p_interaction <- anova_table$`Pr(>F)`[3]

F_temp; p_temp

## [1] 33.07547

## [1] 1.310636e-05

F_presoak; p_presoak

## [1] 19.32075

## [1] 0.0008721909

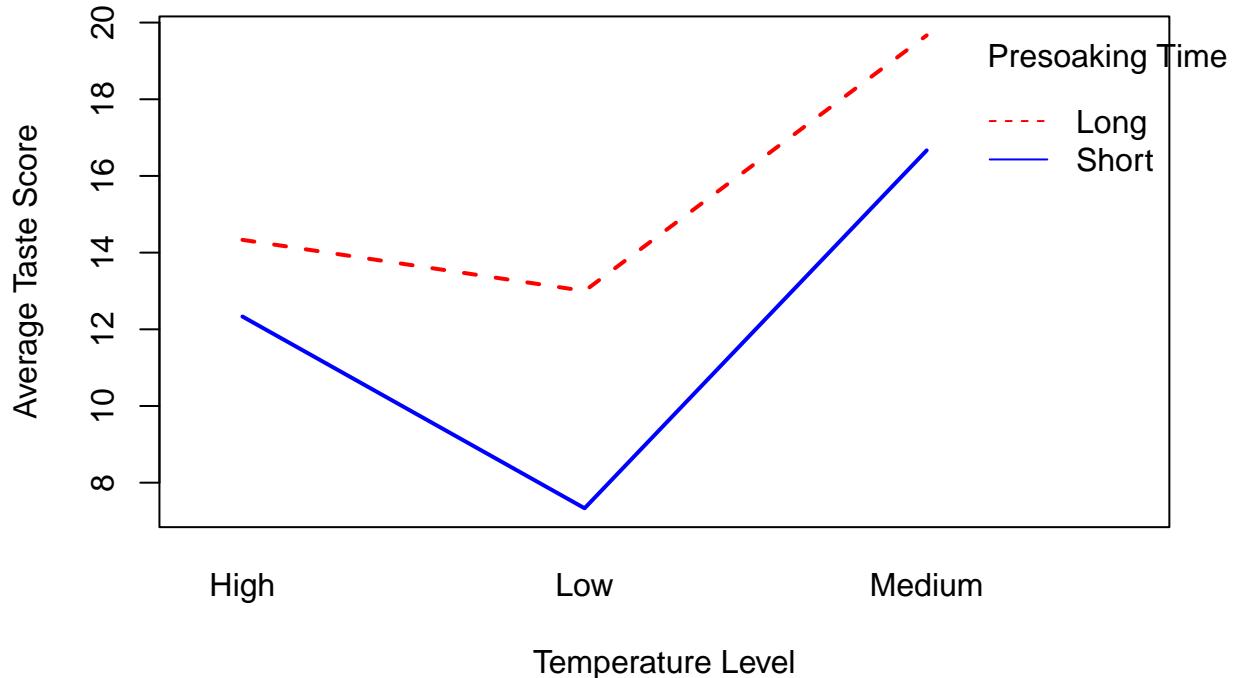
F_interaction; p_interaction

## [1] 1.830189

## [1] 0.2024297

interaction.plot(taste_data$temperature, taste_data$presoaking,
                  taste_data$score,
                  xlab = "Temperature Level",
                  ylab = "Average Taste Score",
                  trace.label = "Presoaking Time",
                  col = c("red","blue"),
                  lwd = 2)

```



temperature:

$F = 33.08$; p-value = $1.31e-05$

Reject H₀. There is a significant effect of temperature presoaking:

$F = 19.32$; p-value = 0.000872

Reject H₀. There is a significant effect of presoaking interaction:

$F = 1.83$; p-value = 0.202

Fail to reject H₀. No significant interaction effect between temperature and presoaking

Question 3

```
library(readxl)
psychological_test_data <- read_excel("~/Desktop/DATA 499/Week 5/psychological test data.xlsx")
psychological_test_data

