$$\frac{dSOM}{dT} = (\sigma_S + \sigma_{\varepsilon}\bar{\varepsilon})SOM \qquad \qquad \frac{dBIO}{dT} = (\sigma_B + \sigma_{\varepsilon}\bar{\varepsilon})BIO$$

$$y_t = y_{\text{max}} \left(1 - \exp\left\{ -\frac{1}{N_{\text{req}}} (F_t + \alpha \text{SOM}) \right\} \right) \left(1 - \beta \exp\left\{ -\gamma \text{BIO} - (1 - \gamma) \left(\frac{P_t}{P_{\text{req}}} \right) \right\} \right)$$

$$F_{t} = (1 - \kappa_{\text{Profit}} - \kappa_{\text{Other}}) F_{t-1} + \kappa_{\text{Profit}} F_{\text{OPT}} + k_{\text{Other}} \langle F_{t-1} \rangle$$

$$P_{t} = (1 - \kappa_{\text{Profit}} - \kappa_{\text{Other}}) P_{t-1} + \kappa_{\text{Profit}} P_{\text{OPT}} + k_{\text{Other}} \langle P_{t-1} \rangle$$

$$F_{\text{OPT}}, P_{\text{OPT}} = \max_{F \in [0.5 \cdot F_{t-1}, 1.5 \cdot F_{t-1}], P \in [0.5 \cdot P_{t-1}, 1.5 \cdot P_{t-1}]} \mathcal{P}(\hat{p}_{t}^{M})$$

$$p_t^M = p_{i-1}^M \left(1 + \frac{D - Y}{Y} \right) \quad p_0^M = \mu \frac{(p_F F_0 + p_P P_0 + p_{\text{other}})}{y_0}$$