# C++ For C Coders 7

Data Structures
C++ for C Coders

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bubble sort insertion sort selection sort quicksort

## 1. Bubble sort(거품 정렬)

- It sorts by repeatedly swapping the adjacent elements if they are in wrong order. It is a stable sort. For example,
- 1st Pass:
  - (51428) -> (15428), It compares the first two elements, and swaps since 5 > 1.
  - (1 **5 4** 2 8) -> (1 **4 5** 2 8), Swap since 5 > 4
  - (14**52**8) -> (14**25**8), Swap since 5 > 2
  - (14258) -> (14258), Now, since these elements are already in order (8 > 5), it does not swap them.
- 2nd Pass:
  - (14258) -> (14258)
  - (14258) -> (12458), Swap since 4 > 2
  - (12**45**8) -> (12**45**8)
  - (12458) -> (12458)
  - Now, the sequence is already sorted, but the algorithm does not know if it is completed.
     It needs one whole pass without any swap to know it is sorted.

## 1: Bubble sort(거품 정렬)

- 3<sup>rd</sup> Pass:
  - (**12**458) -> (**12**458)
  - (1**24**58) -> (1**24**58)
  - (12**45**8) -> (12**45**8)
  - $(12458) \rightarrow (12458)$
  - Sorting is over since no element is swapped.

6 5 3 1 8 7 2 4

It compares every adjacent pair, swap their position if they are not in the right order (the latter one is smaller than the former one). After each iteration, one less element (the last one) is needed to be compared until there are no more elements left to be compared.

# 2: Insertion sort(삽입 정렬)

- It works the way we sort playing cards in our hands. It builds the final sorted array one item at a time.
- "Stable" does not change the relative order of elements with equal keys.
- "In-place" only requires a constant amount O(1) of additional memory space.
- "Online" can sort a list as it receives it.

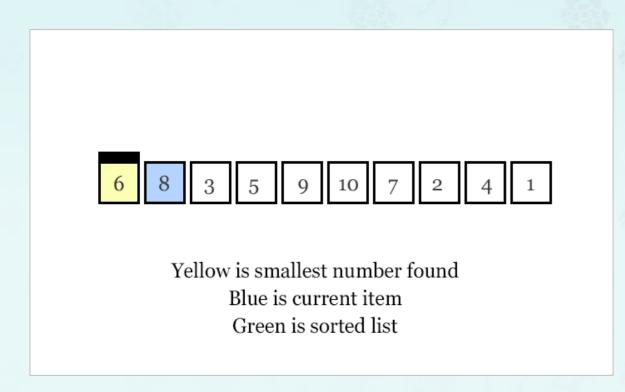
6 5 3 1 8 7 2 4

The partial sorted list (black) initially contains only the first element in the list.

With each iteration one element (red) is removed from the "not yet checked for order" input data and inserted in-place into the sorted list.

# 3: Selection sort(선택 정렬)

- It selects the smallest element from an unsorted list in each iteration and places that element at the beginning of the unsorted list.
- It is unstable. Why?



It divides its list into a sorted and an unsorted section.

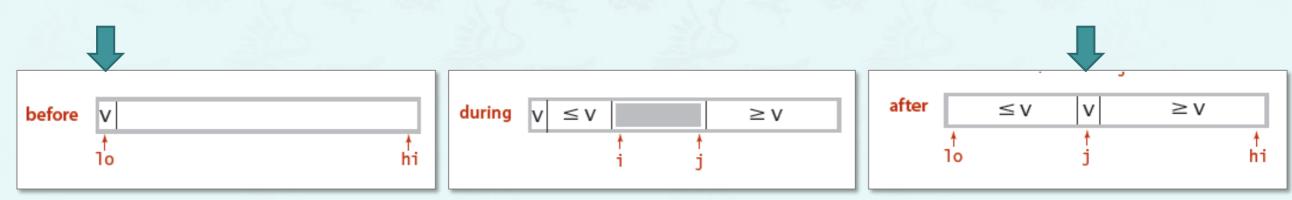
Then it swaps the smallest element it finds in each iteration, and add it to the sorted section of elements.

# 3: Selection sort(선택 정렬)

- Why is a selection sort algorithm unstable?
  - It picks the minimum and swaps it with the element at current position.
  - Suppose the array is:
    - 5 2 9 5 4 3 1 6
  - Let's distinguish the two 5's as 5(a) and 5(b).
    5(a) 2 9 5(b) 4 3 1 6
  - After the first iteration, will be swapped with the element in 1st position:
     So the array becomes:
    - 1 2 9 5(b) 4 3 5(a) 6
  - Now, we clearly see that 5(a) and 5(b) are swapped in the sorted array.
     Therefore, this algorithm is unstable.