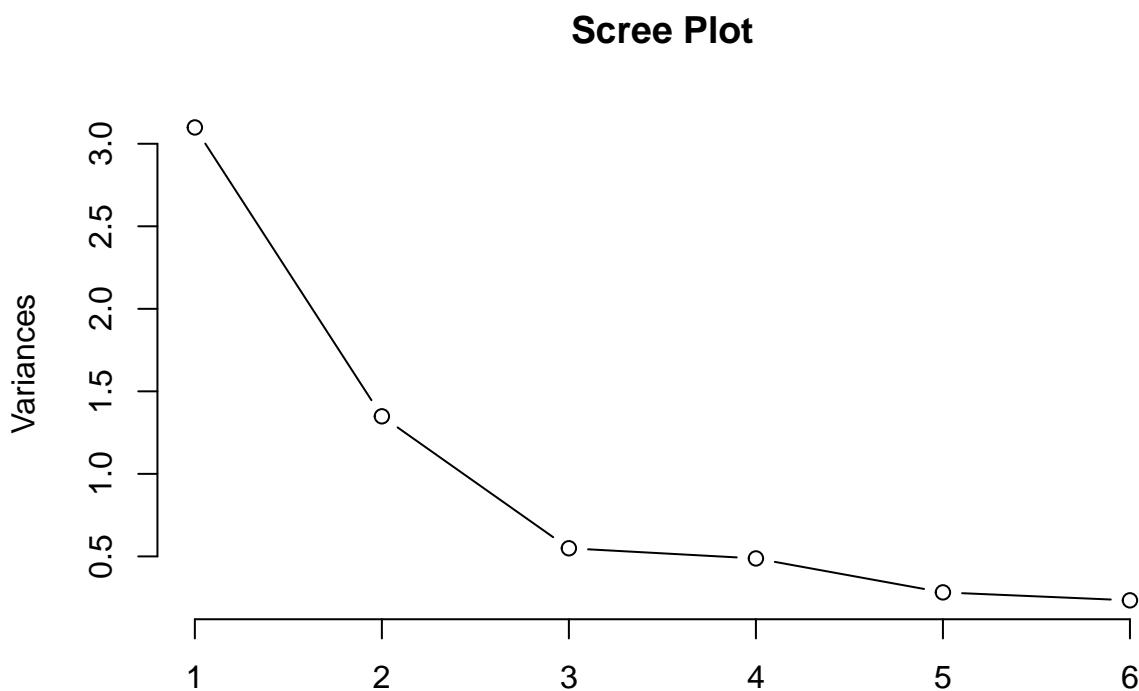
## # A tibble: 73 x 6
##   visperc cubes  lozenges paragrap sentence wordmean
##   <dbl>    <dbl>    <dbl>    <dbl>    <dbl>    <dbl>
## 1     33      22      17       8      17      10
## 2     30      25      20      10      23      18
## 3     36      33      36      17      25      41
## 4     28      25       9      10      18      11
## 5     30      25      11      11      21       8
## 6     20      25       6       9      21      16
## 7     17      21       6       5      10      10
## 8     33      31      30      11      23      18
## 9     30      22      20       8      17      20
## 10    36      28      22      13      24      36
```

```

## # i 63 more rows

psych_pca <- prcomp(psychological_test_data, scale. = TRUE) # PCA
plot(psych_pca, type = "l", main = "Scree Plot")

```



```

eigenvalues <- psych_pca$sdev^2
eigenvalues

```

[1] 3.0988862 1.3486867 0.5491883 0.4876152 0.2819058 0.2337179

- a) Keep 2 PCAs
- b) PC1 explains about 60–65% of the variance, PC2 explains about 15–20%. Together about 80–85%.
- c) Each PC is a linear combination of the six variables.
- d) From the biplot, the six variables can be grouped into Group 1: visperc, cubes, lozenges (visual/spatial tests) and Group 2: paragrap, sentence, wordmean (verbal/linguistic tests).

Question 4

```

library(readxl)
ClusterFaculty <- read_excel("~/Desktop/DATA 499/Week 5/ClusterFaculty.xlsx")
ClusterFaculty

```

A tibble: 44 x 5