# 4. quicksort(퀵 정렬)

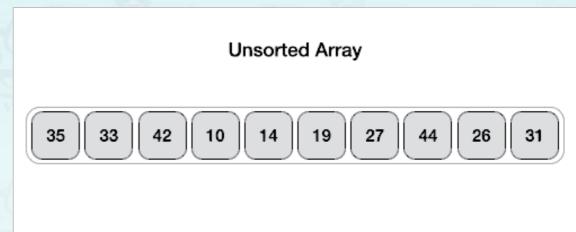
- Quicksort is a divide-and-conquer algorithm.
- It works by selecting a 'pivot' element from the array and partitioning the other elements into two subarrays, according to whether they are less than or greater than the pivot.
- The sub-arrays are then sorted recursively.



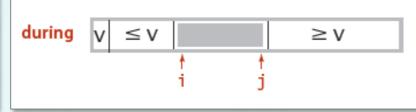
https://en.wikipedia.org/wiki/Quicksort

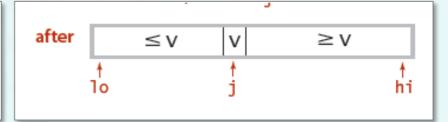
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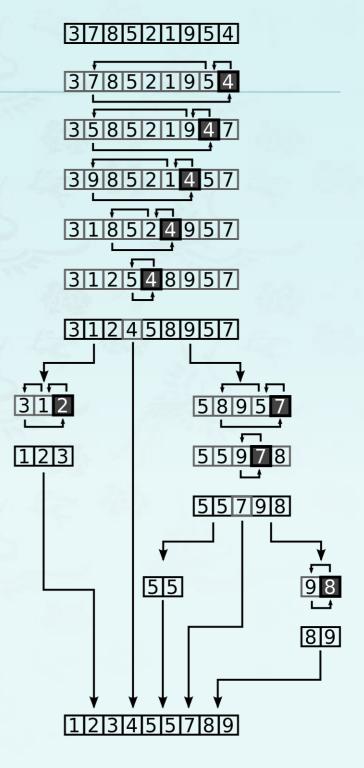




# 4. quicksort(퀵 정렬)

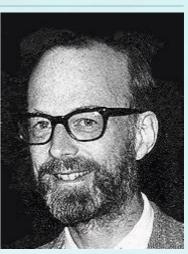
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The shaded element is the **pivot**. It is chosen as the last element of the partition here.



# 4. Quicksort - by Hoare in 1961

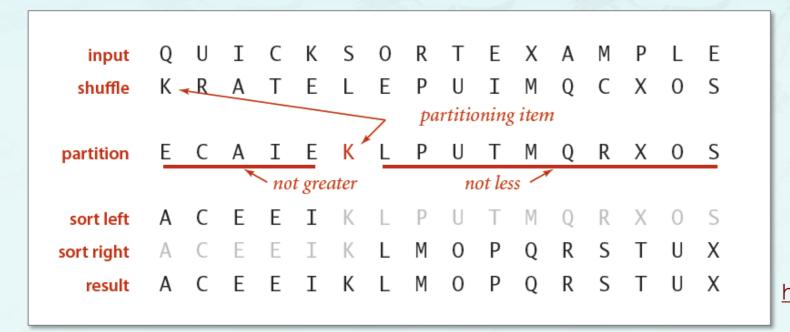
- Algorithm:
  - Shuffle the array.
  - Partition so that, for some j
    - entry a[j] is in place
    - no larger entry to the left of j
    - no smaller entry to the right of j
  - Sort each piece recursively.

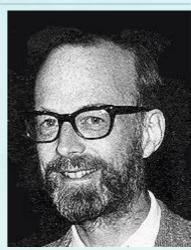


Sir Charles Antony Richard Hoare 1980 Turing award

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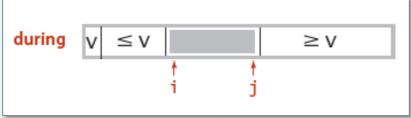
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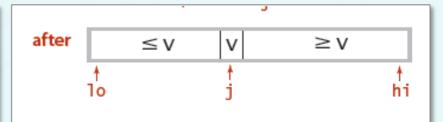
https://algs4.cs.princeton.edu/23quicksort/

- Phase I. Repeat until i and j pointers cross:
  - Scan *i* from left to right so long as (a[i] < a[lo])
  - Scan j from right to left so long as (a[j] > a[lo]).
  - Exchange a[i] with a[j].





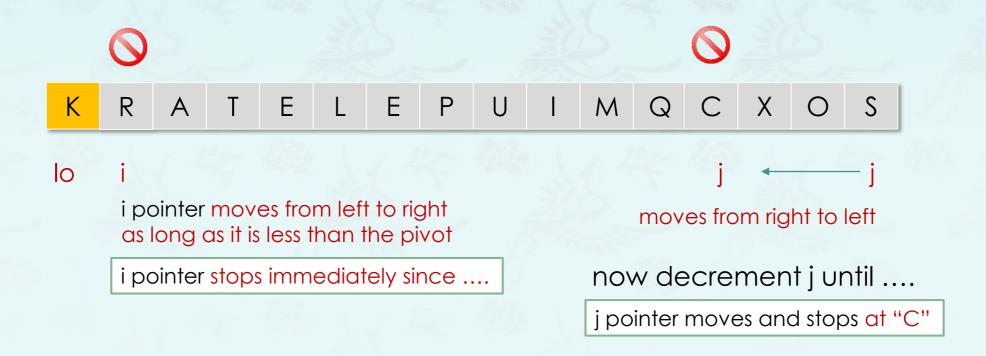




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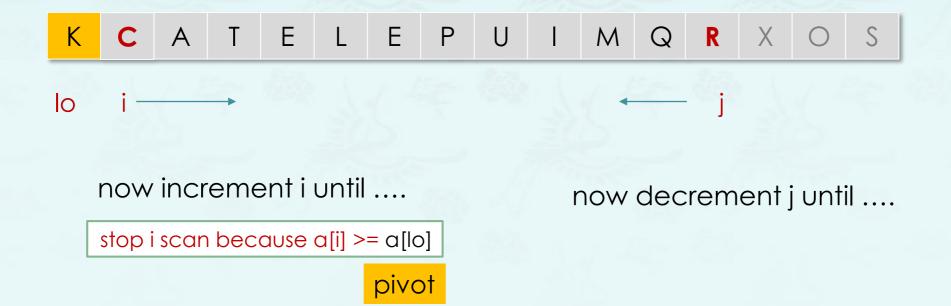


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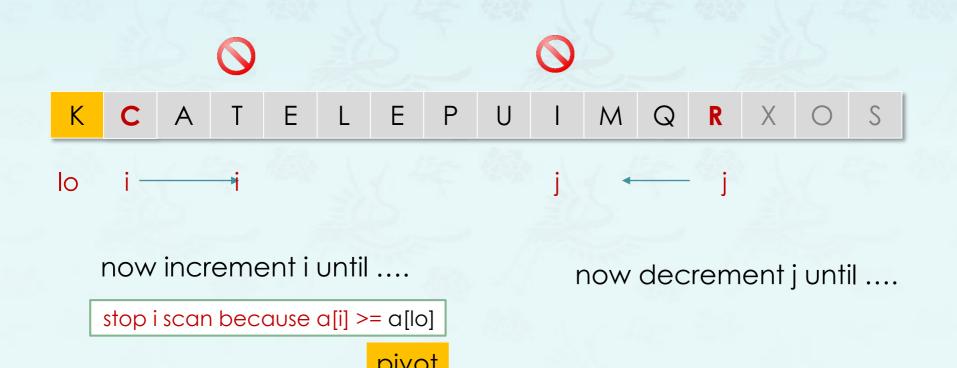


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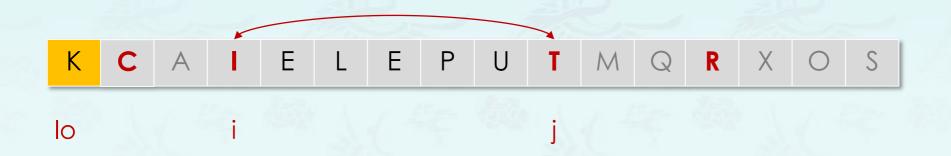
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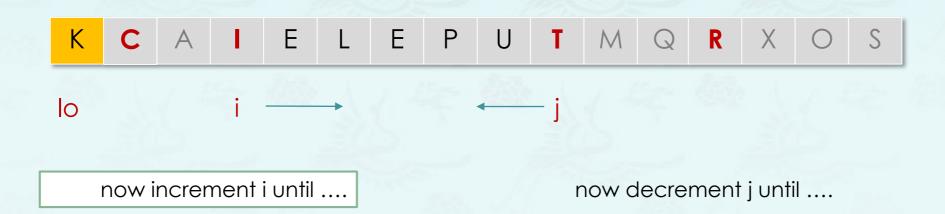