```

##      Name      Salary Rank Articles Experience
##    <chr>     <dbl> <dbl>    <dbl>      <dbl>
## 1 Rosalyn 123600.     5      21       32
## 2 Lawrence 96800.     5      71       27
## 3 Sunila   83358.     5      19       24
## 4 Randolph 83236.     5      17       38
## 5 Mickey   75041.     5      18       11
## 6 Louis    74957.     5      50       26
## 7 Tony     72226.     4      25       28
## 8 Raul     72056.     5      41       18
## 9 Catalina 68128.     5      40       22
## 10 Johnson 66158.     5      26       24
## # i 34 more rows

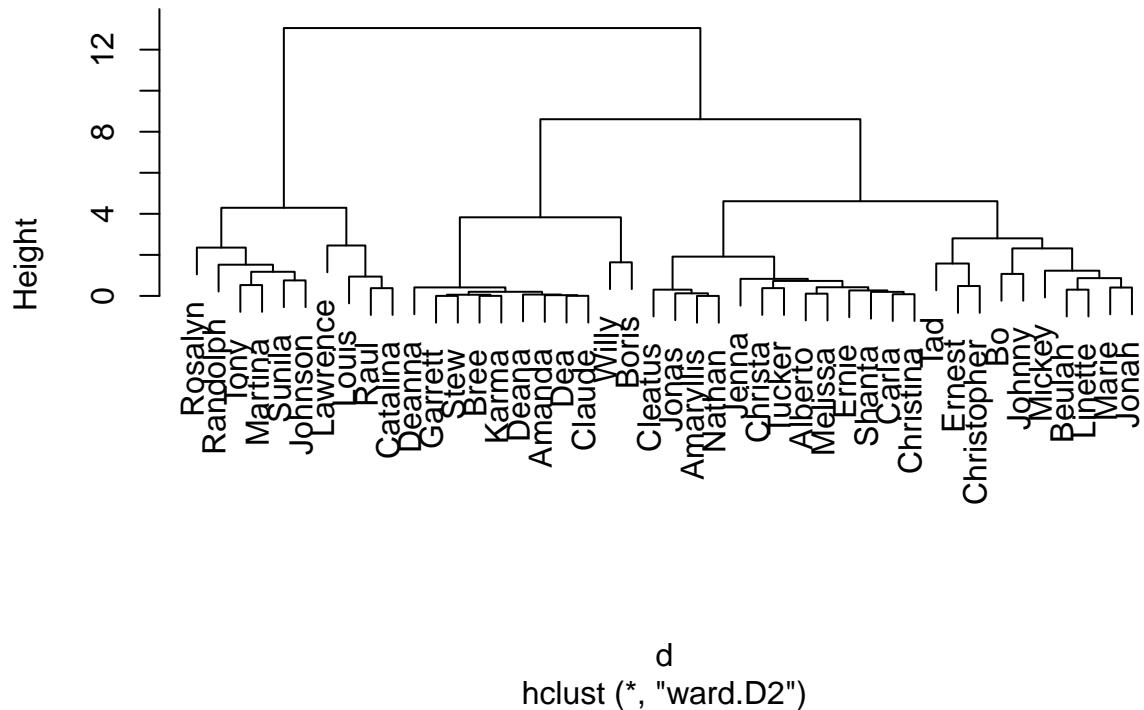
```

```

# remove the Name column for clustering (keep it separate for labeling later)
faculty_names <- ClusterFaculty$Name
cluster_vars <- ClusterFaculty[, -1]
# scale the variables so they are on the same scale
cluster_scaled <- scale(cluster_vars)
# perform hierarchical clustering using Ward's method
d <- dist(cluster_scaled, method = "euclidean")
hc <- hclust(d, method = "ward.D2")
# dendrogram
plot(hc, labels = faculty_names, main = "Faculty Clustering Dendrogram")

```

Faculty Clustering Dendrogram



```

clusters <- cutree(hc, k = 4) # cut into 4 clusters
table(clusters) # find the smallest cluster

## clusters
## 1 2 3 4
## 10 10 13 11

smallest_cluster <- which.min(table(clusters))
# faculty names in the smallest cluster
faculty_names[clusters == smallest_cluster]