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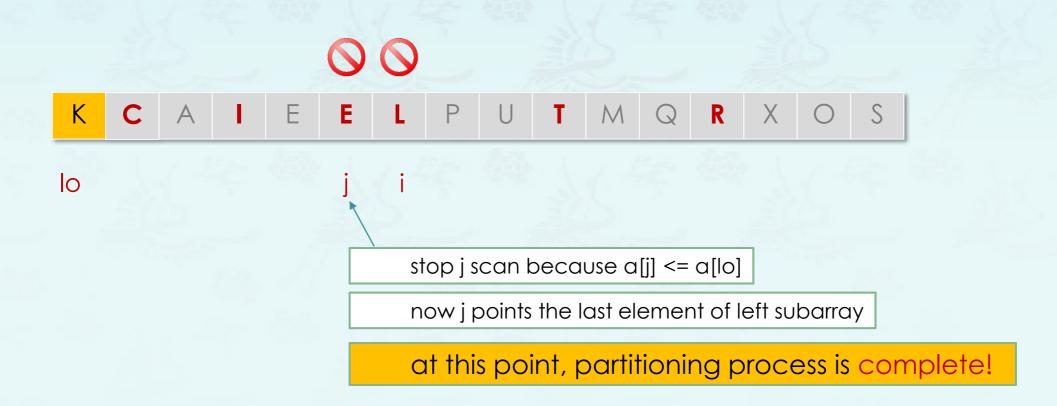


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- Phase II. When pointers cross.
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at this point, partitioning process is complete!

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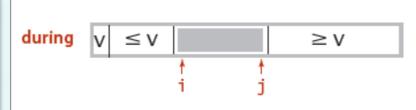


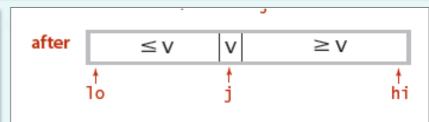
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#### **Quicksort implementation**

```
bool less(char a, char b) { return a < b; }</pre>
void swap(char *a, int i, int j) { char t = a[i]; a[i] = a[j]; a[j] = t; }
int partition(char *a, int lo, int hi) {
   int i = lo; int j = hi + 1;
                                          pivot
   while (1) {
       while (less(a[++i], a[lo]))
                                             find item on left to swap
            if (i == hi) break;
        while (less(a[lo], a[--j]))
                                             find item on right to swap
            if (i == lo) break;
        if (i >= j) break;
                                             check if pointers cross
        swap(a, i, j);
                                             swap
    swap(a, lo, j);
                                             swap with pivot
                                             return index of item now sorted
    return j;
```