## [1] "Rosalyn"  "Lawrence" "Sunila"   "Randolph" "Louis"    "Tony"
## [7] "Raul"      "Catalina" "Johnson"  "Martina"

```

- a) Rosalyn, Lawrence, Sunila, Randolph, Louis, Tony, Raul, Catalina, Johnson, Martina.

Question 5

```

library(readxl)
SpendingScore <- read_excel("~/Desktop/DATA 499/Week 5/SpendingScore.xlsx")
SpendingScore

```

```

## # A tibble: 20 x 3
##   CustomerID AnnualIncome SpendingScore
##       <dbl>        <dbl>        <dbl>
## 1           1         150          39
## 2           2         290          91
## 3           3         160          41
## 4           4         170          49
## 5           5         159          36
## 6           6         143          31
## 7           7         121          19
## 8           8         120          23
## 9           9         110          20
## 10          10         98           17
## 11          11         121          22
## 12          12         132          19
## 13          13         137          25
## 14          14         126          12
## 15          15         289          76
## 16          16         300          81
## 17          17         291          79
## 18          18         117          19
## 19          19         105          21
## 20          20         101          20

# use only AnnualIncome and SpendingScore for clustering
spend_data <- SpendingScore[, c("AnnualIncome", "SpendingScore")]

spend_scaled <- scale(spend_data) # scale the data

```

```

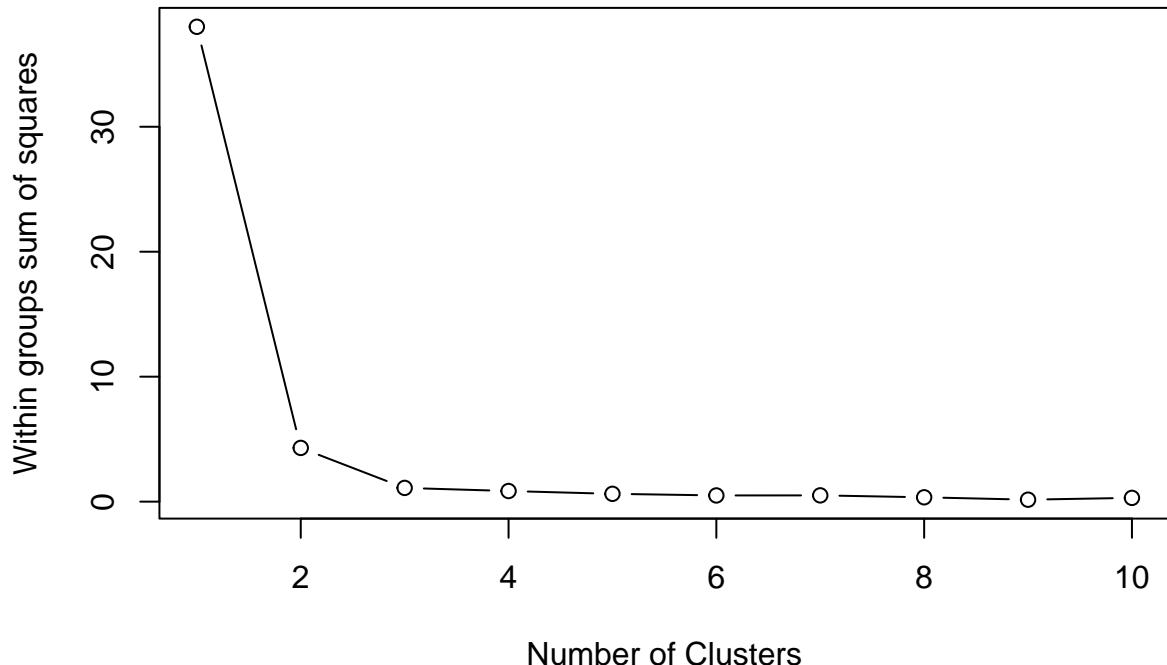
# decide number of clusters using the elbow method
wss <- (nrow(spend_scaled)-1)*sum(apply(spend_scaled,2,var))
for (i in 2:10) {
  km <- kmeans(spend_scaled, centers=i)
  wss[i] <- km$tot.withinss
}
plot(1:10, wss, type="b", xlab="Number of Clusters", ylab="Within groups sum of squares",
  main="Elbow Method for K-means")