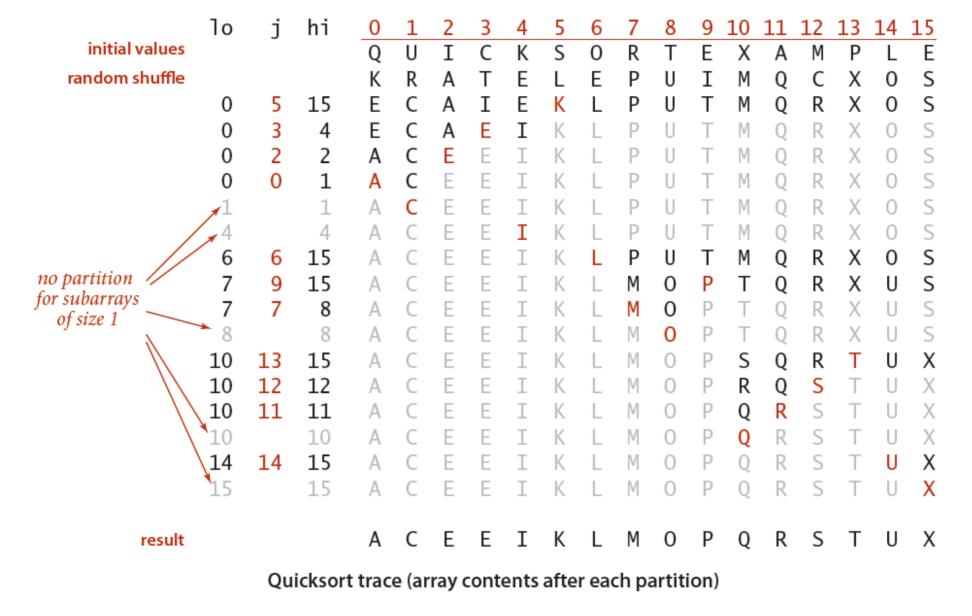




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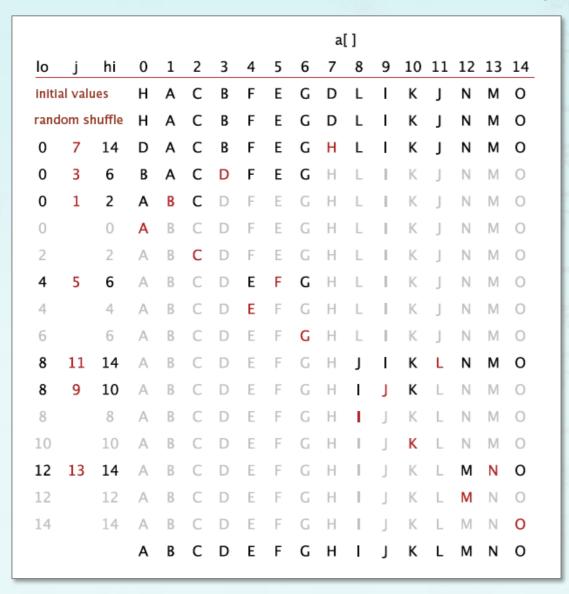
```
void quicksort(char *a, int lo, int hi) {
   if (hi <= lo) return;</pre>
   int j = partition(a, lo, hi);
   quicksort(a, lo, j - 1);
   quicksort(a, j + 1, hi );
void main() {
 char a[] = {'Q', 'U', 'I', 'C', 'K', 'S', 'O', 'R', 'T', 'E', 'X', 'A', 'M', 'P', 'L', 'E'};
 int N = sizeof(a) / sizeof(a[0]);
 cout << "UNSORTED: \n";</pre>
 for (int i = 0; i < N; i++) cout << a[i]; cout << endl;
 // shuffle(a, N);
 quicksort(a, 0, N-1);
 cout << "SORTED: \n";</pre>
 for (int i = 0; i < N; i++) cout << a[i]; cout << endl;
```

## **Quicksort implementation**



#### Quicksort: best-case analysis

• Best case: Number of compares is  $\sim N \lg N$ .



#### Quicksort: worst-case analysis

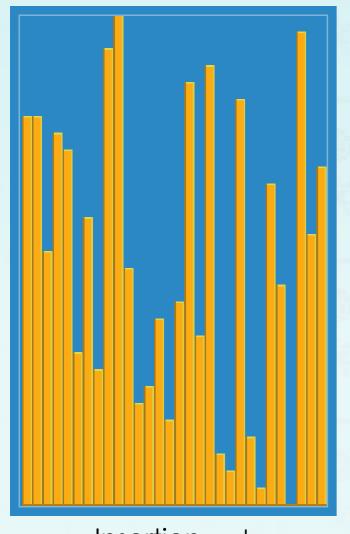
• Worst case: Number of compares is  $\sim \frac{1}{2} N^2$ .



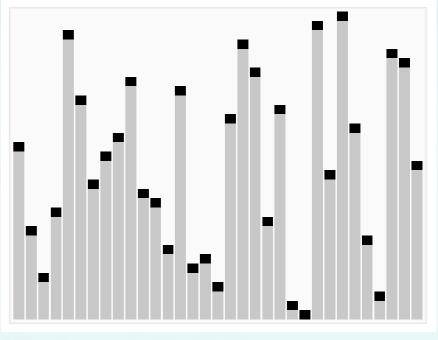
## Quicksort: average-case analysis

- Worst case: Number of compares is quadratic.
  - $N + (N-1) + (N-2) + ... + 1 \sim \frac{1}{2} N^2$ .
  - More likely that your computer is struck by lightning bolt
- Average case: Number of compares is ~ 1.39 N Ig N.
  - 39% more compares than mergesort.
  - But faster than mergesort in practice because of less data movement.
- Random shuffle:
  - Probabilistic guarantee against worst case.
  - Basis for math model that can be validated with experiments.

# **Sorting Algorithm Animation**



5 9 6 4 7 2 3 1 8 **Bubble sort** 5 1 8 4 9 6 7 2 3 Selection sort



Insertion sort

Quicksort

https://commons.wikimedia.org/wiki/File:Insertion-sort-example.gif <a href="https://en.wikipedia.org/wiki/Insertion">https://en.wikipedia.org/wiki/Insertion</a> sort

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