# from the elbow plot, pick k
set.seed(123)
kmeans_result <- kmeans(spend_scaled, centers=4)    # adjust 4 if elbow suggests different
# add cluster labels to data
SpendingScore$Cluster <- as.factor(kmeans_result$cluster)

library(ggplot2)

```

Elbow Method for K-means

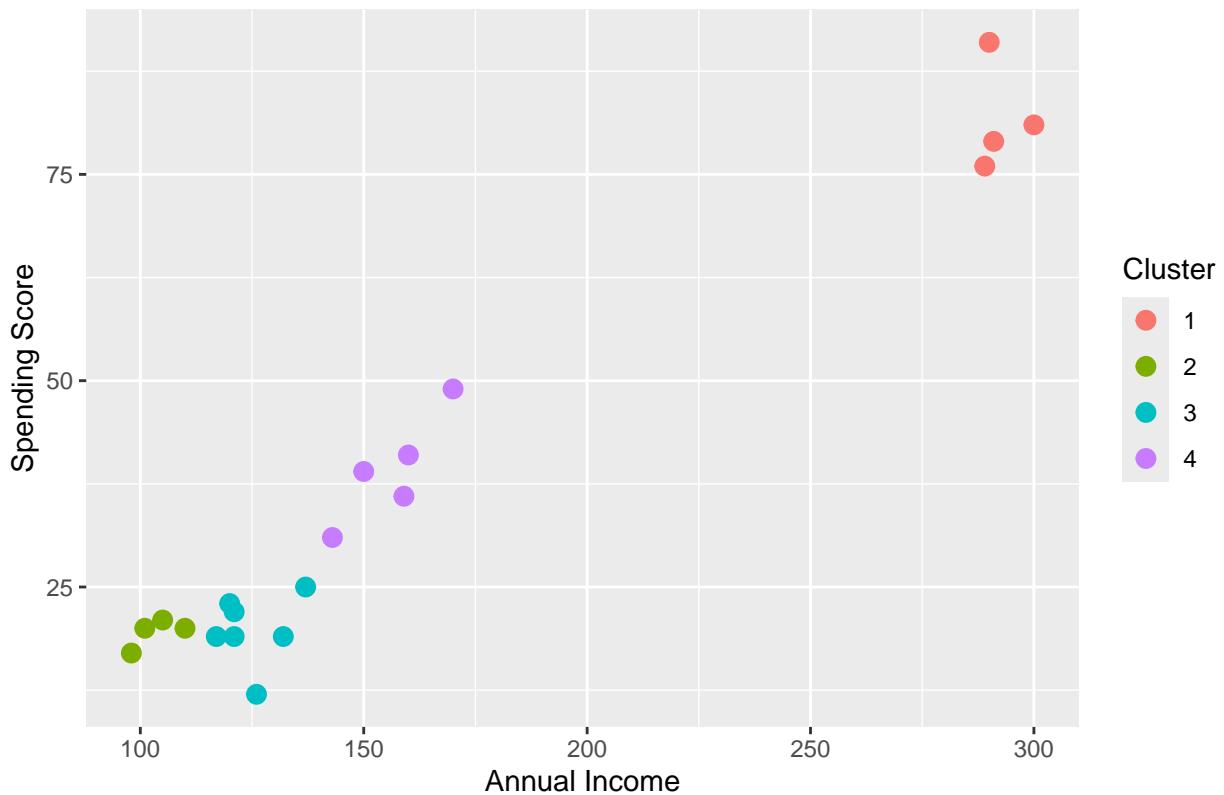


```

ggplot(SpendingScore, aes(x=AnnualIncome, y=SpendingScore, color=Cluster)) +
  geom_point(size=3) +
  labs(title="K-means Clustering of Customers", x="Annual Income", y="Spending Score")

```

K-means Clustering of Customers



b) From the elbow plot, the sharp bend occurs at $k = 4$. Therefore, it was decided to use 4 clusters because adding more clusters does not significantly reduce the within-cluster variation.